

Logic, First Course, Winter 2020. Week 8, Section Meeting. [Back to course website](#)

## Combinations of arrows-statements and derived rules

In this section meeting, we just focus on doing some simple examples of proofs in classical logic. We focus on proofs that involve combinations of arrows-statements and our derived rules.

*Example 1.*

exercise

$$(s \rightarrow \neg(p \vee (\neg q \vee r))), s \vdash (\neg p \wedge (\neg r \wedge q))$$

1.  $s \rightarrow \neg(p \vee (\neg q \vee r))$  :assumption
2.  $s$  :assumption

*Example 2.*

exercise

$$(a \wedge (b \vee (c \wedge d))), \neg((a \wedge c) \wedge d) \vdash b$$

1.  $a \wedge (b \vee (c \wedge d))$  :assumption
2.  $\neg((a \wedge c) \wedge d)$  :assumption

*Example 3 (Pierce's Law).*

exercise

$$\top \vdash (((p \rightarrow q) \rightarrow p) \rightarrow p)$$

- 1.

*Example 4.*

exercise

$(\neg p \vee q) \vdash (p \rightarrow q)$

1.  $\neg p \vee q$  :assumption

*Example 5.*

exercise

$(p \rightarrow q) \vdash (\neg p \vee q)$

1.  $p \rightarrow q$  :assumption

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