



# BoolMinGeo

Decay Analysis: 3D Minimization Beyond 8 Variables

9-16 Variable Boolean Functions

Total Tests: 72

Date: 2026-01-07

## EXPERIMENTAL SETUP & CONFIGURATION

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### STUDY INFORMATION

Study Type: Decay Analysis (3D minimization beyond 8 vars)  
Scope: 9-16 variable Boolean functions  
Total Tests: 72  
Date: 2026-01-07

### SYSTEM CONFIGURATION

Platform: Windows-11-10.0.26200-SP0  
Processor: Intel64 Family 6 Model 142 Stepping 12, GenuineIntel  
Python: 3.12.10

### SOFTWARE VERSIONS

NumPy: 2.3.4  
SciPy: 1.16.3  
Matplotlib: 3.10.7

### EXPERIMENTAL PARAMETERS

Random Seed: 42  
Variable Range: 9-12  
Tests per Distribution: 3

### TEST DISTRIBUTIONS

- Sparse: 20% ones, 5% don't-cares
- Dense: 70% ones, 5% don't-cares
- Balanced: 50% ones, 10% don't-cares
- Minimal DC: 45% ones, 2% don't-cares
- Heavy DC: 30% ones, 30% don't-cares
- Edge cases: all-zeros, all-ones, all-dc

### METRICS COLLECTED

- Execution time (seconds)
- Memory consumption (MB)
- Peak memory usage (MB)
- Solution complexity (literal count, term count)
- Time per truth table entry (ms)
- Memory per truth table entry (KB)

### METHODOLOGY

1. Random Boolean functions generated per distribution
2. BoolMinGeo minimization executed (SOP form)
3. Execution time measured using perf\_counter
4. Memory tracked using tracemalloc + psutil
5. Results aggregated by variable count and distribution
6. Decay patterns analyzed across variable range

### STUDY OBJECTIVE

This study demonstrates performance decay in 3-dimensional minimization beyond 8 variables, where the geometric advantages of three-dimensional K-map visualization are eliminated. Results show degradation in time and memory efficiency.

### REPRODUCIBILITY

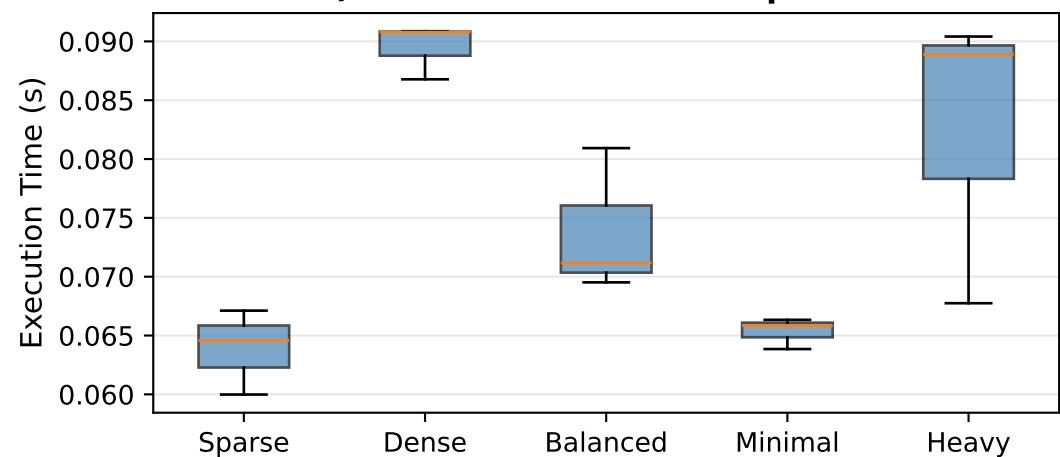
To reproduce this experiment:

1. Set random seed: `random.seed(42)`
2. Run with identical system configuration
3. Use same library versions as documented above
4. Execute: `python test_kmapsolver3d_9to16var_performance.py`

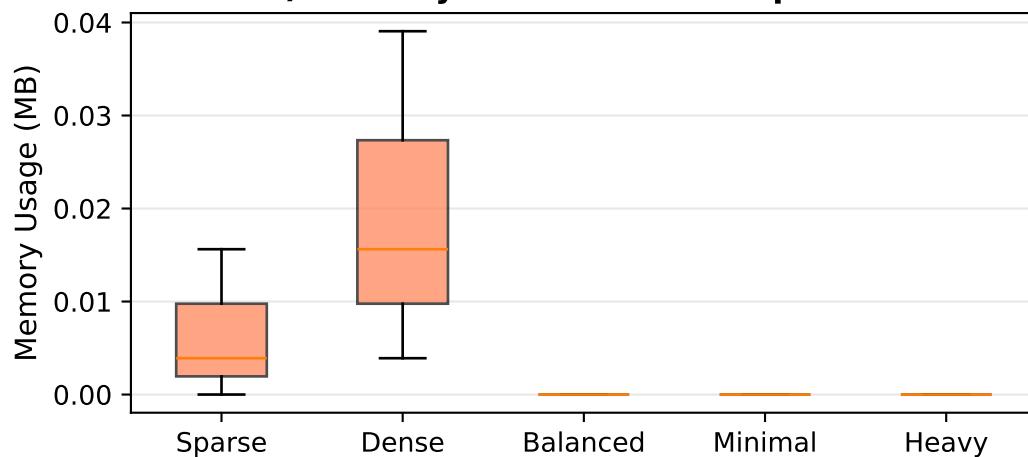
# 9-Variable Analysis: Distribution Performance

Truth Table Size:  $2^9 = 512$  entries | Decay Study

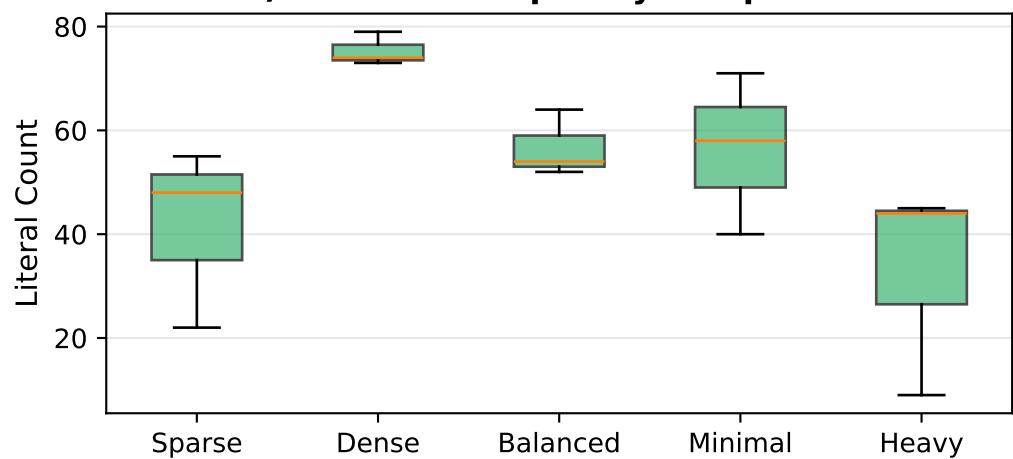
**A) Time Distribution Comparison**



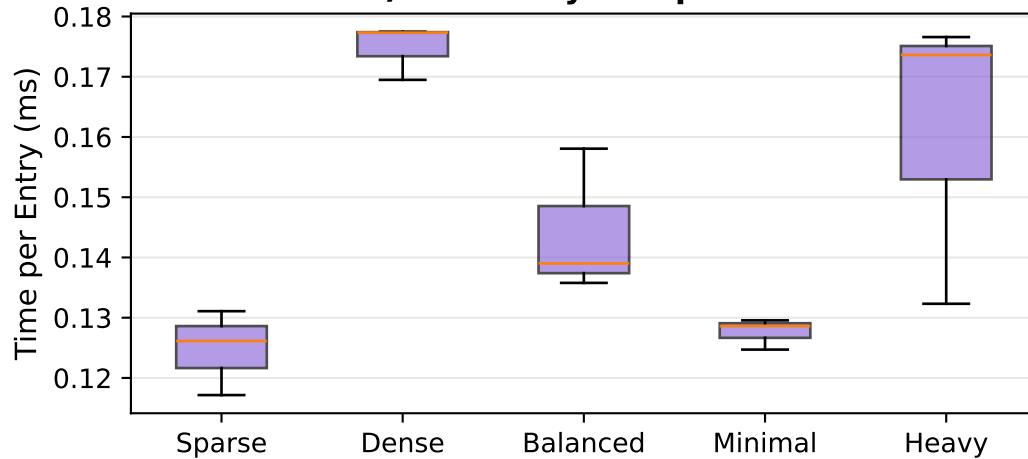
**B) Memory Distribution Comparison**



**C) Solution Complexity Comparison**



**D) Efficiency Comparison**



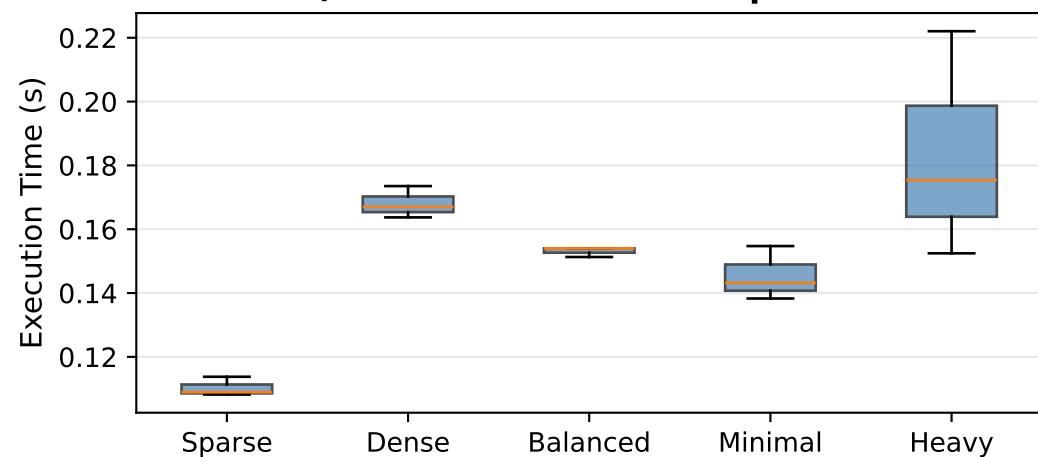
**E) Statistical Summary**

| Distribution      | N | Mean Time (s) | Std Time | Mean Mem (MB) | Mean Lits | Mean Terms |
|-------------------|---|---------------|----------|---------------|-----------|------------|
| Sparse (20% 1s)   | 3 | 0.0639        | 0.0030   | 0.01          | 41.7      | 9.3        |
| Dense (70% 1s)    | 3 | 0.0895        | 0.0019   | 0.02          | 75.3      | 22.7       |
| Balanced (50% 1s) | 3 | 0.0739        | 0.0050   | 0.00          | 56.7      | 14.0       |
| Minimal DC (2%)   | 3 | 0.0653        | 0.0011   | 0.00          | 56.3      | 15.7       |
| Heavy DC (30%)    | 3 | 0.0824        | 0.0103   | 0.00          | 32.7      | 8.3        |

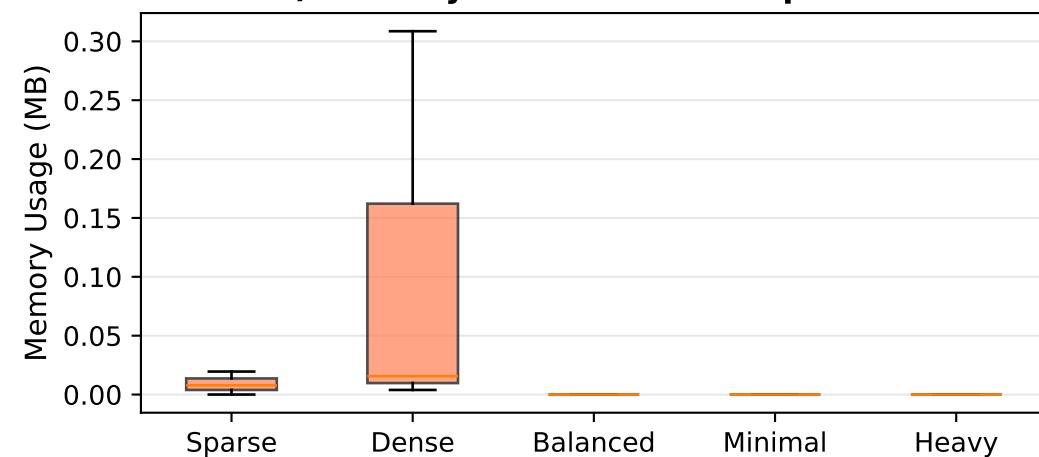
# 10-Variable Analysis: Distribution Performance

Truth Table Size:  $2^{10} = 1,024$  entries | Decay Study

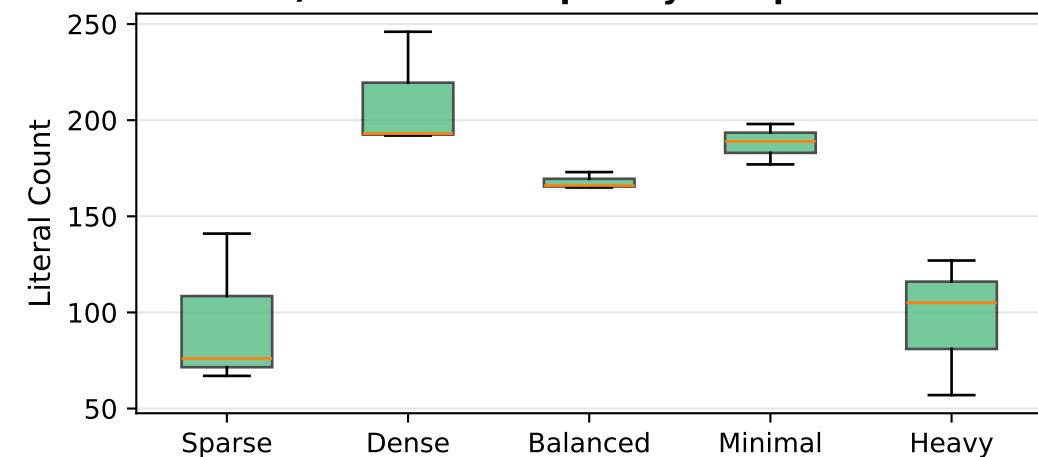
**A) Time Distribution Comparison**



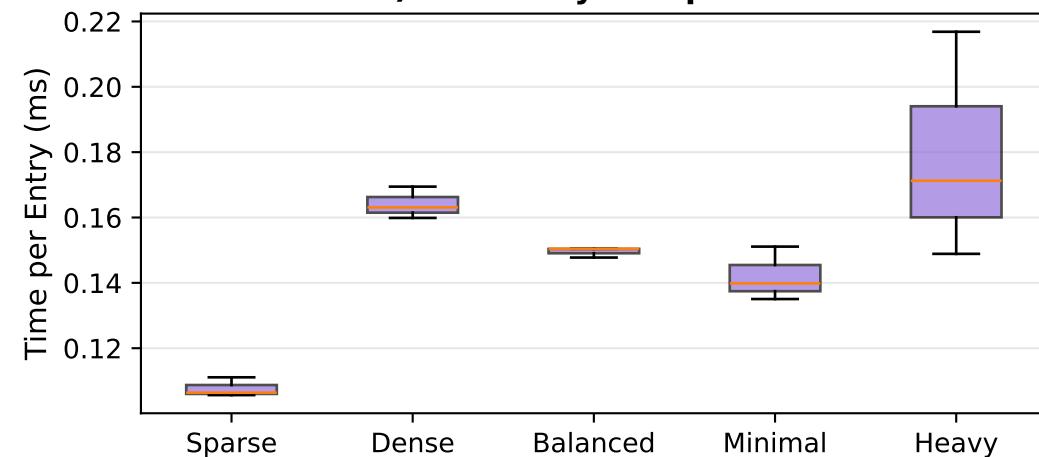
**B) Memory Distribution Comparison**



**C) Solution Complexity Comparison**



**D) Efficiency Comparison**

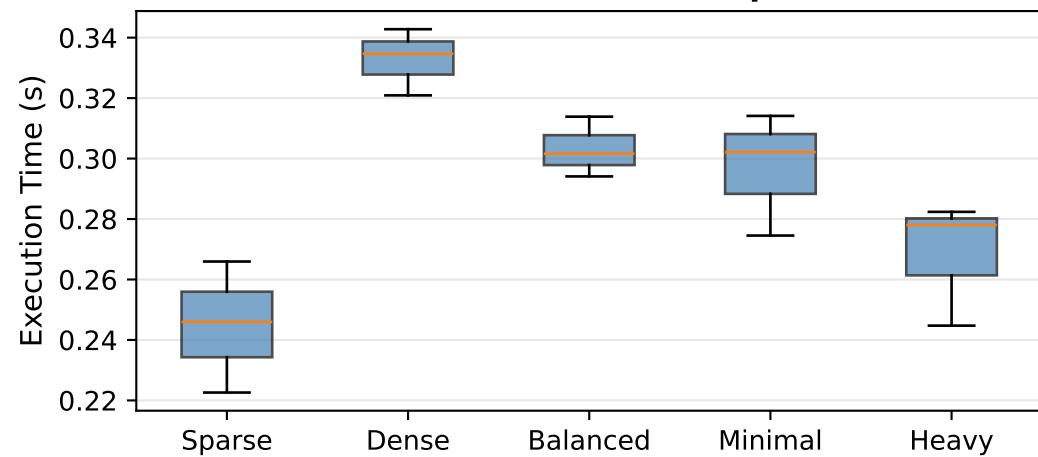


**E) Statistical Summary**

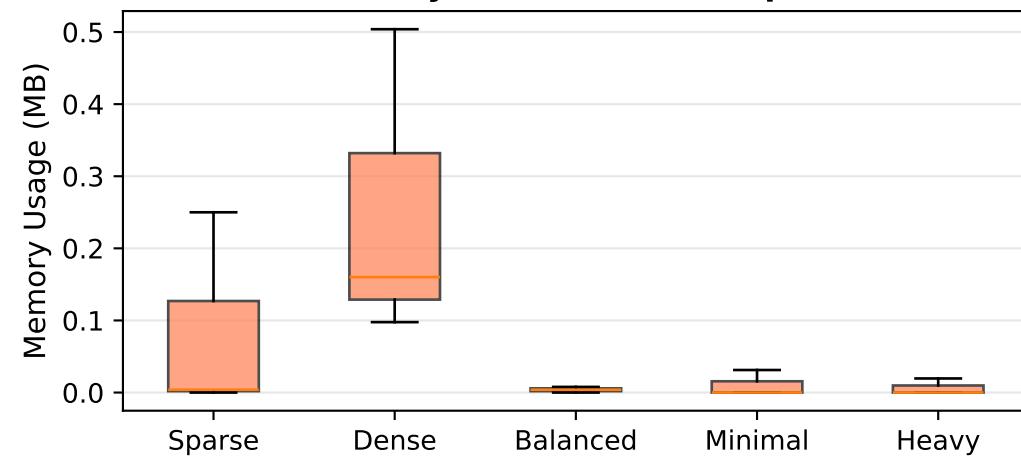
| Distribution      | N | Mean Time (s) | Std Time | Mean Mem (MB) | Mean Lits | Mean Terms |
|-------------------|---|---------------|----------|---------------|-----------|------------|
| Sparse (20% 1s)   | 3 | 0.1103        | 0.0025   | 0.01          | 94.7      | 20.3       |
| Dense (70% 1s)    | 3 | 0.1681        | 0.0041   | 0.11          | 210.3     | 53.7       |
| Balanced (50% 1s) | 3 | 0.1531        | 0.0013   | 0.00          | 168.0     | 38.7       |
| Minimal DC (2%)   | 3 | 0.1454        | 0.0069   | 0.00          | 188.0     | 41.7       |
| Heavy DC (30%)    | 3 | 0.1833        | 0.0290   | 0.00          | 96.3      | 23.3       |

**11-Variable Analysis: Distribution Performance**  
**Truth Table Size:  $2^{11} = 2,048$  entries | Decay Study**

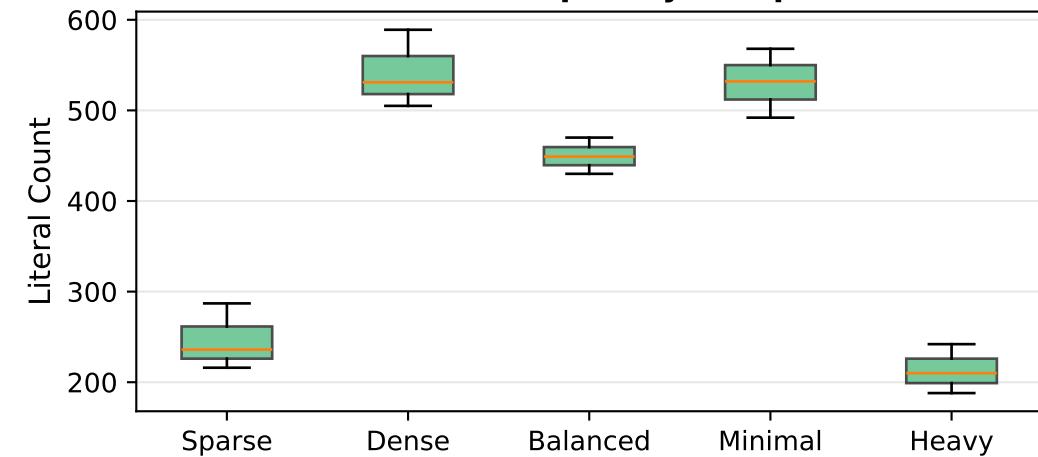
**A) Time Distribution Comparison**



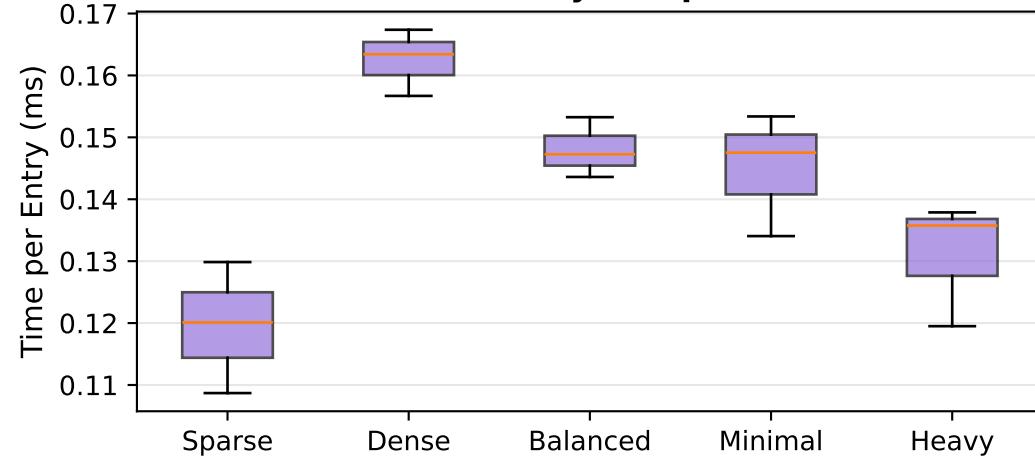
**B) Memory Distribution Comparison**



**C) Solution Complexity Comparison**



**D) Efficiency Comparison**

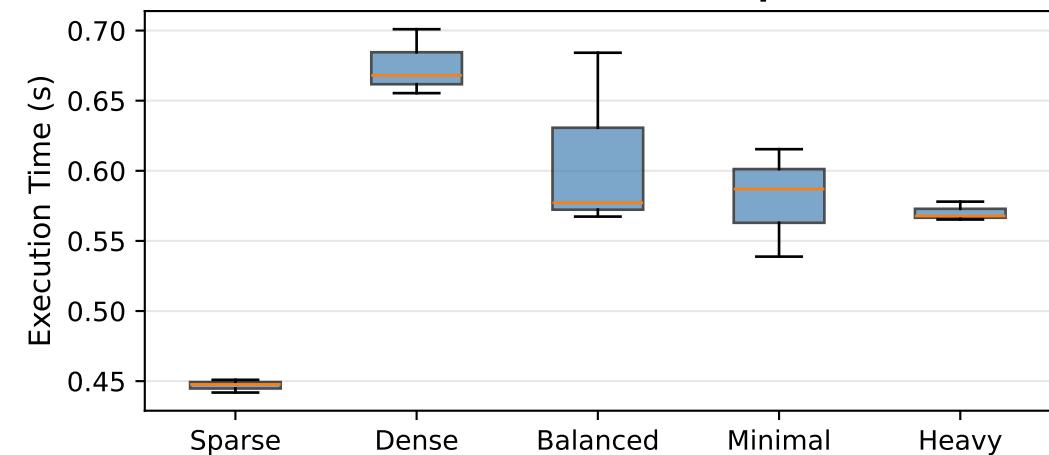


**E) Statistical Summary**

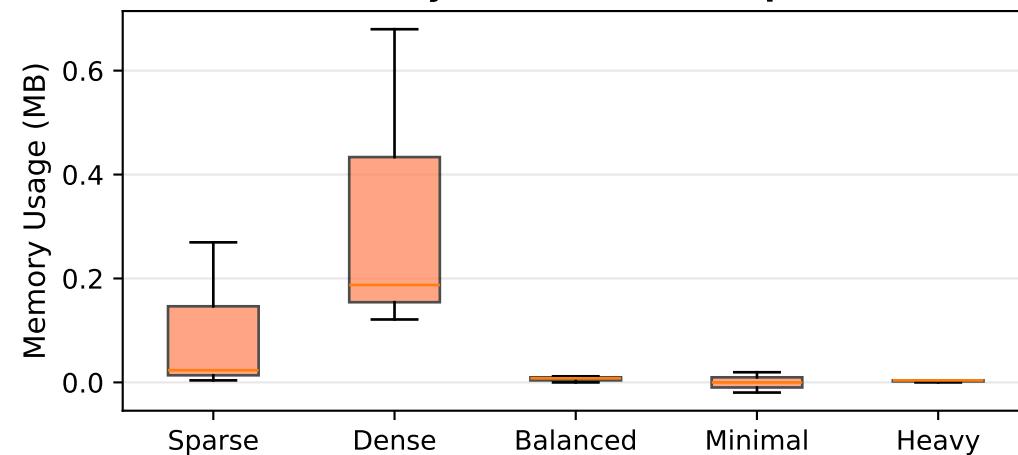
| Distribution      | N | Mean Time (s) | Std Time | Mean Mem (MB) | Mean Lits | Mean Terms |
|-------------------|---|---------------|----------|---------------|-----------|------------|
| Sparse (20% 1s)   | 3 | 0.2448        | 0.0177   | 0.08          | 246.3     | 44.7       |
| Dense (70% 1s)    | 3 | 0.3328        | 0.0090   | 0.25          | 541.7     | 118.0      |
| Balanced (50% 1s) | 3 | 0.3032        | 0.0081   | 0.00          | 449.7     | 100.3      |
| Minimal DC (2%)   | 3 | 0.2969        | 0.0166   | 0.01          | 530.7     | 105.3      |
| Heavy DC (30%)    | 3 | 0.2684        | 0.0168   | 0.01          | 213.3     | 45.7       |

**12-Variable Analysis: Distribution Performance**  
**Truth Table Size:  $2^{12} = 4,096$  entries | Decay Study**

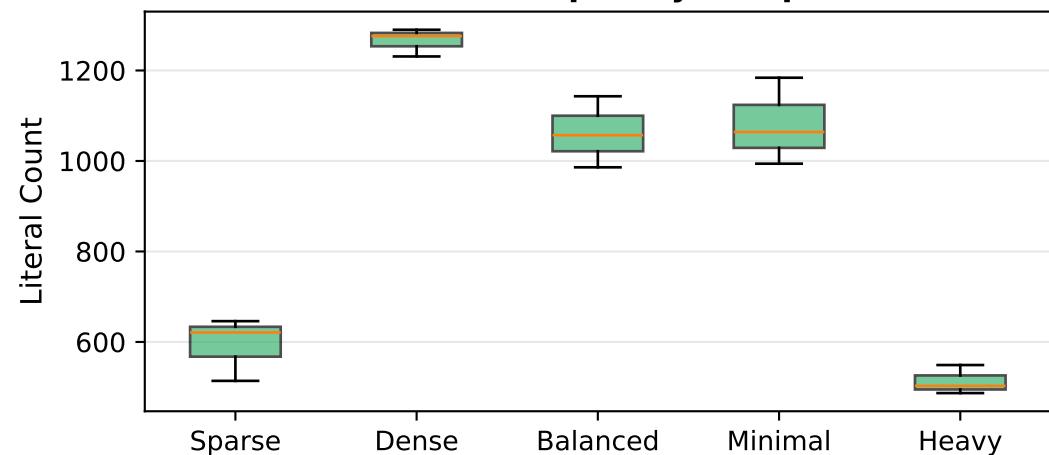
**A) Time Distribution Comparison**



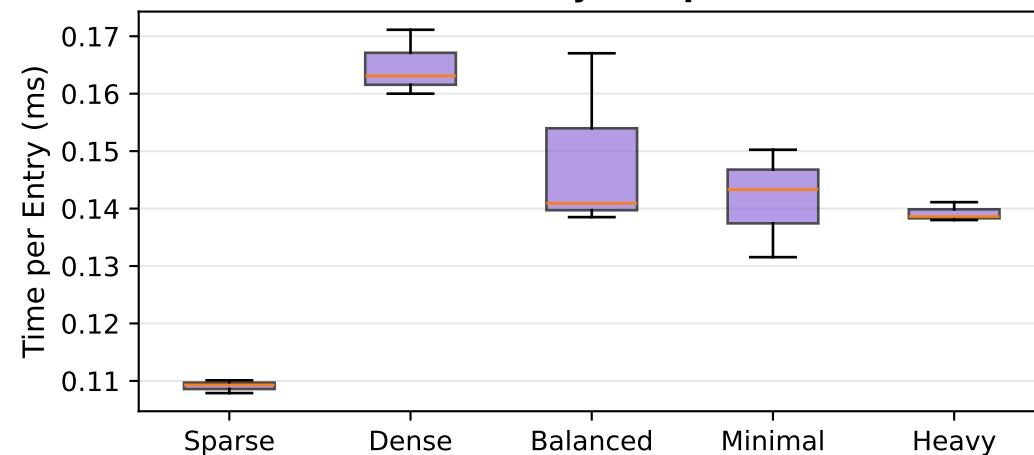
**B) Memory Distribution Comparison**



**C) Solution Complexity Comparison**



**D) Efficiency Comparison**



**E) Statistical Summary**

| Distribution      | N | Mean Time (s) | Std Time | Mean Mem (MB) | Mean Lits | Mean Terms |
|-------------------|---|---------------|----------|---------------|-----------|------------|
| Sparse (20% 1s)   | 3 | 0.4468        | 0.0038   | 0.10          | 593.7     | 102.7      |
| Dense (70% 1s)    | 3 | 0.6748        | 0.0192   | 0.33          | 1265.7    | 252.3      |
| Balanced (50% 1s) | 3 | 0.6096        | 0.0529   | 0.01          | 1062.0    | 204.0      |
| Minimal DC (2%)   | 3 | 0.5804        | 0.0316   | 0.00          | 1080.7    | 199.0      |
| Heavy DC (30%)    | 3 | 0.5703        | 0.0055   | 0.00          | 513.0     | 98.7       |