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Towards a Co-Design Framework for Future Mobility Systems
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1. Abstract

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The design of Autonomous Vehicles (AVs) and the design of AVs-enabled mobility systems are closely coupled. Indeed, knowledge about the intended service of AVs would impact their design and deployment process, whilst insights about their technological development could significantly affect transportation management decisions. This calls for tools to study such a coupling and co-design AVs and AVs-enabled mobility systems in terms of different objectives. In this paper, we instantiate a framework to address such co-design problems. In particular, we leverage the recently developed theory of co-design to frame and solve the problem of designing and deploying an intermodal Autonomous Mobility-on-Demand system, whereby AVs service travel demands jointly with public transit, in terms of fleet sizing, vehicle autonomy, and public transit service 10 frequency. Our framework is modular and compositional, allowing to describe the design problem as the interconnection of its individual components and to tackle it from a system-level perspective. Moreover, it only requires very general monotonicity assumptions and it naturally handles multiple objectives, delivering the rational solutions on the Pareto front and thus enabling policy makers 14 to select a solution through "political" criteria. To showcase our methodology, we present a real-16 world case study for Washington D.C., USA. Our work suggests that it is possible to create userfriendly optimization tools to systematically assess the costs and benefits of interventions, and that 17 such analytical techniques might gain a momentous role in policy-making in the future. 18

20 Keywords: Co-Design, Autonomous Vehicles, Future Mobility Systems.

2. Introduction

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Arguably, the current design process for Autonomous Vehicles (AVs) largely suffers from the lack of clear, specific requirements in terms of the service such vehicles will be providing. Yet, knowledge about their intended service (e.g., last-mile versus point-to-point travel) might dramatically impact how the AVs are designed, and, critically, significantly ease their development process. For example, if for a given city we knew that for an effective on-demand mobility system autonomous cars only need to drive up to 25 mph and only on relatively easy roads, their design would be 7 greatly simplified and their deployment could certainly be accelerated. At the same time, from the system-level perspective of transportation management, knowledge about the trajectory of technology development for AVs would certainly impact decisions on infrastructure investments and 10 provision of service. In other words, the design of the AVs and the design of a mobility system 11 leveraging AVs are intimately *coupled*. This calls for methods to reason about such a coupling, 12 and in particular to co-design the AVs and the associated AVs-enabled mobility system. A key 14 requirement in this context is to be able to account for a range of heterogeneous objectives that are often not directly comparable (consider, for instance, travel time and emissions). 15

Accordingly, the goal of this paper is to lay the foundations for a framework through which one can co-design future AVs-enabled mobility systems. Specifically, we show how one can leverage the recently developed mathematical theory of co-design [1–3], which provides a general methodology to co-design complex systems in a modular and compositional fashion. This tool delivers the set of rational design solutions lying on the Pareto front, allowing to reason about the costs and benefits of the individual design options. The framework is instantiated in the setting of co-designing intermodal Autonomous Mobility-on-Demand (AMoD) systems [4], whereby fleets of self-driving vehicles provide on-demand mobility jointly with public transit. Aspects that are subject to co-design include fleet size, vehicle-specific characteristics for the AVs, and public transit service frequency.

Literature Review: The design of mobility systems can be divided in classic urban transportation network design problems and more recent design problems for AMoD systems. The first research stream was reviewed in [5] and can be divided in road [6, 7], public transit [8, 9], and multi-modal [10] network design problems which can be classified as strategic long-term infrastructure modification decisions such as building new streets, tactical infrastructure-allocation problems on lanes allocation and public transit service frequency, and operational short-term scheduling problems. They are usually formulated as bilevel problems whereby the upper-level is related to the policy in discussion and the lower-level is concerned with solving the trip assignment problem by computing the user equilibrium or the system optimum under given congestion and demand models. Overall, these problems are solved with non-convex and combinatorial mathematical methods, heuristics, and metaheuristics consisting of gradient-free optimization algorithms. Often, the problems are formulated with a unique objective or, in the case of multi-objective settings, the different objectives are reduced to a unique one through monetary metrics precluding Pareto solutions. The design of AMoD systems mostly considers their fleet sizing. In particular, it was studied through simulations in [11-13] and with analytical methods in [14], whilst in [15] the problem was combined with the charging infrastructure sizing and placement problem and solved using mixed integer linear programming techniques. The fleet sizing and vehicle allocation problem for conventional vehicles was presented in [16]. The fleet size and pricing scheme of Mobility-on-Demand systems was designed in [17] with Bayesian optimization, whereas in [18] a rail-car fleet sizing problem was solved with simulated annealing. More recently, the joint design of multimodal

transit networks and AMoD systems was formulated in [19] as a bilevel optimization problem and solved with heuristic methods. Overall, to the best of the authors' knowledge, most design methods for AMoD rely either on simulation-based approaches or nonlinear and combinatorial optimization techniques, and do not study AVs-specific characteristics such as the achievable vehicle speed. In conclusion, the frameworks proposed for the design of mobility systems mainly have a fixed problem-specific structure and are thus non-modular. Moreover, they do not deliver a Pareto front of solutions, focusing on a unique objective. 7

Statement of Contribution: In this paper we lay the foundations for the systematic study of 8 the design of AVs-enabled mobility systems. Specifically, we leverage the mathematical theory of 10 co-design [1] to devise a framework to study the design of intermodal AMoD (I-AMoD) systems in terms of fleet characteristics and public transit service, enabling the computation of the ratio-11 12 *nal* solutions lying on the Pareto front of minimal travel time, transportation costs, and emissions. Our framework allows to structure the design problem in a modular way, in which each different transportation option can be "plugged in" in a larger model. Each model has minimal assumptions: Rather than properties such as linearity and convexity, we ask for very general monotonicity assumptions. For example, we assume that the cost of automation increases monotonically with 16 17 the speed achievable by the self-driving car. We are able to obtain the full Pareto front of rational solutions, or, given more "political" criteria, to weigh incomparable costs (such as travel time and 18 emissions), to present one optimal solution to stakeholders, such as AVs companies and municipal-19 ities. We consider the real-world case study for Washington D.C., to showcase our methodology. 20 We show how, given the model, we can easily formulate and answer several questions regarding the introduction of new technologies and investigate possible infrastructure interventions. 22

2.1. Organization 23

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- The remainder of this paper is structured as follows: Section 3 presents the mathematical back-
- 25 ground of co-design. Section 4 presents the co-design problem for AVs-enabled mobility systems.
- We showcase our approach with real-world case studies for Washington D.C., USA, in Section 5. 26
- Section 6 concludes the paper with a discussion and an overview on future research directions. 27

3. Mathematical Background 28

- In this section, we present the basics of partial order theory and the mathematical theory of co-29
- design. The interested reader is referred to [1-3].
- Partial Order Theory
- Consider a set \mathscr{P} and a partial order $\leq_{\mathscr{P}}$, defined as a reflexive, antisymmetric, and transitive
- relation [20]. Then, \mathscr{P} and $\preceq_{\mathscr{P}}$ define the partially ordered set (poset) $\langle \mathscr{P}, \preceq_{\mathscr{P}} \rangle$. The least
- and maximum elements of a poset are called bottom and top, and are denoted by $\perp_{\mathscr{D}}$ and $\top_{\mathscr{D}}$,
- respectively. A set $S \subseteq \mathcal{P}$ is *directed* if each pair of elements $x, y \in S$ has an upper bound. A
- poset is a directed complete partial order (DCPO) if each of its directed subsets has a top, and it 36
- is a complete partial order (CPO) if it has a bottom as well. A chain is a subset $S \subseteq \mathscr{P}$ where 37
- all elements are comparable, i.e., for $x, y \in S$, $x \leq_{\mathscr{D}} y$ or $y \leq_{\mathscr{D}} x$. Conversely, an *antichain* is a
- subset $S \subseteq \mathscr{P}$ where no elements are comparable, i.e., for $x, y \in S$, $x \prec_{\mathscr{P}} y$ implies x = y. A map
- $g: \mathscr{P} \to \mathscr{Q}$ between two posets is *monotone* iff $x \leq_{\mathscr{P}} y$ implies $g(x) \leq_{\mathscr{Q}} g(y)$.
- Mathematical Theory of Co-Design 41
- 42 As in [1], we abstract a Design Problem (DP) as a monotone map h between provided function-

alities and the antichain of required resources, represented as elements of the CPOs $\langle \mathscr{F}, \preceq_{\mathscr{F}} \rangle$, $\langle \mathscr{R}, \preceq_{\mathscr{R}} \rangle$, respectively. Different to classical approaches, mostly relying on properties such as continuity, linearity, or convexity, our approach only requires monotone relations between the antichain of resources and the functionalities. The Co-Design Problem (CDP) of the full system results then from the interconnection, typically given in form of a graph, of the DP of its individual components. Indeed, this allows to describe complex models in a modular and compositional fashion. We focus on the problem of finding the antichain of all rational resources $r_1, \ldots, r_N \in \mathscr{R}$ which provide a given functionality $f \in \mathscr{F}$. Nevertheless, the framework can readily accommodate alternative problem formulations, such as finding the antichain of all rational functionalities $f_1, \ldots, f_N \in \mathscr{F}$ which are provided given a resource $r \in \mathscr{R}$. Rather than computing a single solution, this method provides therefore an antichain, or equivalently, a set of incomparable rational

13 4. Co-Design of AV-enabled Mobility Systems

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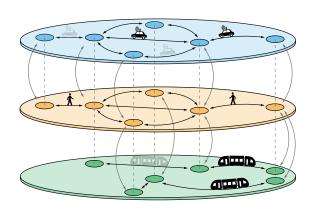
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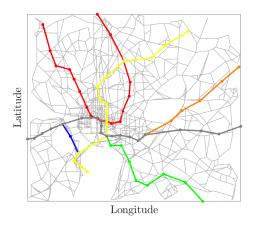
In this section, we instantiate our proposed co-desing framework in the setting whereby a central, social welfare maximizing authority (e.g., a central authority) strives to co-design a mobility sys-15 tem comprising AMoD and public transportation, in terms of AV fleet size, vehicle-specific characteristics, and public transit service frequency. This rather idealized setting serves a number of 17 purposes: First, it grounds our co-design framework within a concrete urban transportation design 19 problem. Second, the insights we derive can be interpreted as upper bounds on the performance gains one might achieve via co-design. Third, this setting subsumes as special cases the co-design 20 21 of AV and AMoD services (of interest, e.g., to AV and mobility-as-a-service companies alike) and the co-design of AMoD and intermodal transportation systems (of interest, e.g., to municipal au-23 thorities). Fourth, it provides a starting point to address the more challenging (and more realistic) 24 setting whereby multiple stakeholders, with different objectives, might converge via co-design to 25 an optimized transportation system.

We start by describing in Section 4.1 the urban transportation design problem we want to address in this paper; we then present its associated co-desing framework in Section 4.2.

28 4.1. Intermodal AMoD Framework

- In this section, we present the I-AMoD framework from [4] used to describe our setting. We adopt a mesoscopic planning perspective and formulate the problem as a multi-commodity network flow problem, whereby we allow customers to be routed in an intermodal fashion.
- 32 4.1.1. Multi-Commodity Flow Model
- 33 The transportation system and its different modes are modeled using the digraph $\mathscr{G} = (\mathscr{V}, \mathscr{A})$,
- 34 shown in Figure 1a. It is composed of a set of nodes $\mathscr V$ and a set of arcs $\mathscr A\subseteq\mathscr V\times\mathscr V$. Specifically,
- 35 it contains a road network layer $\mathscr{G}_R = (\mathscr{V}_R, \mathscr{A}_R)$, a public transportation layer $\mathscr{G}_P = (\mathscr{V}_P, \mathscr{A}_P)$, and a
- 36 walking layer $\mathscr{G}_W = (\mathscr{V}_W, \mathscr{A}_W)$. The road network is characterized through intersections $i \in \mathscr{V}_R$ and
- 37 road segments $(i, j) \in \mathcal{A}_R$. Similarly, public transportation lines are modeled through station nodes
- (v, y) cork. Similarly, profile transportation may be a selected in order
- 38 $i \in \mathcal{V}_P$ and line segments $(i, j) \in \mathcal{A}_P$. The walking network contains walkable streets $(i, j) \in \mathcal{A}_W$
- 39 connecting intersections $i \in \mathcal{V}_W$. Our model allows mode-switching arcs $\mathscr{A}_C \subseteq \mathscr{V}_R \times \mathscr{V}_W \cup \mathscr{V}_W \times \mathscr{C}_W \cup \mathscr{C}_W \times \mathscr{C}_W \times \mathscr{C}_W \cup \mathscr{C}_W \times \mathscr{C}_W \times \mathscr{C}_W \cup \mathscr{C}_W \times \mathscr{C}_W \cup \mathscr{C}_W \times \mathscr{C}_W \cup \mathscr{C}_W \times \mathscr{C}_W \times \mathscr{C}_W \cup \mathscr{C}_W \times \mathscr{C}_W \times \mathscr{C}_W \cup \mathscr{C}_W \times \mathscr{C$
- 40 $\mathcal{V}_R \cup \mathcal{V}_P \times \mathcal{V}_W \cup \mathcal{V}_W \times \mathcal{V}_P$ connecting the road and the public transportation layers to the pedestrian
- 41 layer. Consequently, $\mathscr{V} = \mathscr{V}_W \cup \mathscr{V}_R \cup \mathscr{V}_P$ and $\mathscr{A} = \mathscr{A}_W \cup \mathscr{A}_R \cup \mathscr{A}_P \cup \mathscr{A}_C$. Consistently with the
- 42 structural properties of road and walking networks in urban environments, we assume the graph \mathscr{G}





(a) Intermodal AMoD network.

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(b) Washington D.C. road and subway graphs.

FIGURE 1: (a) The intermodal AMoD network consists of a road, a walking, and a public transportation digraph. The coloured circles represent stops or intersections and the black arrows denote road links, pedestrian pathways, or public transit arcs. The dotted lines represent nodes which are close geographically, while the grey arrows represent the mode-switching arcs connecting them. (b) The Washington D.C. transportation network, consisting of the MetroRail subway lines and the city roads.

to be strongly connected. We model a travel request ρ as a triple $(o,d,\alpha) \in \mathcal{V} \times \mathcal{V} \times \mathbb{R}_+$, described by its origin node o, its destination node d, and its request rate $\alpha > 0$, namely, how many customers want to travel from o to d per unit time. We assume that the origin and destination vertices of the *M* requests lie in the walking digraph, i.e., $o_m, d_m \in \mathcal{V}_W$ for all $m \in \mathcal{M} := \{1, \dots, M\}$.

The flow $f_m(i,j)$ represents the number of customers per unit time traversing arc $(i,j) \in \mathcal{A}$ and satisfying a travel request m. Furthermore, $f_0(i, j)$ denotes the flow of empty vehicles on road arcs $(i,j) \in \mathscr{A}_R$, accounting for rebalancing flows of AMoD vehicles between a customer's dropoff and the next customer's pick-up. Assuming the vehicles to carry one customer at a time, the flows satisfy

$$\sum_{i:(i,j)\in\mathscr{A}} f_m(i,j) + \mathbb{1}_{j=o_m} \cdot \alpha_m = \sum_{k:(j,k)\in\mathscr{A}} f_m(j,k) + \mathbb{1}_{j=d_m} \cdot \alpha_m, \quad \forall m \in \mathscr{M}, j \in \mathscr{V}$$
 (1a)

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$$\sum_{i:(i,j)\in\mathscr{A}} f_m(i,j) + \mathbb{1}_{j=o_m} \cdot \alpha_m = \sum_{k:(j,k)\in\mathscr{A}} f_m(j,k) + \mathbb{1}_{j=d_m} \cdot \alpha_m, \quad \forall m \in \mathscr{M}, j \in \mathscr{V}$$
(1a)
$$\sum_{i:(i,j)\in\mathscr{A}_R} \left(f_0(i,j) + \sum_{m\in\mathscr{M}} f_m(i,j) \right) = \sum_{k:(j,k)\in\mathscr{A}_R} \left(f_0(j,k) + \sum_{m\in\mathscr{M}} f_m(j,k) \right), \quad \forall j \in \mathscr{V}_R$$
(1b)

12
$$f_m(i,j) \ge 0, \quad \forall m \in \mathcal{M}, (i,j) \in \mathcal{A}$$
 (1c)

$$f_0(i,j) \ge 0, \quad \forall (i,j) \in \mathscr{A}_{\mathbb{R}}, \tag{1d}$$

where $\mathbb{1}_{i=x}$ denotes the boolean indicator function. Specifically, (1a) guarantees flows conservation

for every transportation demand, and (1b) preserves flow conservation for vehicles on every road 16

node. Combining conservation of customers (1a) with the conservation of vehicles (1b) guarantees 17

rebalancing vehicles to match the demand. Finally, (1c), (1d) ensure non-negativity of flows. 18

1 4.1.2. Travel Time and Travel Speed

- 2 The variable t_{ij} denotes the time needed to traverse an arc (i, j) of length s_{ij} . We assume a constant
- 3 walking speed on pedestrian arcs and infer travel times on public transportation arcs from the
- 4 public transit schedules. Considering that the public transportation system at node j operates with
- 5 the frequency φ_i , switching from a pedestrian vertex i to a public transit station j takes, on average,
- 6 $t_{\rm WS} + 1/\varphi_j$, where $t_{\rm WS}$ is a constant sidewalk-to-station travel time. We assume that the average
- 7 waiting time for AMoD vehicles is t_{WR} and that switching from the road graph and the public
- 8 transit graph to the pedestrian graph takes the transfer times $t_{\rm RW}$ and $t_{\rm SW}$, respectively. While each
- 9 road arc $(i, j) \in \mathcal{A}_R$ is characterized by a speed limit $v_{L,ij}$, AVs safety protocols impose a maximum
- 10 achievable velocity v_a . In order to prevent too slow and therefore dangerous driving behaviours
- 11 [21], we only consider road arcs through which the AVs can drive at least at a fraction β of the
- 12 speed limit: Arc $(i, j) \in \mathcal{A}_R$ is kept in the road network if and only if

$$v_{a} \geq \beta \cdot v_{L,ij}, \tag{2}$$

14 where $\beta \in (0,1]$. We set the velocity of all arcs fulfilling condition (2) to $v_{ij} = \min\{v_a, v_{L,ij}\}$ and

15 compute the travel time to traverse them as

$$t_{ij} = \frac{s_{ij}}{v_{ij}}. (3)$$

- 17 4.1.3. Road Congestion
- In our setting, we assume that each road arc $(i, j) \in \mathcal{A}_R$ is subject to a baseline usage u_{ij} , capturing
- 19 the presence of exogenous traffic (e.g., private vehicles), and that it has a nominal capacity c_{ij} .
- 20 Furthermore, we assume that the central authority operates the AMoD fleet such that vehicles
- 21 travel at free-flow speed throughout the road network of the city, meaning that the total flow on
- 22 each road link must be below the link's capacity. Therefore, we capture congestion effects with the
- 23 threshold model

24
$$f_0(i,j) + \sum_{m \in \mathcal{M}} f_m(i,j) + u_{ij} \le c_{ij} \quad \forall (i,j) \in \mathcal{A}_{\mathbb{R}}.$$
 (4)

- 25 4.1.4. Energy Consumption
- 26 We compute the energy consumption of the AVs for each road link considering an urban driving
- 27 cycle, scaled so that the average speed $v_{\text{avg,cycle}}$ matches the free-flow speed on the link s_{ij}/t_{ij} , and
- 28 scale the energy consumption with the length of the arc s_{ij} as

29
$$e_{ij} = e_{\text{cycle}} \cdot \frac{s_{ij}}{s_{\text{cycle}}} \quad \forall (i,j) \in \mathcal{A}_{\mathbf{R}}.$$
 (5)

- 30 For the public transportation system, we assume a constant energy consumption per unit time. This
- 31 approximation is acceptable in urban environments, as the operation of the public transportation
- 32 system is independent from the number of customers serviced, and its energy consumption is
- 33 therefore customers-invariant.
- 34 *4.1.5.* Fleet Size
- We consider a fleet of $n_{v,max}$ AVs. In a time-invariant setting, the number of vehicles on arc (i, j) is
- expressed as the multiplication of the total vehicles flow on the arc and its travel time. Therefore,

1 we constrain the number of vehicles employed as

$$n_{\text{v,e}} = \sum_{(i,j)\in\mathscr{A}_{\mathbf{R}}} \left(f_0(i,j) + \sum_{m\in\mathscr{M}} f_m(i,j) \right) \cdot t_{ij} \le n_{\text{v,max}}.$$
 (6)

- 3 *4.1.6. Discussion*
- 4 A few comments are in order. First, we assume the demand to be time-invariant and allow flows to
- 5 have fractional values. This assumption is in line with the *mesoscopic* and system-level *planning*
- 6 perspective of our study. Second, we model congestion using a threshold model. This approach
- 7 can be interpreted as the municipal authority not allowing the AMoD vehicles to exceed the critical
- 8 density of the flows on road arcs, so that cars can be assumed to travel at free flow speed [22]. This
- 9 way, we can assume that the route planning of AMoD vehicles does not influence the exogenous
- 10 traffic. Finally, in line with the status quo, we allow AMoD vehicles to transport one customer at
- 11 the time [23]. For further discussions on our modeling assumptions, we refer the readers to [4, 24].

2 **4.2. Co-Design Framework**

- 13 We integrate the I-AMoD framework presented in Section 4.1 in the co-design formalism, allow-
- 14 ing the decoupling of the CDP of a complex system in the DP of its individual components in a
- 15 modular, compositional, and systematic fashion. We aim to compute the antichain of resources,
- 16 quantified in terms of costs, average travel time per trip, and emissions required to provide the
- 17 mobility service to a set of customers. In order to achieve this, we decouple the CDP in the DPs
- 18 of the individual AV (Section 4.2.1) and of the AVs fleet (Section 4.2.3) as well as of the public
- 19 transportation system (Section 4.2.2). Their interconnection is presented in Section 4.2.4.
- 20 4.2.1. The Autonomous Vehicle Design Problem
- 21 The AV DP (Figure 2a) consists of selecting the maximal speed of the AVs. Under the rationale
- 22 that driving safely at higher speed requires more advanced sensing and algorithmic capabilities,
- 23 we model the achievable speed of the AVs v_a as a monotone function of the vehicle fixed costs $C_{v,f}$
- 24 (resulting from the cost of the vehicle $C_{v,v}$ and the cost of its automation $C_{v,a}$) and the mileage-
- 25 dependent operational costs $C_{v,o}$ (accounting for maintenance, cleaning, energy consumption, de-
- preciation, and opportunity costs [25]). In this setting, the AV DP provides the functionality v_a and
- 27 requires the resources $C_{v,f}$ and $C_{v,o}$. Consequently, the functionality space is $\mathscr{F}_v = \overline{\mathbb{R}}_+$ (in mph),
- 28 and the resources space is $\mathscr{R}_{v} = \overline{\mathbb{R}}_{+} \times \overline{\mathbb{R}}_{+}$ (in USD × USD/mile).
- 29 4.2.2. The Subway Design Problem
- 30 We design the public transit infrastructure (Figure 2b) by means of the service frequency intro-
- duced in Section 4.1.2. Specifically, we assume the service frequency φ_i to scale linearly with the
- 32 size of the train fleet n_s as

$$\frac{\varphi_j}{\varphi_{j,\text{baseline}}} = \frac{n_{\text{S}}}{n_{\text{S,baseline}}}.$$
 (7)

- We relate a train fleet of size n_s to the fixed costs $C_{s,f}$ (accounting for train and infrastructural
- costs) and to the operational costs $C_{s,o}$ (accounting for energy consumption, vehicles depreciation,
- 36 and train operators' wages). Given the passengers-independent public transit operation in today's
- 37 cities, we reasonably assume the operational costs $C_{s,o}$ to be mileage independent and to only

- 1 vary with the size of the fleet. Formally, the number of acquired trains $n_{s,a} = n_s n_{s,baseline}$ is
- 2 a functionality, whereas $C_{s,f}$ and $C_{s,o}$ are resources. The functionality space is $\mathscr{F}_s = \overline{\mathbb{N}}$ and the
- 3 resources space is $\mathcal{R}_s = \overline{\mathbb{R}}_+ \times \overline{\mathbb{R}}_+$ (in USD × USD/year).
- 4 4.2.3. The I-AMoD Optimization Framework Design Problem
- 5 The I-AMoD DP (see Figure 2c) provides the demand satisfaction as a functionality, expressed
- 6 through the total customer request rate

$$7 \alpha_{\text{tot}} := \sum_{m \in \mathcal{M}} \alpha_m. (8)$$

- 8 To successfully satisfy a given set of travel requests, we require the following resources: (i) the
- 9 achievable speed of the AVs v_a , (ii) the number of available AVs per fleet $n_{v,max}$, (iii) the number
- of trains $n_{s,a}$ acquired by the public transportation system, and (iv) the average travel time of a trip

11
$$t_{\text{avg}} := \frac{1}{\alpha_{\text{tot}}} \cdot \sum_{m \in \mathscr{M}, (i,j) \in \mathscr{A}} t_{ij} \cdot f_m(i,j), \tag{9}$$

12 (v) the total distance driven by the AVs per unit time

13
$$s_{\text{v,tot}} := \sum_{(i,j) \in \mathscr{A}_{\mathbf{R}}} s_{ij} \cdot \left(f_0(i,j) + \sum_{m \in \mathscr{M}} f_m(i,j) \right), \tag{10}$$

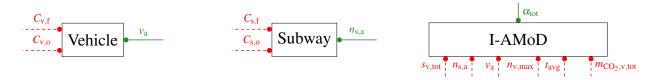
14 and (vi) the total AVs CO₂ emissions per unit time

15
$$m_{\text{CO}_2, \text{v,tot}} := \gamma \cdot \sum_{(i,j) \in \mathcal{A}_{\mathbf{R}}} e_{ij} \cdot \left(f_0(i,j) + \sum_{m \in \mathcal{M}} f_m(i,j) \right),$$
 (11)

- where γ relates the energy consumption and the CO₂ emissions. We assume that customers trips
- 17 and AMoD rebalancing strategies are chosen to maximize the customers welfare, defined through
- 18 the average travel time t_{avg} . Hence, we link the functionality and resources of the I-AMoD DP
- 19 through the following optimization problem:

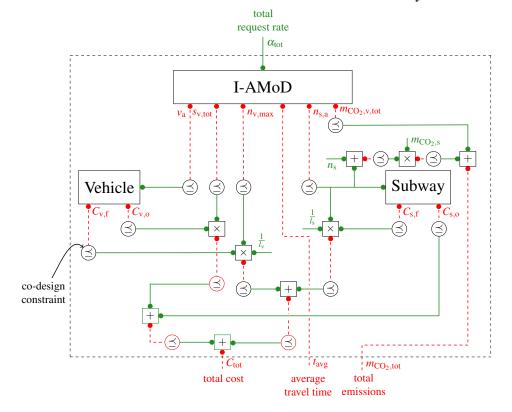
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$$\min_{\{f_m(\cdot,\cdot)\}_m, f_0(\cdot,\cdot)} t_{\text{avg}} = \frac{1}{\alpha_{\text{tot}}} \sum_{m \in \mathscr{M}, (i,j) \in \mathscr{A}} t_{ij} \cdot f_m(i,j) \quad \text{s.t. Eq. (1), Eq. (4), Eq. (6)}.$$
 (12)

- 21 Formally, $\mathscr{F}_{o} = \overline{\mathbb{R}}_{+}$, and $\mathscr{R}_{o} = \overline{\mathbb{R}}_{+} \times \overline{\mathbb{N}} \times \overline{\mathbb{N}} \times \overline{\mathbb{R}}_{+} \times \overline{\mathbb{R}}_{+} \times \overline{\mathbb{R}}_{+}$. Note that in general, the optimization
- 22 problem (12) might possess multiple optimal solutions, making the relation between resources and
- 23 functionality ill-posed. To overcome this subtlety, if two solutions share the same average travel
- 24 time, we select the one incurring in the *lowest* mileage.
- 25 4.2.4. The Monotone Co-Design Problem
- 26 The full-system CDP results from the interconnection of the DPs presented above. A schematic
- 27 representation is shown in Figure 2d. The functionality of the system is to provide mobility service
- 28 to the customers, quantified, as in (8), by means of the total request rate. To this end, the following
- 29 three resources are required. First, on the customers side, we require an average travel time, defined



(a) Design problem of the au- (b) Design problem of the subway (c) Design problem of the I-tonomous vehicles.

AMoD system.



(d) Co-design problem of the full system.

FIGURE 2: Schematic representation of the individual design problems (a-c) as well as of the codesign problem of the full system (d). In solid green the provided functionalities and in dashed red the required resources. The edges in the co-design diagram (d) represent co-design constraints: The resources required by a first design problem are the lower bound for the functionalities provided by the second one.

- 1 as in (9). Second, on the central authority side, the resource is the total transportation cost of the
- 2 intermodal mobility system: Assuming an average vehicles' life of l_v , an average trains' life of l_s ,
- 3 and a baseline subway fleet of $n_{s,baseline}$ trains, we express the total costs as

$$4 C_{\text{tot}} = C_{\text{v}} + C_{\text{s}}, (13)$$

1 where C_v is the AVs-related cost

$$C_{v} = \frac{C_{v,f}}{l_{v}} \cdot n_{v} + C_{v,o} \cdot s_{v,tot}, \tag{14}$$

and C_s is the public transit-related cost

4
$$C_{\rm s} = \frac{C_{\rm s,f}}{l_{\rm s}} \cdot n_{\rm s,a} + C_{\rm s,o}.$$
 (15)

5 Third, on the environmental side, the resources is the total CO_2 emissions

$$6 m_{\text{CO}_2,\text{tot}} = m_{\text{CO}_2,\text{v,tot}} + m_{\text{CO}_2,\text{s}} \cdot n_{\text{s}}, (16)$$

7 where $m_{\text{CO}_2,s}$ represents the CO₂ emissions of a single train. Formally, α_{tot} is the CDP function-

8 ality, whereas t_{avg} , C_{tot} , and $m_{CO_2,tot}$ are the resources. Consistently, the functionality space is

9 $\mathscr{F} = \overline{\mathbb{R}}_+$ and the resources space is $\mathscr{R} = \overline{\mathbb{R}}_+ \times \overline{\mathbb{R}}_+ \times \overline{\mathbb{R}}_+$. Note that the resulting CDP is indeed

monotone, since it consists of the interconnection of monotone DPs [1].

11 4.3. Discussion

- 12 A few comments are in order. First, we lump the vehicle autonomy in its achievable velocity.
- 13 We leave to future research more elaborated AV models, accounting for instance for accidents
- 14 rates [26] and for safety levels. Second, we assume the service frequency of the subway system
- 15 to scale linearly with the number of trains. We inherently rely on the assumption that the existing
- 16 infrastructure can homogeneously accommodate the acquired train cars. To justify the assumption,
- 17 we include an upper bound on the number of potentially acquirable trains in our case study design
- in Section 5. Third, we highlight that the I-AMoD framework is only one of the many feasible
- 19 ways to map total demand to travel time, costs, and emissions. Specifically, practitioners can easily
- 20 replace the corresponding DP with more sophisticated models (e.g., simulation-based frameworks
- 21 like MATSim [27]), as long as the monotonicity of the system is preserved. In our setting, we
- 22 conjecture the customers and vehicles routes to be centrally controlled by the central authority in a
- 23 socially-optimal fashion. Fourth, we assume a homogenous fleet of AVs. Nevertheless, our model
- 24 is readily extendable to capture heterogeneous fleets. Finally, we consider a fixed travel demand,
- 25 and compute the antichain of resources providing it. Nonetheless, our formalization can be readily
- 26 extended to arbitrary demand models preserving the monotonicity of the CDP (accounting for
- 27 instance for elastic and stochastic effects). We leave this topic to future research.

28 5. Results

- 29 In this section, we leverage the framework presented in Section 4 to evaluate the real-world case
- 30 of Washington D.C., USA. Section 5.1 details the case study. We then present numerical results in
- 31 Sections 5.2 and 5.3.

32 5.1. Case Study

- 33 We present our studies on the real-world case of Washington D.C., USA. We import the road net-
- work (Figure 1b) and its features from OpenStreetMap [28]. The public transit network and its
- 35 schedules are extracted from the GTFS data [29]. The travel demand is obtained by unifying the
- origin-destination pairs of the morning peak of May 31st 2017 provided by the taxi companies [30]

and the Washington Metropolitan Area Transit Authority (WMATA) [23]. Given the lack of reliable demand data for the MetroBus system, we focus our studies on the MetroRail system and its design, inherently assuming MetroBus commuters to be unaffected by our design methodology. To account for the large presence of ride-hailing companies, we scale the taxi demand rate by a factor of 5 [31]. Overall, the demand dataset includes 15,872 travel requests, corresponding to a demand rate of 24.22 requests/s. To account for congestion effects, we compute the nominal road capacity as in [32] and assume an average baseline road usage of 93%, in line with [33]. We summarize the main parameters together with their bibliographic sources in Table 1. In the remainder of this section, we tailor and solve the co-design problem presented in Section 4 through the PyM-10 CDP solver [34], and investigate the influence of different AVs costs on the design objectives and strategies.

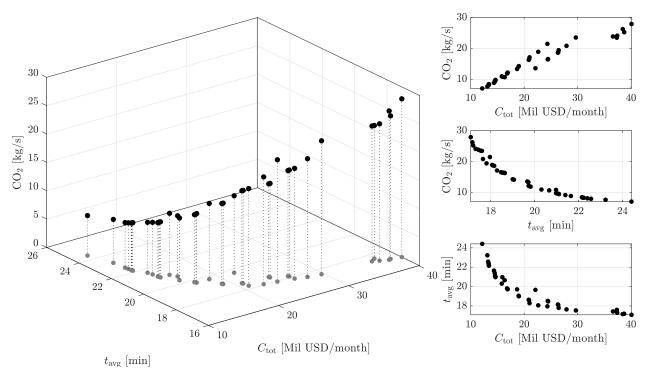
Parameter Baseline road usage		Variable u_{ij}			Value 93			Units %	Source [33]
			Case 1	Case 2.1	Case 2.2	Case 3.1	Case 3.2		
Vehicle operational cost		$C_{\rm v,o}$	0.084	0.084	0.062	0.084	0.084	USD/mile	[35, 36]
Vehicle cost		$C_{ m v,v}$	32,000	32,000	26,000	32,000	32,000	USD/car	[35]
	20 mph		15,000	20,000	3,700	0	500,000	USD/car	[36-40]
	25 mph		15,000	30,000	4,400	0	500,000	USD/car	[36-40]
	30 mph		15,000	55,000	6,200	0	500,000	USD/car	[36-40]
Vehicle automation cost	35 mph	$C_{ m v,a}$	15,000	90,000	8,700	0	500,000	USD/car	[36-40]
	40 mph		15,000	115,000	9,800	0	500,000	USD/car	[36-40]
	45 mph		15,000	130,000	12,000	0	500,000	USD/car	[36-40]
	50 mph		15,000	150,000	13,000	0	500,000	USD/car	[36-40]
Vehicle life		$l_{ m v}$	5	5	5	5	5	years	[35]
CO ₂ per Joule		γ	0.14	0.14	0.14	0.14	0.14	g/kJ	[41]
Time from \mathscr{G}_W to \mathscr{G}_R		$t_{ m WR}$	300	300	300	300	300	S	-
Time from \mathscr{G}_R to \mathscr{G}_W		$t_{ m RW}$	60	60	60	60	60	S	-
Speed limit fraction		β	$\frac{1}{1.3}$	$\frac{1}{1.3}$	$\frac{1}{1.3}$	$\frac{1}{1.3}$	$\frac{1}{1.3}$	-	[21]
Subway operational cost	100 %				148,000,000			USD/year	[42]
	133 %	$C_{\mathrm{s,o}}$			197,000,000			USD/year	[42]
	200 %				295,000,000			USD/year	[42]
Subway fixed cost		$C_{ m s,f}$			14,500,000			USD/train	[43]
Train life		$l_{\rm s}$			30			years	[43]
Subway CO ₂ emissions per train		$m_{\text{CO}_2,s}$			140			ton/year	[44]
Train fleet baseline		$n_{\rm s,baseline}$			112			trains	[43]
		$\varphi_{j,\text{baseline}}$			$\frac{1}{6}$			1/minutes	[45]
Time from \mathscr{G}_W to \mathscr{G}_P and vice-versa		$t_{ m WS}$			60			S	-

TABLE 1: Parameters, variables, numbers, and units for the case studies.

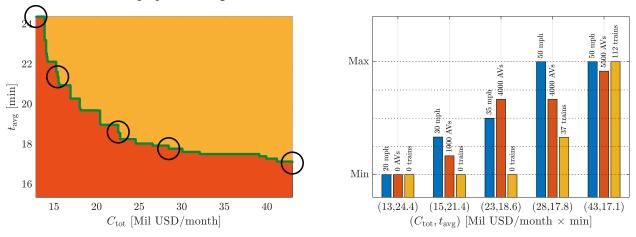
12 **5.2.** Case 1 - Constant Cost of Automation

In line with [36–40], we first assume an average achievable-velocity-independent cost of automation. As discussed in Section 4, we design the system by means of subway service frequency, AVs fleet size, and achievable free-flow speed. Specifically, we allow the municipality to (i) increase the subway service frequency φ_j by a factor of 0%, 33%, or 100%, (ii) deploy an AMoD fleet of size $n_{v,max} \in \{0,500,1000,...,6000\}$ vehicles, and (iii) design the single AV achievable velocity $v_a \in \{20 \text{ mph}, 25 \text{ mph}, ..., 50 \text{ mph}\}$. We assume the AMoD fleet to be composed of battery electric BEV-250 mile vehicles [35]. In Figure 3a, we show the solution of the co-design problem by reporting the antichain consisting of the total transportation cost, average travel time, and total CO₂ emissions. These solutions are *rational* (and not comparable) in the sense that there exists

no instance which simultaneously yields lower cost, average travel time, and emissions. For the



(a) Tri-dimensional representation antichain elements and their projection in the cost-time space (left) and their two-dimensional projections (right).



(b) Results for asymptotic automation costs. On the left, the two-dimensional representation of the antichain elements: in red are the unfeasible strategies, in orange the feasible but irrational solutions, and in green the Pareto front. On the right, the implementations corresponding to the highlighted antichain elements, quantified in terms of achievable vehicle speed, AVs fleet size, and train fleet size.

FIGURE 3: Solution of the Co-Design Problem (CDP) for the state-of-the art case.

ing the emissions in the total cost. To do so, we consider the conversion factor 40 USD/kg [46]. 2 Note that since this transformation preserves the monotonicity of the CDP it smoothly integrates in our framework. Doing so, we can conveniently depict the co-design strategies through the twodimensional antichain (Figure 3b, right) and the corresponding municipality actions (Figure 3b, left). Generally, as the municipality budget increases, the average travel time per trip required to satisfy the given demand decreases, reaching a minimum of about 17.1 minutes with a monthly expense of around 43,000,000 USD/month. This configuration corresponds to a fleet 5,500 AVs able to drive at 50 mph and to the doubling of the current MetroRail train fleet. On the other hand, the smallest rational investment of 12,900,000 USD/month leads to a 42 % higher average travel time, 10 corresponding to a non-existent autonomous fleet and an unchanged subway infrastructure. No-11 tably, an expense of 23,000,000 USD/month (48 % lower than the highest rational investment) only increases the minimal required travel time by 9 %, requiring a fleet of 4,000 vehicles able to drive at 35 mph and no acquisition of trains. Conversely, an investment of 15,600,000 USD/month (just 2,700,000 USD/month more than the minimal rational investment) provides a 3 min shorter travel time. Remarkably, the design of AVs able to exceed 40 mph only improves the average travel time 16 by 6 %, and it is rational just starting from an expense of 22,800,000 USD/month. This suggests that the design of faster vehicles mainly results in higher emission rates and costs, without substantially 17 contributing to a more time-efficient demand satisfaction. Finally, it is rational to improve the sub-18 way system only starting from a budget 28,500,000 USD/month, leading to a travel time improvement 20 of just 4%. This trend can be explained with the high train acquisition and increased operation costs, related to the subway reinforcement. We expect this phenomenon to be more marked for 21 other cities, considering the moderate operation costs of the MetroRail subway system due to its 22 automation [45] and related benefits [47].

5.3. Case 2 - Speed-Dependent Automation Costs 24

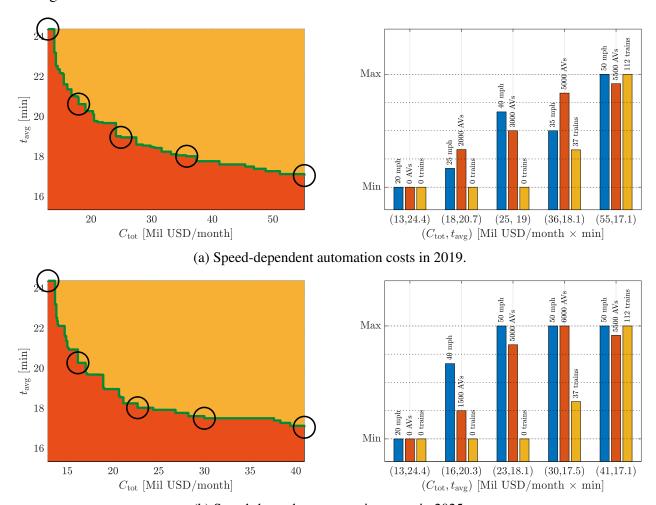
- 25 To relax the potentially unrealistic assumption of a velocity-independent automation cost, we con-
- sider a performance-dependent cost structure. The large variance in sensing technologies and their 26
- reported performances [48] suggests that this rationale is reasonable. Indeed, the technology re-27
- quired today to safely operate an autonomous vehicle at 50 mph is substantially more sophisticated,
- and therefore more expensive, than the one needed at 20 mph. To this end, we adopt the cost struc-
- 30 ture reported in Table 1. Furthermore, the frenetic evolution of automation techniques intricates
- their monetary quantification [49]. Therefore, we perform our studies with current (2019) costs as
- well as with their projections for the upcoming decade (2025) [35, 50]. 32

33 5.3.1. Case 2.1 - 2019

23

- Here, we study the hypothetical case of an immediate AVs fleet deployment, assuming the techno-
- logical advances to be provided. We introduce the aforementioned velocity-dependent automation 35
- cost structure and obtain the results reported in Figure 4a. Comparing these results with the state-
- of-the-art values presented in Figure 3 confirms the previously observed trend concerning elevated 37
- vehicle speeds. Indeed, spending 24,900,000 USD/month (55 % lower than the highest rational ex-
- pense) only increases the average travel time by 10 %, requiring a fleet of 3,000 AVs at 40 mph and
- no subway interventions. Nevertheless, the comparison shows two substantial differences. First, 40
- the budget required to reach the minimum travel time of 17.1 minutes is 28 % higher compared to 41
- the previous case, and consists of the same strategy for the municipality, i.e., doubling the train 42
- fleet and having a fleet of 5,500 AVs at 50 mph. Second, the higher vehicle costs result in an av-

1 erage AVs fleet growth of 5%, an average velocity reduction of 9%, and an average train fleet
 2 growth of 7%. The latter suggests a shift towards a poorer AVs performance in favour of fleets enlargements.



(b) Speed-dependent automation costs in 2025.

FIGURE 4: Results for the speed-dependent automation costs. On the left, the two-dimensional representation of the antichain elements: in red are the unfeasible strategies, in orange the feasible but irrational solutions, and in green the Pareto front. On the right, the implementations corresponding to the highlighted antichain elements.

5.3.2. Case 2.2 - 2025

3

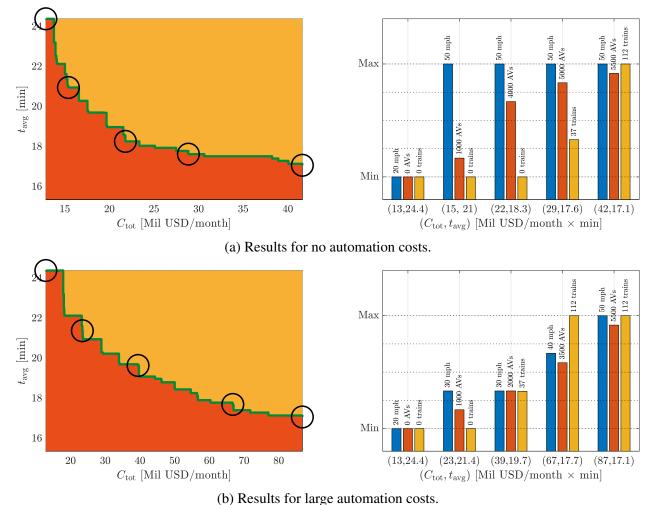
Experts forecast a large automation cost reduction (up to 90%) in the next decade, due to massforecast a large automation cost reduction (up to 90%) in the next decade, due to massforecast a large automation cost reduction, we inspect the futuristic forecast a large automation cost reduction, we inspect the futuristic forecast a large automation cost reduction, we inspect the futuristic forecast a large automation cost reduction, we inspect the futuristic forecast a large automation cost reduction in automation, we inspect the futuristic forecast a large automation cost reduction in automation, we inspect the futuristic forecast a large automation (up to 90%) in the next decade, due to massforecast a large automation (up to 90%) in the next decade, due to massforecast a large automation (up to 90%) in the next decade, due to massforecast a large automation (up to 90%) in the next decade, due to massforecast a large automation (up to 90%) in the next decade, due to massforecast a large automatic forecast and report the results for a large automation cost, and report the results for a large automation cost and report the results for a large automation cost, and report the results for a large automation, we inspect the futuristic for a large automation, we inspect the futuristic for a large automation cost, and report the results for a large automation cost, and report the results for a large automation cost, and report the results for a large automation cost, and report the results for a large automation cost, and report the results for a large automation cost, and report the results for a large automation cost, and report the results for a large automation cost, and report the results for a large automation cost, and report the results for a large automation cost, and report the results for a large automation cost, and report the results for a large automation cost, and report the results for a large automation cost, and report the results for a large automation cost, and report the results for a l

1 5.4. Case 3 - Asymptotic Automation Cost Analysis

- 2 We conclude our numerical analysis with a study on asymptotic cost structures. Specifically, we
- 3 compare the constrasting cases of a free-of-charge and a very high (500,000 USD/car) automation
- 4 cost.

5 5.4.1. Case 3.1- No Automation Cost

- 6 This case could represent the future full deployment of AVs, where the cost of automation is
- 7 naturally included in the normal production costs and does not represent an additional expense.
- 8 The results for this cost structure are reported in Figure 5a. Notably, the Pareto front is very
- 9 similar to the one presented in Figure 3, leading to just a 5% increase in the AVs speed and to
- 10 invariate fleet sizes. Clearly, the assumption a cost-free automation favours the deployment of AVs
- 11 at the expenses of subway improvements.



(b) Results for large automation costs.

FIGURE 5: Results for asymptotic automation costs. On the left, the two-dimensional representation of the antichain elements: in red are the unfeasible strategies, in orange the feasible but irrational solutions, and in green the Pareto front. On the right, the implementations corresponding to the highlighted antichain elements.

1 5.4.2. Case 3.2- High Automation Cost

- 2 In this case we assume a performance-independent automation cost of 500,000 USD/car. Although
- 3 this cost may appear unreasonably large, it roughly captures the extremely onerous research and
- 4 development costs which AVs companies are facing today [51]. Indeed, no company has shown the
- 5 ability to safely and reliably deploy large fleets of AVs yet. The results, reported in Figure 5b, show
- 6 different trends from the ones depicted in Figure 5a. First, we observe substantial shift towards
- 7 an increase of 163 % in the average train fleet size, followed by a 17 % decrease in the average
- 8 AVs fleet size. Second, to reach the minimal rational average travel time, one needs an expense of
- 9 roughly 87,000,000 USD/month, corresponding to a 107 % higher investment.

5.5. Discussion

A few comments are in order. First, the presented case studies illustrate the ability of our framework to extract the set of rational design strategies for an AVs-enabled mobility system. This way, stakeholders such as AVs companies, transportation authorities, and policy makers get transparent and interpretable insights on the impact of future interventions. Second, we perform a sensitivity analysis (Figure 6) through the variation of the autonomy cost structures. On the one hand, this reveals a clear transition from small fleets of fast AVs (in the case of low autonomy costs) to a fleet of numerous slow vehicles (in the case of high autonomy costs). On the other hand, our studies highlight that investments in the public transit infrastructure are rational only when large budgets are available. Indeed, the onerous train acquisition and operation costs lead to a compara-

20 tive advantage of AVs-based mobility. In the future, we plan to collect more high-resolution data to corroborate our conclusions with quantitative results.

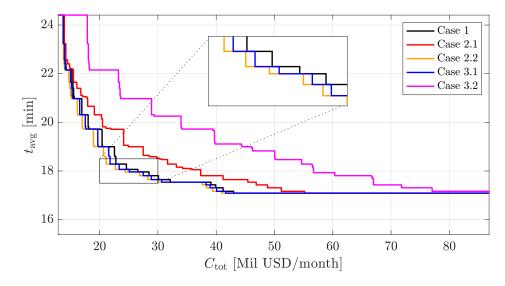


FIGURE 6: Comparison of the antichains resulting from different case studies.

22 **6. Conclusion**

21

In this paper, we leveraged the mathematical theory of co-design to propose a design framework for AVs-enabled mobility systems. Specifically, the nature of our framework allows both for the modular and compositional interconnection of the design problems of different mobility options

- and for multiple objectives. Starting from the multi-commodity flow model of an intermodal au-
- 2 tonomous mobility-on-demand system, we designed autonomous vehicles and public transit both
- 3 from a vehicle-centric and fleet-level perspective. In particular, we studied the problem of de-
- 4 ploying a fleet of self-driving vehicles providing on-demand mobility in cooperation with public
- 5 transit, adapting the speed achievable by the vehicles, the fleet size, and the service frequency of
- 6 the subway lines. Our framework allows the stakeholders involved in the mobility ecosystem, from
- 7 vehicle developers all the way to mobility-as-a-service companies and governmental authorities, to
- 8 characterize rational trajectories for technology and investment development. We showcased our
- 9 methodology on the real-world case study of Washington D.C., USA. Notably, we showed how
- 10 our problem formulation allows for a systematic analysis of incomparable objectives, providing
- stakeholders with analytical insights for the socio-technical design of AVs-enabled mobility sys-
- The state of the s
- 12 tems. This work opens the field for the following future research streams:
- 13 Modeling: First, we would like to extend the presented framework to capture additional modes of
- 14 transportation, such as buses, bikes, and e-scooters, and heterogeneous fleets with different self-
- 15 driving infrastructures, propulsion systems, and passenger capacity. Second, we would like to
- 16 include the possibility of accommodating the design of public transit lines. Third, we would like
- 17 to investigate variable demand models. Finally, we would like to analyze the interactions between
- 18 multiple stakeholders, characterizing the equilibrium arising from their conflicting interests.
- 19 Algorithms: It is of interest to tailor general co-design algorithmic frameworks to the particular
- 20 case of transportation design problems, possibly leveraging their specific structure.
- 21 Application: Finally, we would like to devise a web interface which supports mobility stakeholders
- 22 to reason on strategic interventions in urban areas.

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32 **8. Statement of Contributions**

- 33 The authors confirm contribution to the paper as follows: study conception and design: Gioele Zar-
- 34 dini, Nicolas Lanzetti, Mauro Salazar, Andrea Censi, and Marco Pavone, data collection: Gioele
- 35 Zardini, Nicolas Lanzetti, analysis and interpretation of results: Gioele Zardini, Nicolas Lanzetti,
- 36 Mauro Salazar, Andrea Censi, and Marco Pavone, draft manuscript preparation: Gioele Zardini,
- 37 Nicolas Lanzetti, Mauro Salazar, Andrea Censi, Emilio Frazzoli, and Marco Pavone.
- 38 All authors reviewed the results and approved the final version of the manuscript.

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