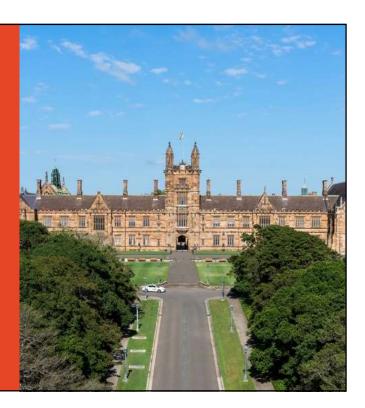
Statistical Model Building

Presented by
Dr Kathrin Schemann
Sydney Informatics Hub
Core Research Facilities
The University of Sydney





Acknowledging SIH



All University of Sydney resources are available to Sydney researchers **free of charge**. The use of the SIH services including the Artemis HPC and associated support and training warrants acknowledgement in any publications, conference proceedings or posters describing work facilitated by these services.

The continued acknowledgment of the use of SIH facilities ensures the sustainability of our services.

Suggested wording:

General acknowledgement:

"The authors acknowledge the technical assistance provided by the Sydney Informatics Hub, a Core Research Facility of the University of Sydney."

Acknowledging specific staff:

"The authors acknowledge the technical assistance of (name of staff) of the Sydney Informatics Hub, a Core Research Facility of the University of Sydney."

For further information about acknowledging the Sydney Informatics Hub, please contact us at sih.info@sydney.edu.au.

How to use this workshop

Workshops developed by the Statistical Consulting Team within the Sydney Informatics Hub form an integrated modular framework. Researchers are encouraged to choose modules to create custom programmes tailored to their specific needs. This is achieved through:

- Short 90 minute workshops, acknowledging researchers rarely have time for long multi day workshops.
- Providing statistical workflows appliable in any software, that give practical step by step instructions which researchers return to when analysing and interpreting their data or designing their study e.g. workflows for designing studies for strong causal inference, model diagnostics, interpretation and presentation of results.
- Each one focusing on a specific statistical method while also integrating and referencing the
 others to give a holistic understanding of how data can be transformed into knowledge
 from a statistical perspective from hypothesis generation to publication.

For other workshops that fit into this integrated framework refer to our training link page under statistics https://www.sydney.edu.au/research/facilities/sydney-informatics-hub/workshops-and-training.html#stats

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Research Workflows

- So... what is a workflow?
 - The process of doing any statistical analysis follows the same general "shape".
 - We provide a general research workflow, and a specific workflow for each major step in your research (currently experimental design, power calculation, analysis using linear models/survival/multivariate/survey methods)
 - You will need to tweak them to your needs
- Why do we need a research workflow?
 - As researchers we are motivated to find answers quickly
 - But we need to be systematic in order to
 - Find the right method
 - Use it correctly
 - Interpret and report our results accurately
 - The payoff is huge, we can avoid mistakes that would affect the quality of our work and get to the answers sooner

ect

Using this workshop after today

These slides should be used after the workshop as reference material and include these workflows for you to follow

- Todays workshop gives you the statistical workflow, which is software agnostic in that they can be applied in any software.
- There may also be accompanying software workflows that show you how to do it.
 We won't be going through these in detail. But if you have problems we have a monthly hacky hour where people can help you.

lon1 assistance You can request a consultation for more in-depth discussion of the material as it relates to your specific project. Consults can be requested via our Webpage (link is at the end of this presentation)

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During the workshop



Ask short questions or clarifications during the workshop. There will be breaks during the workshop for longer questions.



Slides with this blackboard icon are mainly for your reference, and the material will not be discussed during the workshop.



Challenge Question

- A wild boar is coming towards you at 200mph. Do you:?
 - A. Ask it directions
 - B. Wave a red flag
 - C. Wave a white flag
 - D. Begin preparing a trap



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General Research Workflow

- 1. Hypothesis Generation (Research/Desktop Review)
- 2. Experimental and Analytical Design (sampling, power, ethics approval)
- 3. Collect/Store Data
- 4. Data cleaning
- 5. Exploratory Data Analysis (EDA)
- 6. Data Analysis aka inferential analysis
- 7. Predictive modelling
- 8. Publication

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Contents

General Research Workflow

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Workflow: Steps in Model Building

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- 9. Check model goodness-of-fit
- 10. Interpret and report the results $% \left(1\right) =\left(1\right) \left(1\right) \left($

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Types of statistical models

- Any "regression type" model, e.g.
 - Linear Model (LM numeric outcome variable)
 - Generalised Linear Model (GLM e.g. binary or count outcome variable)
 - Linear Mixed Model (LMM LM with a random effect, e.g. repeated measures)
 - Generalised Linear Mixed Model (GLMM GLM with random effect)
 - Survival analysis (e.g. Cox semi-parametric regression; parametric regression)
 - Structural Equation Modelling
 - Bayesian Modelling
 - Models of spatial data
- Modelling is a very important part of quantitative research work

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A question for you:

What is your experience level with regression-type modelling?

- a) No theoretical or practical experience.
- b) Some theoretical experience only from coursework, Linear Models WS)
- c) Some practical experience I have run a model for my research.
- d) Experienced I have run a number of models on different data.
- e) Very experienced I use models routinely.

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age 10

A case study example



Results from a multivariable model for Math test score

Estimate Std. Error t value Pr(>|t|)
(Intercept) 2.105206 1.104172 1.907 0.0569.
IQ 0.997123 0.006561 151.981 <2e-16 ***
verbal.IQ -9.995200 0.067418 -148.257 <2e-16 ***

Multiple R-squared: 96%

$$y = b_0 + b_1 x_1 + b_2 x_2$$

Math test score = 2.1 + 1*IQ - 10*verbal.IQ

What is your interpretation? Is this a good model?

Simulated data

math.lQ <- rnorm(1000, 60, 10)
math.test.score <- math.lQ + rnorm(length(math.lQ),0,2)

verbal.IQ <- rnorm(1000, 80, 5)

IQ <- 10*verbal.IQ + math.IQ

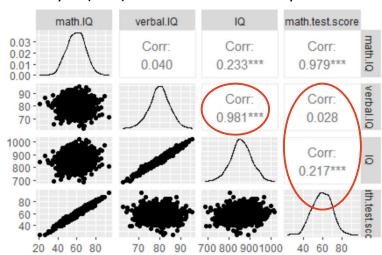
- > math.test.score is math.IQ with a bit of noise
- > IQ is a sum of verbal IQ and math.IQ (IQ:verbal.IQ r = 0.98)
- A model with verbal.IQ and IQ can re-arrange itself to:
 Math.IQ = IQ verbal.IQ

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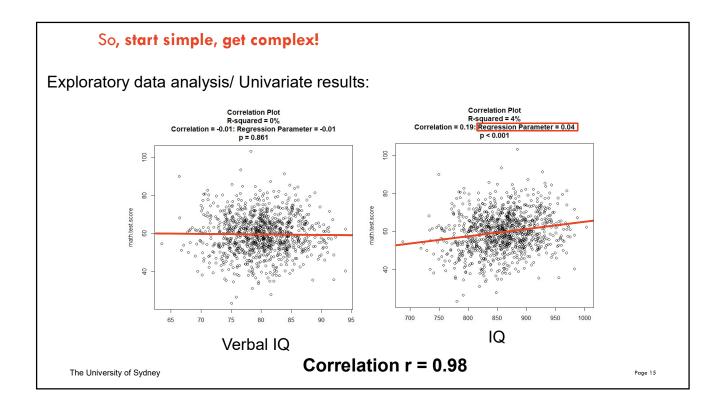
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Start simple, get complex!

Exploratory Data Analysis (EDA) – examine relationships between variables



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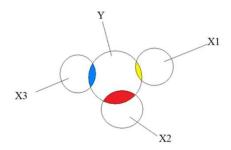
Example summary

Results:

- Verbal IQ is not negatively correlated with Math Test Score as shown by the simple marginal model and the simulated data
- Yet a model with Verbal IQ and IQ suggests Verbal IQ is negatively corelated with Math Test Score.
- WHY: because IQ=verbal IQ + math IQ meaning a model which has both IQ and verbal IQ (which are correlated) can rearrange itself as math IQ = IQ verbal IQ.
- This a reversal of verbal IQ verbal IQ is SUPRESSING IQ (the part of IQ that is uncorrelated with Math results).
- → This is an example of the **reversal paradox** due to multi-collinearity this may be called Simpson's paradox, Lord's paradox, and suppression depending on whether the outcome and explanatory variables are categorical, continuous or a combination of both
- → This is why we always look for multi-collinearity during the Exploratory Data Analysis using a scatterplot matrix to learn about the relationships between variables.

→ Start simple, get complex!

Relationships between variables - Correlation



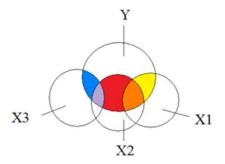
Why is 'high' correlation an issue for model building?

The model makes an assumption that the predictors are 'independent'.

What is correlation? This is NOT it!! X1, x2 and x3 are statistically independent. No conditional effects – effects the same as in univariate analysis.

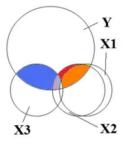
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Relationships between variables - Correlation



Moderate correlation: there is overlap, but conditional effects are still interpretable.

Relationships between variables - Correlation

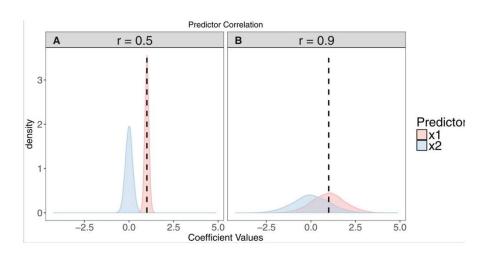


High correlation: x1 and x2 are almost identical

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The effect of high correlation: Example: $y \sim x1 + x2$



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Effect of high correlation/multi-collinearity on modelling

Extent of Multicollinearity Effect on the Regression Analysis



Little Not a problem

Moderate Not usually a problem

Strong Statistical consequences: Often a problem if you want to estimate effects of individual

X variables (ie, regression coefficients); may not be a problem if your goal is just to

predict or forecast Y

Extremely Numerical consequences: Always a problem; computer calculations may even be

strong wrong due to numerical instability

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Potential indicators of multi-collinearity:



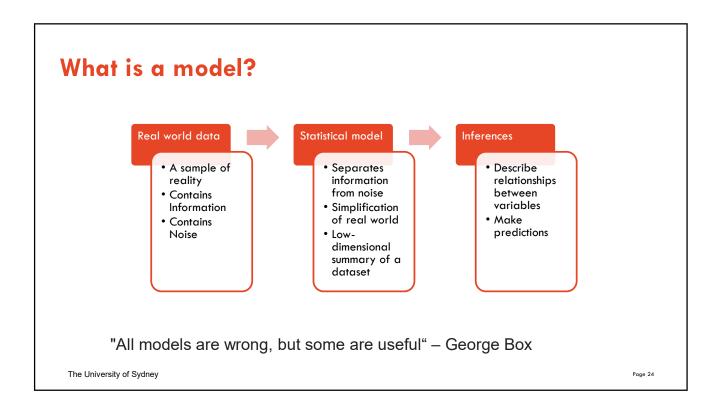
- Coefficients have signs opposite to what you'd expect from theory (suppression see DAG in appendix for explanation)
- Very high standard errors for regression coefficients
- Overall model is significant, but none of the coefficients are
- Large changes in coefficients when adding predictors
- Coefficients on different samples are wildly different
- High Variance Inflation Factor (VIF) and low tolerance (VIF reciprocal) direct measure of how much the variance of the coefficient is being inflated due to multicollinearity – e.g. linear combinations of variables correlated with a variable
- High condition index in PCA ratio between first and last PC

For further information see:

https://www.theanalysisfactor.com/eight-ways-to-detect-multicollinearity/

Back to Models





Model Building – what is the 'best fit'?

- What is the purpose of a model?
 - 1. Hypothesis testing/Inference Interpret the relationships between predictors and the outcome
 - Gain knowledge get the most precise estimates
 - Be careful of interaction and confounding
 - 2. Prediction of future observations
 - Best model fit
 - Exclude predictors that are questionably related to outcome
- Subject matter knowledge
 - Understand and consider the relationships between variables
 - · Consider ease of measurement and reliability of variables
- Parsimony (using as few predictors as required) versus fit
 - But include design variables/ known confounders

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Workflow: Steps in Model Building

- 1. Identify the outcome variable and a full set of predictor variables to be considered
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- 9. Check model goodness-of-fit
- 10. Interpret and report the results

Step 1: Identify the outcome variable and a full set of predictor variables to be considered – the full or maximal model

Identify the outcome variable - what is the study aim/research question?

Consider all possible predictors of interest

- Include 'design variables' depends on study design and type, controlled versus observational, e.g.
 - Include a block 'design' variable for block randomisation in RCT
 - Include predictor variable of interest to the research question/ hypothesis (e.g. exposure variable)
 - Include 'cluster' variables, e.g. patients in hospitals; animals on farms; students in classes in schools
- Consider potential confounders e.g. age, sex, BMI, comorbidity, previous experience,...
- Consider what interaction terms to include

This is as much a scientific/clinical task as it is a statistical task.

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Step 1: Identify the outcome variable and a full set of predictor variables to be considered – control of confounding

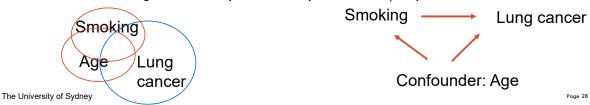
Potential confounders – e.g. age, sex, BMI, comorbidity, previous experience, etc.

Control at study design stage:

- Use exclusion (restricted sampling; e.g. only people without comorbidity)
- Use stratification (divide sample into different groups)
- Use matching e.g. matched case-control study (matched on same comorbidity);
 blocking in RCT

At analysis stage:

Use multivariable regression analysis for analytical control/adjustment



Step 1: Identify a full set of predictor variables - Interactions

Decide what interactions between predictors are to be considered

- Avoid 3-way interactions unless indicated by subject matter (difficult to interpret)
- Consider multiple testing adjustment if using large number of interactions see Linear Models 3 WS
- Evaluate interactions graphically where possible.

Five general strategies for creating and evaluating interactions*:



- Create and evaluate all 2-way interaction terms (ok for number of predictors <=8)
- Create 2-way interactions among all predictors that are significant in the final main effects model (after model building)
- Create 2-way interactions among all predictors found to have an unconditional (univariate) association with the outcome.
- 4. Create 2-way interactions only among pairs of variables which you suspect might interact (based on literature, expert knowledge etc), e.g. those involving the primary predictor of interest and important confounders.
- 5. Only create 2-way interaction terms that involve the predictor of interest.
- * May be adjusted for 'biologically plausible' interactions only.

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Step 1: Identify a full set of predictor variables - pitfalls



Over-fitting the data - too many predictors, not enough data/sample size.

Rule of thumb: one should have at least 10 data points for each estimate

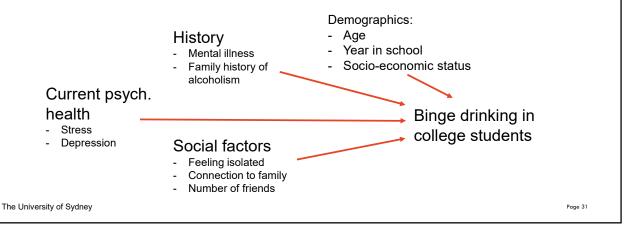
- An intercept needs an estimate
- Each numeric or binary predictor needs an estimate
- Each dummy variable needs an estimate, i.e. a categorical variable with 4 categories needs 3 estimates (one category will be the reference group)
- Interaction terms need estimates if an interaction term is included in the model the main effects need to also be included in order to be able to interpret the interaction estimates

If the goal is to create knowledge then we need our estimates to be as precise as possible – too little data will lead to large confidence intervals.

A large maximum model should include all potentially important predictors but it increases the chance of multi-collinearity, unstable estimates and finding spurious associations that are not important in the real world or are difficult to interpret. Consider a focused study design collecting high quality data on far fewer predictors versus administrative 'big' data not collected for research purposes.

Step 1: Identify a full set of predictor variables – other strategies

- Consider the causal structure of your data
- Consider drawing a causal diagram (Directed acyclic graph DAG, see appendix)
- Group variables into logical clusters (for large numbers of predictor variables you may consider working in clusters for model building)



Workflow: Steps in Model Building

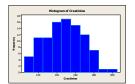
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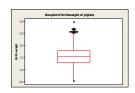
Step 2: Clean and check data

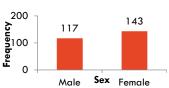
For each variable including the outcome: identify the data type (numeric/categorical) and use appropriate summary statistics and plotting to check the distribution:

- Numeric variable histogram/boxplot; mean, median, standard deviation, percentiles, etc.
- Categorical variable bar charts; frequency tables with count and percent
- For model building we want variables that:
 - are measured accurately, precisely + are reasonably complete (not too much missing data, e.g. no more than 10-15% missing observations)
 - have substantial variability (e.g. if 99% are male, than sex is not a good predictor)

Categorical variables: consider combining categories with small number of observations/ eliminate.







→ See our Research Essentials — Analysing your Data Workshop for further details
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Step 3: Pick a suitable type of model

Outcome variable:

Its data type indicates which types of models may be used

See our specific workshops for more information on different models, e.g.:

- Linear Models 1 (numeric outcome)
- Linear Models 2 (binary outcome or count data)
- Survival analysis (time-to-event data).

Does the Step 2 plot suggest that the outcome variable may need modification, e.g. a log-transformation (Linear Model - numeric outcome) or recategorization (GLM - categorical outcome)?

Workflow: Steps in Model Building so far

- 1. Identify the outcome variable and a full set of predictor variables to be considered
- 2. Clean and check data
- 3. Pick a suitable model
- 4. Pick predictors to fit using Exploratory Data Analysis (EDA)
 - 4.1 Assess relationships between each predictor and the outcome
 - 4.2 Assess the relationships among predictors and consider variable reduction

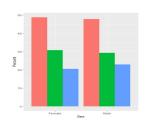
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Step 4: Pick predictors to fit using Exploratory Data Analysis (EDA) 1

4.1 Assess relationships between each predictor and the outcome to select, modify + understand predictors

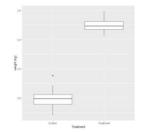
Plot the data in relation to the research question, e.g.

- plot the relationship of each predictor with the outcome
- plot multiple variables in one plot; plot variables over time; plot data for individuals

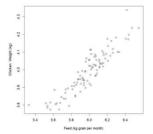


2 categorical variables - side-by-side bar charts

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1 categorical, 1 numeric variable - side-by-side boxplots



2 numeric variables
– xy scatter plot

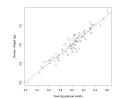
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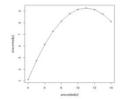
Step 4: Pick predictors to fit using Exploratory Data Analysis (EDA)

4.1 Assess relationships between each predictor and the outcome to select, modify + understand predictors

For numeric variables – assess the assumption of linearity – is the relationship between outcome and predictor a line, a curve or something else?

For practical reasons we assess the model assumption of linearity before model building.





Linear Model (a straight line): $y = b_0 + b_1x_1 + error$

Quadratic model (a curve): $y = b_0 + b_1x_1 + b_2x_1^2 + error$

Alternatively, avoid the assumption by categorising the numeric predictor, but this loses information and may introduce bias. However, sometimes we are interested in specific categories for interpretation, e.g. BMI – underweight/normal weight/ overweight/obese.

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Non-linear regression models



Add power terms to linear model with predictor x , e.g. x^2 or x^3 – this allows the regression line to follow a curve

- Complexity/ number of bends depends on the number of power terms
- Global influence influenced by the whole dataset
 - · May perform better with future data
 - Less sensitive to local disturbance and may miss features
 - · May be heavily influenced by values at the extreme ends
 - · Do not predict outside of data range
- avoid collinearity among new variables centre variables by subtracting the mean (mean of new variable = 0) to create orthogonal (uncorrelated) polynomials → limited to positive integer power terms

Functional form of continuous predictor's 'best fit' can be determined by statistical significance, but for strong subject matter reasons may choose polynomial anyway, particularly for small dataset and confounding predictor

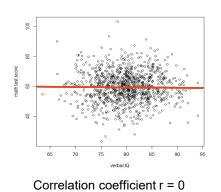
Fractional polynomials and piecewise functions/splines - even more flexibility in fit (and complexity!)

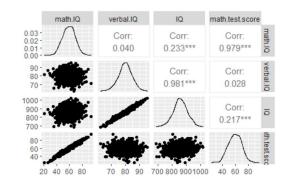
Step 4: Pick predictors to fit using Exploratory Data Analysis (EDA)

4.2 Assess the relationships among predictors and consider variable reduction

Numeric predictors: use xy scatter plot and conduct **pairwise correlation analysis**

'High' correlation is domain-specific, generally r>|0.7|, |0.8|or |0.9| but r<0.7 can be problematic too





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Correlation matrix

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Step 4: Pick predictors to fit using Exploratory Data Analysis (EDA)

4.2 Assess the relationships among predictors and consider variable reduction

High pairwise correlations – what to do?

- If few variables: select only one of the pair based on biological plausibility, fewer missing values, ease/reliability of measurement or lower univariate p value (may not fix problems arising from collinearity among linear combinations of predictors --> check Variance Inflation Factors (VIF) after analysis)
- If many (related?) predictors: explore their relationship/consider reducing the number of variables using multivariate techniques - see our Multivariable Analysis workshop
- Summarise the variables by creating an index/scale

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Step 4: Multivariate analysis - Principal component Analysis + Factor Analysis

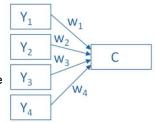


Principal component Analysis (PCA) and Factor Analysis (FA) are data reduction techniques to consolidate the information contained in a set of numeric predictor variables into a new set of fewer, uncorrelated variables. If used subsequently in a model one cannot statistically test individual predictors.

PCA:

Creates one or more index variables (components) from a larger set of variables by using linear combinations (basically a weighted average) of a set of variables.

Component coefficients from a subsequent model can be backtransformed into coefficients for the original predictors – these are more stable as multi-collinearity is avoided.



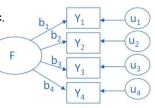
FA:

-Models the measurement of a latent variable which cannot be directly measured with a single variable, e.g. intelligence, statistical anxiety etc.

-For subsequent modelling, determining which original predictor is important is subjective based on high correlations/factor loadings.

See SIH Multivariate analysis – dimension reduction workshop.

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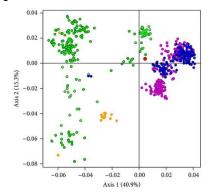
Step 4: Multivariate analysis - Correspondence analysis



- A form of exploratory data analysis (EDA) designed to analyse the relationships among a set of categorical predictor and outcome variables
- Produces a visual summary which is a scatter plot with factorial axes that reflect the most variability in the original predictor variables
- Allows identification of clusters of predictors that are closely associated, with clusters further from the intersection of the axes having stronger associations

Summary:

PCA/FA and correspondence analysis are complementary techniques to modelling and provide insight into relationships between groups of predictors and there association with the outcome



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Step 4: Create an index or scale



Combine a number of related predictor variables into a single index

- Subjectively, ideally based on prior research can have different weights for different contributing factors, e.g. an infection control index may be created by counting the number of hygiene practices performed and expressing this as a percentage of all practices. This could also be categorised into low/medium/high.
- Objectively, e.g. fan capacity, size and number of air inlets and building size may be
 used to calculate the number of air changes per hour which could also be expressed as
 proportion of recommended ventilation level
- When predictors are assumed to be reflective of an underlying, unmeasured characteristic (a latent variable) can combine into index or scale by summing or averaging predictors and use Cronbach's alpha statistic to evaluate internal consistency of the scale. Use correlation analysis to assess correlation between each item (variable) and the scale and pairs of items to identify any items that do not fit into the scale well.
 - See SIH workshop on Surveys' 2 for further information

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Step 4: Create an index or scale - Comorbidity



Definition:

Comorbidity is defined as the co-occurrence of one or more disorders in the same patient either at the same time or in some causal sequence and a common confounder

- Indices are calculated (weighted sum) from international ICD-10 diagnoses codes (+/- other data) from administrative data (e.g. admitted patients data)
- Indices are based on Elixhauser, the Charlson/Deyo, and the Charlson/Romano methods and well-established for risk adjustment and mortality prediction
- Calculation in R software: <u>comorbidity package –</u> Rdocumentation

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Charlson comorbidity index

Condition	Points in CCI		
Myocardial Infarction	1		
CHF	1		
Peripheral Vascular Disease	1		
Cerebrovascular Disease	1		
COPD	1		
Dementia	1		
Paralysis	1		
Diabetes	1		
Diabetes With Sequelae	2		
Chronic Renal Failure	2		
Various Cirrhodites	1		
Moderate-Severe Liver Disease	3		
Ulcers	1		
Rheumatitis	1		
AIDS	6		
Any Malignancy	2		
Metastatic Solid Tumor	6		

Step 2: Clean and check the data and Step 4: Pick predictors to fit using Exploratory Data Analysis (EDA) - R code/ resources



R code: EDA

- Introductory R and visualisation for EDA: R-essential-training-wrangling-and-visualizing-data
- Data management and summaries with R tidyverse: <u>Learning the R Tidyverse</u> (These two LinkedIn Learning course are free with your Sydney uni login details)

R correlation matrix example:

Create/simulate data
math.IQ <- rnorm(1000, 60, 10)
verbal.IQ <- rnorm(1000, 80, 5)
IQ <- 10*verbal.IQ + math.IQ
math.test.score <- math.IQ + rnorm(length(math.IQ),0,2)
my_data <- data.frame(math.IQ, verbal.IQ, IQ, math.test.score)

install Ggally package and run ggpairs on all numeric variables (in this example all four variables are numeric) install.packages("GGally") library(GGally) ggpairs(my_data)

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Step 4: Pick predictors to fit using Exploratory Data Analysis (EDA) - Summary

EDA for selection/modification of predictor variables for model building:

4.1 Assess relationships between each predictor and the outcome

- Plot relationships and consider excluding variables with low variability
- Assess assumption of linearity for numeric predictors

4.2 Assess the relationships among predictors and consider variable reduction

- Check for multi-collinearity and only select unrelated variables into model building
- Consider using univariable screening to reduce the number of variables for model building

Quick break, feel free to stretch your legs!

Any questions?





Workflow: Steps in Model Building

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- 10. Interpret and report the results

Step 5: Specify the selection criteria

How to decide which variables to keep in the model?

Selection criteria are formal 'Goodness of Fit' criteria and other statistical considerations

Other statistical considerations - retain variables that are:

- a primary predictor of interest
- a priori confounders for the primary predictor of interest
- Shown confounders for the primary predictor of interest (should not be an intervening variable – see appendix)
- A component of an interaction term included in the model (for interpretation)

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Step 5: Specify the selection criteria

Formal Goodness of Fit criteria – nested models

Nested models are based on the same set of observations (n) and the predictors in one model are a subset of predictors in the other model

Tests based on nested models to evaluate significance of a predictor:

- Partial F test (linear model)
- Wald test or likelihood ratio test (LRT) (other types of regression such as logistic, Poisson) – Wald test often most convenient, but LRT has best statistical properties and should be used if p value or standard error are questionable

Formal Goodness of Fit criteria- non-nested models

Information Criteria: $IC = -2 \log$ -likelihood + alpha*number of parameters

Akaike's Information Criteria (AIC): alpha = 2

Bayesian Information Criteria (BIC) alpha = log n (with some variation)

Step 5: Specify the selection criteria

AIC/BIC:

- Assess overall model so can be used to compare different models
- The smaller the IC, the better the model
- Can be used to compare nested and non-nested models
- Can be used to compare different regression models, e.g. linear vs Poisson
- Can't be used to compare models based on different sets of observations
- Can't be used to compare models with different likelihood computation, e.g. Cox semiparametric survival model versus Weibull parametric model
- BIC depends on n and it can be unclear what n to use for clustered data
- BIC has guidelines (see Table) and favours most parsimonious model

Absolute difference in BIC	Evidence for superiority of the better model
0 - <2	Weak
2- <6	Positive
6 - <10	Strong
=> 10	Very strong

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Step 5: Specify the selection criteria

Two additional approaches for linear regression models:

R squared - amount of variance explained by a univariable model

Adjusted R squared = amount of variance explained by a multi-variable model,
penalised for model complexity/number of predictors (larger is better)

- Avoids including predictors that explain a small amount of variance only
- Maximising R squared, minimises mean square error (MSE)

Mallow's Cp Statistic (special case of AIC):

$$Cp = Sum((Y-Y_hat)^2)/sigma^2) - n + 2k$$

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Step 6: Specifying the selection strategy

How to get from a full/maximal model (all predictors selected for model building) to the final model?

- →Choose a selection strategy to build a model
 - Manual options
 - Automated processes
 - Other considerations

Step 6: Specifying the selection processes - the options

All possible:

Examine all possible combinations of predictors.

Best subset:

Software identifies 'best' model of all possible based on criteria (e.g. a model with 2 predictors, largest adjusted R squared; a model with 3 predictors, largest adjusted R squared)

Forward selection

First a model with only the intercept is fitted and then each variables is added selectively based on a specified criterion, e.g. having the largest Wald test statistic provided it corresponds to p<0.05 (or other chosen significance level). The predictor with the largest Wald test statistic is added first and then the process is repeated and continues until no term meets the entry criterion.

Backward elimination

As for forward selection but the process is reversed and model building starts with the full/maximal model. Predictors are removed sequentially until none of the predictors remaining in the model has a Wald test statistic meeting the specified criterion.

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Step 6: Specifying the selection process – the options

Stepwise regression

A combination of forward selection and backward elimination.

Forward stepwise starts with forward selection but after the addition of each variable, the criterion for backward elimination is applied to each variable in the model to see if it should remain.

Backward stepwise starts with a full/maximal model and sequentially removes predictors but after the removal of each variable, all removed variables are checked to see if any of them would meet the forward selection criteria for inclusion.

So, what strategy to choose?



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Variable selection process - comparison

Selection strategy	Comment
All possible	Good for early exploratory work to find multiple good model candidates. Can compare nested and non-nested models.
Best subset	Researcher identifies when increasing the number of predictors brings little predictive improvement. Can compare nested and nonnested models.
Forward	Limited assessment of confounding.
Backwards	Statistical significance of terms is assessed after adjustment for potential confounders
Forward stepwise	Useful for large number of predictors/interaction terms
Backwards stepwise	Generally favoured over forward stepwise.

Different procedures often result in the same final model with the exception of small data sets + analyses with large numbers of predictors.

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Step 6: Specifying the selection strategy

Automated approaches:

Be cautious! While convenient, they should be considered exploratory methods rather than definite approaches.

- some journals will no longer accept automated selection
- They yield R squared values that are too high
- Based on Hypotheses tests p values too small and not adjusted for multiple testing → see LM3 Workshop
- Ignore multi-collinearity important to do your EDA/ correlation analysis!! Use VIF after model building to check.
- DO NOT incorporate other statistical criteria:

Select 'design' variables/predictor a priori, e.g.

- Predictor variable of interest for the research question
- Randomisation blocking factor in an experiment
- A priori confounder of the predictor variable of interest

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Model building strategy styles (adapted from Keith McCormick)

	Hierarchical	Simultaneous	Stepwise
Style	most academic		least academic
Theory	Strong theory	Limited theory	no theory
Analyst role in model building	choose variables, and the order of entry	choose a list of variables believed to be important	Variables are chosen through automated process
Possible use	Designed experiments	Exploratory	Data mining type approach

Source: LinkedIn Learning video: Three regression strategies, Keith McCormick.

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Model Building Strategy - Collett



Collett's general strategy for model selection:

- 1. Fit univariate models for each predictor variable of interest. Compare the 2loglikelihood values to the null model (using chi square statistic, or AIC, BIC)
- 2. Significant variables from step 1 are fitted in a single model and compared to 'leave one out' models
- 3. Variables omitted at step 1 are then added to the best model from step 2 and compared
- 4. A final check to ensure no term in the model can be omitted without increasing -2LL significantly and no new term added without reducing -2LL significantly.

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Pitfalls with automated selection processes:

Avoids researcher thinking about their data and taking responsibility for their analysis!

"Start simple, get complex"

"Every model you run tells you a story. Stop and listen to it."

- Avoid Overfitting (have at least 10 (better 20!) observations per parameter in the model keep in mind dummy coded categorical variables with > 2 categories e.g. a predictor with 5 categories requires 4 parameters to be estimated)
- For interpretability of parameters keep the main effects of both variables that make up a significant
 2-way interaction term in the model (irrespective of their p values)
- Analysis will only be based on observations for which all variables are not missing (with many missing observations the final data set analysed may be a small subset) – do EDA!

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Workflow: Steps in Model Building

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Step 7: Fit the model/conduct the analysis

- An iterative process
- Build and evaluate models
- Gain insights into the complex relationships among the variables → allows for more refined, biologically reasonable models to be build
- Incorporate expert knowledge of the system being studied along with the results of the analyses

Variables in the Equation									
								95.0% Cl for Exp(B)	
		В	SE	Wald	df	Sig.	Exp(B)	Lower	Upper
Step 1	Age at hospital admission	.066	.006	118.799	1	.000	1.068	1.056	1.081
Step 2	Age at hospital admission	.059	.006	92.407	1	.000	1.060	1.048	1.073
	Congestive heart complications	861	.142	36,570	1.	.000	.423	.320	.559
Step 3	Age at hospital admission	.059	.006	92.280	1	.000	1.061	1.048	1.074
	Cardiogenic shock	883	.261	11.414	- 1	.001	.413	.248	.690
	Congestive heart complications	820	.143	32.745	1.	.000	.440	.332	.583
Step 4	Age at hospital admission	.060	.006	90.699	1	.000	1.061	1.048	1.074
	hr	.009	.003	10.649	-1	.001	1.009	1.004	1.015
	Cardiogenic shock	959	.261	13.464	1	.000	.383	.230	.640
	Congestive heart	707	.147	23.109	4	.000	.493	.370	.658

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Workflow: Steps in Model Building

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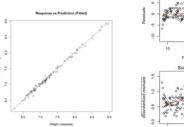
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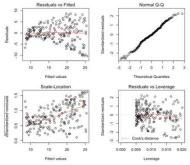
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Step 8: Check the model assumptions

Use "diagnostics" to assess the validity of the model, e.g.

- Evaluate normality of residuals in LM
- Check HR/OR proportionality assumptions
- Check for influential values
- Check assumption of independent predictors using Variance Inflation
 Factors (VIF) for correlation among predictors after analysis:
 VIF >4 moderate multi-collinearity
 VIF >10 strong multi-collinearity





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Workflow: Steps in Model Building

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Step 9: Check model fit

Evaluate the *reliability* of the model – how well will the model predict observations in future samples?

Different approaches, e.g.:

- Split-sample analysis
- Cross-validation
- Leave-one-out analysis
- Bootstrap



- Goodness-of-fit test, e.g. Hosmer-Lemeshow test

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Workflow: Steps in Model Building

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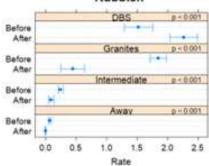
Step 10: Interpret and report the results

- Present point estimates - the coefficients (including the intercept)

 Present the measure of uncertainty – their standard errors and/or their confidence interval.

Rubbish

Depending on target audience, non-numerical presentation of study results may be preferable.



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Step 10: Interpret and report the results

Predictors eliminated from a model

- You may also want to discuss the potential effects of predictors not included in the model (alpha = 0.05 is an arbitrary cut-off and a predictor with p = 0.06 still shows evidence of a (weak) association
- Observational studies: often one Table presents univariate results and one Table shows the final
 multivariable model (if there are a lot and/or journal does not want non-significant univariate
 results in the manuscript theunivariate Table(s) can be presented in an appendix/online
 supplementary file
- You can discuss the unconditional associations
- For backward elimination the coefficients of the predictor at the last step before it was eliminated can be reported
- Eliminated predictors may be forced back into the final model one-by-one and the coefficient used to estimate its effect

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Step 10: Interpret and report the results



Assessing the impact of continuous variables:

- Continuous variables are measured on different scales, so a 'one unit change' could be small or large.
- It is difficult to compare the impact of different continuous variables
- → use standardised coefficients (multiply by ratio of SD of predictor to SD of outcome)
- → compute and present a range of predicted effects as a continuous predictor changes over its IQR

Variable	Estimate	Basis	Estimated effect change	Effect
Held-back	0.666	dichotomous	0 - 1	0.666
Herd size	0.669	IQR	0.55-1.60	0.702
experience	0.023	IQR	8.5 – 26.0	0.401

Modelling log-prevalence of respiratory disease in pigs

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Step 10: Interpret and report the results



Control of confounding at the analysis stage:

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Use change in measure of association as an indication of confounding

Calculate % change between estimates for statistically significant predictor of interest with confounder in the model versus without confounder in the model

Include confounder as covariate in regression analysis; assess confounding effect by examining the % change in regression parameter estimate in a model with and without a (potential) confounder.

Confounder are often included a *priori*, irrespective of p-value or the effect of its inclusion/exclusion on change in other parameters.

e.g. crude log odds versus adjusted log odds – specify "substantial difference" a priori, e.g. >20-30% change in log odds)

Step 10: Interpret and report the results



Scale of the results

In Linear Models transformation of the outcome is done to meet the model's underlying assumptions.

For interpretation it is desirable to present results at a different scale than what was used in analysis.

- back-transformations after analysis of log-transformed data following linear regression
 obtain predicted outcome and confidence interval in transformed scale, then back-transform and illustrate graphically
- Converting results from the logit scale (log odds) to the predicted probability scale after logistic regression and plot for both categories of the outcome

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Questions?



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Linear Model Regression example



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Step 1: Identify the outcome variable and a full set of predictor variables to be considered

Diamonds data (from R's ggplot package) – see further details on this example here: 24 Model building | R for Data Science (had.co.nz)

Outcome: Price (\$ - continuous)

Predictors:

- Cut (5 categories: fair/good/very good/ premium/ideal)
- Colour (7 colour categories)
- Clarity (8 categories)
- Carat (diamond weight, numeric) potential confounder
- No interactions considered for this model.

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Step 2 and 3: Clean + check the data and pick a suitable model

Step 2: Clean + check the data - not shown; no data entry errors/typos; good numbers in each category; no missing data; numeric data price and carat within the expected ranges, both right skewed.

Step 3: Pick a suitable model

Research question: Is quality a good predictor of diamond price? Hypothesis: Low quality diamonds (poor cut, bad colour, inferior clarity) have higher prices.

The data type of the outcome variable Price in \$'s is numeric and we are using a Linear Model.

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Step 4: Pick predictors to fit using Exploratory Data Analysis (EDA) Outcome is numeric, predictors are categorical → use side-by-side boxplots for EDA: The University of Sydney Step 4: Pick predictors to fit using Exploratory Data Analysis (EDA) Cut Cut Cut Fage 79

Step 4: Pick predictors to fit using Exploratory Data Analysis (EDA) - Test linearity of numeric predictor carat (EDA = xy scatter plot) Carat Both price and Carat have a positively skewed distribution. The plot of the original variables shows a fanning pattern (that we would also see if we examined

residuals from a model with the raw data). Log transformation of both variables

creates a linear relationship.

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Step 5: Specify the criteria

Formal Goodness of Fit Criteria:

- AIC/Chi-squared statistic
- p < 0.05

Other statistical considerations - variables believed to be important, or that we need to control for:

 Carat considered a confounder – carat/weight is the biggest determinator of price but low quality diamonds tend to be larger.

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Step 6: Specify the strategy

Here I have a very large sample size and only 4 predictors with a good prior theoretical understanding (I believe all 4 variables are determinants of price).

Because of this I chose a backwards elimination strategy.

Start with a full model with all 4 predictors. Remove predictors sequentially until none remain in the model that have a Wald test statistic corresponding to $p \ge 0.05$.

Step 7: Fit the model

Fit a model with all 4 predictors.

Check chi-squared p values – all p<0.001 - significant at p<0.05.

Compare the model to the null model (no predictors) – F statistic associated p value p<0.001 - significant at p<0.05.

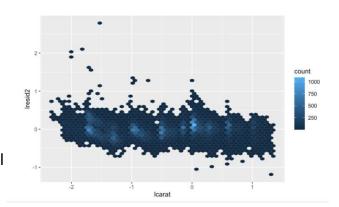
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Step 8: Check the model assumptions

Check model assumptions via diagnostics: residual analysis

- Assumption of normality met.
- No unexplained structure, nonlinearity or non-constant variance
- No outliers
- Check Cook's distance for influential outliers



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Step 9: Check model goodness-of-fit

Assess fit and predictive ability:

- Plot and evaluate observed versus predicted values of price
- Adjusted R^A2 statistic 98% variation in price explained by the model (this is very high and may point to an over-fitted model; many research domains get much lower values for this statistic, e.g. 20% in ecology is great!)

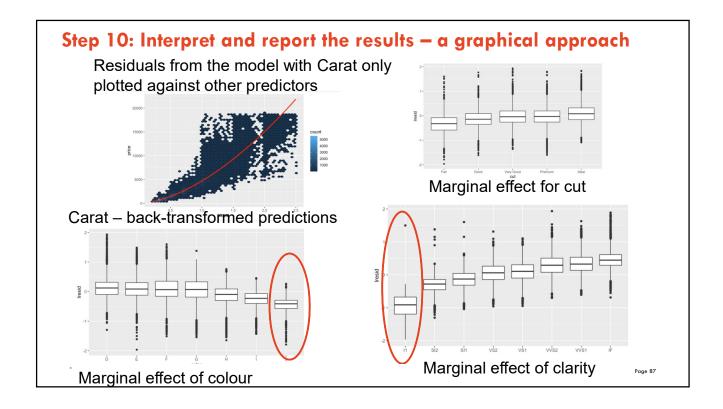
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Step 10: Interpret and report the results

```
Estimate Std. Error t value
                                  Pr(>|+|)
lcarat 1.886239 0.001124 1677.809 < 2e-16 ***
color.L -0.633998 0.002910 -217.872 < 2e-16 ***
color.Q -0.137580 0.002676 -51.409 < 2e-16 ***
color.C -0.022072 0.002503 -8.819 < 2e-16 ***
color^5 -0.002828 0.002169 -1.304 0.192
color^6 0.003533 0.001971 1.793 0.073.
cut.L 0.173866 0.003386 51.349 < 2e-16 ***
cut.Q -0.050346 0.002980 -16.897 < 2e-16 ***
cut.C 0.019129 0.002583 7.407 1.31e-13 ***
cut^4 -0.002410 0.002066 -1.166 0.243
clarity.L 1.308155 0.005179 252.598 < 2e-16 ***
clarity.Q -0.334090 0.004839 -69.047 < 2e-16 ***
clarity.C 0.178423 0.004140 43.093 < 2e-16 ***
clarity^4 -0.088059 0.003298 -26.697 < 2e-16 ***
clarity^5 0.035885 0.002680 13.389 < 2e-16 ***
clarity^6 -0.001371 0.002327 -0.589 0.556
clarity^7 0.048221 0.002051 23.512 < 2e-16 ***
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```

At a minimum report the point estimate and a measure of its uncertainty, i.e. its standard error or use estimate and standard error to calculate a 95% confidence interval.



Model Building: R software resources



Linear model building example in R and other relevant resources for R: https://r4ds.had.co.nz/model-building.html

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Questions?



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Upcoming SIH statistical trainings

Check out the SIH training calendar or sign up to the mailing list for details on all upcoming trainings: https://www.sydney.edu.au/research/facilities/sydney-informatics-hub/workshops-and-training/training-calendar.html

- 9th November: Research Essentials, Meta-analysis, Survival analysis
- 17th November: Hacky Hour Sydney Hacky Hour The University of Sydney
- 22nd November: Experimental Design, Power + sample size, Multivariate analysis
- 15th December: Hacky Hour Sydney Hacky Hour The University of Sydney

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Further Assistance at Sydney University



SIH

Workshops

This is just one workshop from a modular training programme made up of 1.5 hour workshops, each focusing on a single statistical method offered by Statistical Consulting within the Sydney Informatics Hub. Statistical Workflows giving practical step-by-step instructions applicable in any software are used and include experimental design, exploratory analysis, modelling, assumption testing, model interpretation and presentation of results. They are integrated into Training Pathways (insert link) to give a holistic understanding of data analysis from a statistical perspective. Researchers are also encouraged to design a custom programme tailored to their research needs. Look for the statistics workshops (and other SIH workshops) on our training page https://www.sydney.edu.au/research/facilities/sydney-informatics-hub/workshops-and-training.html#stats.

- Training: Sign up to our mailing list to be notified of upcoming training:
 mailman.svdney.edu.gu/mailman/listinfo/computing training
- Hacky Hour www.sydney.edu.au/research/facilities/sydney-informatics-hub/workshops-and-training/hacky-hour.html
 OR Google "Sydney Hacky Hour"
- 1 on 1 Consults can be requested on our website www.sydney.edu.au/research/facilities/sydney-informatics-hub.html OR Google "Sydney Informatics Hub"

OTHER

- Open Learning Environment (OLE) courses
- Linkedin Learning: https://linkedin.com/learning/
 - SPSS https://www.linkedin.com/learning/machine-learning-ai-foundations-linear-regression/welcome?u=2196204

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We recommend our Experimental Design and Sample Size Workshops

Experimental Design Workshop

- Far too many researchers think they know all they need to in this area. We commonly see
 designs that could be substantially improved for stronger causal inference and improved
 results which leads to publication in higher impact journals (amongst other benefits).
- Even if you have already collected your data it is well worth attending since it may improve your write up and analysis e.g. we had a client who didn't realise they had a very strong Before/After Control/Impact (BACI) design.

Sample and Power Workshop

- Shows the steps and decisions researchers need to make when designing an experiments to ensure sufficient sample e.g. Power, minimum required to fit the necessary model, etc.
- Also how much Power the study has i.e. does it have sufficient power to detect the effects you expect to see, or is your study a complete waste of time and resources.

A reminder about Acknowledging SIH



All University of Sydney resources are available to Sydney researchers **free of charge**. The use of the SIH services including the Artemis HPC and associated support and training warrants acknowledgement in any publications, conference proceedings or posters describing work facilitated by these services.

The continued acknowledgment of the use of SIH facilities ensures the sustainability of our services.

Suggested wording:

General acknowledgement:

"The authors acknowledge the technical assistance provided by the Sydney Informatics Hub, a Core Research Facility of the University of Sydney."

Acknowledging specific staff:

"The authors acknowledge the technical assistance of (name of staff) of the Sydney Informatics Hub, a Core Research Facility of the University of Sydney."

For further information about acknowledging the Sydney Informatics Hub, please contact us at sih.info@sydney.edu.au.

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We value your feedback



We want to hear about you and whether this workshop has helped you in your research. What worked and what didn't work.

We actively use the feedback to improve our workshops.

Completing this survey really does help us and we would appreciate your help! It only takes a few minutes to complete (promise!)

Here is the link to the survey!

https://redcap.sydney.edu.au/surveys/?s=FJ33MYNCRR&training=50



References used when building this Workshop

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Appendix

DAG - a graphical aid to understand multivariable systems and relationships between variables



What is a DAG?

- DAG (Directed Acyclic Graph) = causal diagram = modified path model
- Start with a plausible (biological) causal structure and translate it into a graph with hypothesised and known relationships among variables
- Lines represent:
 - Arrow (directed edge) = (assumed) causal relationship
 - No arrow = no causal relationship

Example study aim: Identify factors of causal importance to pneumonia (lung disease)

Objective: Investigate the association of Strep infection and the occurrence of lung disease. Researchers also measured sero-conversion for COVID-19.

Streptococcus pneumoniae Infection - Strep

Pneumonia/lung disease - Disease

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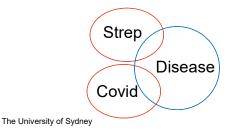
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Relationship: Exposure-independent predictor variable

Causal model (DAG)



Statistical model (Venn diagram)



The two predictor circles do not overlap – they are statistically independent.

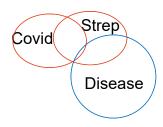
Both overlap with the outcome indicating their significant statistical associations with Disease. A patient could have one infection, both infections or none.

Relationship: A simple antecedent predictor variable

Causal model (DAG)

Covid --- Strep --- Disease

Statistical model (Venn diagram)



There is weak overlap of Covid with the outcome but statistical association favour direct causes over indirect causes, so strength of association and significance of Covid may be low. The association of Strep and Disease would not change when the model is adjusted for Covid. Covid occurs before Strep infection making patients more susceptible – Covid may be very important for disease control!

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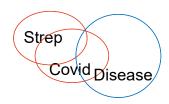
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Relationship: An explanatory antecedent variable - complete confounding

Causal model (DAG)



Statistical model (Venn diagram)



The Strep circle overlaps with the outcome, as they are statistically related until Covid is added to the model. Then the association becomes non-significant as all of the previous crude association is covered by the Covid-Disease association.

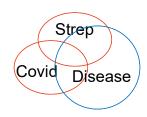
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Relationship: an explanatory antecedent variable - partial confounding

Causal model (DAG)



Statistical model (Venn diagram)



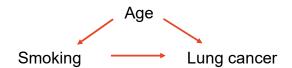
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The Strep circle overlaps with the outcome. The association remains significant when Covid is added to the model but some of the previous association is now covered by the Covid-Disease association.

The Strep-Disease association is not as strong when Covid confounding is controlled but the model with both predictors explains more variation in Disease than just Strep.

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More on confounding: a classic example



Age confounds the relationship of smoking and lung cancer – smoking may be more prevalent among older people and older people are more likely to get lung cancer irrespective of smoking.

Examples of common confounders:

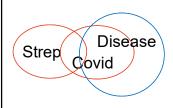
Age, Sex, Socio-economic status, Comorbidity, previous experience, etc.

Relationships: an intervening predictor variable

Causal model (DAG)



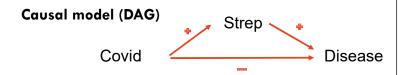
Statistical model (Venn diagram)



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The Strep circle might or might not overlap with the outcome. However, any association of Strep with Disease disappears when Covid is added to the model. The effect of Strep on Disease is mediated by Covid. Adding Covid to the model would lead us to believe that Strep is not associated with Disease (and hence we may wrongly conclude that Strep is not a cause of Disease). Intervening variables should be identified and not be used/controlled when estimating the causal effect of an exposure → consider Structural equation modelling, mediation analysis instead if interested in the mediator.

Relationship: a distorter predictor variable, can cause association reversal - one relationship represents prevention (-ve) rather than causal effect



Strep is a cause of Disease. Having Covid prevents getting Disease. Covid is positively correlated with Strep.

Causal model (DAG)



Strep and Covid are both causes of Disease. Having Covid prevents Strep infection.

In either case – need to control for the distorter variable Covid

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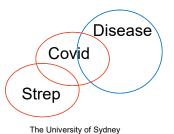
Relationship: a suppressing predictor variable

Causal model (DAG)

Hospital contact

Strep Covid Strep and the suppressor Covid are both members of the same global variable 'Hospital contact' (a proxy variable for exposure to infectious agents)

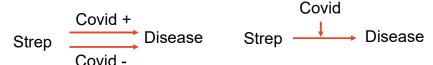
Statistical model



The variable 'hospital contact' has no or only weak unconditional association with the outcome. Once Covid is controlled in the analysis, the Strep circle overlaps with the outcome indicating an association of 'hospital contact' with Disease. By controlling the non-causal component of the global variable we reveal and strengthen the suppressed association of the remaining factor with the outcome. The global variable should be refined to exclude Covid. Suppression of the outcome can also occur, e.g. if the disease is not well defined (no association with lung disease but a strong association with a specific type of lung disease).

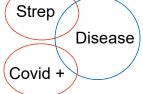
Relationship: a moderator variable - statistical interaction

Causal model (DAG)



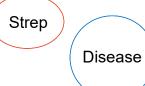
Disease





The effect of Strep is present when Covid is present (Covid +)

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The effect of Strep is absent when Covid is absent (Covid -)

The Strep circle overlaps with Disease only when Covid is present. No disease occurs unless both predictors are present. Interaction has large implications for disease control. Moderators may or may not be confounders.

Summary of effects of extraneous variables

Covid is a(n) variable	Likely effect on Strep coefficient when adding Covid	Comments
Exposure independent	No change	Covid explains some of the Disease incidence, so the residual variance is smaller and significance of Strep increases.
Simple antecedent	No change	No effect on the analysis by Covid, but Covid might be important to know about from a prevention perspective, e.g. if easier to address than Strep.
Explanatory antecedent (complete confounding)	Becomes 0	Control of Covid will remove any Strep association with Disease. R squared should increase as residual variance decreases.
Explanatory antecedent (incomplete confounding)	\	Controlling Covid will impact on significance of Strep depending on the strength of Covid effect on Strep and disease. R squared should increase.
Intervening	\	Because Covid is more closely related with Disease it probably has a stronger association and explains more variability. Strep coefficient is reduced in size and significance. If all effect passes through intervenor it will remove Strep effect on Disease.
Distorter	≥ ≥	Essentially same impact as explanatory antecedent except the Strep effect is increased or in opposite direction to the crude association.
Suppresor	<i>></i>	As the global variable containing Strep is refined, it will now have a stronger relationship with Disease and probably explain more variation.
Moderator	N/A	With interaction the effect of one variable depends on the level of the other variable, hence separate estimates of effects are required.

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RCT DAG - what is an 'instrumental' variable?

Example: A randomised Controlled Trial (RCT) experiment

Vaccination Exposure to Covid infection

Treatment:

Control group – not vaccinated Treatment group – vaccinated

Vaccination is an 'Instrumental variable', it has direct causal effect on exposure, is unrelated to the outcome and shares no common cause with the outcome