EE24BTECH11060 - Sruthi Bijili

Question:

Find a point which is equidistant from the points (-5,4) and (-1,6). How many such points are there ?

solution:

Variable	Description	formula
A(-5,4)	coordinates of first point	_
B(-1,6)	coordinates of second point	_
С	midpoint of A and B	_
k	ratio in which \mathbf{c} divides the line joining AB	$\frac{\mathbf{B}+k\mathbf{A}}{k+1}$

TABLE 0: Variables Used

$$\|\mathbf{C} - \mathbf{A}\| = \|\mathbf{C} - \mathbf{B}\| \tag{0.1}$$

$$\implies \|\mathbf{C} - \mathbf{A}\|^2 = \|\mathbf{C} - \mathbf{B}\|^2 \tag{0.2}$$

$$\implies \|\mathbf{C}\|^2 - 2\mathbf{C}^T\mathbf{A} + \|\mathbf{A}\|^2 = \|\mathbf{C}\|^2 - 2\mathbf{C}^T\mathbf{B} + \|\mathbf{B}\|^2$$
 (0.3)

$$\implies (A - B)^2 \mathbf{C} = \frac{\|\mathbf{A}^2\| - \|\mathbf{B}^2\|}{2} \tag{0.4}$$

by substituting the values from table
$$(0.5)$$

$$\implies 2x + y = -1 \tag{0.6}$$

$$if x = -3 \tag{0.7}$$

$$\implies y = 5$$
 (0.8)

$$\mathbf{C} = \begin{pmatrix} -3\\5 \end{pmatrix} \tag{0.9}$$

There are infinitely many points that are equidistant from the points (-5, 4) and (-1, 6)

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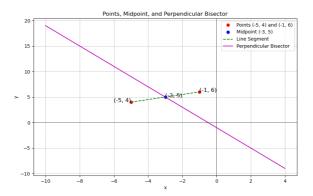


Fig. 0.1: line passing through the midpoint AB