

# Deductive Reasoning Agents

Based on “An Introduction to MultiAgent Systems” and slides  
by Michael Wooldridge

# Agent Architectures

- An agent architecture is a software design for an agent
- Top-level decomposition into perception – state – decision – action
- An agent architecture defines:
  - key data structures
  - operations on data structures
  - control flow between operations

# Types of Agents

- 1950's – now: *Symbolic Reasoning Agents*  
Its purest expression, proposes that agents use explicit logical reasoning in order to decide what to do
- 1980's – now: *Reactive Agents*  
Problems with symbolic reasoning led to a reaction against this — led to the reactive agents movement
- 1990's – now: *Hybrid Agents*  
Hybrid architectures attempt to combine the best of symbolic and reactive architectures

# Deductive Reasoning Agents

- Traditional approach to build AI systems (*symbolic AI*)
  - Symbolic representation of environment and behavior
  - Syntactic manipulation of symbolic representation
- Symbolic representation  $\rightarrow$  *logical formulae*
- Syntactic manipulation  $\rightarrow$  *logical deduction (theorem proving)*

# Transduction Problem

- The problem of translating the real world into an accurate, adequate symbolic description, in time for that description to be useful
- ...vision, speech understanding, learning

# Representation/Reasoning Problem

- The problem of how to symbolically represent information about complex real-world entities and processes, and how to get agents to reason with this information in time for the results to be useful
- ...knowledge representation, automated reasoning, automatic planning


# Agents as Theorem Provers

- Theory of agency  $\varphi$  – some theory that explains how an intelligent agent should behave to optimize some performance measure
- Theory  $\varphi$  is viewed as executable specification that is directly executed in order to produce the agent's behavior

# Agents as Theorem Provers

Deliberate agents  simple model of logic-based agents

- Internal state assumed to be a database of formulae (predicate logic)

Example 

```
Open(valve221)
Temperature(reactor4726, 321)
Pressure(tank776, 28)
```

- Analogous to *beliefs* in humans – internal state may include incorrect (outdated, invalid) information

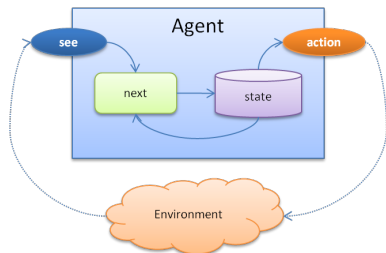


# Agents as Theorem Provers

Let:

- $L$  be the set of formulae of classical first-order logic
- $D \subseteq 2^L$  be the set of  $L$  databases
  - $DB, DB_1, \dots$  are the members of  $D$
  - $DB$  represents the internal state of an agent
- $\rho$  is a set of deduction rules that models the agent's decision making process
- $DB \vdash_{\rho} \phi$  means that the formula  $\phi$  can be proved from the database  $DB$  using only the deduction rules  $\rho$

# Agents with State



- Perception function *see*
- Next state function *next*
- Action-selection function *action*

# Agents as Theorem Provers

- Perception function

$$see : E \rightarrow Per$$

- Next function

$$next : D \times Per \longrightarrow D$$

- Action-selection function (defined in terms of the agent's deduction rules)

$$action : D \rightarrow Ac$$

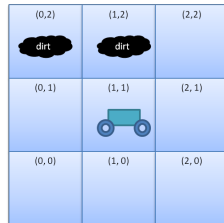
# Action Selection as Theorem Proving

```
foreach  $\alpha \in Ac$  do
|   if  $DB \vdash_{\rho} Do(\alpha)$  then
|   |   return  $\alpha$ ;
|   end
end
foreach  $\alpha \in Ac$  do
|   if  $DB \not\vdash_{\rho} \neg Do(\alpha)$  then
|   |   return  $\alpha$ ;
|   end
end
```

# Example – Vacuum World



- A small robotic agent that cleans up a room divided into a grid of equally sized squares
- Agent is equipped with a dirt sensor and a vacuum cleaner
- Agent always has a definite orientation (north, south, east, west)
- Agent can move forward one step and turn right  $90^\circ$
- For simplicity we assume the room is  $3 \times 3$  and agent always starts in square 0,0 facing north



# Representing Vacuum World

- Possible percepts

$Per = \{dirt, null\}$

- Domain predicates describing internal state

$In(x, y)$  – agent is at  $(x, y)$

$Dirt(x, y)$  – there is dirt at  $(x, y)$

$Facing(d)$  – agent is facing direction  $d$


- Possible actions

$Act = \{forward, suck, turn\}$

# Reasoning in Vacuum World



## Deduction rules

- 1  $In(x, y) \wedge Dirt(x, y) \longrightarrow Do(suck)$
- 2  $In(0, 0) \wedge Facing(north) \wedge \neg Dirt(0, 0) \longrightarrow Do(forward)$
- 3  $In(0, 1) \wedge Facing(north) \wedge \neg Dirt(0, 1) \longrightarrow Do(forward)$  
- 4  $In(0, 2) \wedge Facing(north) \wedge \neg Dirt(0, 2) \longrightarrow Do(turn)$
- 5  $In(0, 2) \wedge Facing(east) \wedge \neg Dirt(0, 2) \longrightarrow Do(forward)$
- 6 ...

# Problems with Deductive Reasoning

- How to convert video camera input to  $\{dirt, null\}$  and how to represent properties of dynamic environment
- Decision making assumes a static environment: *calculative rationality*
  - Decision making process suggests an action that was optimal when the process started
  - If decision making is immediate, then we can discard this problem
- Decision making via theorem proving is complex (it may never terminate)



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# EXAMPLE: VACUUM WORLD

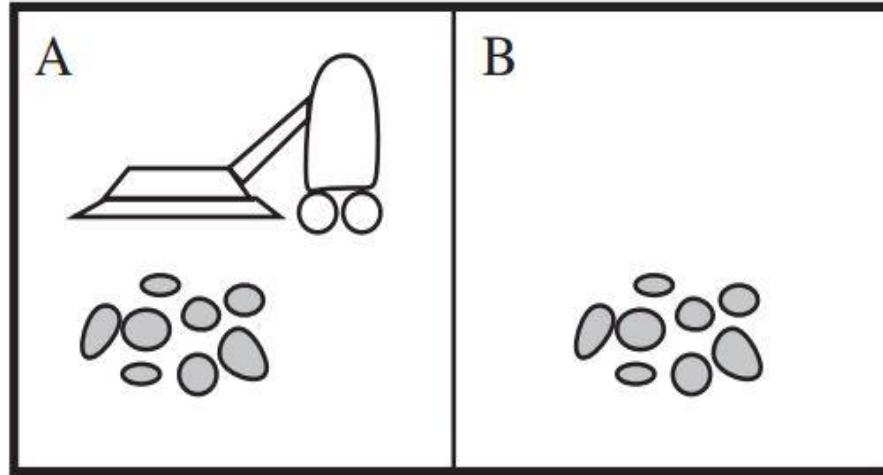
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# Formulating a problem

The real world is absurdly complex.

We solve problems by defining appropriate abstractions.

# Example: Vacuum world

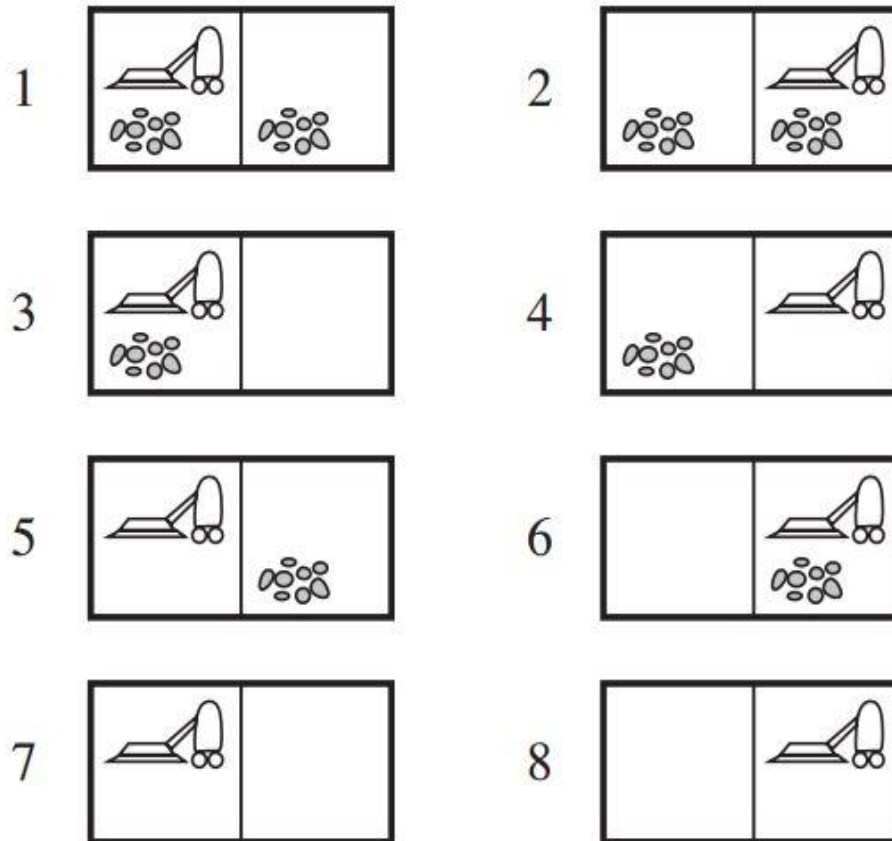


Percepts: Location and room contents, e.g., [A, Dirty]

Actions: Left, Right, Suck, NoOp

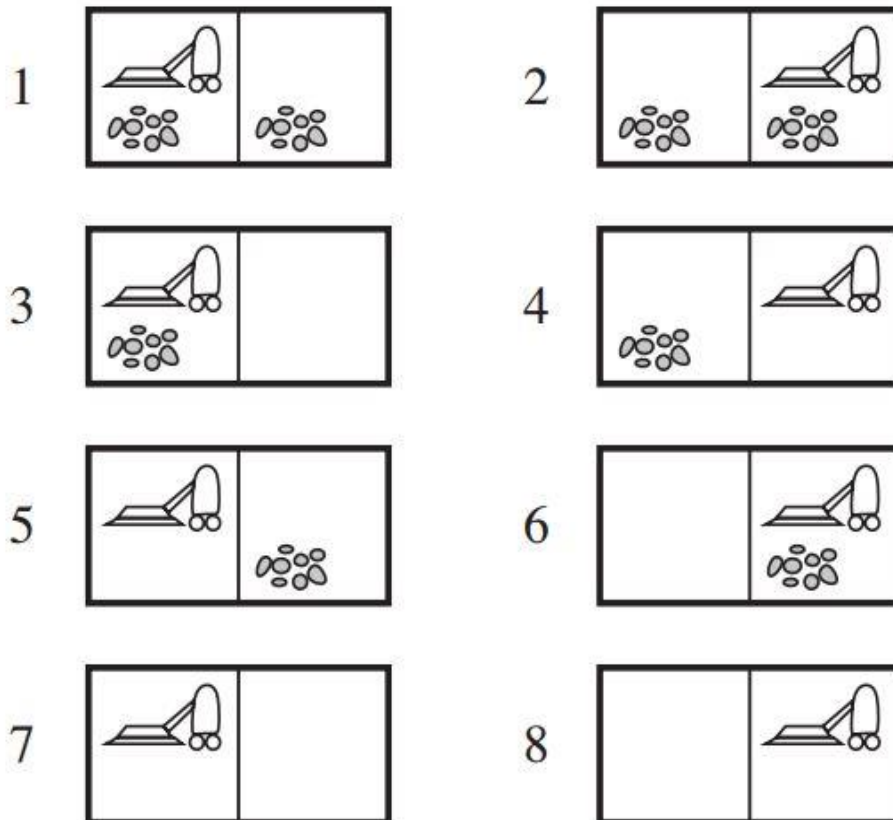
# Example: Vacuum world

Complete state space



# Example: Vacuum world

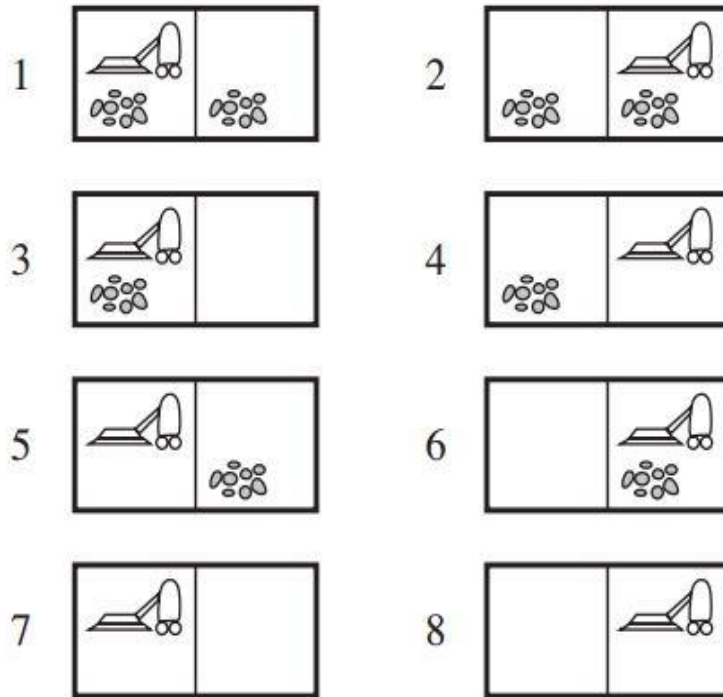
Single-state. Start in 5. Solution? (What's the goal?)



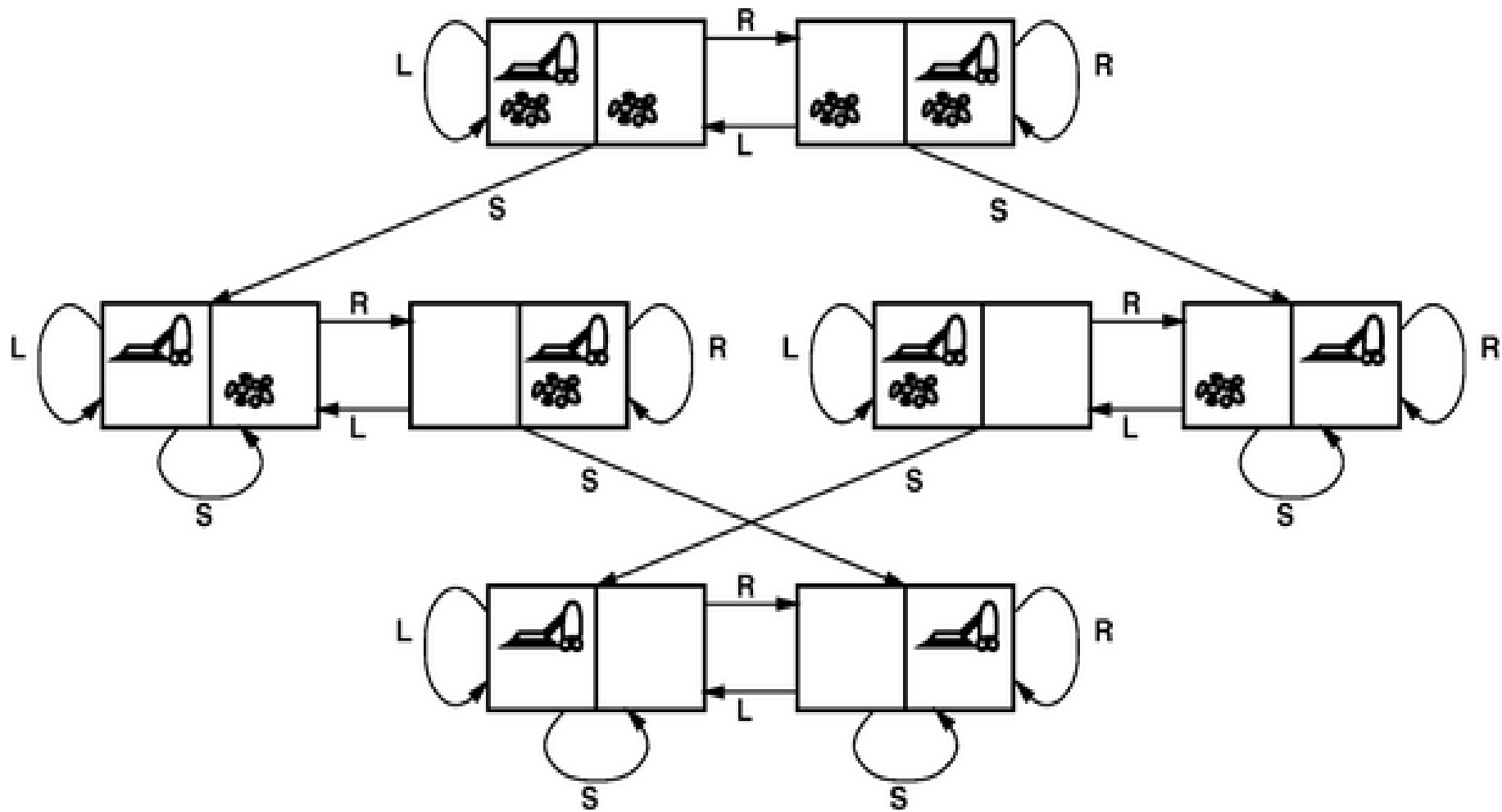
# Example: Vacuum world

Single-state. Start in 5. Solution?

Solution: [Right, Suck]



# Example: Vacuum World<sup>0</sup>



# Formulating a problem

Any lessons we can learn?

- States are abstractions of real-world configurations.
- Actions can be abstract but should be executable.
- Solutions should be feasible.
- Costs should be meaningful.