Proving $\frac{n}{0}$ is not ∞

The inverse of division is multiplication, so:

$$\frac{6}{2} = 3$$

$$3 * 2 = 6$$

So if we pretend for a moment that $\frac{n}{0} = \infty$, then the following is true (where n is any number):

$$\frac{n}{0} = \infty$$

$$\infty * 0 = n$$

However, a fundemental rule in multiplication is that anything times 0 is 0 (as you have 0 groups of n), so $\infty * 0 \neq n$, thus proving that anything divided by 0 is not infinity.

Proving $\frac{0}{0}$ is undefined Let $\alpha=1*0$ and $\beta=2*0$. As anything times 0 is 0, $\alpha=\beta$. Now let's set up the following equation:

$$\alpha = \beta$$

Expanded, this would be:

$$1*0 = 2*0$$

So far so good. Now let's try dividing 0 on both sides:

$$\frac{1*0}{0} = \frac{2*0}{0}$$

If we pretend for a moment that $\frac{0}{0}$ is defined, then the following occurs:

$$\frac{1*\emptyset}{\emptyset} = \frac{2*\emptyset}{\emptyset}$$

Leaving:

$$1 = 2$$

For obvious reasons this is false, but just to prove it is false, if 1 = 2, then the following can be concluded:

$$1+1=1$$

$$1+1+(-1)=1+(-1)$$

$$1+0=0$$

$$1=0$$