

```

.i 4
.o 1
.ilb a b c d
.ob F
.p 7
00-0 1
0-11 1
1-01 1
0101 1
1111 -
100- 1
-01- 1
.e

```

$$F = a'b'd' + a'cd + ac'd + a'bc'd + ab'c' + b'c$$

Don't care: $abcd$

$a'b'd'$: m_0, m_2

$a'cd$: m_3, m_7

$ac'd$: m_9, m_{13}

$a'bc'd$: m_5

$ab'c'$: m_8, m_9

$b'c$: m_2, m_3, m_{10}, m_{11}

$abcd$: m_{15}

$$F = \sum m(0, 2, 3, 5, 7, 8, 9, 10, 11, 13) + d(15)$$

Group	Minterm	4-literal term	Minterms	3-literal term	Minterms	2-literal term
0	m ₀	0000	m ₀ , m ₂	00-0	m ₀ , m ₂ , m ₈ , m ₁₀	-0-0
			m ₀ , m ₈	-000		
1	m ₂	0010	m ₂ , m ₃	001-	m ₂ , m ₃ , m ₁₀ , m ₁₁	-01-
			m ₂ , m ₁₀	-010		
	m ₈	1000	m ₈ , m ₉	100-	m ₈ , m ₉ , m ₁₀ , m ₁₁	10--
			m ₈ , m ₁₀	10-0		
2	m ₃	0011	m ₃ , m ₇	0-11	m ₃ , m ₇ , m ₁₁ , m ₁₅	--11
			m ₃ , m ₁₁	-011		
	m ₅	0101	m ₅ , m ₇	01-1	m ₅ , m ₇ , m ₁₃ , m ₁₅	-1-1
			m ₅ , m ₁₃	-101		
	m ₉	1001	m ₉ , m ₁₁	10-1	m ₉ , m ₁₁ , m ₁₃ , m ₁₅	1--1
			m ₉ , m ₁₃	1-01		
	m ₁₀	1010	m ₁₀ , m ₁₁	101-		
3	m ₇	0111	m ₇ , m ₁₅	-111		
	m ₁₁	1011	m ₁₁ , m ₁₅	1-11		
	m ₁₃	1101	m ₁₃ , m ₁₅	11-1		
4	m ₁₅	1111				

灰底字表示 prime implicant (PI)

Symbol	Notation	Product term	m ₀	m ₂	m ₃	m ₅	m ₇	m ₈	m ₉	m ₁₀	m ₁₁	m ₁₃
U	-0-0	b'd'	✓	✓				✓		✓		
V	-01-	b'c		✓	✓					✓	✓	
W	10--	ab'						✓	✓	✓	✓	
X	--11	cd			✓		✓				✓	
Y	-1-1	bd				✓	✓					✓
Z	1--1	ad							✓		✓	✓

Essential prime implicant (EPI): b'd', bd (\because m₀, m₅ is covered by only one PI)

Symbol	Notation	Product term	m ₃	m ₉	m ₁₁
V	-01-	b'c	✓		✓
W	10--	ab'		✓	✓
X	--11	cd	✓		✓
Z	1--1	ad		✓	✓

$$\begin{aligned}
 & (V + X) (W + Z) (V + W + X + Z) \\
 &= (VW + VZ + WX + XZ) (V + W + X + Z) \\
 &= VW + VWX + VWZ + VZ + VXZ + WX + WXZ + XZ
 \end{aligned}$$

\therefore VW, VZ, WX, XZ are feasible solutions (i.e., minimum number of product terms)

$$F = b'd' + bd + b'c + ab'$$

$$F = b'd' + bd + b'c + ad$$

$$F = b'd' + bd + ab' + cd$$

$$F = b'd' + bd + cd + ad$$

Output one of the above 4 functions to a PLA file.

Take $F = b'd' + bd + b'c + ab'$ as an example.

```

.i 4
.o 1
.ilb a b c d
.ob f
.p 4
-0-0 1
-1-1 1
-01- 1
10-- 1
.e

```