Modular neural nets In the previous homework, we implemented modular neural networks for a two-layer neural network with fully connected layers. Now, we will do the same for convolutional layers. Once again, the benefit of modular designs is that we can snap together different types of layers and loss functions in order to quickly experiment with different architectures. # As usual, a bit of setup In [45]: import numpy as np import matplotlib.pyplot as plt from cs231n.gradient check import eval numerical gradient array, eval numerical gradient from cs231n.conv_layers import * %matplotlib inline plt.rcParams['figure.figsize'] = (10.0, 8.0) # set default size of plots plt.rcParams['image.interpolation'] = 'nearest' plt.rcParams['image.cmap'] = 'gray' # for auto-reloading external modules # see http://stackoverflow.com/questions/1907993/autoreload-of-modules-in-ipython %load_ext autoreload %autoreload 2 def rel error(x, y): """ returns relative error """ return np.max(np.abs(x - y) / (np.maximum(1e-8, np.abs(x) + np.abs(y))))The autoreload extension is already loaded. To reload it, use: %reload ext autoreload **Convolution layer: forward naive** Implement the function conv forward naive in the file cs231n/conv layers.py. You don't have to worry too much about efficiency at this point; just write the code in whatever way you find most clear. You can test your implementation by running the following: In [46]: x shape = (2, 3, 4, 4) $w_{shape} = (3, 3, 4, 4)$ $x = np.linspace(-0.1, 0.5, num=np.prod(x_shape)).reshape(x_shape)$ w = np.linspace(-0.2, 0.3, num=np.prod(w shape)).reshape(w shape)b = np.linspace(-0.1, 0.2, num=3)conv_param = {'stride': 2, 'pad': 1} out, _ = conv_forward_naive(x, w, b, conv_param) $correct_out = np.array([[[[-0.08759809, -0.10987781],$ [-0.18387192, -0.2109216]],[[0.21027089, 0.21661097], [0.22847626, 0.23004637]], [[0.50813986, 0.54309974], [0.64082444, 0.67101435]]], [[[-0.98053589, -1.03143541],[-1.19128892, -1.24695841]], [[0.69108355, 0.66880383], [0.59480972, 0.56776003]], [[2.36270298, 2.36904306], [2.38090835, 2.38247847]]]]) # Compare your output to ours; difference should be around 1e-8 print('Testing conv_forward_naive') print('difference: ', rel_error(out, correct_out)) Testing conv forward naive difference: 2.2121476417505994e-08 Aside: Image processing via convolutions As fun way to both check your implementation and gain a better understanding of the type of operation that convolutional layers can perform, we will set up an input containing two images and manually set up filters that perform common image processing operations (grayscale conversion and edge detection). The convolution forward pass will apply these operations to each of the input images. We can then visualize the results as a sanity check. In [47]: from PIL import Image kitten, puppy = np.array(Image.open('kitten.jpg')), np.array(Image.open('puppy.jpg')) # kitten is wide, and puppy is already square d = kitten.shape[1] - kitten.shape[0] kitten cropped = kitten[:, d//2:-d//2, :] img_size = 200 # Make this smaller if it runs too slow $x = np.zeros((2, 3, img_size, img_size))$ x[0, :, :, :] = np.array(Image.fromarray(puppy).resize((img_size, img_size))).transpose((2, 0, 1)) x[1, :, :] = np.array(Image.fromarray(kitten cropped).resize((img size, img size))).transpose((2, 0, img size))).transpose((2, 0, img size))).1)) # Set up a convolutional weights holding 2 filters, each 3x3 w = np.zeros((2, 3, 3, 3))# The first filter converts the image to grayscale. # Set up the red, green, and blue channels of the filter. w[0, 0, :, :] = [[0, 0, 0], [0, 0.3, 0], [0, 0, 0]]w[0, 1, :, :] = [[0, 0, 0], [0, 0.6, 0], [0, 0, 0]]w[0, 2, :, :] = [[0, 0, 0], [0, 0.1, 0], [0, 0, 0]]# Second filter detects horizontal edges in the blue channel. w[1, 2, :, :] = [[1, 2, 1], [0, 0, 0], [-1, -2, -1]]# Vector of biases. We don't need any bias for the grayscale # filter, but for the edge detection filter we want to add 128 # to each output so that nothing is negative. b = np.array([0, 128])# Compute the result of convolving each input in x with each filter in w, # offsetting by b, and storing the results in out. out, _ = conv_forward_naive(x, w, b, {'stride': 1, 'pad': 1}) def imshow noax(img, normalize=True): """ Tiny helper to show images as uint8 and remove axis labels """ if normalize: img max, img min = np.max(img), np.min(img) img = 255.0 * (img - img min) / (img max - img min)plt.imshow(img.astype('uint8')) plt.gca().axis('off') # Show the original images and the results of the conv operation plt.subplot(2, 3, 1) imshow noax(puppy, normalize=False) plt.title('Original image') plt.subplot(2, 3, 2) imshow noax(out[0, 0]) plt.title('Grayscale') plt.subplot(2, 3, 3) imshow noax(out[0, 1]) plt.title('Edges') plt.subplot(2, 3, 4)imshow noax(kitten cropped, normalize=False) plt.subplot(2, 3, 5)imshow noax(out[1, 0]) plt.subplot(2, 3, 6) imshow noax(out[1, 1]) plt.show() Original image Grayscale Edges Convolution layer: backward naive Next you need to implement the function conv backward naive in the file cs231n/conv layers.py. As usual, we will check your implementation with numeric gradient checking. In [48]: x = np.random.randn(4, 3, 5, 5)w = np.random.randn(2, 3, 3, 3)b = np.random.randn(2,)dout = np.random.randn(4, 2, 5, 5)conv param = {'stride': 1, 'pad': 1} dx num = eval numerical gradient array(lambda x: conv forward naive(x, w, b, conv param)[0], x, dout) dw_num = eval_numerical_gradient_array(lambda w: conv_forward_naive(x, w, b, conv_param)[0], w, dout) db_num = eval_numerical_gradient_array(lambda b: conv_forward_naive(x, w, b, conv param)[0], b, dout) out, cache = conv forward naive(x, w, b, conv param) dx, dw, db = conv backward naive(dout, cache) # Your errors should be around 1e-9' print('Testing conv backward naive function') print('dx error: ', rel_error(dx, dx_num)) print('dw error: ', rel_error(dw, dw_num)) print('db error: ', rel_error(db, db_num)) Testing conv backward naive function dx error: 9.682029025656176e-10 dw error: 5.431767655780389e-10 db error: 2.929860525174844e-11 Max pooling layer: forward naive The last layer we need for a basic convolutional neural network is the max pooling layer. First implement the forward pass in the function max_pool_forward_naive in the file cs231n/conv_layers.py . In [49]: $x_{shape} = (2, 3, 4, 4)$ x = np.linspace(-0.3, 0.4, num=np.prod(x shape)).reshape(x shape)pool_param = {'pool_width': 2, 'pool_height': 2, 'stride': 2} out, _ = max_pool_forward_naive(x, pool_param) $correct_out = np.array([[[-0.26315789, -0.24842105],$ [-0.20421053, -0.18947368]],[[-0.14526316, -0.13052632],[-0.08631579, -0.07157895]],[[-0.02736842, -0.01263158],[0.03157895, 0.04631579]]], [[[0.09052632, 0.10526316], [0.14947368, 0.16421053]], [[0.20842105, 0.22315789], [0.26736842, 0.28210526]], [[0.32631579, 0.34105263],[0.38526316, 0.4]]]) # Compare your output with ours. Difference should be around 1e-8. print('Testing max_pool_forward_naive function:') print('difference: ', rel_error(out, correct_out)) Testing max_pool_forward_naive function: difference: 4.1666665157267834e-08 Max pooling layer: backward naive Implement the backward pass for a max pooling layer in the function <code>max_pool_backward_naive</code> in the file cs231n/conv_layers.py . As always we check the correctness of the backward pass using numerical gradient checking. In [50]: x = np.random.randn(3, 2, 8, 8)dout = np.random.randn(3, 2, 4, 4)pool param = {'pool height': 2, 'pool width': 2, 'stride': 2} dx num = eval numerical gradient array(lambda x: max pool forward naive(x, pool param)[0], x, dout) out, cache = max_pool_forward_naive(x, pool_param) dx = max pool backward naive(dout, cache) # Your error should be around 1e-12 print('Testing max_pool_backward_naive function:') print('dx error: ', rel_error(dx, dx_num)) Testing max pool backward naive function: dx error: 3.2756192835058297e-12 **Fast layers** Making convolution and pooling layers fast can be challenging. To spare you the pain, we've provided fast implementations of the forward and backward passes for convolution and pooling layers in the file cs231n/fast layers.py. The fast convolution implementation depends on a Cython extension; to compile it you need to run the following from the cs231n directory: python setup.py build ext --inplace The API for the fast versions of the convolution and pooling layers is exactly the same as the naive versions that you implemented above: the forward pass receives data, weights, and parameters and produces outputs and a cache object; the backward pass recieves upstream derivatives and the cache object and produces gradients with respect to the data and weights. NOTE: The fast implementation for pooling will only perform optimally if the pooling regions are non-overlapping and tile the input. If these conditions are not met then the fast pooling implementation will not be much faster than the naive implementation. You can compare the performance of the naive and fast versions of these layers by running the following: In [51]: from cs231n.fast_layers import conv_forward_fast, conv_backward_fast from time import time x = np.random.randn(100, 3, 31, 31)w = np.random.randn(25, 3, 3, 3)b = np.random.randn(25,)dout = np.random.randn(100, 25, 16, 16)conv param = {'stride': 2, 'pad': 1} t0 = time()out_naive, cache_naive = conv_forward_naive(x, w, b, conv_param) t1 = time()out_fast, cache_fast = conv_forward_fast(x, w, b, conv_param) t2 = time()print('Testing conv_forward_fast:') print('Naive: %fs' % (t1 - t0)) print('Fast: %fs' % (t2 - t1)) print('Speedup: %fx' % ((t1 - t0) / (t2 - t1))) print('Difference: ', rel_error(out_naive, out_fast)) t0 = time()dx_naive, dw_naive, db_naive = conv_backward_naive(dout, cache_naive) t1 = time()dx fast, dw fast, db fast = conv backward fast(dout, cache fast) t2 = time()print('\nTesting conv backward fast:') print('Naive: %fs' % (t1 - t0)) print('Fast: %fs' % (t2 - t1)) print('Speedup: %fx' % ((t1 - t0) / (t2 - t1))) print('dx difference: ', rel_error(dx_naive, dx_fast)) print('dw difference: ', rel_error(dw_naive, dw_fast)) print('db difference: ', rel_error(db_naive, db_fast)) Testing conv_forward_fast: Naive: 0.098736s Fast: 0.015957s Speedup: 6.187587x Difference: 3.104202640264915e-11 Testing conv backward fast: Naive: 0.221409s Fast: 0.025931s Speedup: 8.538363x dx difference: 3.008014534569333e-12 dw difference: 1.0814979782973717e-13 db difference: 0.0 In [52]: from cs231n.fast_layers import max_pool_forward_fast, max_pool_backward_fast x = np.random.randn(100, 3, 32, 32)dout = np.random.randn(100, 3, 16, 16) pool param = {'pool height': 2, 'pool width': 2, 'stride': 2} t0 = time()out naive, cache naive = max pool forward naive(x, pool param) t1 = time()out_fast, cache_fast = max_pool_forward_fast(x, pool_param) t2 = time()print('Testing pool forward fast:') print('Naive: %fs' % (t1 - t0)) print('fast: %fs' % (t2 - t1)) print('speedup: %fx' % ((t1 - t0) / (t2 - t1))) print('difference: ', rel_error(out_naive, out_fast)) t0 = time()dx_naive = max_pool_backward_naive(dout, cache_naive) t1 = time()dx fast = max pool backward fast(dout, cache fast) t2 = time()print('\nTesting pool backward fast:') print('Naive: %fs' % (t1 - t0)) print('fast: %fs' % (t2 - t1)) print('speedup: %fx' % ((t1 - t0) / (t2 - t1))) print('dx difference: ', rel error(dx naive, dx fast)) Testing pool_forward_fast: Naive: 0.014960s fast: 0.004987s speedup: 3.000143x difference: 0.0 Testing pool backward fast: Naive: 3.017929s fast: 0.012967s speedup: 232.732942x dx difference: 0.0 Sandwich layers There are a couple common layer "sandwiches" that frequently appear in ConvNets. For example convolutional layers are frequently followed by ReLU and pooling, and affine layers are frequently followed by ReLU. To make it more convenient to use these common patterns, we have defined several convenience layers in the file cs231n/layer utils.py. Lets grad-check them to make sure that they work correctly: In [53]: from cs231n.layer_utils import conv relu pool forward, conv relu pool backward x = np.random.randn(2, 3, 16, 16)w = np.random.randn(3, 3, 3, 3)b = np.random.randn(3,)dout = np.random.randn(2, 3, 8, 8)conv param = {'stride': 1, 'pad': 1} pool_param = {'pool_height': 2, 'pool_width': 2, 'stride': 2} out, cache = conv relu pool forward(x, w, b, conv param, pool param) dx, dw, db = conv relu pool backward(dout, cache) dx num = eval numerical gradient array(lambda x: conv relu pool forward(x, w, b, conv param, pool param)[0], x, dout) dw num = eval numerical gradient array(lambda w: conv relu pool forward(x, w, b, conv param, pool param)[0], w, dout) db num = eval numerical gradient array(lambda b: conv relu pool forward(x, w, b, conv param, pool param)[0], b, dout) print('Testing conv_relu_pool_forward:') print('dx error: ', rel error(dx num, dx)) print('dw error: ', rel error(dw num, dw)) print('db error: ', rel error(db num, db)) Testing conv relu pool forward: dx error: 1.5359714066853973e-08 dw error: 6.730359554066423e-10 db error: 3.0926810572024394e-11 In [54]: from cs231n.layer_utils import conv relu forward, conv relu backward x = np.random.randn(2, 3, 8, 8)w = np.random.randn(3, 3, 3, 3)b = np.random.randn(3,)dout = np.random.randn(2, 3, 8, 8)conv param = {'stride': 1, 'pad': 1} out, cache = conv relu forward(x, w, b, conv param) dx, dw, db = conv_relu_backward(dout, cache) dx num = eval numerical gradient array(lambda x: conv relu forward(x, w, b, conv param)[0], x, dout) dw num = eval numerical gradient array(lambda w: conv relu forward(x, w, b, conv param)[0], w, dout) db_num = eval_numerical_gradient_array(lambda b: conv_relu_forward(x, w, b, conv_param)[0], b, dout) print('Testing conv_relu_forward:')

print('dx error: ', rel_error(dx_num, dx))
print('dw error: ', rel_error(dw_num, dw))
print('db error: ', rel error(db num, db))

In [55]: from cs231n.layer_utils import affine_relu_forward, affine_relu_backward

dx_num = eval_numerical_gradient_array(lambda x: affine_relu_forward(x, w, b)[0], x, dout)
dw_num = eval_numerical_gradient_array(lambda w: affine_relu_forward(x, w, b)[0], w, dout)
db_num = eval_numerical_gradient_array(lambda b: affine_relu_forward(x, w, b)[0], b, dout)

Testing conv_relu_forward:

x = np.random.randn(2, 3, 4)
w = np.random.randn(12, 10)
b = np.random.randn(10)

dout = np.random.randn(2, 10)

Testing affine_relu_forward:

In []:

dx error: 1.6226945537770296e-09
dw error: 3.5321483340718618e-09
db error: 1.8928900002169046e-11

out, cache = affine relu forward(x, w, b)

print('Testing affine_relu_forward:')
print('dx error: ', rel_error(dx_num, dx))
print('dw error: ', rel_error(dw_num, dw))
print('db error: ', rel_error(db_num, db))

dx, dw, db = affine relu backward(dout, cache)

dx error: 1.6412906626008716e-09
dw error: 1.8805714936176815e-09
db error: 2.183516243068678e-11