

## 数据库作业week7

### 7.1

Suppose that we decompose the schema  $R = (A, B, C, D, E)$  into

$$\begin{aligned}(A, B, C) \\ (A, D, E)\end{aligned}$$

Show that this decomposition is a lossless decomposition if the following set  $F$  of functional dependencies holds:

$$\begin{aligned}A &\rightarrow BC \\ CD &\rightarrow E \\ B &\rightarrow D \\ E &\rightarrow A\end{aligned}$$

because of  $R_1 = (A, B, C), R_2 = (A, D, E), R_1 \cap R_2 = A$ , so it is important to check if  $A$  is the superkey.

Now we compute Attribute of  $A$ . since of `result:=A -> result:=ABC -> result:=ABCD -> result:=ABCDE`.

so  $A$  is the superkey of  $R$  (same as  $R_1 \setminus R_2$ ), this decomposition is a lossless decomposition.

### 7.13

Show that the decomposition in Exercise 7.1 is not a dependency-preserving decomposition

because in the  $CD \rightarrow E$ ,  $CDE$  are not include in any schema

Now we doing algorithm

$$\begin{aligned}&\text{for } R_1 \\&CD \rightarrow E \\&result := CD \\&result \cup ((result \cap R_1)_F^+ \cap R_1) = \{C, D\} \\&\text{for } R_2 \\&result := CD \\&E \notin result = result \cup ((result \cap R_2)_F^+ \cap R_1) = \{C, D\}\end{aligned}$$

because  $CD \rightarrow E$  is wrong in both  $R_1, R_2$ , so the decomposition in Exercise 7.1 is not a dependency-preserving decomposition

### 7.21

Give a lossless decomposition into BCNF of schema  $R$  of Exercise 7.1.

7.1 Suppose that we decompose the schema  $R = (A, B, C, D, E)$  into

$$\begin{aligned}(A, B, C) \\ (A, D, E)\end{aligned}$$

Show that this decomposition is a lossless decomposition if the following set  $F$  of functional dependencies holds:

$$A \rightarrow BC$$

$$CD \rightarrow E$$

$$B \rightarrow D$$

$$E \rightarrow A$$

Now we can know E is superkey

we should get the non-trivial dependency which left value is not E

*for  $CD \rightarrow E$*

$$CD \cup E = \{C, D, E\}$$

$$R - E = \{A, B, C, D\}$$

*$\{C, D, E\}$  choose  $CD \rightarrow E$  is BCNF*

*$\{A, B, C, D\}$  chose  $A \rightarrow BC$ ,  $B \rightarrow D$ ,  $CD \rightarrow A$*

*is not BCNF and  $A/CD$  is superkey*

*for  $B \rightarrow D$*

$$B \cup D = \{B, D\}$$

$$\{A, B, C, D\} - D = \{A, B, C\}$$

*$\{B, D\}$  choose  $B \rightarrow D$  is BCNF*

*$\{A, B, C\}$  chose  $A \rightarrow BC$  is BCNF*

*so we get :*

*$\{C, D, E\}$  choose  $CD \rightarrow E$*

*$\{B, D\}$  choose  $B \rightarrow D$*

*$\{A, B, C\}$  choose  $A \rightarrow BC$*

## 7.22

Give a lossless, dependency-preserving decomposition into 3NF of schema  $R$  of Exercise 7.1.

7.1 Suppose that we decompose the schema  $R = (A, B, C, D, E)$  into

$$(A, B, C)$$

$$(A, D, E)$$

Show that this decomposition is a lossless decomposition if the following set  $F$  of functional dependencies holds:

$$A \rightarrow BC$$

$$CD \rightarrow E$$

$$B \rightarrow D$$

$$E \rightarrow A$$

$A/E$  is candidate key

after algorithm,  $F_c = F = \{A \rightarrow BC, CD \rightarrow E, B \rightarrow D, E \rightarrow A\}$

candidate key are  $A, E$

for  $A \rightarrow BC$

$R_1 = (A, B, C)$  choose  $A \rightarrow BC$

for  $CD \rightarrow E$

$R_2 = (C, D, E)$  choose  $CD \rightarrow E$

for  $B \rightarrow D$

$R_3 = (B, D)$  choose  $B \rightarrow D$

for  $E \rightarrow A$

$R_4 = (E, A)$  choose  $E \rightarrow A$

and we can verify the lossless of this decomposition because of  $R_4$  include  $AE$

### 7.30

Consider the following set  $F$  of functional dependencies on the relation schema  $(A, B, C, D, E, G)$ :

$$A \rightarrow BCD$$

$$BC \rightarrow DE$$

$$B \rightarrow D$$

$$D \rightarrow A$$

a. Compute  $B^+$ .

$$B^+ = B$$

$$\because B \rightarrow D$$

$$\therefore B^+ = BD$$

$$\because D \rightarrow A$$

$$\therefore B^+ = ABD$$

$$\because A \rightarrow BCD$$

$$\therefore B^+ = ABCD$$

$$\because BC \rightarrow DE$$

$$\therefore B^+ = ABCDE$$

b. Prove (using Armstrong's axioms) that  $AG$  is a superkey.

$$\begin{aligned}
& AG \rightarrow A(\text{reflexivity}) \\
& \therefore AG \rightarrow A, A \rightarrow BCD \\
& \therefore AG \rightarrow BCD(\text{transitivity}) \\
& \therefore AG \rightarrow BCD \rightarrow BC(\text{reflexivity}), BC \rightarrow DE \\
& \therefore AG \rightarrow DE(\text{transitivity}) \\
& \therefore AG \rightarrow BCD, AG \rightarrow DE \\
& \therefore AG = AGAG \rightarrow AGBCD, AGBCD \rightarrow BCDE \\
& \therefore AG \rightarrow BCDE \\
& \text{the same as } AG \rightarrow BCDE, AG \rightarrow AG \\
& \therefore AG \rightarrow ABCDEG \\
& \text{So } AG \text{ is a superkey}
\end{aligned}$$

c. Compute a canonical cover for this set of functional dependencies  $F$ ; give each step of your derivation with an explanation.

$$// \text{canonical cover } F_c = F$$

1. there are not dependency which left attributes are same as another dependency

2. for  $A \rightarrow BCD$ , now check  $D, D \in A_{F_c}^+ = ABCDE$ , so delete  $D$

$$\text{now } F_c = \{A \rightarrow BC, BC \rightarrow DE, B \rightarrow D, D \rightarrow A\}$$

1. there are not dependency which left attributes are same as another dependency

2. for  $BC \rightarrow DE$ , now check  $D, D \in BC_{F_c}^+ = ABCDE$ , so delete  $D$

$$\text{now } F_c = \{A \rightarrow BC, BC \rightarrow E, B \rightarrow D, D \rightarrow A\}$$

1. there are not dependency which left attributes are same as another dependency

2. for  $BC \rightarrow D$ , now check  $C, C \in B_{F_c}^+ = ABCDE$ , so delete  $C$

$$\text{now } F_c = \{A \rightarrow BC, B \rightarrow E, B \rightarrow D, D \rightarrow A\}$$

$$1. \text{union } B \rightarrow E, B \rightarrow D \text{ to } B \rightarrow DE$$

$$\text{now } F_c = \{A \rightarrow BC, B \rightarrow DE, D \rightarrow A\}$$

1. there are not dependency which left attributes are same as another dependency

2. for all dependency, there is no extraneous attribute

$$\text{So canonical cover } F_c = \{A \rightarrow BC, B \rightarrow DE, D \rightarrow A\}$$

d. Give a 3NF decomposition of the given schema based on a canonical cover.

$$F_c = \{A \rightarrow BC, B \rightarrow DE, D \rightarrow A\}$$

candidate key are  $AG/BG/DG$

for  $A \rightarrow BC$

$$R_1 = (A, B, C) \text{ choose } A \rightarrow BC$$

for  $B \rightarrow DE$

$$R_2 = (B, D, E) \text{ choose } B \rightarrow DE$$

for  $D \rightarrow A$

$$R_3 = (A, D) \text{ choose } D \rightarrow A$$

for lossless requirement

$$R_4 = (A, G) \text{ choose } \phi$$

and we can verify the lossless of this decomposition because of  $R_4$  include  $AG$

e. Give a BCNF decomposition of the given schema using the original set  $F$  of functional dependencies.

*// BCNF, the superkey is  $A/B/D$*

*for  $BC \rightarrow DE$*

*$BC \cup DE = \{B, C, D, E\}$  choose  $BC \rightarrow DE$  is BCNF*

*$r - \{D, E\} = \{A, B, C, G\}$  choose  $B \rightarrow A, A \rightarrow BC$  is BCNF*

*So we get*

*$\{B, C, D, E\}$  choose  $BC \rightarrow DE$*

*$\{A, B, C, G\}$  choose  $B \rightarrow A, A \rightarrow BC$*