

Lab 4: Linear Algebra and Probability

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Module: INT104

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Introduction

Given a two-dimensional array, where each row represents an instance (or object). For each row, the first 5 columns are the attributes of the instance and the final column is the label of the instance such as $a_0, a_1, a_2, a_3, a_4, l$.

In this project, it needs to compute some estimated probabilities

Design & Implementation

Dynamic Programming

1. Design principals

First, use some given statement to read the file and transform it into a matrix in python:

Second, using this statement to select the two column a_i and l : $a_{ix} = \text{matrix[:, [x, 5]]}$.

Third, create four new matrixes which have two columns.

Finally, start to calculate. The row of the matrix is N : $\text{int} = \text{len}(\text{matrix})$.

To calculate the situation when $l = 0$ and 1 , use the statement: $l_0 = \text{Counter}(l)[\text{'0'}]$ and $l_1 = \text{Counter}(l)[\text{'1'}]$. $p(l = 0) = l_0/N$, $p(l=1) = l_1/N$.

To calculate $p(a_i = 0 | l = 0)$, use the statement: $p_3 = (a_{i0} == q_1).all(1).sum()/l_0$. The others are the same.

2. Implementation

```
3. import csv
import numpy as np
from collections import Counter
csv_file = open('binary_data.csv' )
csv_reader = csv.reader(csv_file, delimiter=',')
final_list = list(csv_reader)
matrix = np.array(final_list)

# Read the text file and parse its content into a matrix. (20
scores)
print(matrix)

# Compute the prior probabilities  $p(l = 0)$  and  $p(l = 1)$  (20
scores)
```

```

#a0 = matrix[:, 0]
#a1 = matrix[:, 1]
#a2 = matrix[:, 2]
#a3 = matrix[:, 3]
#a4 = matrix[:, 4]
l = matrix[:, 5]

ai0 = matrix[:, [0, 5]]
ai1 = matrix[:, [1, 5]]
ai2 = matrix[:, [2, 5]]
ai3 = matrix[:, [3, 5]]
ai4 = matrix[:, [4, 5]]

q1 = np.array(['0', '0'])
q2 = np.array(['1', '0'])
q3 = np.array(['0', '1'])
q4 = np.array(['1', '1'])

N: int = len(matrix)
#print(N)

l0 = Counter(l) ['0']
p1 = l0/N
print(p1)

l1 = Counter(l) ['1']
p2 = l1/N
print(p2)

#3

##1

p3 = (ai0 == q1).all(1).sum()/10
print(p3)

p4 = (ai1 == q1).all(1).sum()/10

```

```
print(p4)

p5 = (ai2 == q1).all(1).sum()/10
print(p5)

p6 = (ai3 == q1).all(1).sum()/10
print(p6)

p7 = (ai4 == q1).all(1).sum()/10
print(p7)

##2
p8 = (ai0 == q2).all(1).sum()/10
print(p8)

p9 = (ai1 == q2).all(1).sum()/10
print(p9)

p10 = (ai2 == q2).all(1).sum()/10
print(p10)

p11 = (ai3 == q2).all(1).sum()/10
print(p11)

p12 = (ai4 == q2).all(1).sum()/10
print(p12)

##3
p13 = (ai0 == q3).all(1).sum()/11
print(p13)

p14 = (ai1 == q3).all(1).sum()/11
print(p14)

p15 = (ai2 == q3).all(1).sum()/11
print(p15)

p16 = (ai3 == q3).all(1).sum()/11
print(p16)

p17 = (ai4 == q3).all(1).sum()/11
print(p17)
```

```

##4
p18 = (ai0 == q4).all(1).sum()/11
print(p18)

p19 = (ai1 == q4).all(1).sum()/11
print(p19)

p20 = (ai2 == q4).all(1).sum()/11
print(p20)

p21 = (ai3 == q4).all(1).sum()/11
print(p21)

p22 = (ai4 == q4).all(1).sum()/11
print(p22)

```

Result

The result is:

```

[['1' '1' '1' '0' '1' '1']
 ['1' '0' '0' '0' '1' '0']
 ['1' '0' '1' '1' '0' '1']
 ['0' '1' '1' '0' '1' '1']
 ['1' '0' '1' '1' '1' '0']
 ['0' '1' '0' '1' '0' '1']
 ['1' '1' '0' '0' '0' '1']
 ['0' '1' '0' '1' '1' '0']
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 ['0' '0' '0' '0' '1' '1']
 ['0' '1' '0' '1' '1' '1']
 ['1' '0' '1' '1' '0' '0']
 ['1' '1' '1' '0' '1' '1']

```

[1'0'0'1'1'0']
[0'0'1'1'0'1']
[0'0'1'1'0'0']
[1'1'1'0'1'1']
[0'1'1'0'1'1']
[1'0'0'1'0'1']
[0'0'1'1'1'0']
[0'1'0'1'1'0']
[1'0'0'0'1'0']
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['1' '0' '1' '1' '0' '0']
['1' '0' '1' '0' '1' '0']
['1' '0' '0' '1' '1' '0']]]

0.49

0.51

0.46938775510204084

0.673469387755102

0.46938775510204084

0.4897959183673469

0.40816326530612246

0.5306122448979592

0.32653061224489793

0.5306122448979592

0.5102040816326531

0.5918367346938775

0.5294117647058824
0.45098039215686275
0.6274509803921569
0.5686274509803921
0.5490196078431373
0.47058823529411764
0.5490196078431373
0.37254901960784315
0.43137254901960786
0.45098039215686275

Process finished with exit code 0

Observation

These code is in line with expectations.