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PHYSICS OF ELEMENTARY PARTICLES  
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# NLO QCD Corrections to Higgs Boson Production in Association with Gauge Bosons in Proton–Proton Collisions at $\sqrt{s} = 14$ TeV

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**Abstract**—We suggest some predictions for Standard Model Higgs boson production in association with gauge bosons in proton-proton collisions at  $\sqrt{s} = 14$  TeV. Our calculation includes the NLO QCD corrections of these processes using the MadGraph5\_aMC@NLO event generator. We study the impact of these corrections on the total cross sections and on various kinematical distributions.

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## 1. INTRODUCTION

The discovery of the Higgs boson at the LHC in 2012 [1, 2] was a watershed moment in high-energy physics. As a result, it is the source of the Standard Model's electroweak symmetry breaking mechanism and mass generation (SM). The Higgs boson production associated with gauge bosons  $W$  or  $Z$  (also known as the Higgs-strahlung process) is one of the most important Higgs production modes, it provides information about the Higgs boson couplings with the vector bosons and other SM particles, and it can be used to search for signals for Beyond Standard Model physics.

For these reasons, the ATLAS and CMS teams are very interested in the processes  $pp \rightarrow VH$  ( $V = W/Z$ ). The results of  $VH$  generation with the ATLAS detector were published in [3] for  $\sqrt{s} = 7$  and 8 TeV center-of-mass energies. The ATLAS collaboration examined data acquired between 2015 and 2016 [4], and those between 2015 and 2018 [5] at  $\sqrt{s} = 13$  TeV. The CMS experiment has given a search for studying  $VH$  generation at  $\sqrt{s} = 8$  and 13 TeV, which correspond to integrated luminosities of 19.7 and up to 2.7 fb<sup>-1</sup> respectively [6].

In recent years, a large number of theoretical predictions for  $H$  production associated with gauge bosons have been made, first at leading order only via  $q\bar{q}$  [7, 8], then at next-to-leading order with QCD and EW corrections [9–12]. Computations of next-to-next-to-leading order QCD corrections to  $pp \rightarrow VH$  were performed in [13]. The investigations of the off-shell of NLO for  $WH$  synthesis ( $H \rightarrow b\bar{b}$ ,  $W \rightarrow l\nu_l$ ) at

$\sqrt{s} = 8$  and 14 TeV were performed using the MC@NLO simulation [14]. Tests of the relationship between a jet and  $WH$  production at  $\sqrt{s} = 13$  TeV were accomplished with the NNLOJET framework and NNPDF31 from the LHAPDF library in [15]. The  $vh@nnlo$  software was used to compute  $ZH$  production at NNLO QCD corrections at  $\sqrt{s} = 8$  and 14 TeV in [16]. The gluon-gluon and photon-photon collisions that lead to  $ZH$  formation were exposed in reference [17].

The  $VH$  production in proton–proton collisions at  $\sqrt{s} = 14$  TeV is the subject of this research. These processes are carried out at LO and NLO using the MadGraph5\_aMC@NLO [18] event generator. Numerical projections of their LO and NLO total cross sections, as well as the scale uncertainties associated with them are also presented. Using Pythia8 [19], we produce the different distributions of the gauge vector transverse momentum, the two tagging jets, and the missing transverse energy after the showering and the hadronisation.

The following is how the rest of the article is structured. In Section 2, we discuss the influence of the NLO QCD corrections on the contributions of  $VH$  production. We report our phenomenological findings on the total cross section and various distributions in Section 3. Finally, in Section 4, we provide our conclusions.

## 2. DETAILS OF THE CALCULATION

In this section, we focus on the production, on-shell, of the processes  $pp \rightarrow VH$ , where  $V = W^\pm, Z$ .

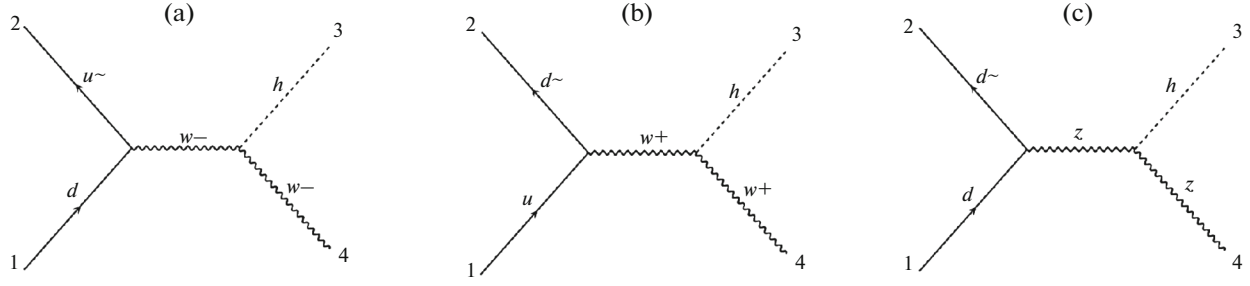


Fig. 1. Examples of Feynman diagrams for the different processes of  $VH$  production at tree-level.

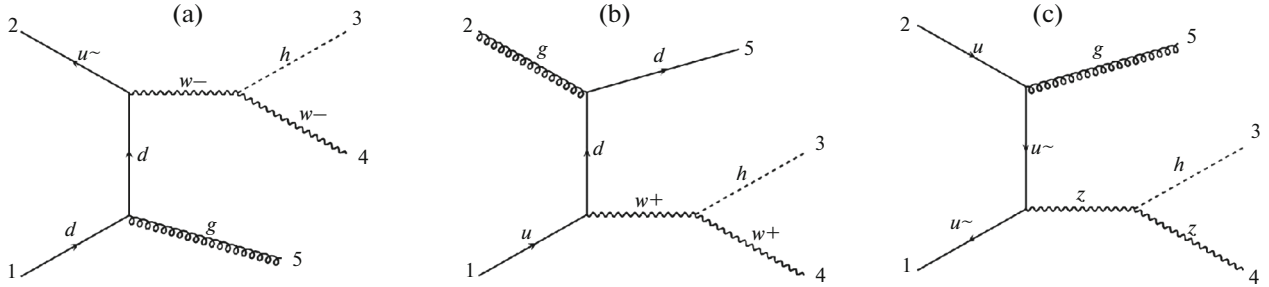


Fig. 2. Examples of Feynman diagrams of real corrections for the different processes of  $VH$  production.

We work in the context of the Standard Model with 4-flavour scheme, i.e.  $p = u, d, c, s$  and gluons. We take into account the virtual bottom-loop, top-loop but not their contributions in the initial states. The collision events are generated at LO and NLO with QCD corrections using MadGraph5\_aMC@NLO version 2.6.0.

We start by generating the processes at leading order, where the  $pp \rightarrow W^\pm H$  processes are exclusively via the  $t$ -channel of  $q\bar{q}'$  annihilation with exchange of  $W^\pm$  bosons, as shown in Figs. 3a and 3b. However, the  $ZH$  production comes from the  $q\bar{q}$  annihilation with exchange of the  $Z$  boson as displayed in Fig. 1c.

The  $O(\alpha_s)$  NLO QCD corrections consist of new channels with a real and virtual contributions. They involve infrared (IR) and ultraviolet (UV) divergences that are regulated using the dimensional regularization (DR) scheme [20].

The real emission for  $VH$  production is essentially the tree-level diagrams with an additional parton and we classify it into two groups:  $q\bar{q}' \rightarrow W^\pm H g$  and  $q(\bar{q}')g \rightarrow W^\pm H q(\bar{q}')$  where some examples are given in Figs. 2a and 2b. The same is true for  $pp \rightarrow ZH$  except that  $q' = q$  as represented in Fig. 2c.

The virtual corrections are also computed. We noticed that the one-loops of  $pp \rightarrow W^\pm H$  have triangle form and they are only obtained by  $q\bar{q}'$  initiated as illustrated in Figs. 3a and 3b. While, those for  $ZH$  production are two types of loops, boxes and triangles,

which are obtained by  $q\bar{q}$  and  $gg$  contributions as shown in Fig. 3c. The gluon-initiated produces a top-quark and bottom loops which represent an interesting feature of the dominant contributions in the SM and beyond the SM.

### 3. PHENOMENOLOGICAL RESULTS AND DISCUSSION

In the following, we present our predictions of the total cross sections and kinematics variables distributions for  $VH$  production at LHC in the case of  $\sqrt{s} = 14$  TeV, using PYTHIA8 for showering and hadronization of the events. We employ NNPDF23 set parton distribution functions from LHAPDF setup [21], adopting the strong coupling constant  $\alpha_s(M_Z) = 0.1137$  and  $0.1251$  at LO and NLO respectively. Moreover, we take the central numerical value of the renormalization and factorization scales set to  $\mu_R = \mu_F = M_H$ .

For all the numerical results, we collect the following SM input parameters B :

$$\begin{aligned} G_\mu &= 1.16637 \times 10^{-5} \text{ GeV}^{-2}, & \alpha^{-1} &= 132.338; \\ M_W &= 80.385 \text{ GeV}, & \Gamma_W &= 2.085 \text{ GeV}; \\ M_Z &= 91.188 \text{ GeV}, & \Gamma_Z &= 2.495 \text{ GeV}; \\ M_H &= 125 \text{ GeV}, & \Gamma_H &= 0.00407 \text{ GeV}; \\ M_t &= 173.2 \text{ GeV}, & \Gamma_t &= 1.4426 \text{ GeV}. \end{aligned}$$

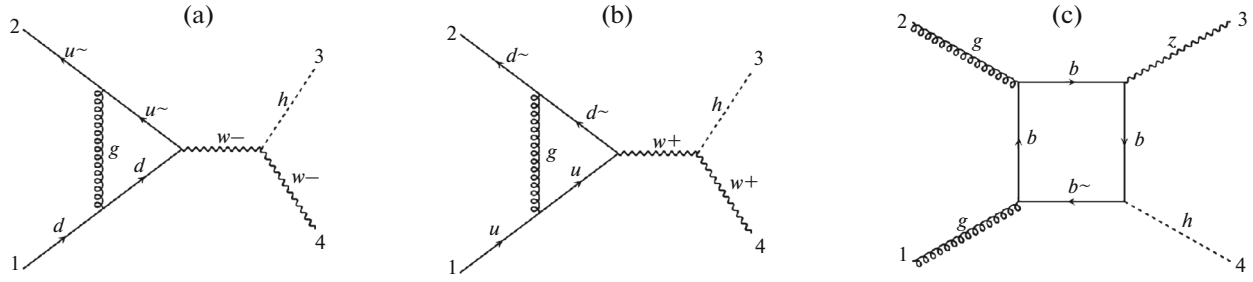


Fig. 3. Examples of Feynman diagrams of virtual corrections for the different processes of  $VH$  production.

Meanwhile, we impose the following cuts on transverse momentum, pseudo-rapidity of the leptons and jets:

$$\begin{aligned} |\eta(l)| &\leq 2.5, \quad p_T(l) > 20 \text{ GeV}, \\ |\eta(j)| &\leq 2.5, \quad p_T(j) > 10 \text{ GeV}. \end{aligned} \quad (1)$$

The jets are reconstructed with the anti-kT algorithm [22] with a radius parameter set to  $R = 0.6$ .

### 3.1. Total Cross Sections

In Table 1, we report the results of our predictions of the LO and NLO total cross sections and their corresponding K-factors for  $VH$  production. The impact of the NLO QCD corrections ranges from 32 to 38% of the LO term for all our processes. This is due to the real and the virtual contributions introduced at NLO. We remind that the  $ZH$  production via the  $gg \rightarrow ZH$  process contributes only at next-to-leading order (NLO) and that its cross section is:  $\sigma_{\text{NLO}}^{gg \rightarrow ZH} = 0.066 \pm 2.8 \times 10^{-4} {}^{+24.3\%}_{-18.6\%}$  which represents 7% of the total cross section. Table also shows that the size of the QCD corrections is large for the  $pp \rightarrow W^- H$  process with the largest value of the K factor equal to 1.38.

Our predictions of the total cross sections are in good agreement with those presented in [23] at 13 TeV. The same is true when we compare them with experimental measurements given by the ATLAS Collabora-

tion [4] in pp collisions at  $\sqrt{s} = 13$  TeV using the data collected during 2015 and 2016:

$$\begin{aligned} \sigma_{WH} \mathcal{B}_{H \rightarrow WW^*} &= 0.67 {}^{+0.31}_{-0.27} (\text{stat.}) {}^{+0.14}_{-0.11} (\text{exp syst.}) {}^{+0.11}_{-0.09} (\text{theo syst.}) \text{ pb}, \\ \sigma_{ZH} \mathcal{B}_{H \rightarrow WW^*} &= 0.54 {}^{+0.31}_{-0.24} (\text{stat.}) {}^{+0.10}_{-0.05} (\text{exp syst.}) {}^{+0.11}_{-0.05} (\text{theo syst.}) \text{ pb}. \end{aligned}$$

with  $\mathcal{B}_{H \rightarrow WW^*}$  is the branching-fraction values.

In the same table, we have estimated the theoretical errors come with our calculations. The first ones are deposited directly after the values of the total cross sections, they are the statical errors of the Monte Carlo simulations and the next ones are the scale uncertainties, simulated by varying simultaneously  $\mu_R$  and  $\mu_F$  between  $0.5 M_H < \mu_R, \mu_F < 2 M_H$  with the constraint  $0.5 < \mu_R/\mu_F < 2$ . We note that the scale uncertainties at NLO are smaller than the corresponding ones of the LO results.

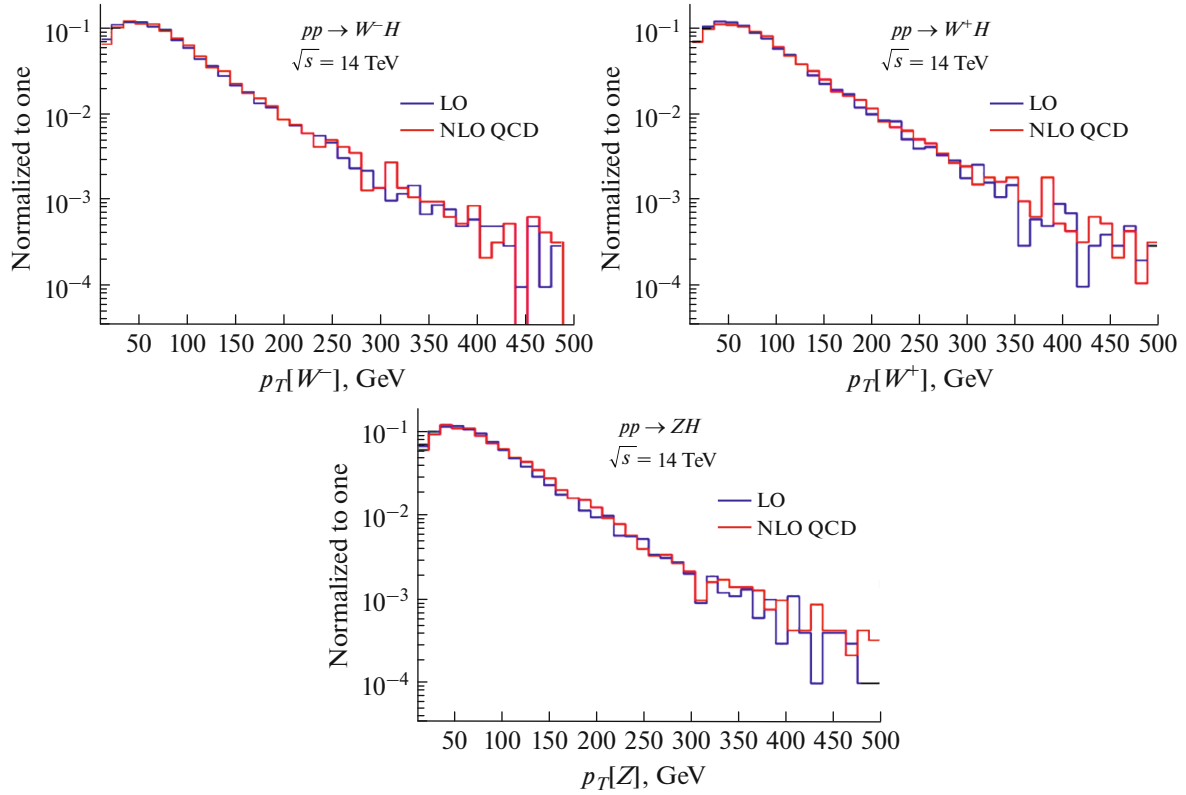
### 3.2. Distributions

Now, we investigate various kinematical distributions, we recall that all these distributions are normalized to one.

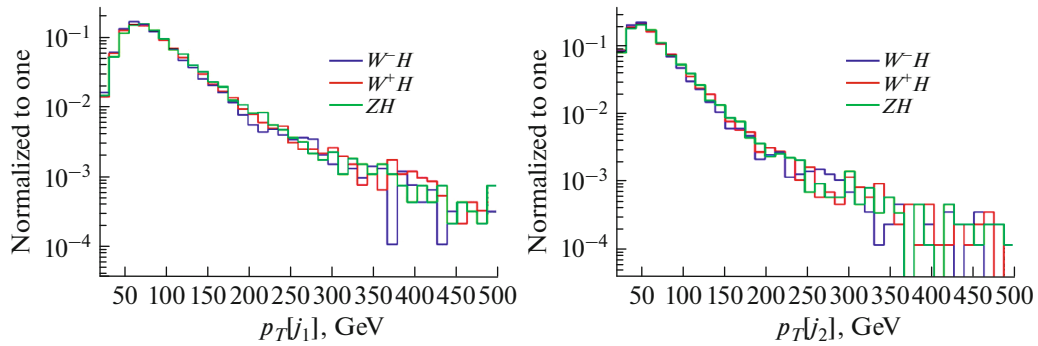
We begin with the transverse moments of the vector bosons at partonic level, as plotted in Fig. 4. We see that the LO and NLO distributions have the same shape for all  $pp \rightarrow VH$  processes ( $V = W^\pm$  and  $Z$ ). We

Table 1. The LO and NLO total cross section of  $VH$  production at  $\sqrt{s} = 14$  TeV

|         | $\sigma_{\text{LO}}, \text{pb}$                       | $\sigma_{\text{NLO}}, \text{pb}$                    | $K = \frac{\sigma_{\text{NLO}}}{\sigma_{\text{LO}}}$ |
|---------|---|---|--|
| $W^- H$ | $0.44 \pm 5.2 \times 10^{-4} {}^{+3.58\%}_{-4.37\%}$  | $0.605 \pm 1.5 \times 10^{-3} {}^{+1.7\%}_{-2.3\%}$ | 1.38   |
| $W^+ H$ | $0.717 \pm 5.3 \times 10^{-4} {}^{+3.22\%}_{-3.95\%}$ | $0.947 \pm 2.4 \times 10^{-3} {}^{+2.2\%}_{-2.6\%}$ | 1.32   |
| $ZH$    | $0.608 \pm 5.9 \times 10^{-4} {}^{+3.11\%}_{-3.85\%}$ | $0.887 \pm 1.4 \times 10^{-3} {}^{+2.0\%}_{-2.4\%}$ | 1.35   |



**Fig. 4.** The LO and NLO transverse momentum distributions of vector bosons for  $VH$  productions at  $\sqrt{s} = 14$  TeV.



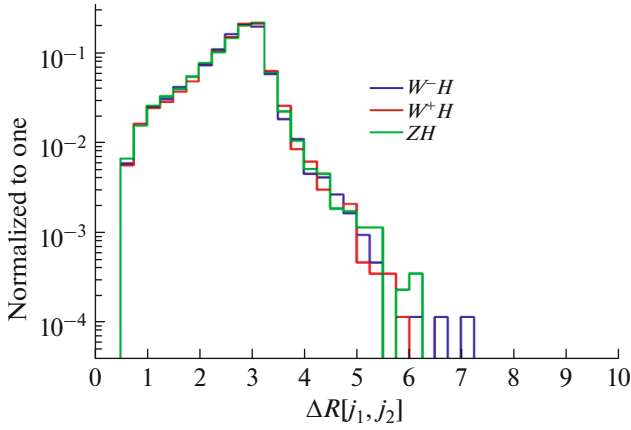
**Fig. 5.** Transverse momentum distributions of the two tagging jets reconstructed at NLO-QCD for  $VH$  productions at  $\sqrt{s} = 14$  TeV.

can distinguish also two regions; the first one corresponds to where the distributions grow lightly, at low values of the transverse momenta  $p_T(V) < 60$  GeV, and the second to the region where the distribution decreases for the rest  $p_T(V)$ .

The transverse momentum distributions of the two tagging jets reconstructed at NLO-QCD and  $\Delta R$  distance (a separation between two hardest jets) are reported in Figs. 5 and 6, respectively.

The behaviour of the hardest jets distributions has globally similar appearance for all processes, indeed at low  $p_T(j_1) < 80$  GeV and  $p_T(j_2) < 50$  GeV, the distributions are the largest, then they increase slightly. The next-to-hardest jet distribution vanishes rapidly comparing to the leading jet one. Additionally, the peaks of the  $\Delta R$  distributions are around 3.

Figure 7 shows the  $E_T^{\text{miss}}$  distributions for the  $W^+H$ ,  $W^-H$  and  $ZH$  processes. These distributions have the



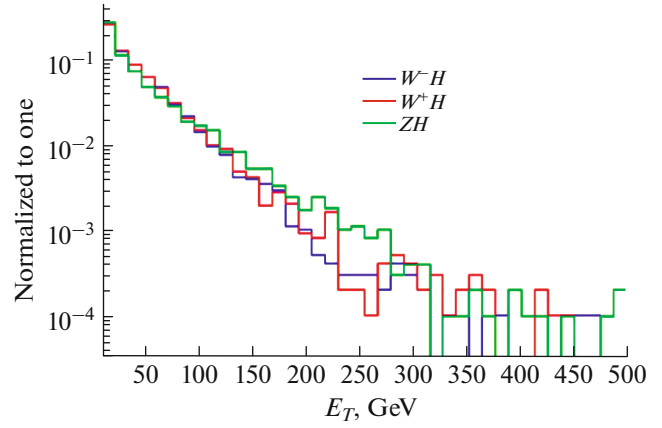
**Fig. 6.** The corresponding separation  $\Delta R$  distributions for  $VH$  productions at  $\sqrt{s} = 14$  TeV.

same behaviour. Indeed, the distributions decrease with the increment of  $E_T^{\text{miss}}$ . From  $E_T^{\text{miss}} > 150$  GeV, the signal for  $ZH$  production is greater than that for  $W^\pm H$ , this is due to the top-quark-loop included by the  $gg$  fusion.

#### 4. CONCLUSIONS

We have simulated the production of the Higgs boson associated with the vector bosons  $W^\pm$  and  $Z$  in proton-proton collisions at  $\sqrt{s} = 14$  TeV. We have illustrated the effects of NLO QCD corrections on this production. The latter produce new channels like gluon-gluon fusion which appears only at this level for the  $ZH$  production. The NLO QCD corrections also affect on the calculation of the total cross sections and we found that these corrections are of the order of 38% of the first term. The scale uncertainties have equally been estimated, they vary from  $-4.37$  to  $+3.58\%$ .

We have shown the shape of the spectrum for transverse momentum of vector bosons at parton level, that are similar for all  $pp \rightarrow VH$  processes ( $W^\pm$ ,  $Z$ ). The transverse momentum of the two tagging jets reconstructed at the first perturbative order allows us to confirm that the distribution is more sizeable at  $p_T(j_1) < M_{V+H}$ . For all  $VH$  production processes, the maximum of the separation distance between two hardest jets is at  $\Delta R = 3$ . We finally have pointed out the behaviour of the transverse missing energy. These distributions have the same behaviour, they decrease with the increment of  $E_T^{\text{miss}}$ . Because of the  $gg$  fusion, the signal for  $ZH$  production has the greatest  $E_T^{\text{miss}}$  that the other signals,  $W^+H$  and  $W^-H$ .



**Fig. 7.** Missing energy transverse distributions for  $VH$  productions at  $\sqrt{s} = 14$  TeV.

We conclude that this study is an interesting analysis and that we can expand it in different channels as  $H \rightarrow b\bar{b}$  and exploit the information in new physics searches, We leave this for investigate in the near future.

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#### CONFLICT OF INTEREST

The authors declare that they have no conflicts of interest.

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