



Predictive routing and multi-objective fleet sizing for shared mobility-on-demand

Javier Alonso-Mora

Autonomous Multi-Robots Lab
Cognitive Robotics
Delft University of Technology



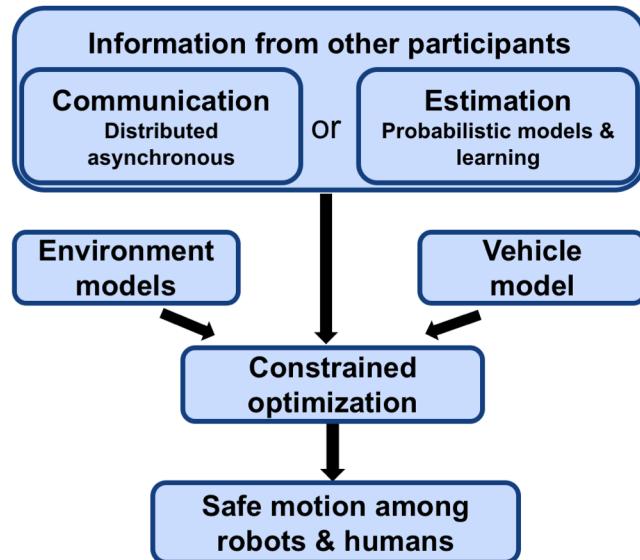
AUTONOMOUS
MULTI-ROBOTS LAB





Autonomous cars will
make transport
reliable, safe, efficient,
comfortable and clean

Motion planning for autonomous vehicles



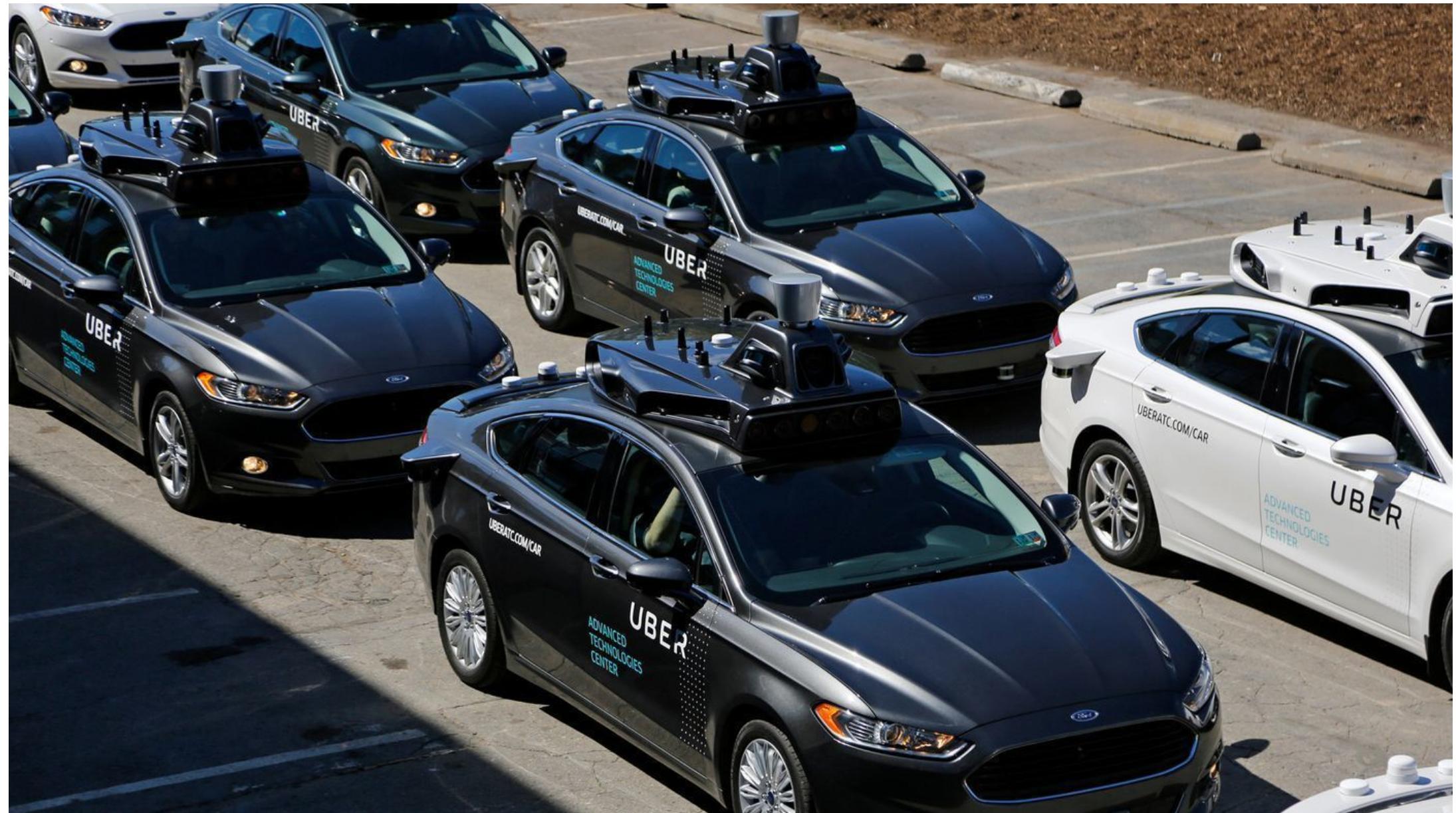
W. Schwarting et al., "Safe Nonlinear Trajectory Generation for Parallel Autonomy With a Dynamic Vehicle Model", T-ITS 2017

B. Zhou et al., "Joint Multi-Policy Behavior Estimation and Receding-Horizon Trajectory Planning for Automated Urban Driving", ICRA 2018

L. Ferranti et al., "SafeVRU: A Research Platform for the Interaction of Self-Driving Vehicles with Vulnerable Road Users", IV 2019



Autonomous cars will
solve all our problems!
Reliable, safe, efficient,
comfortable and clean



A photograph showing a fleet of Uber self-driving cars parked in a parking lot. The cars are dark-colored sedans with "UBER" and "ADVANCED TECHNOLOGIES CENTER" branding on the side doors. Each car has a large, black, rectangular sensor array mounted on its roof. In the center of the image, there is a large, solid black rectangular overlay containing the text "+40 %".

+40 %

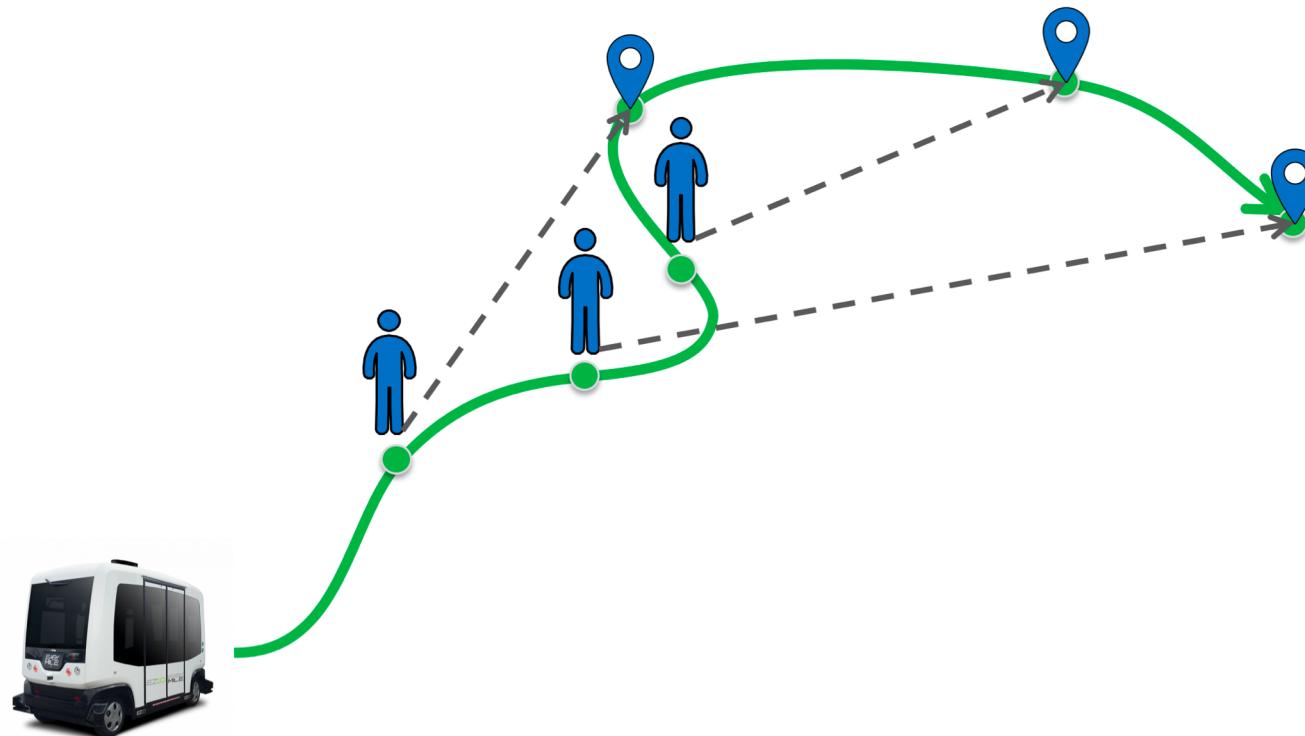


Ridesharing

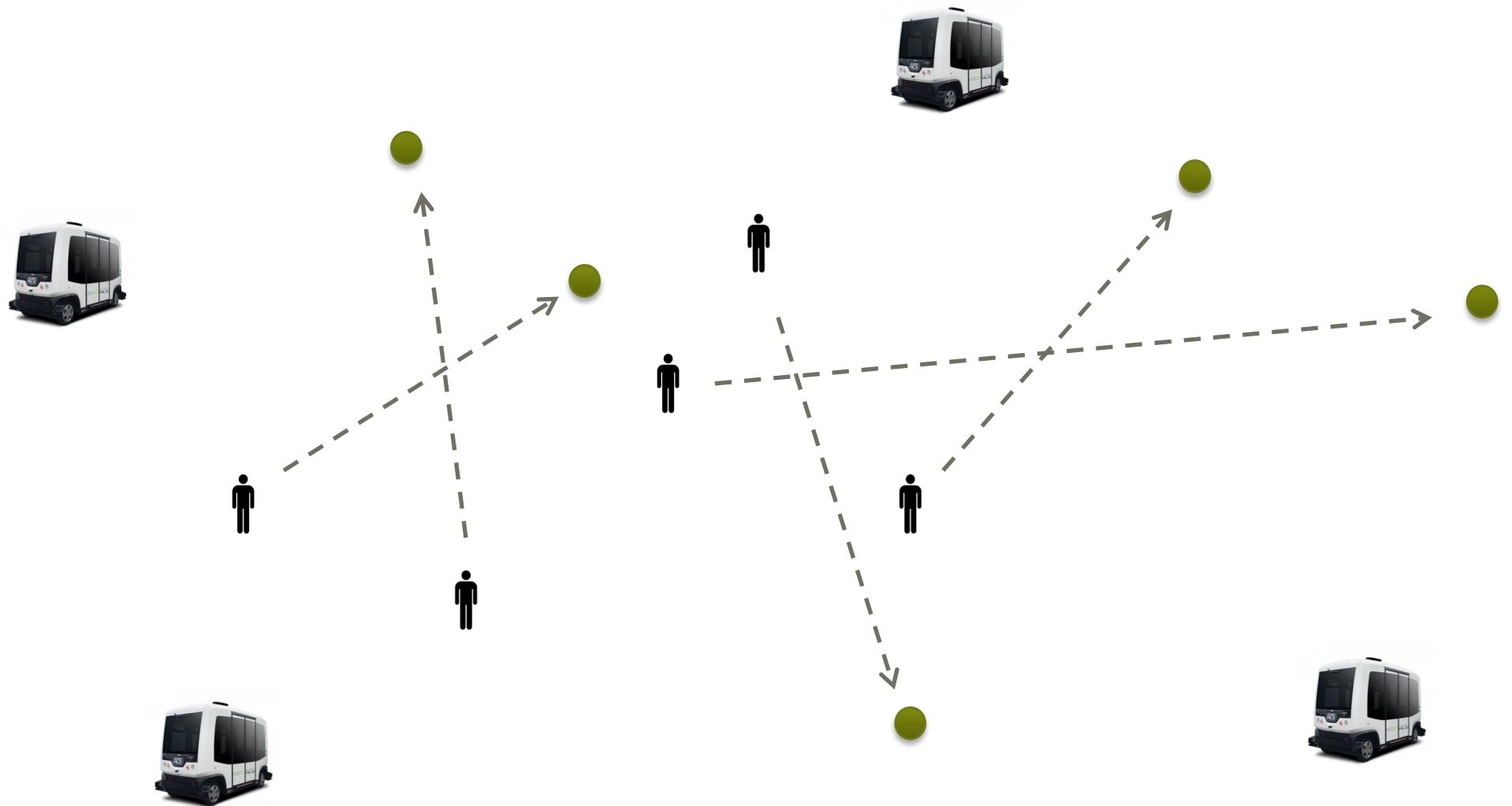
Ride sharing/pooling

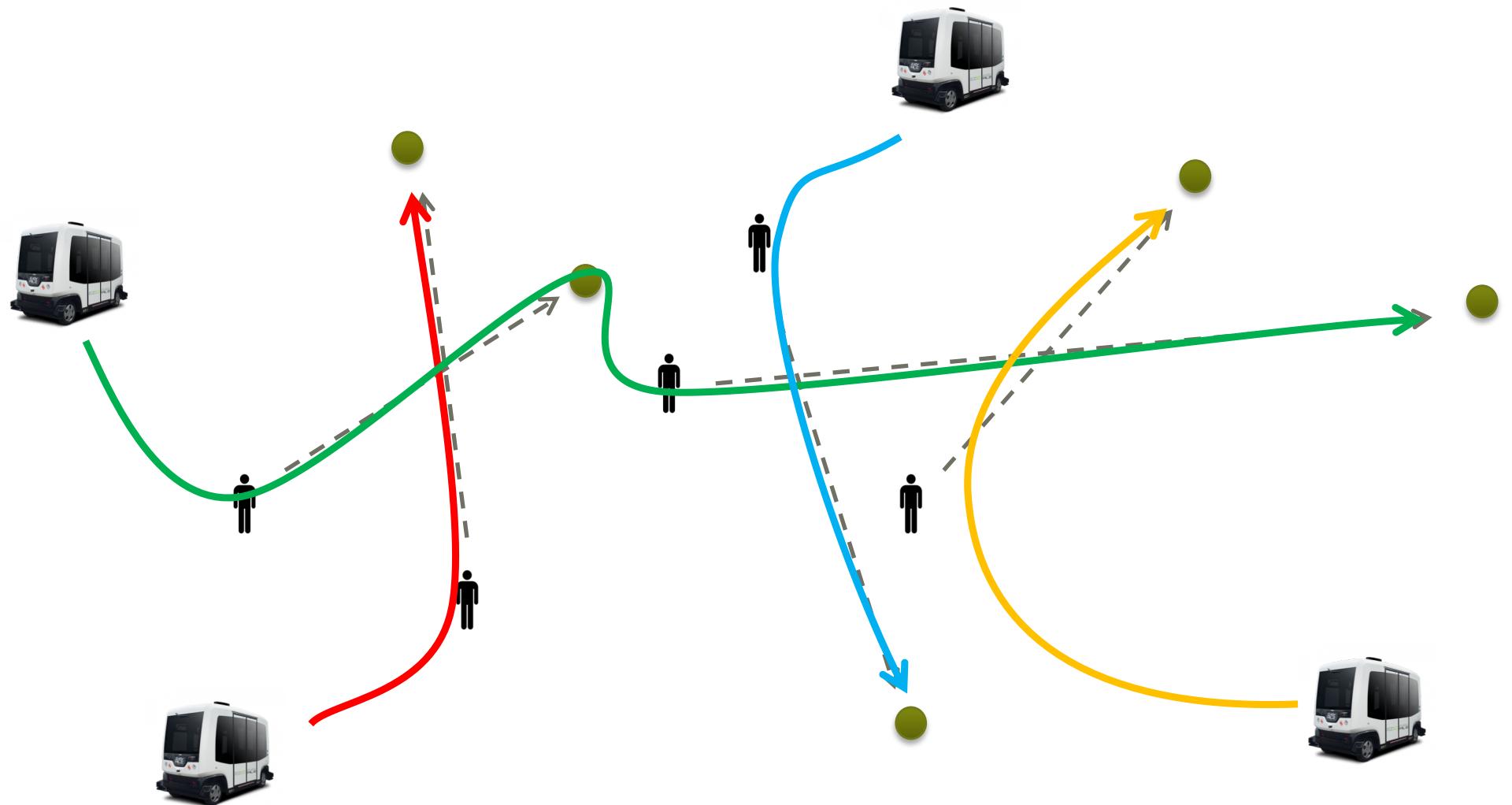
Instead of one passenger per vehicle, we can have **shared rides**

- Several passengers in the same vehicle
- Higher efficiency
- Less cars on the roads



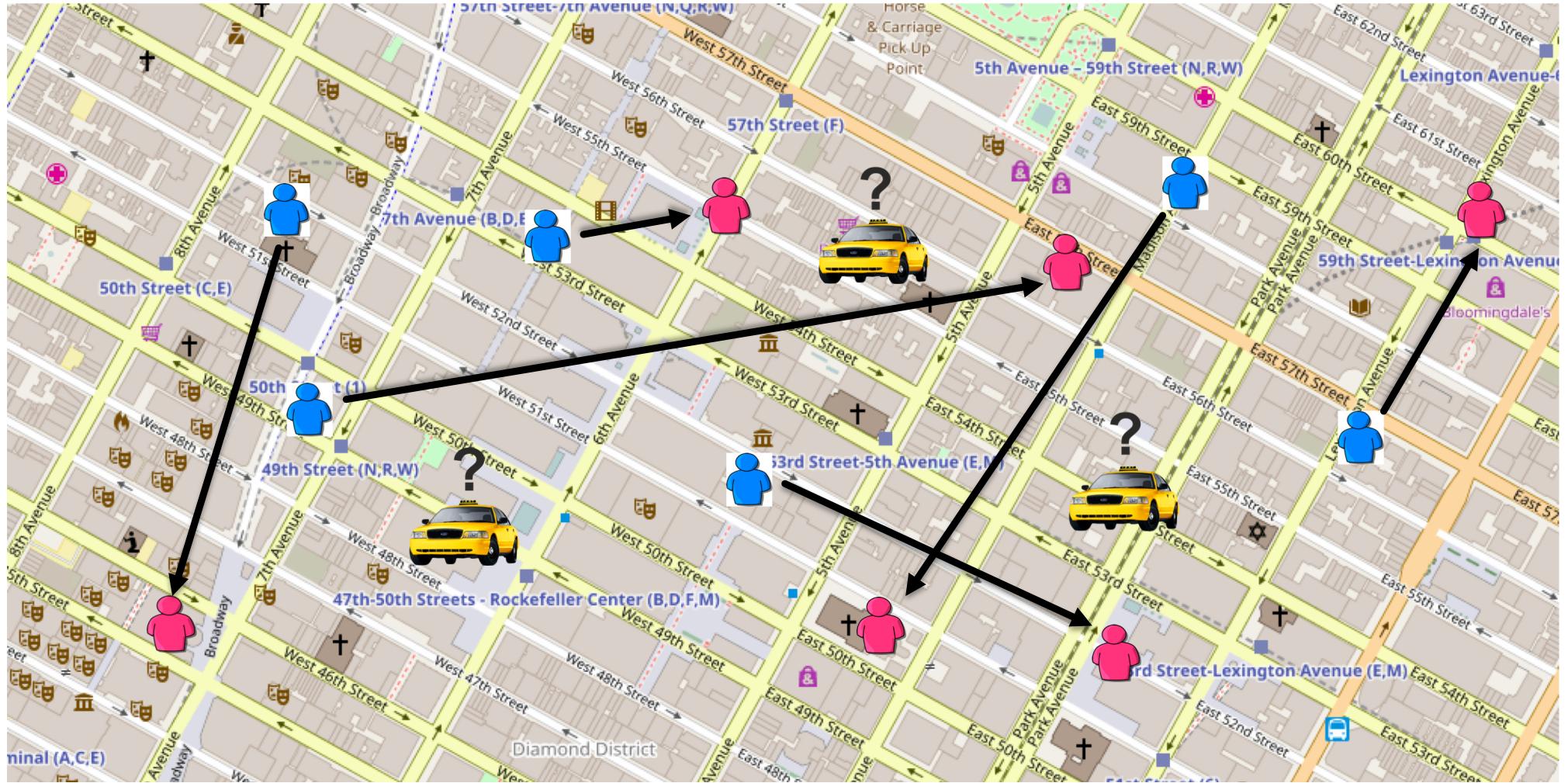






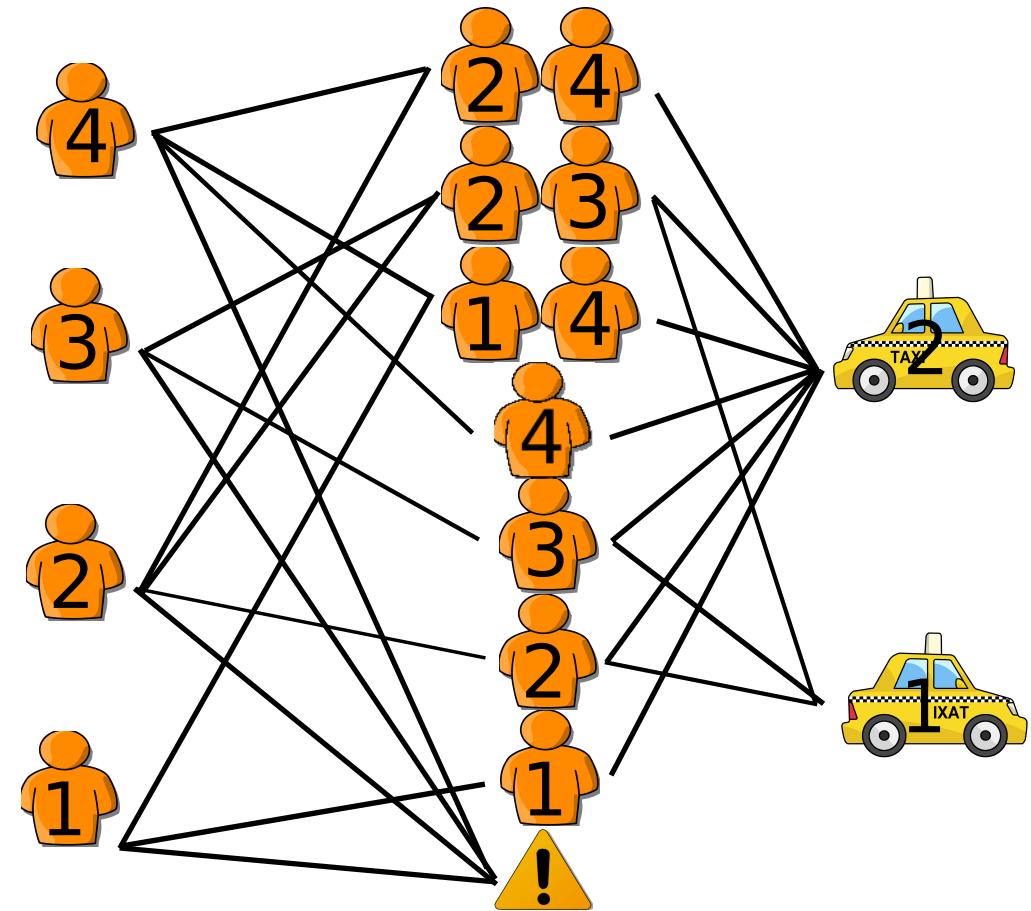
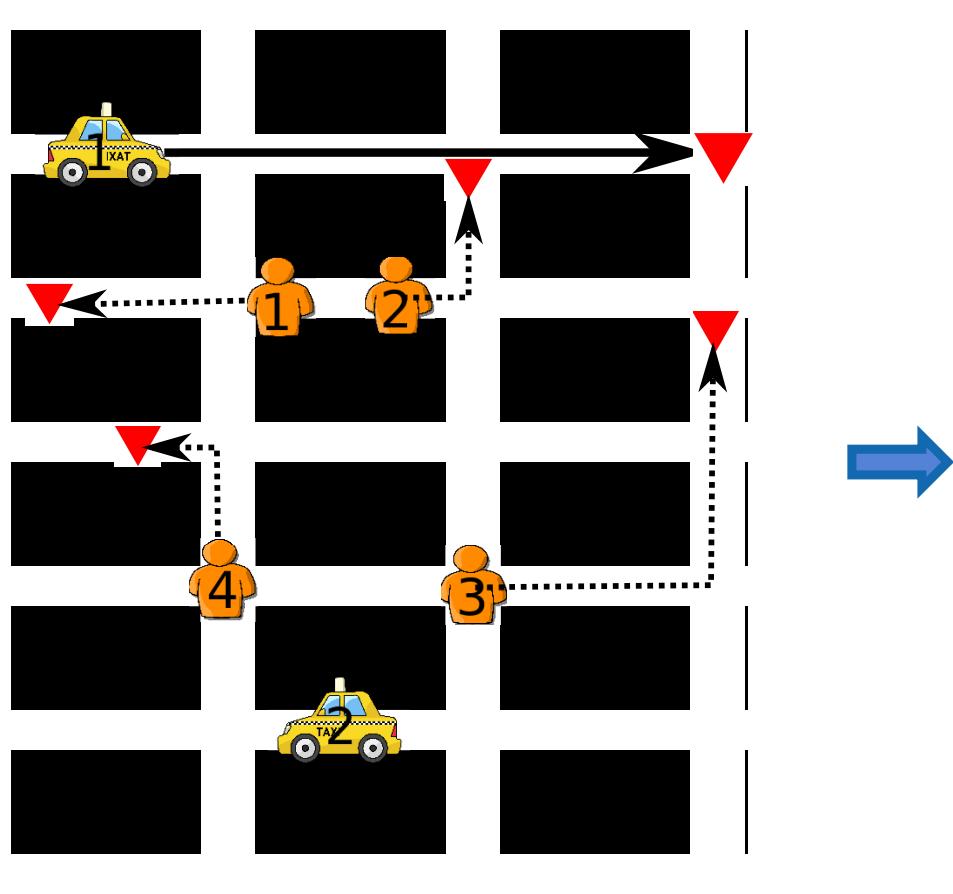
On-demand high-capacity ride-sharing

Large combinatorial complexity → Algorithm that is **scalable, online and anytime optimal**



Step 1: Compute feasible trips

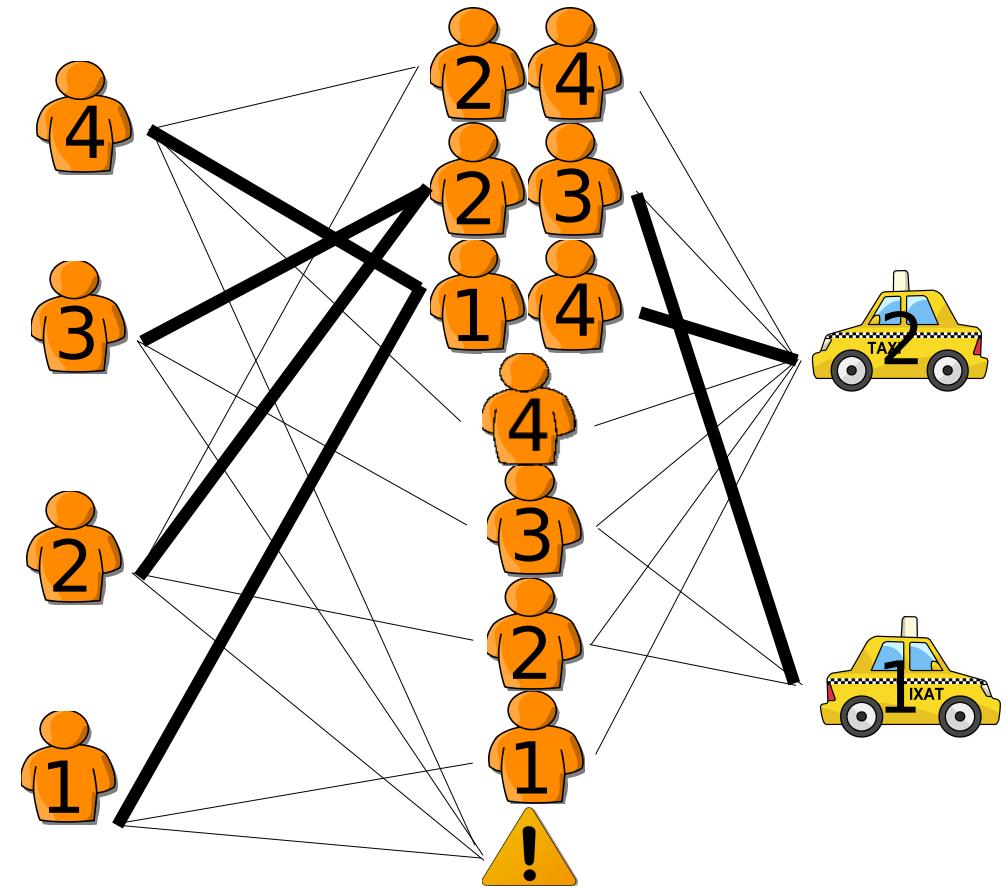
Incremental search of feasible routes/schedules



Step 2: Assignment of vehicles to trips

Formulated as an Integer Linear Program

- Initialized from greedy assignment
- Optimized over time
- Minimize sum of delays



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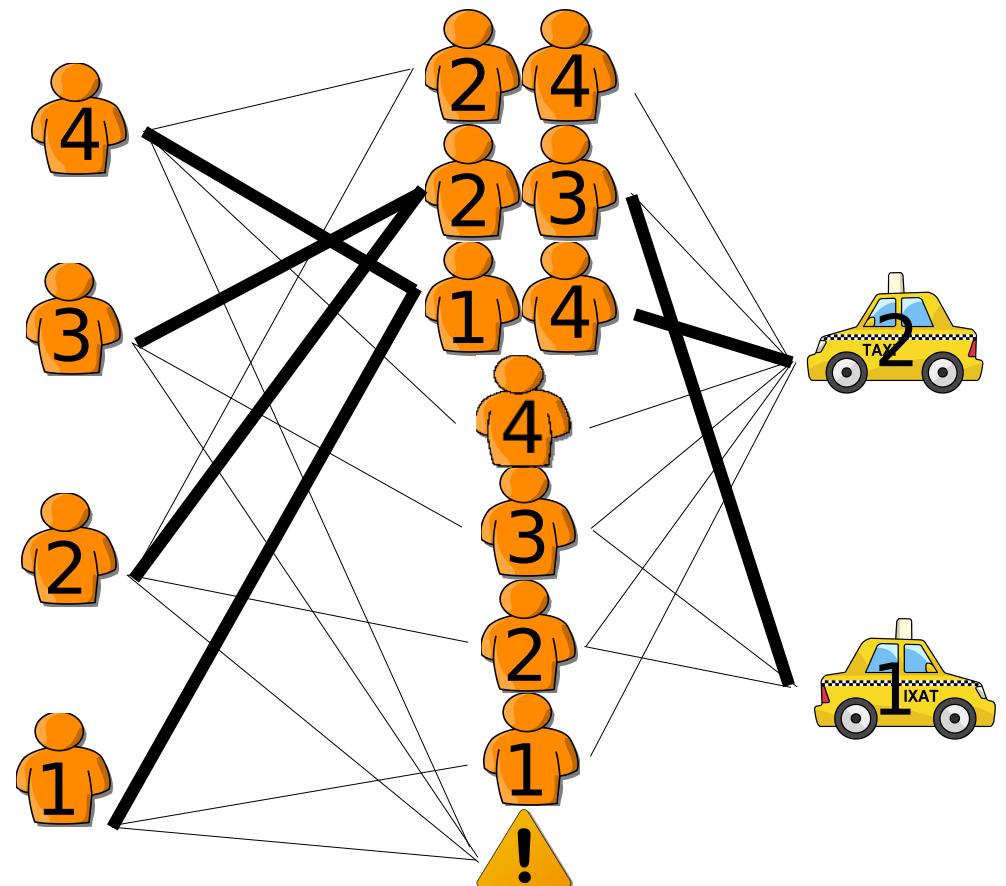
Algorithm 1. Optimal assignment

1: Initial guess: Σ_{greedy}

2: $\Sigma_{optim} := \arg \min_{\chi} \sum_{i,j \in \mathcal{E}_{TV}} c_{i,j} \epsilon_{i,j} + \sum_{k \in \{1, \dots, n\}} c_{ko} \chi_k$

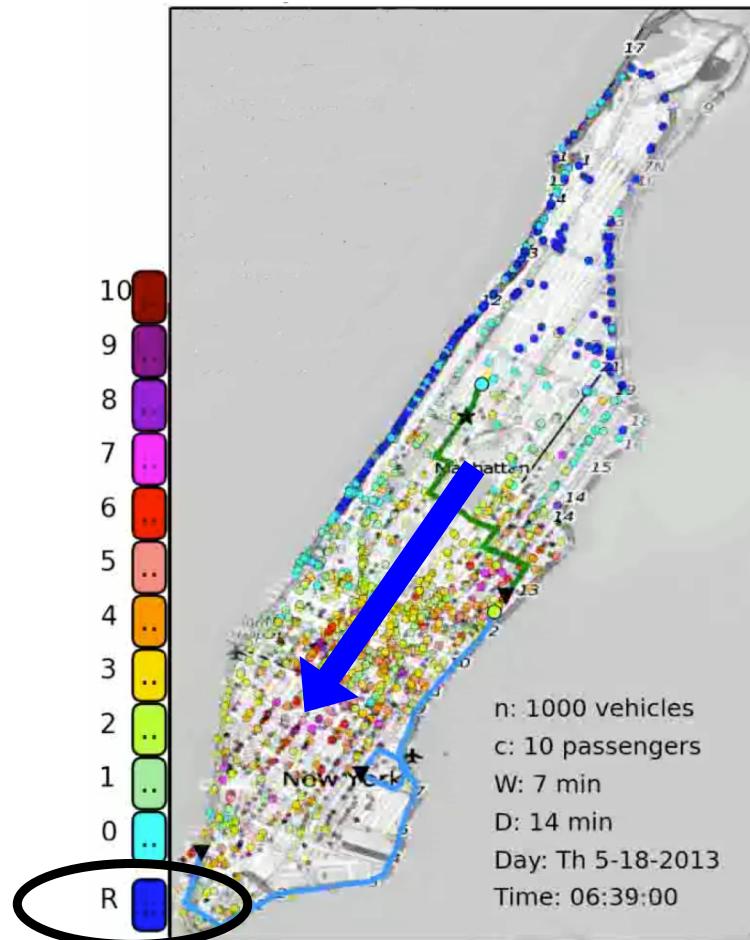
3: s.t. $\sum_{i \in \mathcal{I}_{V=j}^T} \epsilon_{i,j} \leq 1 \quad \forall v_j \in \mathcal{V}$

4: $\sum_{i \in \mathcal{I}_{R=k}^T} \sum_{j \in \mathcal{I}_{T=i}^V} \epsilon_{i,j} + \chi_k = 1 \quad \forall r_k \in \mathcal{R}$



Step 3: Rebalancing

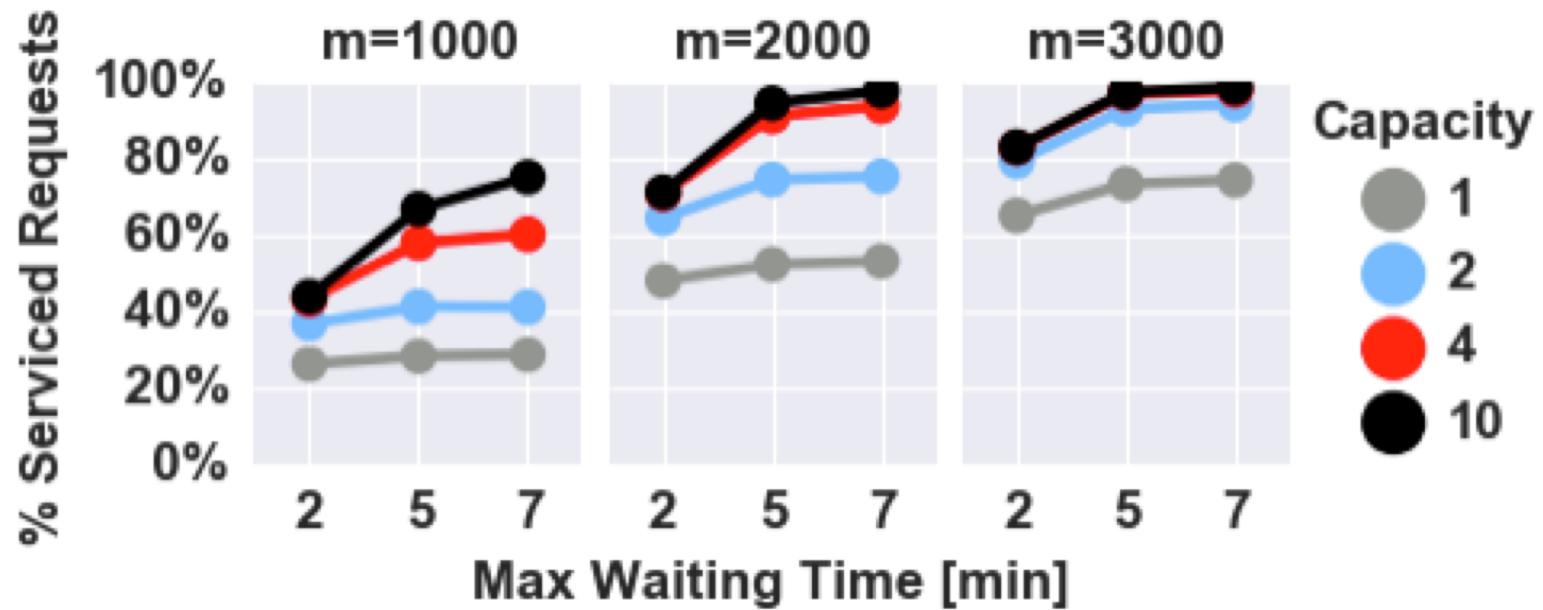
Move idle vehicles towards areas of high demand (formulated as a Linear Program)



1000, 2000 and 3000 vehicles

Capacity Four

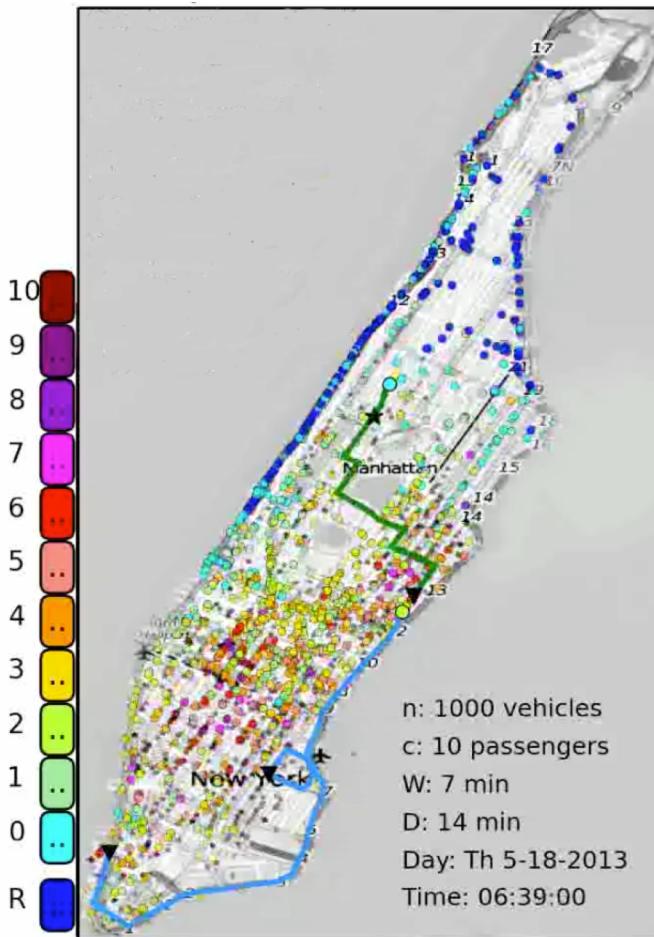
High service rate with less vehicles



High service rate with <25% of taxis

Predictive routing

At peak times mismatch of vehicles & demand

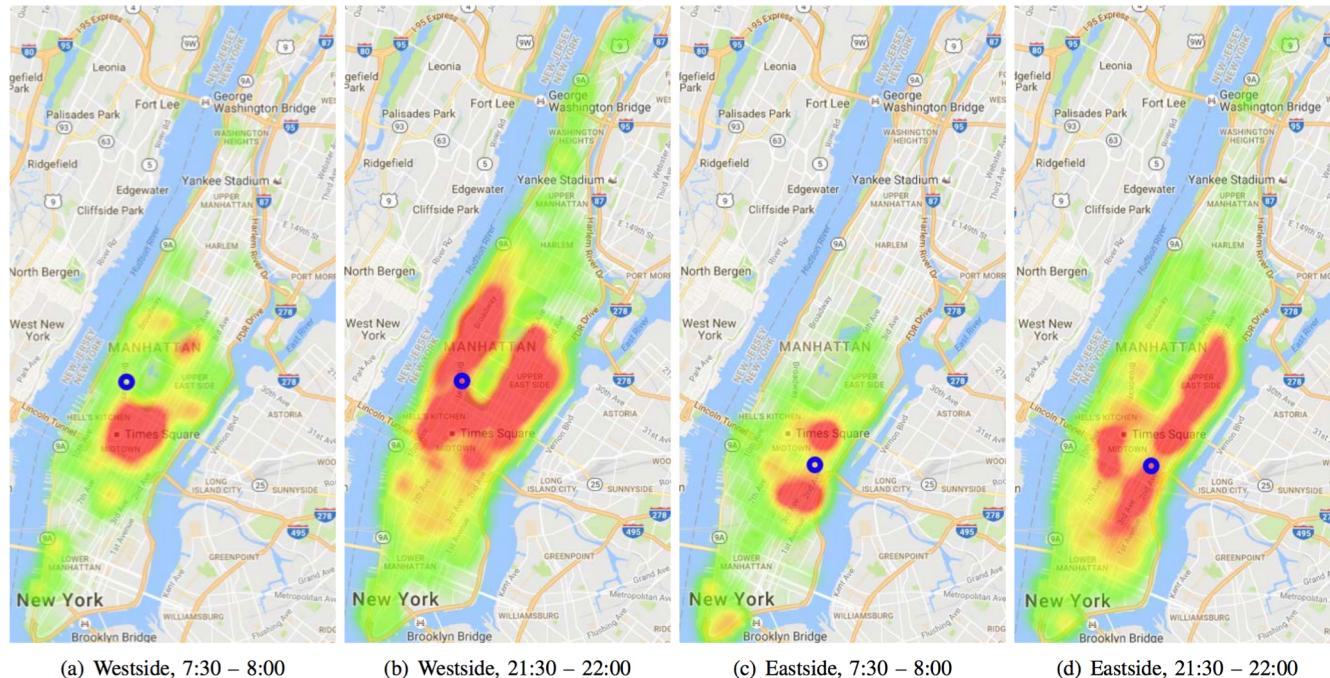


Predictive routing

At peak times mismatch of vehicles & demand

→ Model of future demand [from historical data]

$\text{Pr}(\text{destination} \mid \text{origin, time})$



Predictive routing

At peak times mismatch of vehicles & demand

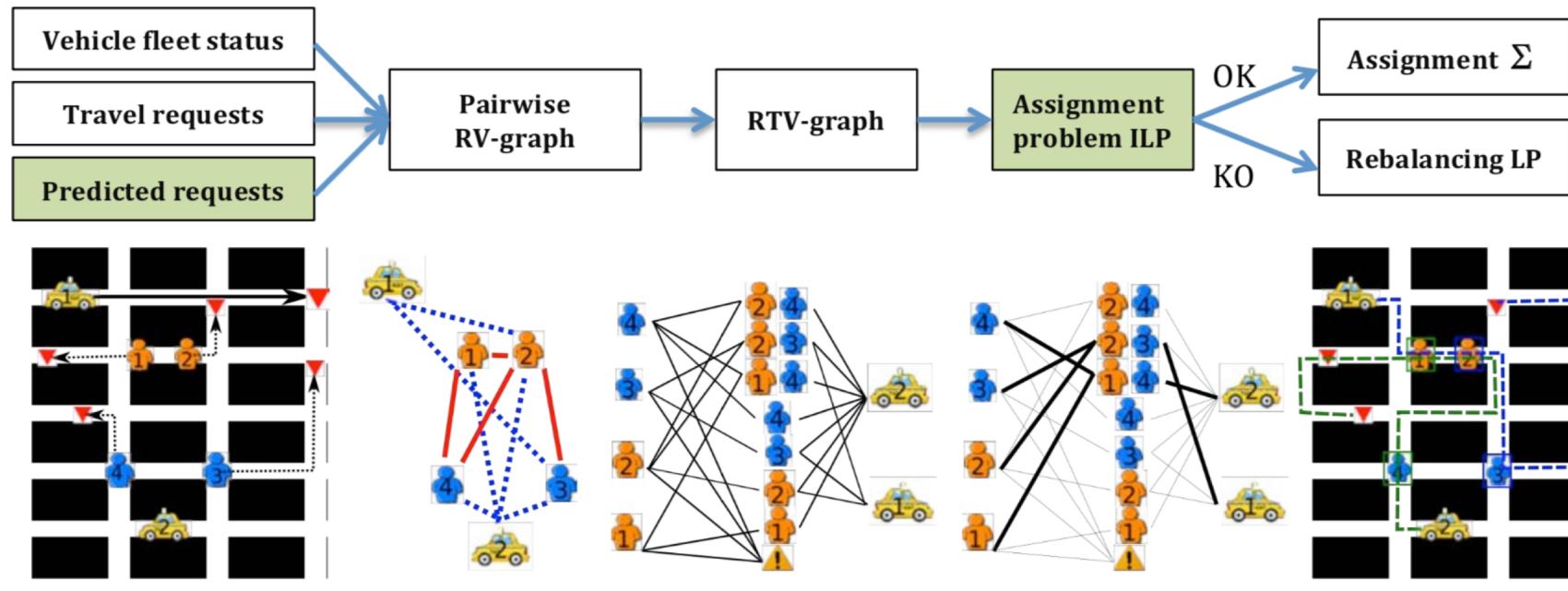
→ **Model of future demand** [from historical data]

$\Pr(\text{destination} \mid \text{origin, time})$

→ Better position the vehicles for the future,
by **sampling expected requests**

$$C_{\text{now}}(\Sigma) + C_{\text{future}}(\Sigma)$$

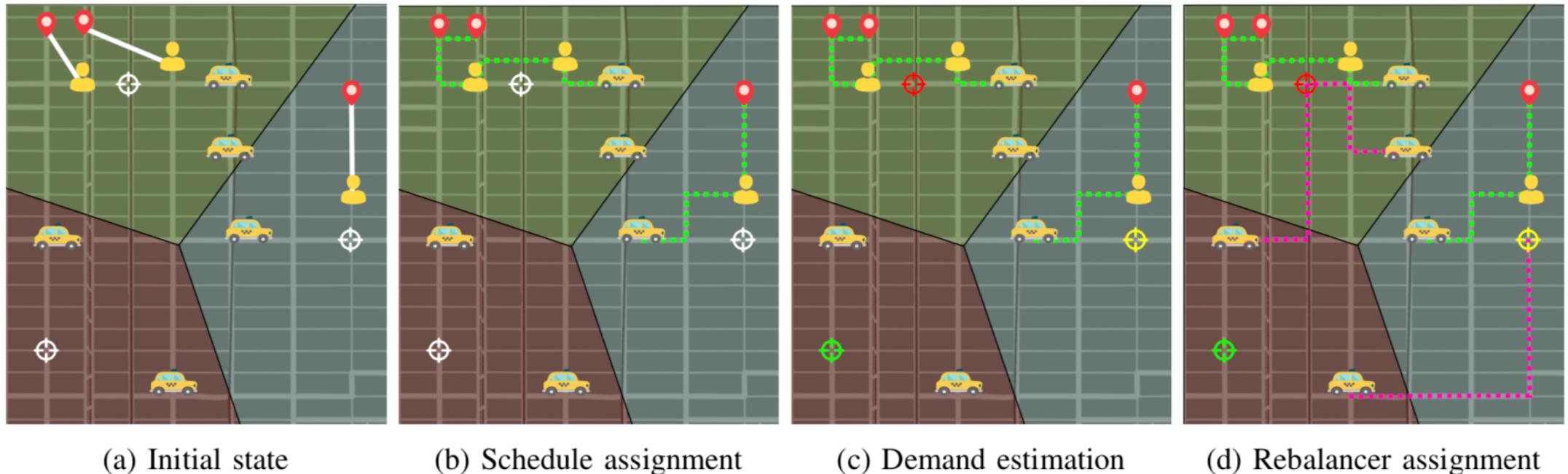
→ Poor scalability



Proactive rebalancing

Estimate vehicle demand per region, based on real-time data

Assign idle vehicles to rebalancing regions using the estimated demand



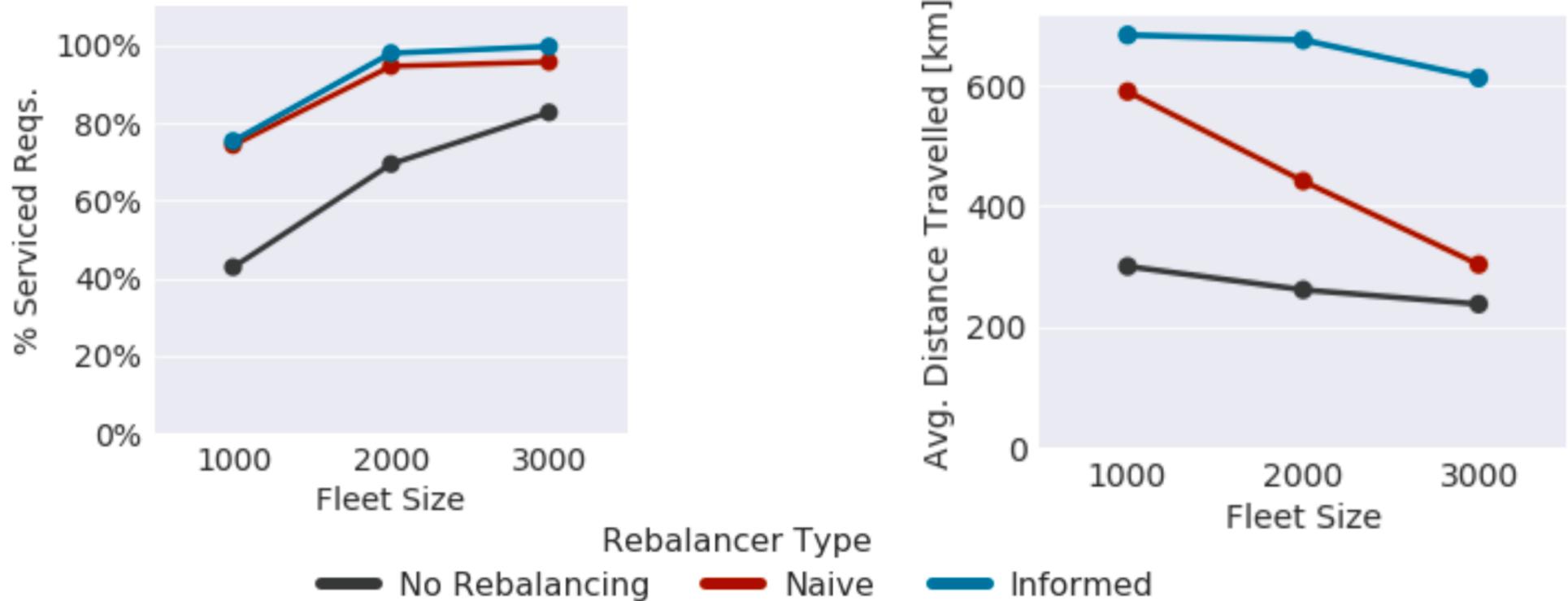
Proactive rebalancing

Estimate vehicle demand per region, based on real-time data

Assign idle vehicles to rebalancing regions using the estimated demand

→ Increase the service rate and reduce the waiting time

→ But, this might come at a cost of (much) **higher distance driven!**



Competing objectives



Quality of Service

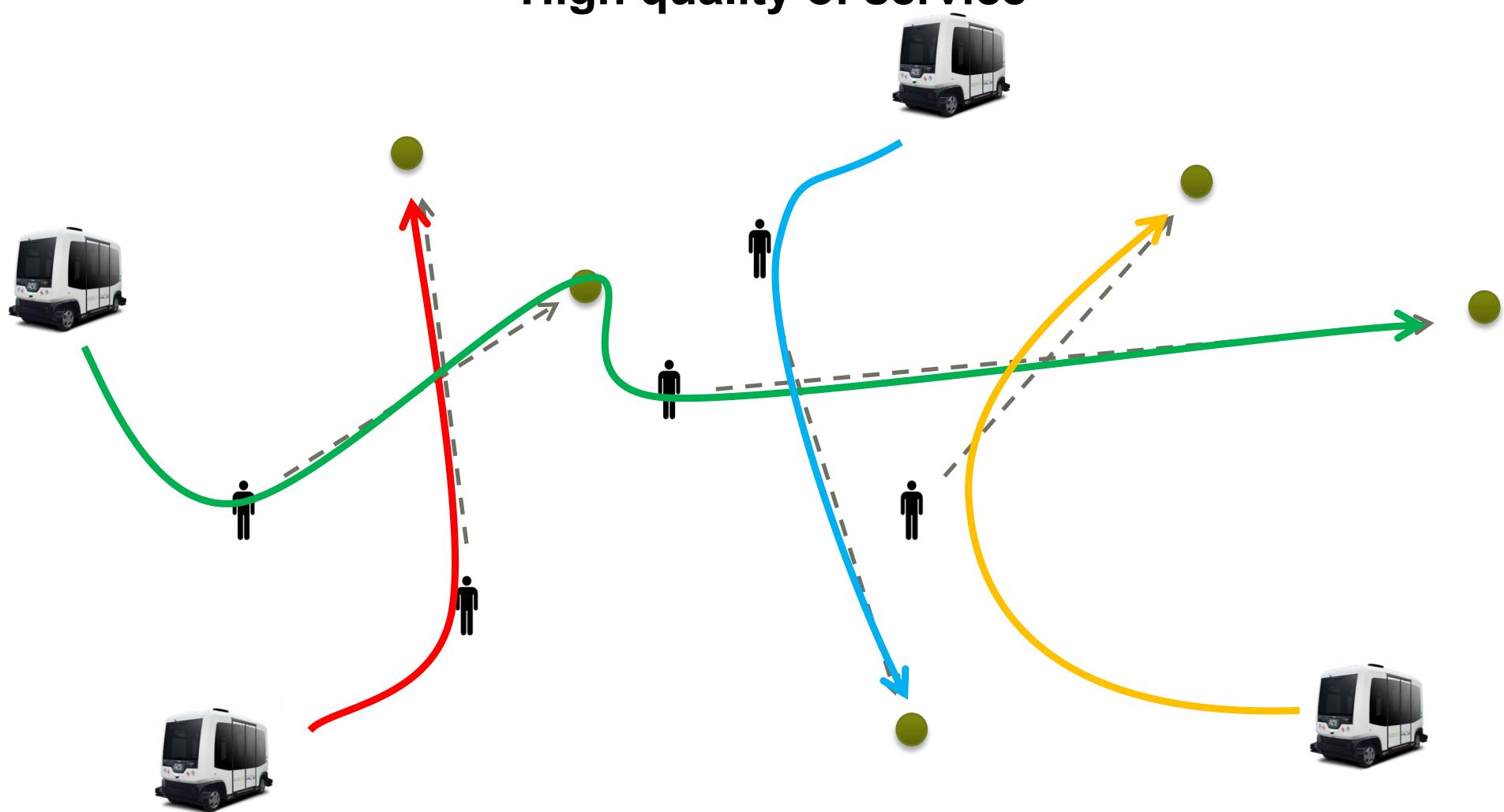


Operation Cost

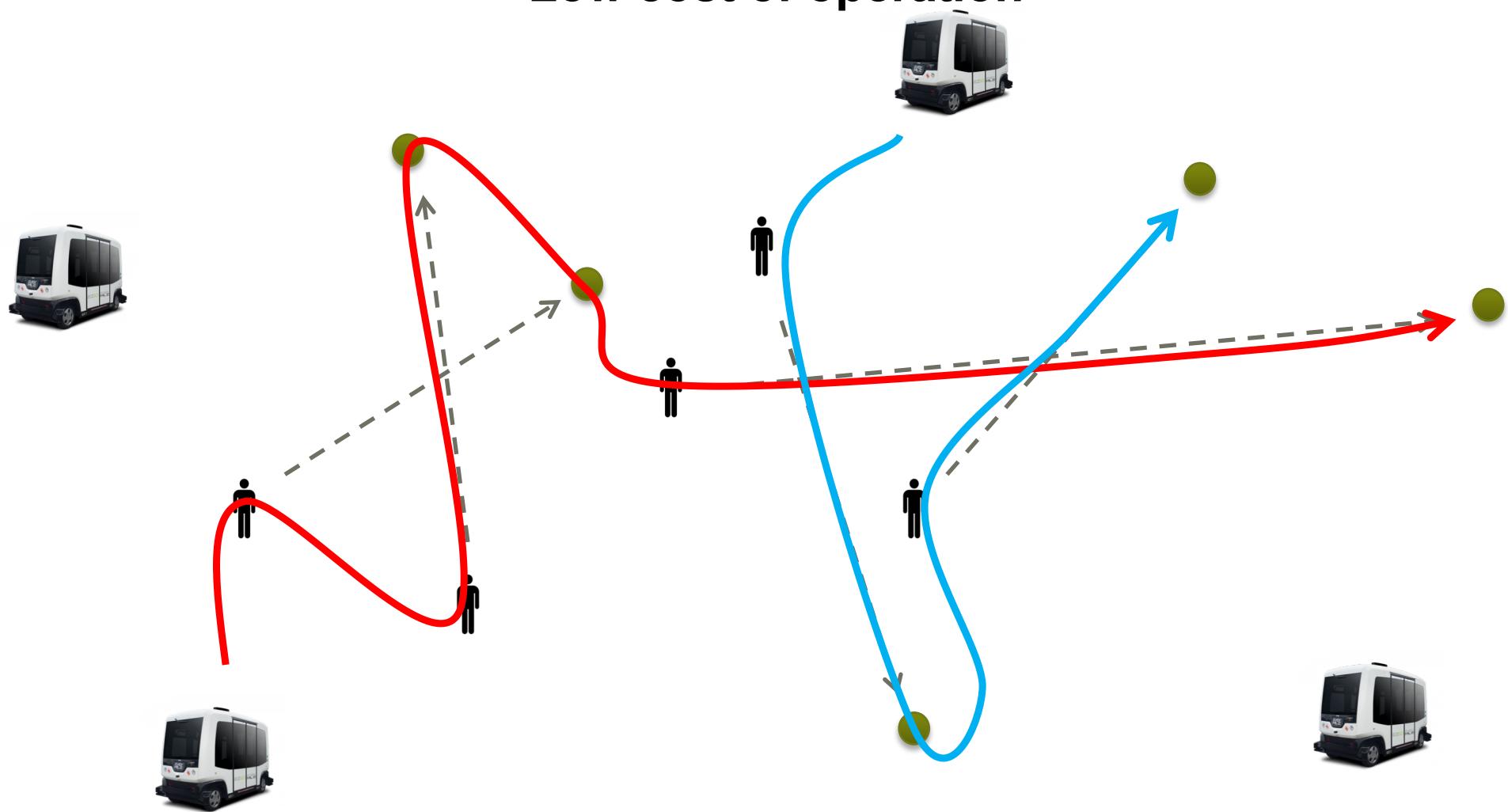
$C_{QoS} := \text{Avg. Passenger Travel Delay}$

$C_{OC} := \text{Total Vehicle Distance Driven}$

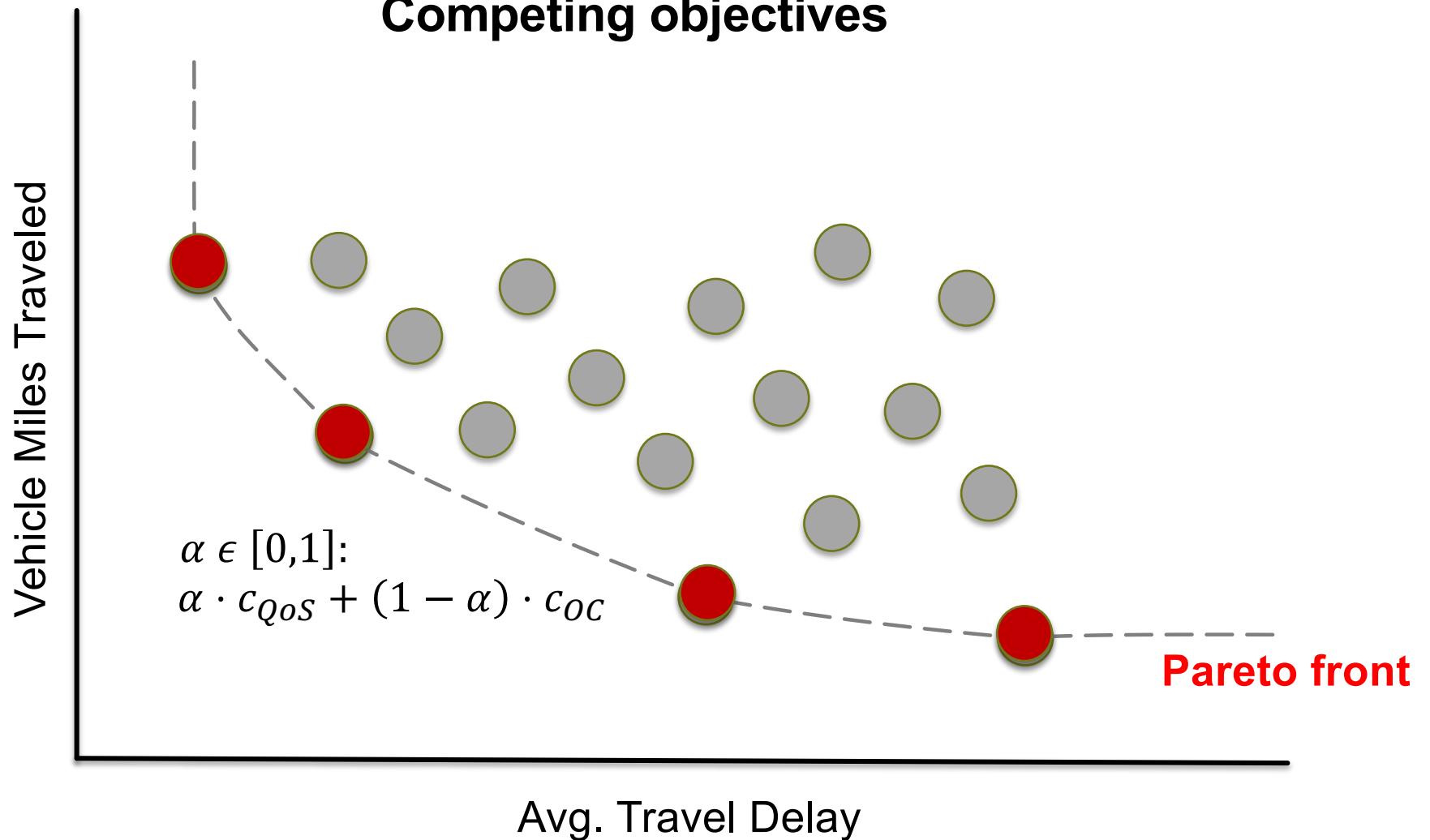
High quality of service



Low cost of operation



Competing objectives



Pareto front

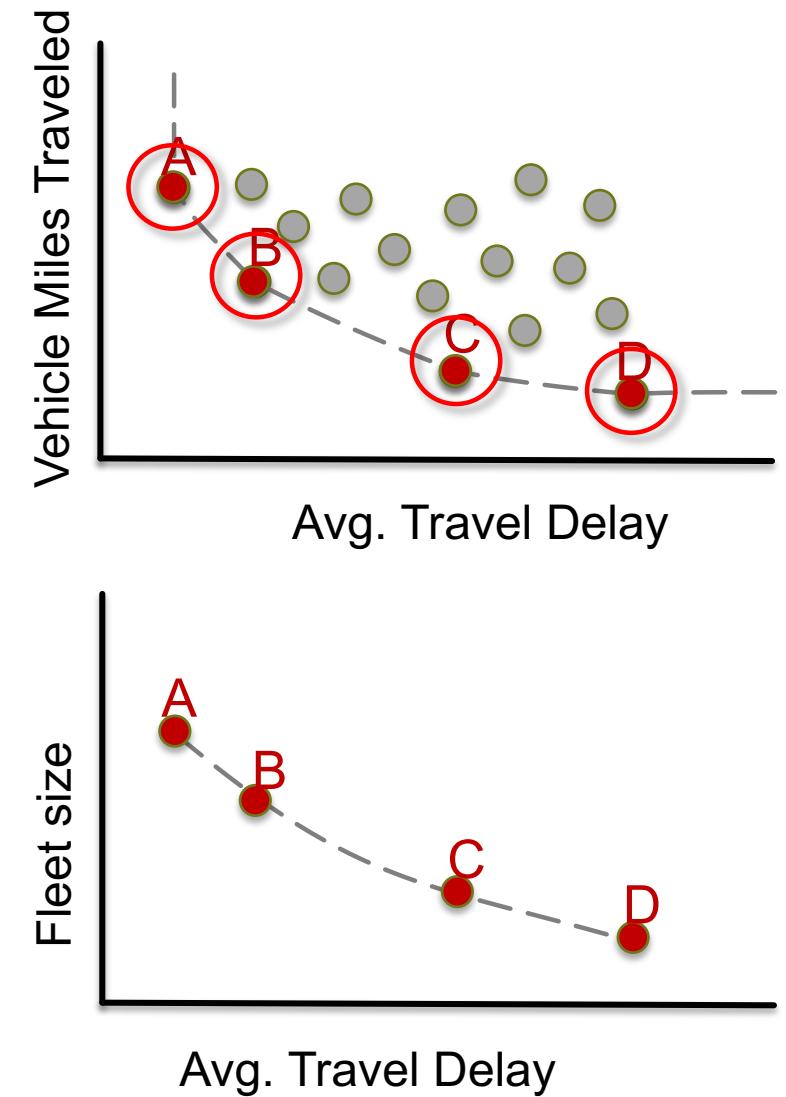
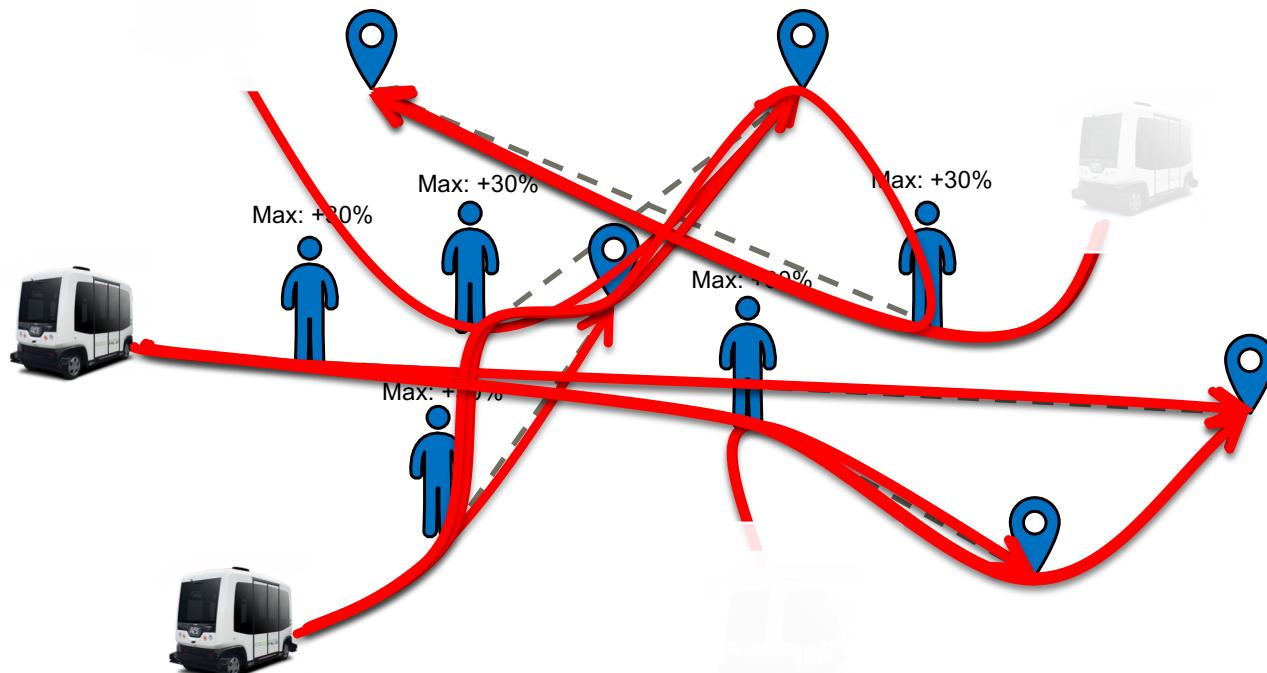


Illustration: Synthetic travel demand (50 requests)

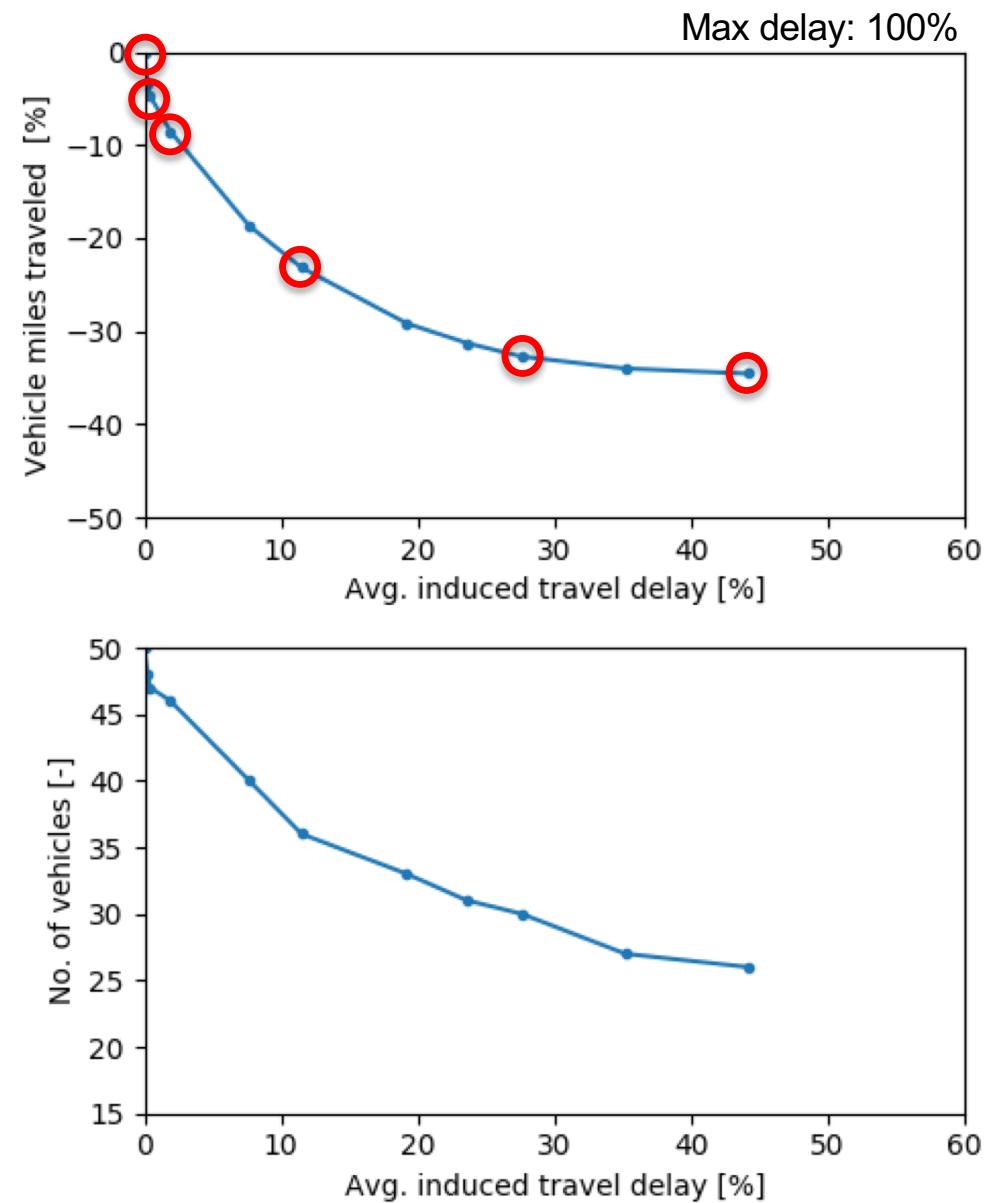
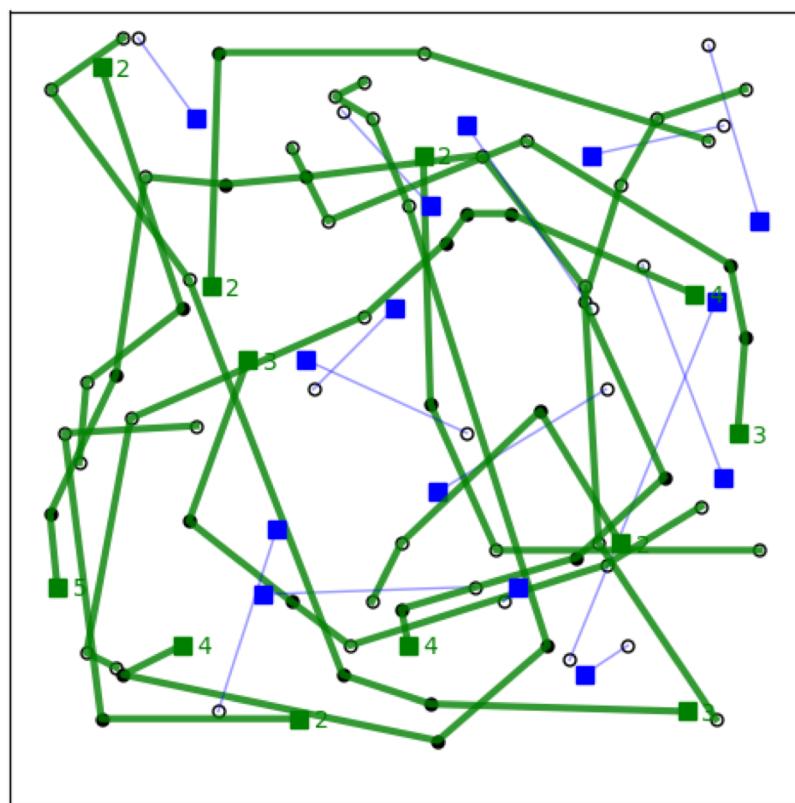


Illustration: Synthetic travel demand (50 requests)

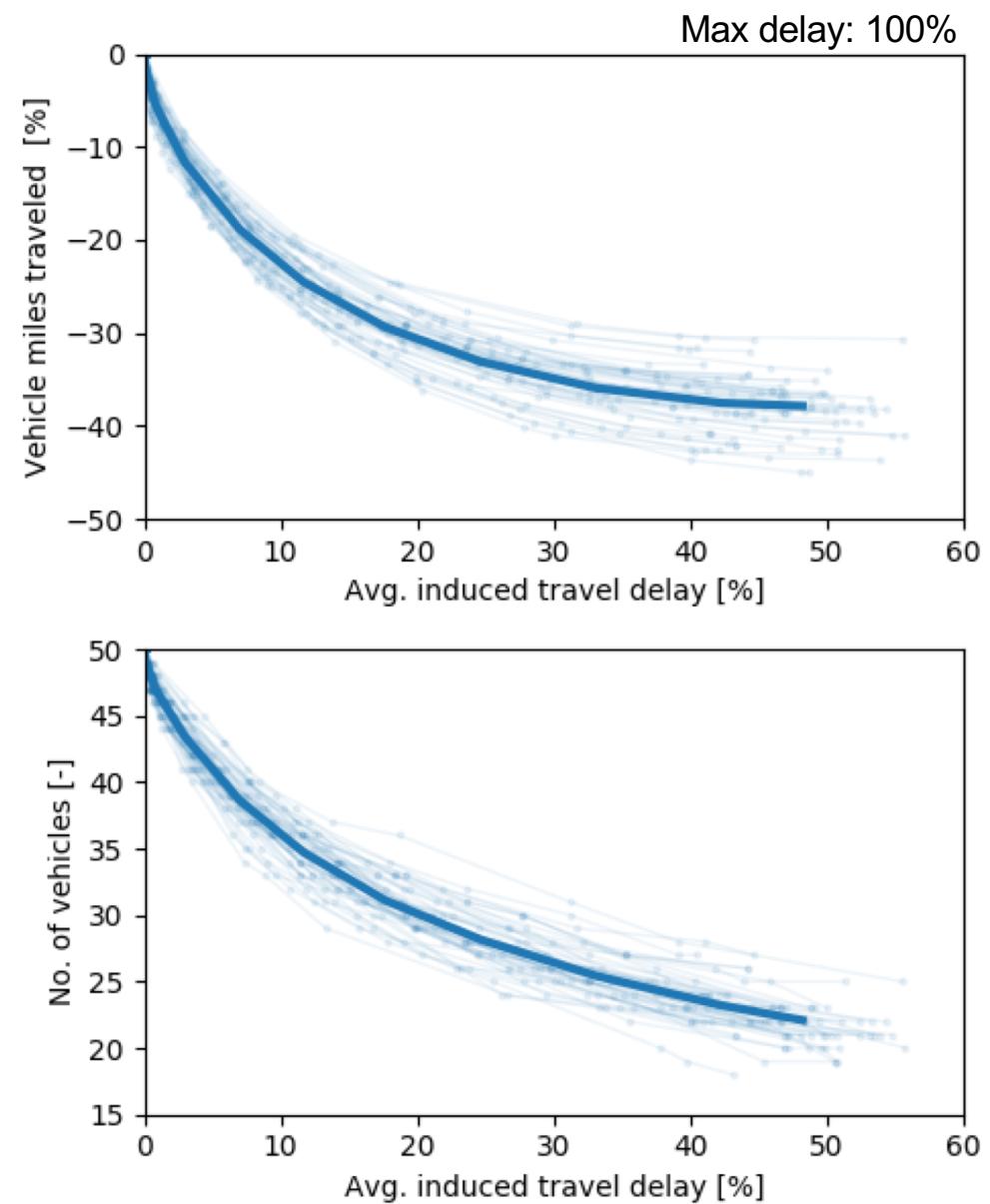
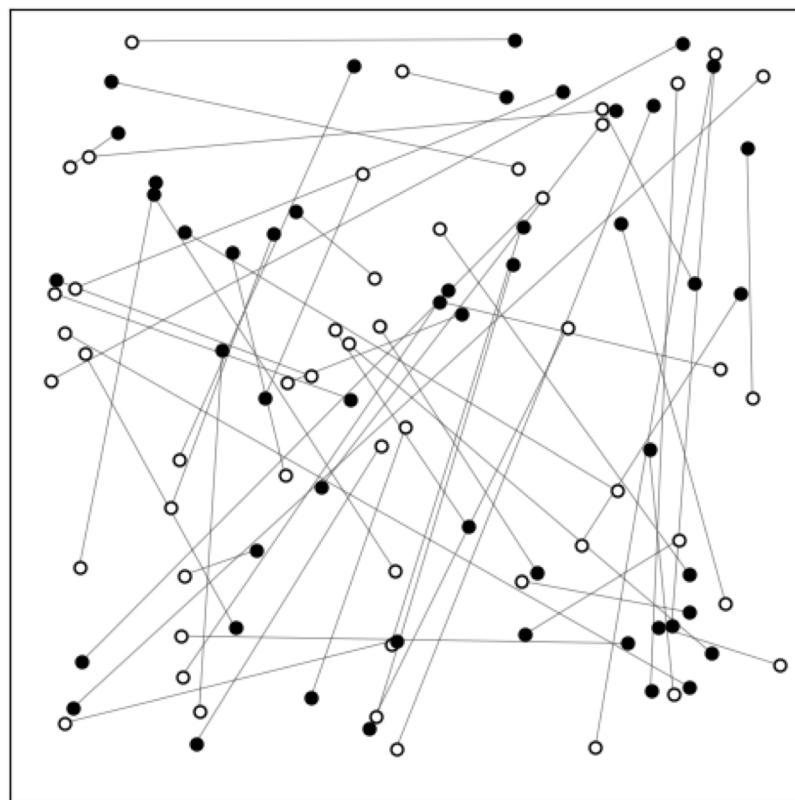
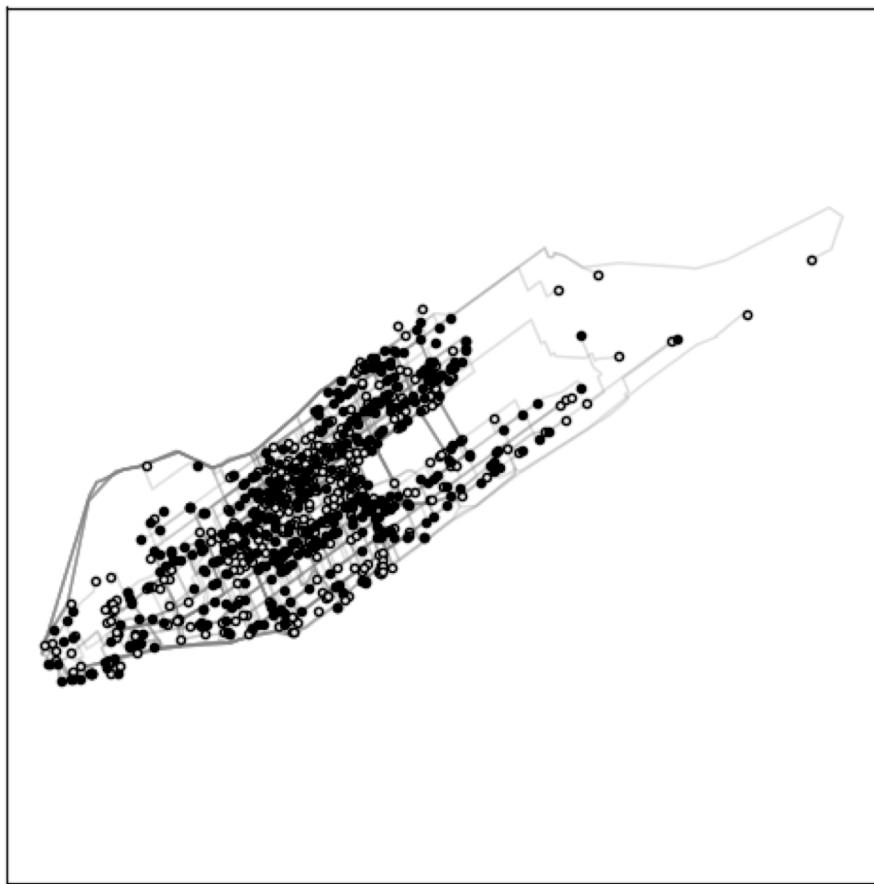
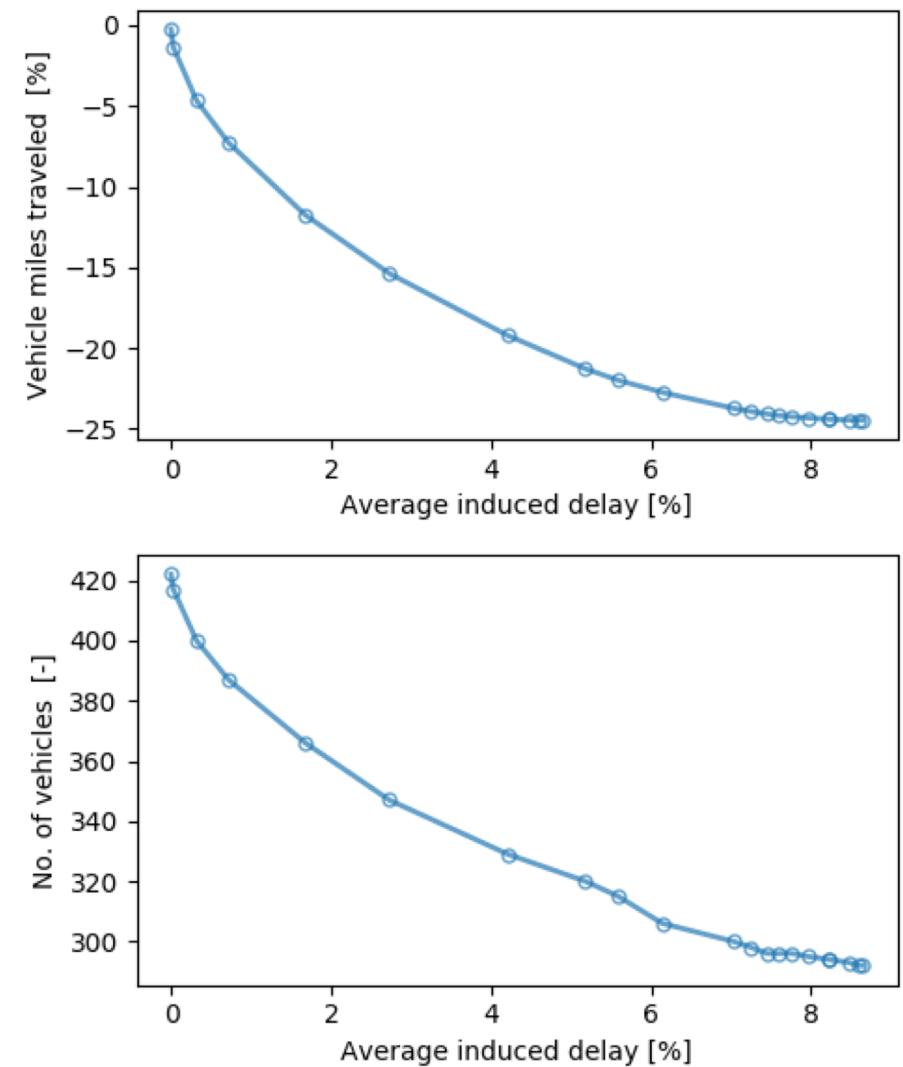


Illustration:

1 minute of Manhattan Taxi Requests
(427 requests)



Max delay: 25%





Number of
vehicles

Fleet size and composition

From historical data we can compute the fleet size and composition required for a given day

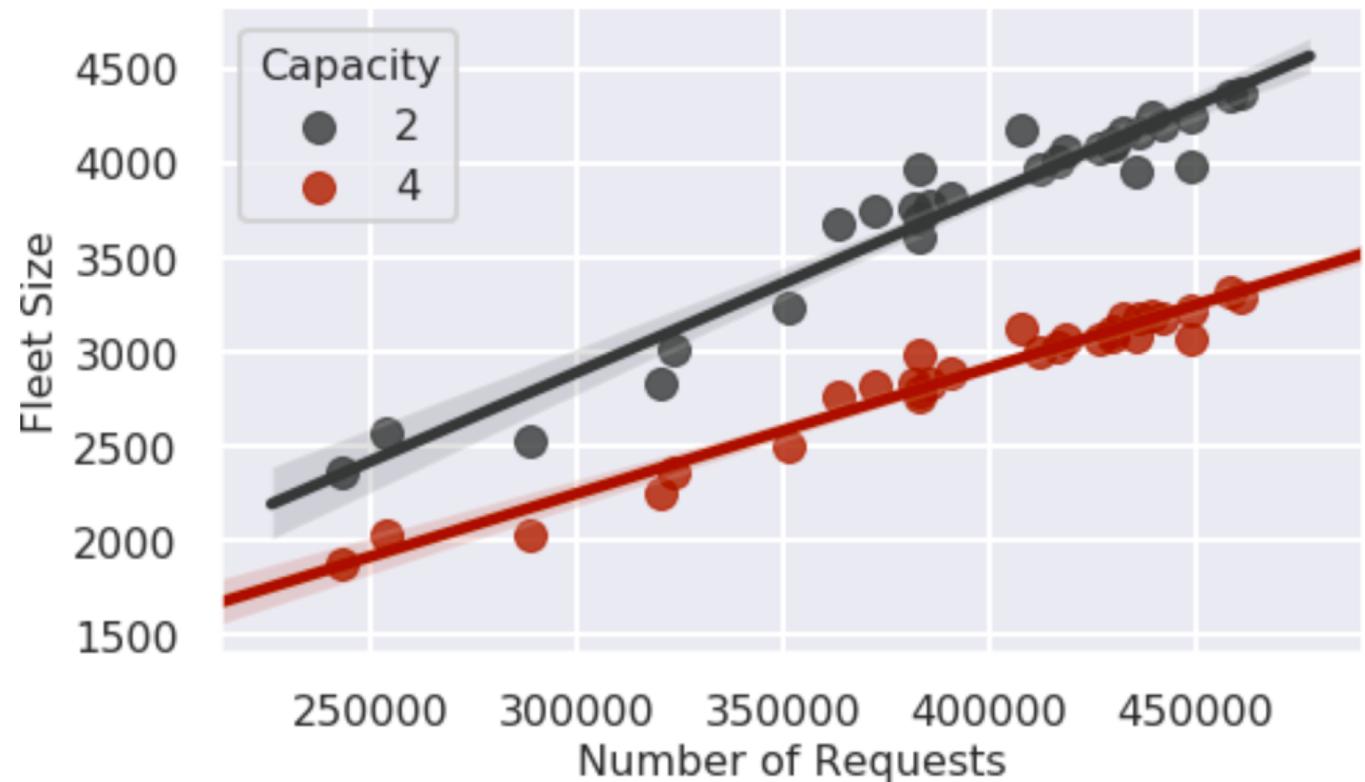
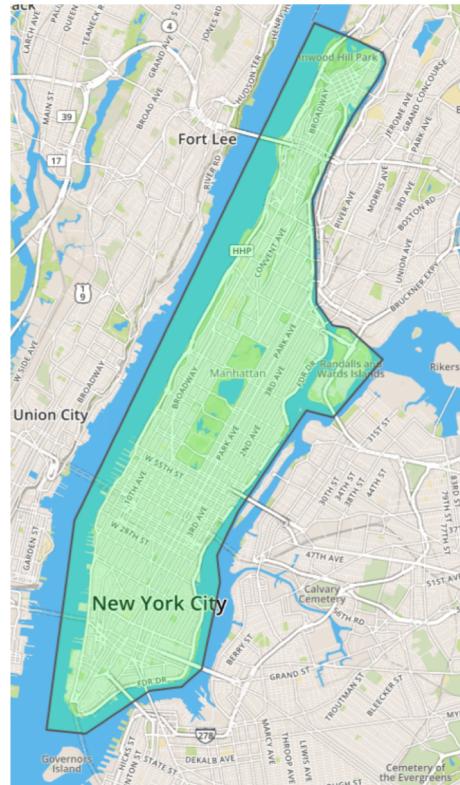
→ Constraints: service all requests, maximum waiting time and delay

1. Compute a set of deposits, e.g., distance from any point to closest deposit < 1 min
2. In small batches, e.g., 1 h, compute feasible and locally optimal schedules [Similar to RTV]
3. Long term rebalancing (chain schedules from multiple batches) [Max. matching ILP]

Fleet size and composition

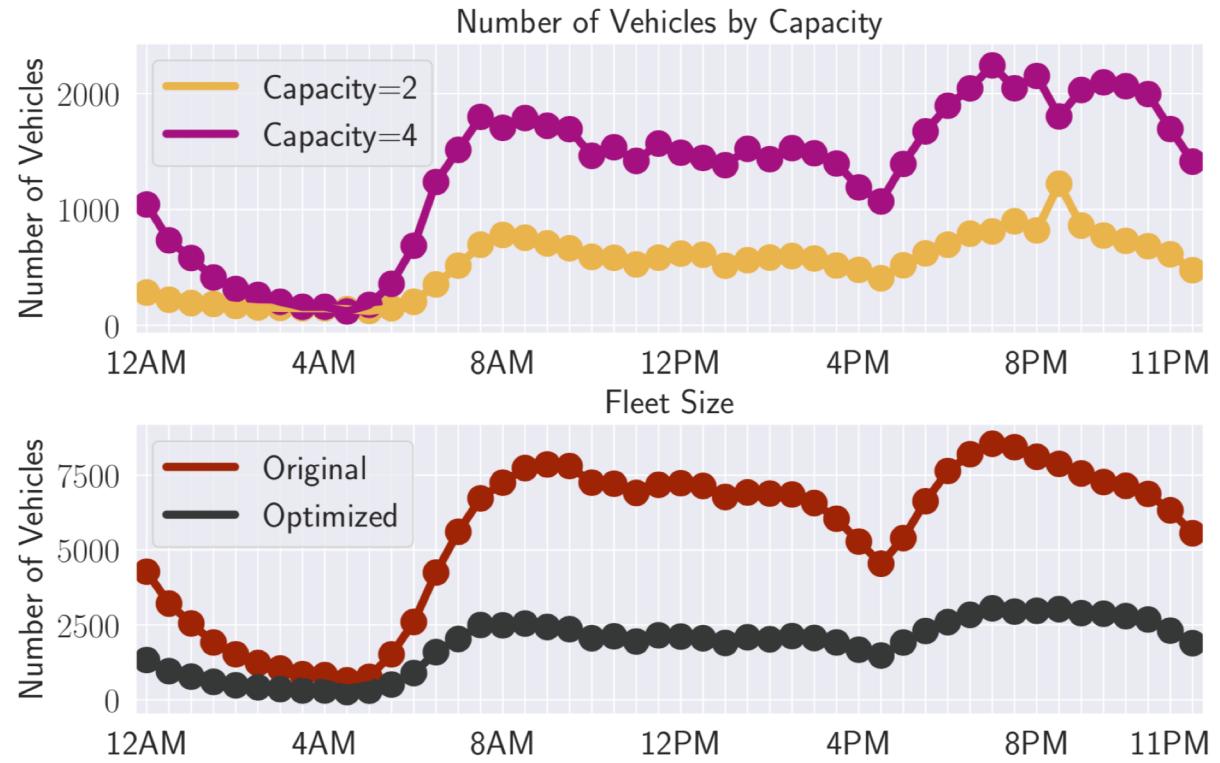
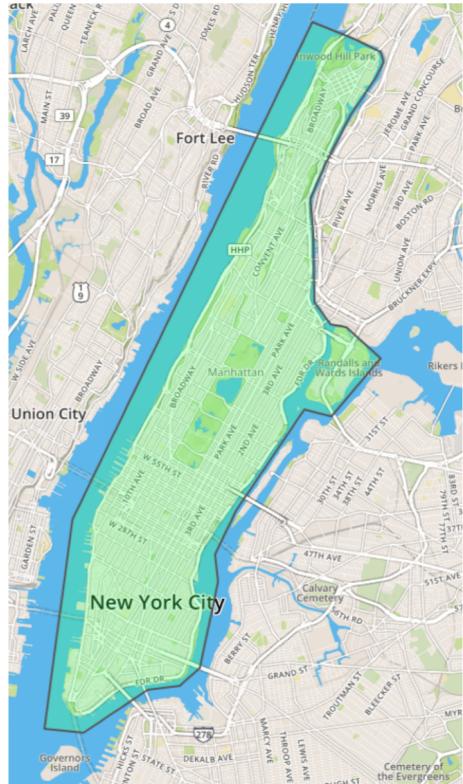
From historical data we can compute the fleet size and composition required for a given day

→ Constraints: service all requests, maximum waiting time (3 min) and delay (6 min)



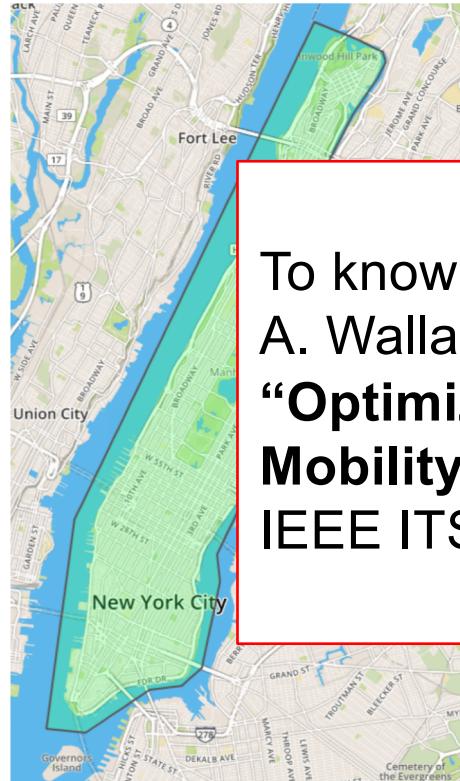
Fleet size and composition [mixed fleet]

From historical data we can compute the fleet size and composition required for a given day
→ Constraints: service all requests, maximum waiting time (3 min) and delay (6 min)

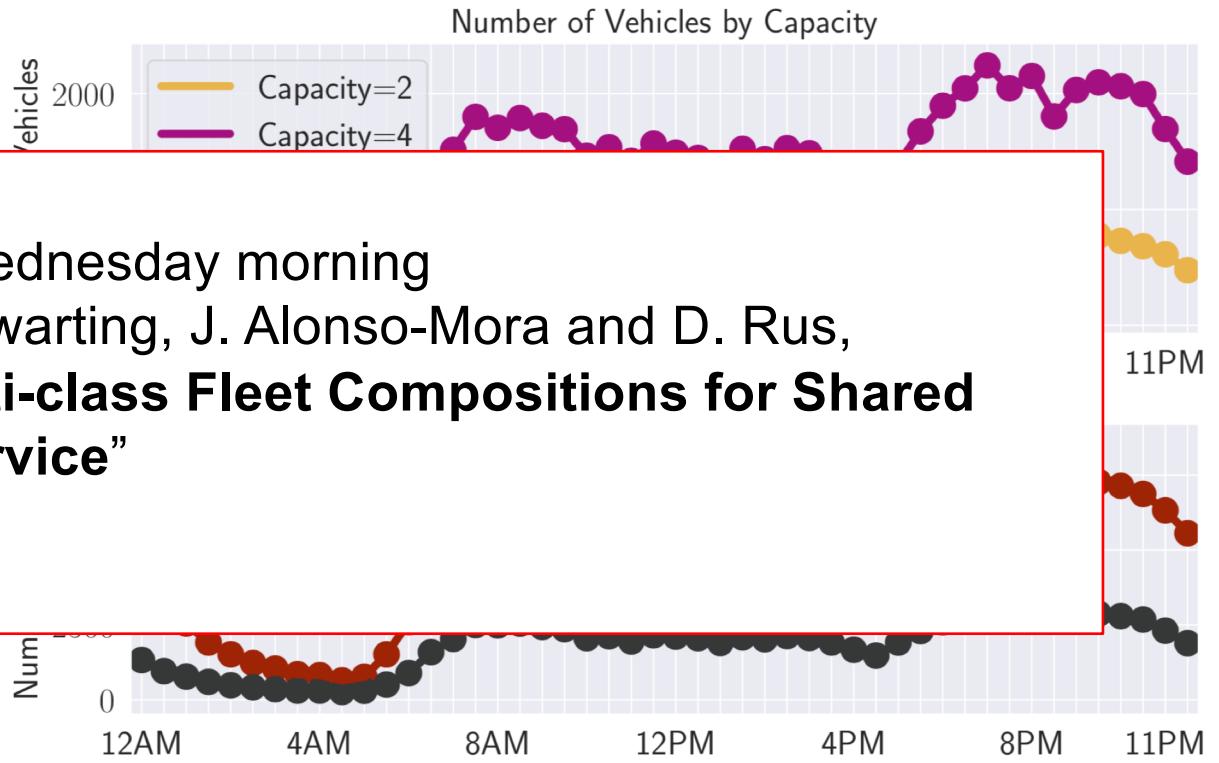


Fleet size and composition

From historical data we can compute the fleet size and composition required for a given day
→ Constraints: service all requests, maximum waiting time (3 min) and delay (6 min)



To know more: Wednesday morning
A. Wallar, W. Schwarting, J. Alonso-Mora and D. Rus,
“Optimizing Multi-class Fleet Compositions for Shared Mobility-as-a-Service”
IEEE ITSC 2019



Summary

Automated Mobility on Demand with Ride-Sharing

- Online method for high-capacity ride-sharing
- Predictive routing
- Multi-objective analysis
- Fleet sizing

To know more: www.alonsomora.com

j.alonsomora@tudelft.nl

Funding:

