

Test 2 Review:

1. Graph the Vector Function: $\vec{r}(t) = t^2\hat{i} + t^4\hat{j} + t^6\hat{k}$ on the interval $t \geq 0$
2. Graph the Vector Function: $\vec{r}(t) = \langle \sin t, 3, \cos t \rangle$ on the interval $0 \leq t \leq 2\pi$
3. Find the limit: $\lim_{t \rightarrow 0} \langle e^{-t}, \frac{\sin t}{t}, \cos t \rangle$
4. Find the equation of the tangent line to $\vec{r}(t) = t^5\hat{i} + t^4\hat{j} + t^3\hat{k}$ at $t = 1$
5. Find the equation of the tangent line to:

$$\vec{r}(t) = (t^2 - 1)\hat{i} + (t^2 + 1)\hat{j} + (t + 1)\hat{k} \text{ at } t = 0$$

6. Find $\vec{r}(t)$ if $\vec{r}'(t) = 2e^{2t}\hat{i} + 3e^{-t}\hat{j} + e^t\hat{k}$ and $\vec{r}(0) = \hat{i} - \hat{j} + 2\hat{k}$
7. Find the arc length of $\vec{r}(t) = \sqrt{2}t\hat{i} + \frac{1}{2}t^2\hat{j} + \ln t\hat{k}$ on $1 \leq t \leq 2$
8. Find the equation for the Osculating Plane and the Curvature for:

$$\vec{r}(t) = 2 \sin(3t)\hat{i} + t\hat{j} + 2 \cos(3t)\hat{k} \text{ at } t = \pi$$

9. Sketch the Domain of $f(x, y) = \sqrt{y - x} \ln(y + x)$
10. Find the Limit or show it D.N.E.: $\lim_{(x,y) \rightarrow (0,0)} \frac{\sqrt{xy+4}}{2y+3}$
11. Find the Limit or show it D.N.E.: $\lim_{(x,y) \rightarrow (0,0)} \frac{x^2y^2}{x^4+3y^4}$
12. Find **ALL** the Second Partial Derivatives: $f(x, y) = x^4 - 2x^2y^3 + y^2 - 2$
13. Find **ALL** the Second Partial Derivatives: $f(x, y) = e^{-xy} \cos(2x + 3y)$
14. Find Both First Partial Derivatives Implicitly: $x^2 + y^2 - z^2 = 2x(y + z)$
15. Find the Differential dz for $z = x^2 \sin(2y)$