

- 16) Let $\alpha > 0, \beta > 0$ be such that $\alpha^3 + \beta^3 = 4$. If the maximum value of the term independent of x in the binomial expansion of $\left(\alpha x^{\frac{1}{9}} + \beta x^{\frac{-1}{6}}\right)$ is $10k$, then k equals to:
- 176
 - 336
 - 352
 - 84
- 17) Let S be the set of all $\lambda \in R$ for which the system of linear equations
- $$\begin{aligned} 2x - y + 2z &= 2 \\ x - 2y + \lambda z &= -4 \\ x + \lambda y + z &= 4 \end{aligned}$$
- has no solution. Then the set S
- is an empty set
 - is a singleton
 - contains more than two elements.
 - contains exactly two elements.
- 18) Let $X = \{x \in N : 1 \leq x \leq 17\}$ and $Y = \{ax + b : x \in X \text{ and } a > 0\}$. If mean and variance of elements of Y are 17 and 216 respectively then $a + b$ is equal to:
- 27
 - 7
 - 7
 - 9
- 19) Let $y = y(x)$ be the solution of the differential equation, $\frac{2 + \sin x}{(y+1)\left(\frac{dy}{dx}\right)} = -\cos x, y > 0, y(0) = 1$. If $y(\pi) = a$, and $\left(\frac{dy}{dx}\right)$ at $x = \pi$ is b , then the ordered pair (a, b) is equal to:
- $\left(2, \frac{2}{3}\right)$
 - $(1, 1)$
 - $(2, 1)$
 - $(1, -1)$
- 20) The plane passing through the points $(1, 2, 1), (2, 1, 2)$ and parallel to the line, $2x = 3y, z = 1$ also passes through the point:
- $(0, -6, 2)$
 - $(0, 6, -2)$
 - $(-2, 0, 1)$
 - $(2, 0, -1)$
- 21) The number of integral values of k for which the line, $3x + 4y = k$ intersects the circle, $x^2 + y^2 - 2x - 4y + 4 = 0$ at two distinct points is
- 22) Let \mathbf{a}, \mathbf{b} and \mathbf{c} be three unit vectors such that $|\mathbf{a} - \mathbf{b}|^2 + |\mathbf{a} - \mathbf{c}|^2 = 8$. Then $|\mathbf{a} + 2\mathbf{b}|^2 + |\mathbf{a} + 2\mathbf{c}|^2$ is equal to:

- 23) If the letters of the word MOTHER be permuted and all the words so formed be listed as in a dictionary, then the position of the word MOTHER is ...
- 24) If $\lim_{x \rightarrow 1} \frac{x+x^2+x^3+\dots+x^n-n}{x-1} = 820$ $n \in N$, then the value of n is equal to:
- 25) The integral $\int_0^2 ||x-1|-x| dx$ is equal to: