## MECE 5397

## Project A – Poisson Equation

Write a computer code to solve the two-dimensional Poisson equation

$$\frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} = -F(x, y) \tag{1}$$

The domain of interest is the rectangle

$$a_x < x < b_x, \qquad a_y < y < b_y \tag{2}$$

and the boundary conditions

$$u(x = a_x, y) = f_a(y), u(x = b_x, y) = g_a(y),$$
 (3)

$$\frac{\partial u}{\partial y}\Big|_{y=a_y} = 0, \qquad u(x, y = b_y) = f_a(b_y) + \frac{x - a_x}{b_x - a_x} [g_a(b_y) - f_a(b_y)] \tag{4}$$

$$a_x = a_y = 0, b_x = b_y = 2\pi (5)$$

$$f_a(y) = (y - a_y)^2 \cos y, \qquad g_b(y) = y(y - a_y)^2$$
 (6)

$$F(x,y) = \sin\left[\pi \frac{x - a_x}{b_x - a_x}\right] \cos\left[\frac{\pi}{2} \left(2\frac{y - a_y}{b_y - a_y} + 1\right)\right]$$
(7)

Use ghost node(s) for Neumann condition(s).

After carrying out all the simulations needed for the report, run one last simulation with F=0 and include the results in the report.