

Msc in Artificial Intelligence and Robotics

# Thesis Presentation

## Sparse LiDAR Odometry using intensity channel: a comparison

A real-time front-end SLAM system for odometry estimation of a vehicle

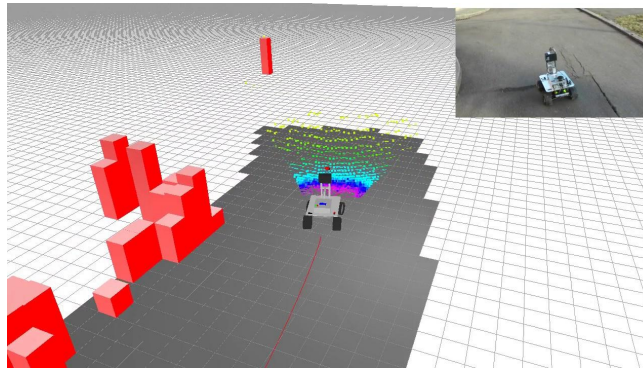
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*Sapienza University of Rome*

# Motivations

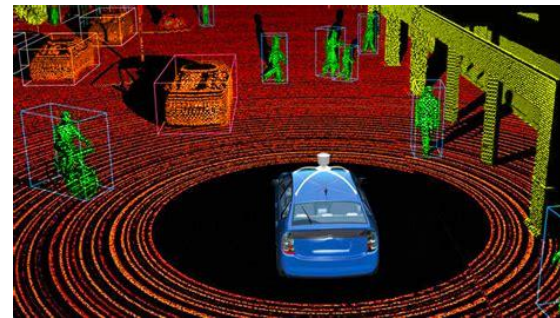
## Robot navigation system

exploration, smart farming, surveillance,  
military, autonomous driving ...



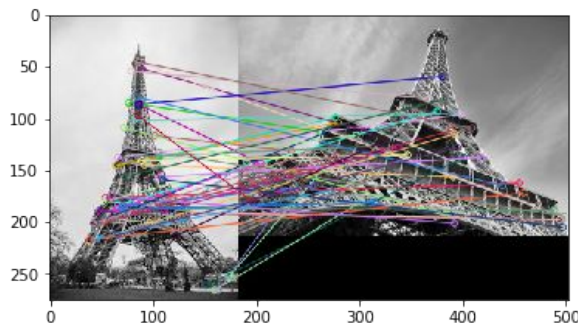
## Modern sensors

laser scanners provide a dense  
representation of the environment



## Variety of techniques

feature detection and matching,  
transform estimation



# Project Goal

## Methods comparison

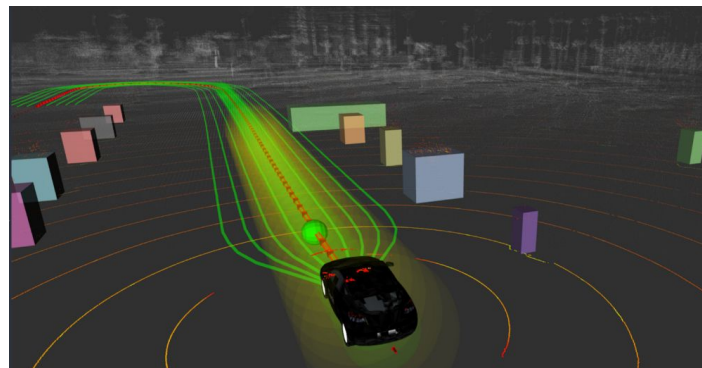
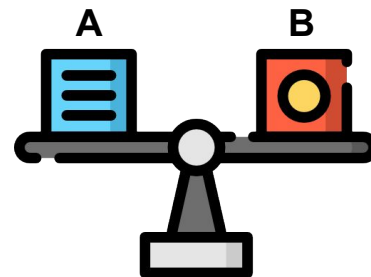
highlighting differences between  
solutions available nowadays

## Odometry estimation pipeline

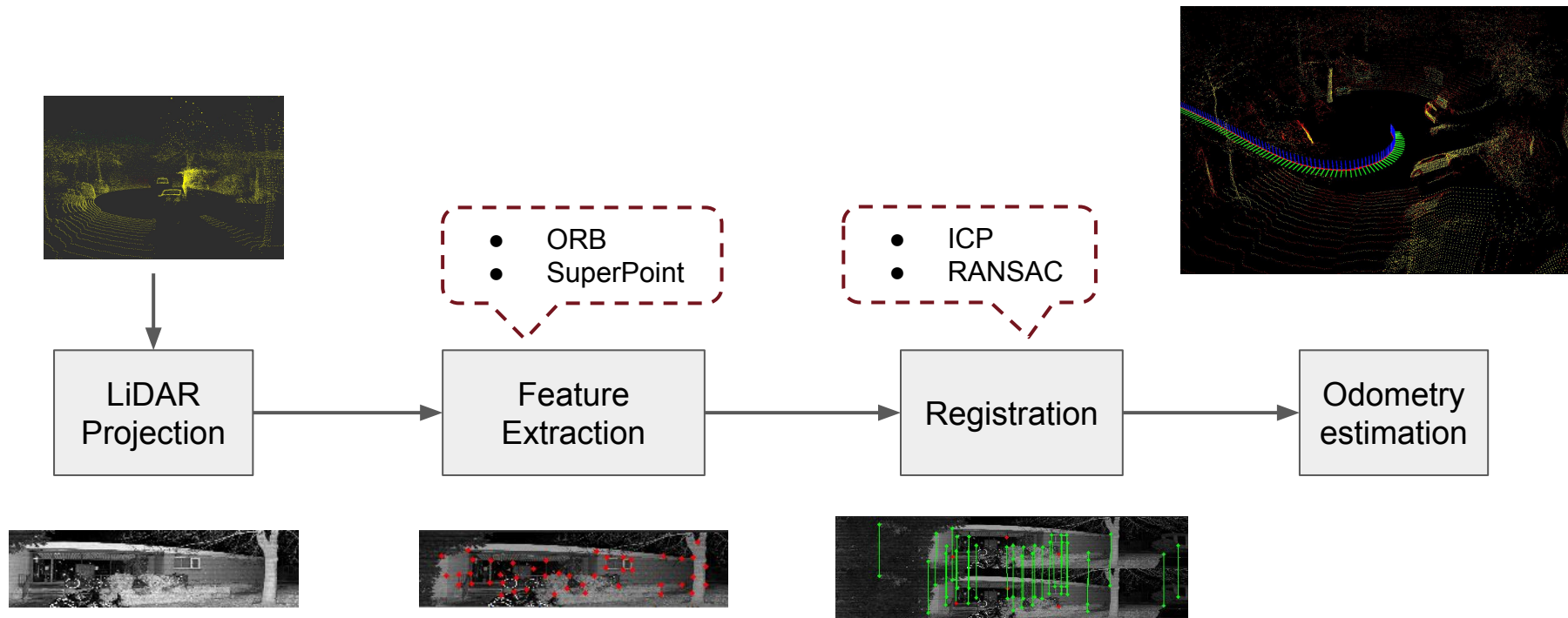
building an entire tracking system which  
estimates the car trajectory along the path

## Real-time performance

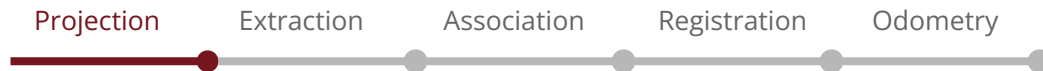
entire process within the sensor frequency



# Pipeline



# LiDAR Projection



## IPB Car dataset

acquired in urban environment, with  
LiDAR and GNSS sensors

## Projection function

from 3D Euclidean space to 2D image

## Conversion issues

- multiple points may fall in the same pixel
- empty pixel



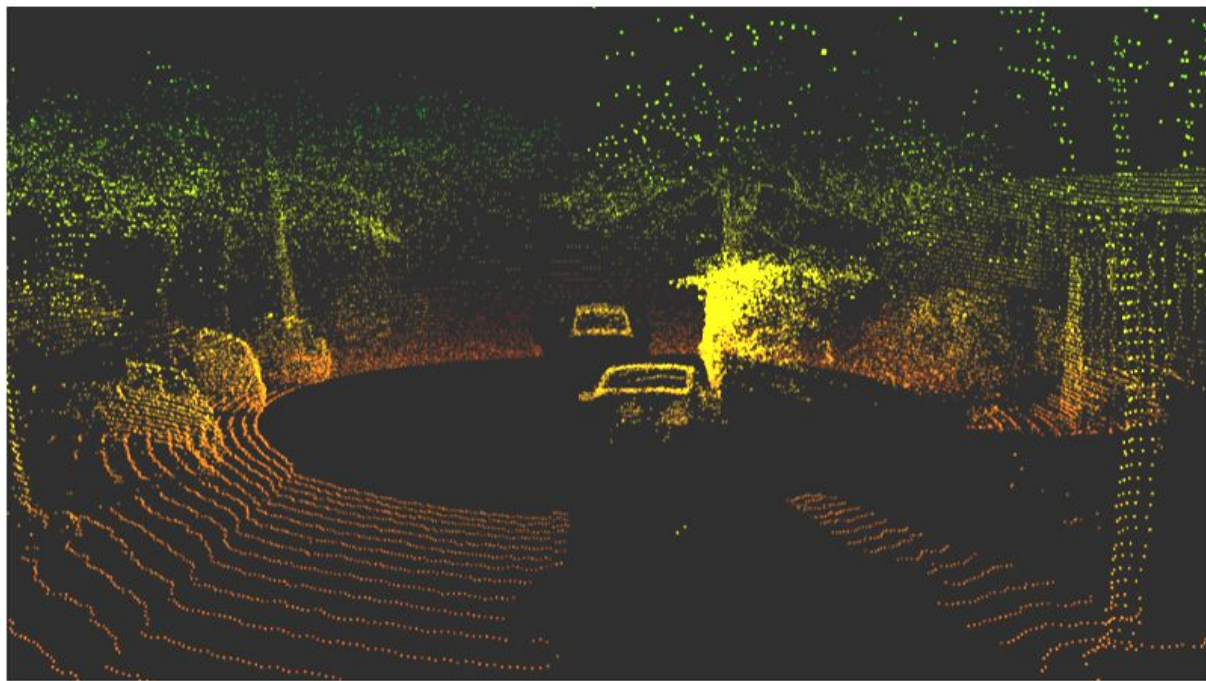
$$r = \sqrt{x^2 + y^2 + z^2} \in \mathbb{R}$$

$$\theta = \text{atan2}(y, x) \in [-\pi/2, \pi/2]$$

$$\varphi = \text{asin}(z/r) \in [-\pi, \pi]$$



$$\begin{pmatrix} u \\ v \end{pmatrix} = \begin{pmatrix} \frac{W}{2} (1 + \frac{\theta}{\pi}) \\ H \frac{f_{up} - \varphi}{f_{up} - f_{down}} \end{pmatrix}$$



(a)



(b)



(c)



# Feature Extraction

Projection

Extraction

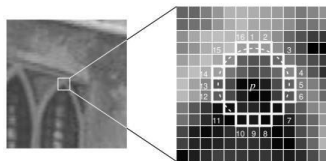
Association

Registration

Odometry

## Traditional vs Deep Learning

- Oriented FAST and Rotated BRIEF (ORB)
- SuperPoint



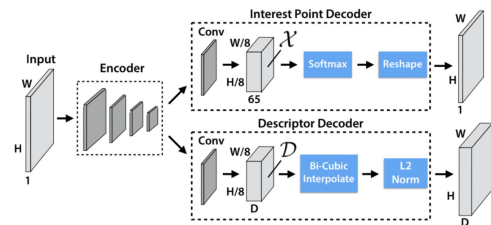
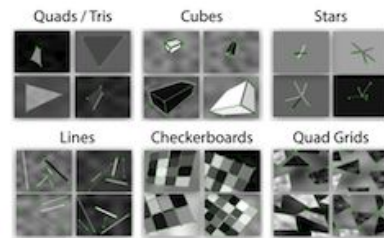
Detection

Multiscale and oriented FAST  
detection of surrounding pixels

Description

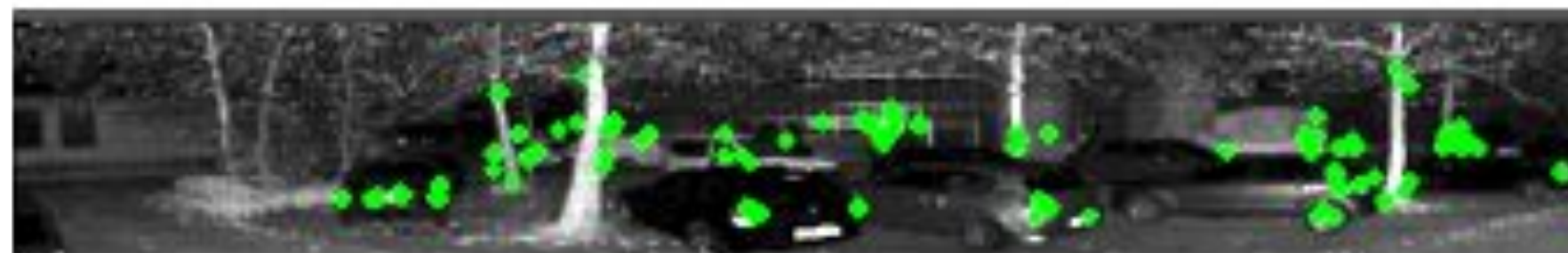
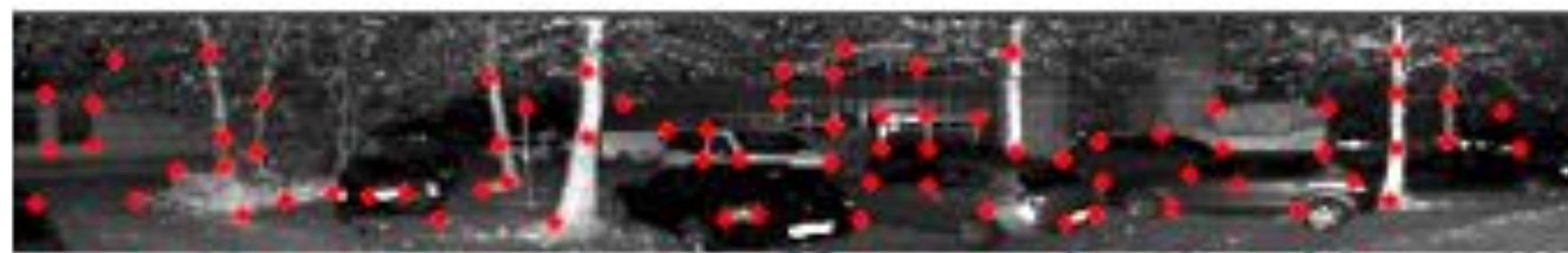
Gaussian kernel smoothing and  
binary test on image patch  
**128 bit vector**

**VS**



MagicPoint + Homographic Adaptation

semi-dense model + bi-cubic  
interpolation + L2 norm  
**256 float vector**





# Data Association

Projection

Extraction

Association

Registration

Odometry

## Brute-force approach

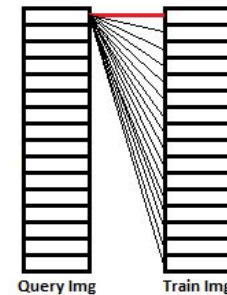
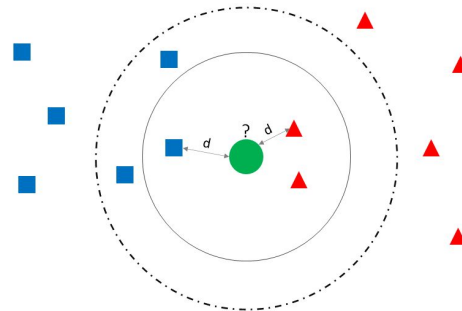
matching each descriptor with all the others

## K-nearest neighbor (k=2)

choice is made by a ratio test

## Euclidean norm check

looking for geometrical consistency



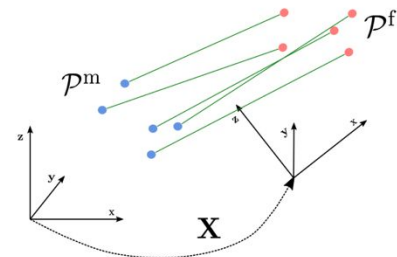
$$L(m_{k=1}, m_{k=2}) = \begin{cases} \text{keep} & \text{if } m_{k=1}.distance < m_{k=2}.distance * \text{threshold} \\ \text{discard} & \text{otherwise} \end{cases}$$



$L2(k_1, k_2)$



# Transform Registration - Method



## Incremental approach

### Iterative Closest Point (ICP)

- State  $\mathbf{X} = [\mathbf{R} \mid \mathbf{t}]$
- Perturbation  $\Delta \mathbf{x} = (\Delta x \ \Delta y \ \Delta z \ \Delta \alpha_x \ \Delta \alpha_y \ \Delta \alpha_z)$
- Operator  $\mathbf{X} \boxplus \Delta \mathbf{x} = v2t(\Delta \mathbf{x})\mathbf{X}$
- Measurement function  $\mathbf{h}_k^{icp}(\mathbf{X}) = \mathbf{R}^T(p_{j(k)}^m - \mathbf{t})$
- Error function  $\mathbf{e}_k^{icp}(\mathbf{X}) = \mathbf{h}_k^{icp}(\mathbf{X}) - p_{j(k)}^f$
- Jacobian  $\mathbf{J}_k^{icp}(\mathbf{X}) = \left( \mathbf{I} - [p_{j(k)}^m]_{\times} \right)$

## Direct approach

### Closed-form solution to Least-Square (SVD)

#### Algorithm 2 Closed-form Solution of Least-Squares Optimization

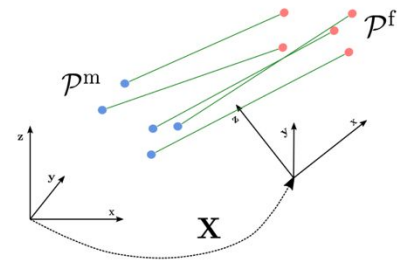
**Require:** point correspondences  $\{\langle x_0, y_0 \rangle, \dots, \langle x_K, y_K \rangle\}$

**Ensure:** closed-form solution of  $\mathbf{R}$  and  $\mathbf{t}$

```

 $\mu_x \leftarrow \frac{1}{k} \sum_{i=1}^k x_i, \quad \mu_y \leftarrow \frac{1}{k} \sum_{i=1}^k y_i$ 
 $\sigma_x \leftarrow \frac{1}{k} \sum_{i=1}^k \|x_i - \mu_x\|^2, \quad \sigma_y \leftarrow \frac{1}{k} \sum_{i=1}^k \|y_i - \mu_y\|^2$ 
 $\Sigma \leftarrow \frac{1}{k} \sum_{i=1}^k (y_i - \mu_y)(x_i - \mu_x)^T$ 
 $\mathbf{U}\mathbf{D}\mathbf{V}^T \leftarrow \text{SVD}(\Sigma)$ 
if  $\det(\mathbf{U})\det(\mathbf{V}) = 1$  then
     $\mathbf{S} = \mathbf{I}_{3 \times 3}$ 
else
     $\mathbf{S} = \text{diag}(1, 1, -1)$ 
end if
 $\mathbf{R} \leftarrow \mathbf{U}\mathbf{S}\mathbf{V}^T$ 
 $\mathbf{t} \leftarrow \mu_y - \mathbf{R}\mu_x$ 
return  $\mathbf{R}, \mathbf{t}$ 
    
```

# Transform Registration - Outlier Rejection



## Incremental approach

### Robust estimator

- L1 Omega norm of the error function
- New error term
- Reducing contributions of higher errors

$$\underset{X}{\operatorname{argmin}} \sum_{k=1}^m \rho(u_k(x))$$

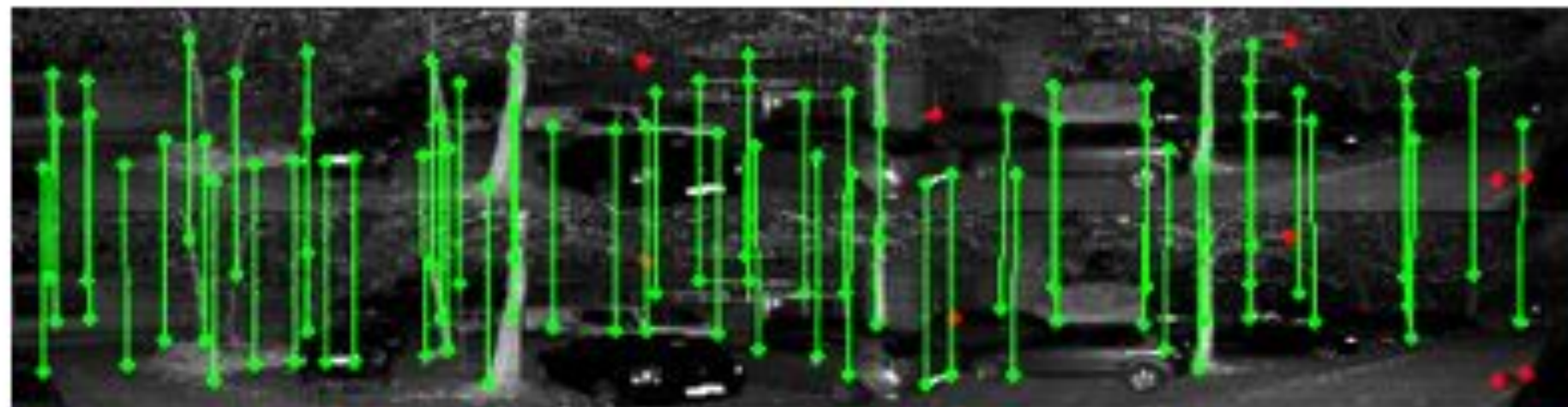
$$\begin{aligned} \mathbf{e}_k &\leftarrow \mathbf{h}_k(\check{\mathbf{x}}) \boxminus \mathbf{z}_k \\ \mathbf{J}_k &\leftarrow \frac{\partial \mathbf{e}(\check{\mathbf{x}} \boxplus \Delta \mathbf{x})}{\partial \Delta \mathbf{x}} \Big|_{\Delta \mathbf{x} = 0} \\ u_k &\leftarrow \sqrt{\mathbf{e}_k(\mathbf{x})^T \Omega_k \mathbf{e}_k(\mathbf{x})} \\ \gamma_k &\leftarrow \frac{1}{u_k} \frac{\partial \rho_k(u)}{\partial u} \Big|_{u=u_k} \\ \Omega_k &= \gamma_k \Omega_k \\ \mathbf{H} &\leftarrow \mathbf{H} + \mathbf{J}_k \Omega_k \mathbf{J}_k^T \\ \mathbf{b} &\leftarrow \mathbf{b} + \mathbf{J}_k \Omega_k \mathbf{e}_k \end{aligned}$$

## Direct approach

### Random Sample Consensus (RANSAC)

1. Randomly select a minimum amount of data
2. Compute a model (closed-form)
3. Evaluate the model (Euclidean distance)
4. Repeat the procedure k times

iterations: 
$$k = \frac{\log(1 - p)}{\log(1 - w^n)}$$



# Odometry Estimation

Projection

Extraction

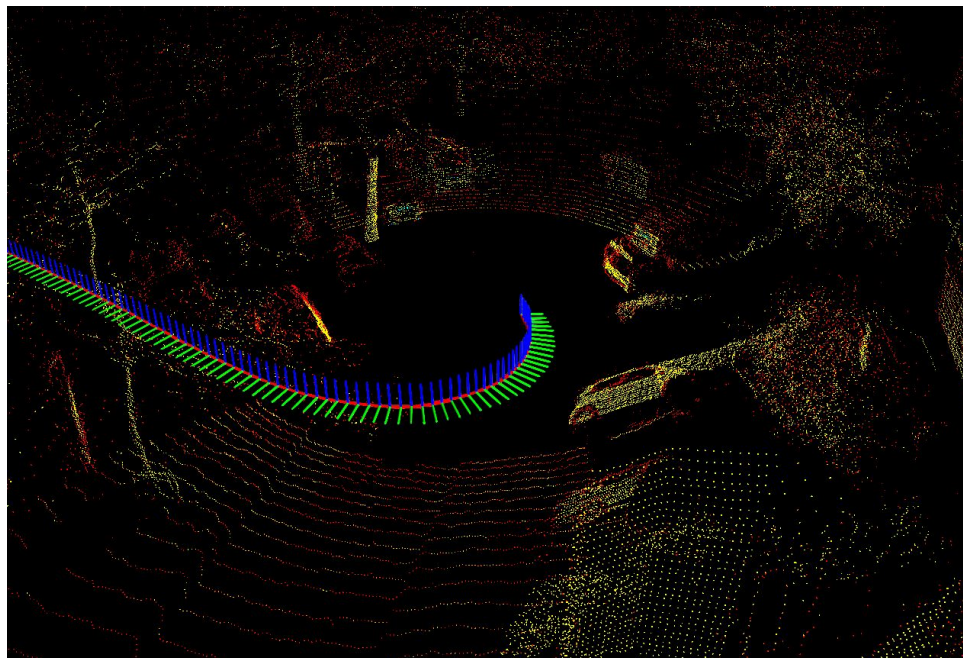
Association

Registration

Odometry

Accumulation of transforms  
frame by frame matrix multiplication

$$\mathbf{T}_k^0 = \mathbf{I}_{4 \times 4} \mathbf{T}_1^0 \mathbf{T}_2^1 \dots \mathbf{T}_k^{k-1}$$



# Experiments

## Hardware

- Ubuntu 20.04, C++
- 8-core Intel core i9 without graphic card
- LiDAR OS1-64 vertical, 1024 horizontal, 10Hz, 65536 points per frame



## GNSS estimation

conversion from geodetic to geocentric coordinates

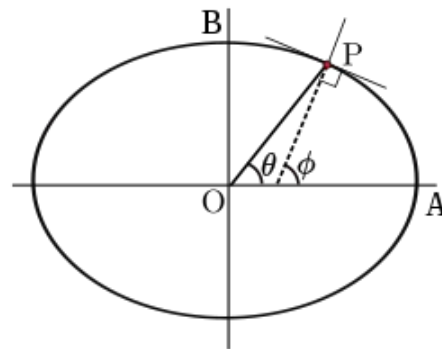
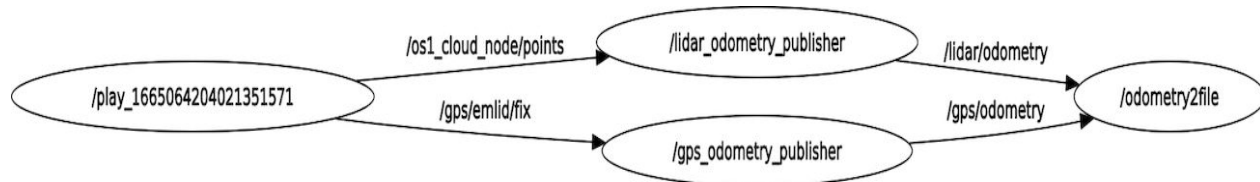
## Robot Operating System

ROS middleware for playing dataset and run pipeline

## Evaluation

Root Mean Square Error

$$RMSE = \sqrt{\frac{1}{k} \sum_{i=1}^k \|\hat{\mathbf{t}}_k - \mathbf{t}_k^{GNSS}\|^2}$$



$$x = R_{Heart}(\mathbf{P}) \cdot \cos(long) \cdot \cos(\mathbf{gLat}(lat))$$

$$y = R_{Heart}(\mathbf{P}) \cdot \sin(long) \cdot \cos(\mathbf{gLat}(lat))$$

$$z = R_{Heart}(\mathbf{P}) \cdot \sin(\mathbf{gLat}(lat))$$

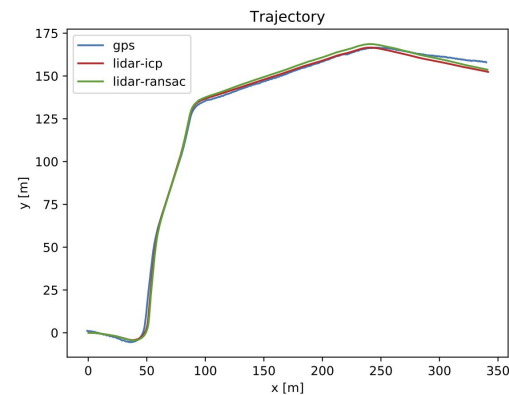
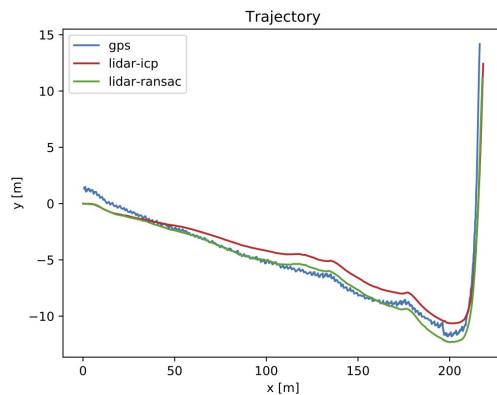
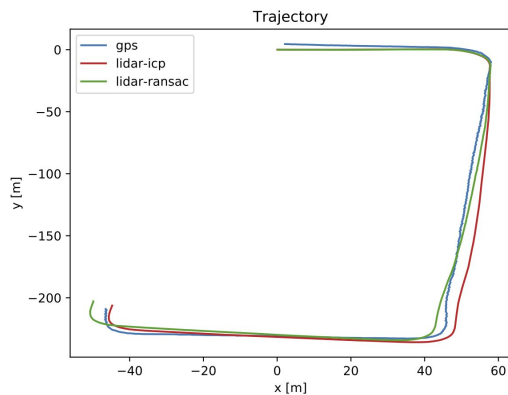
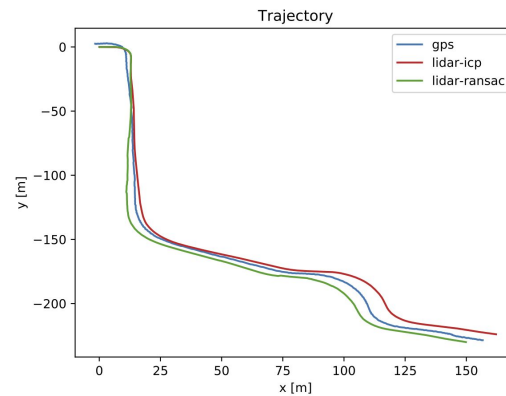
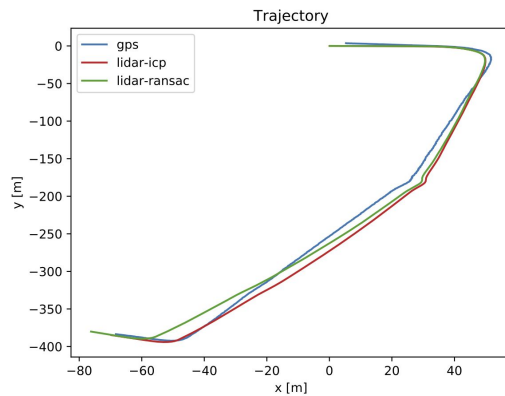
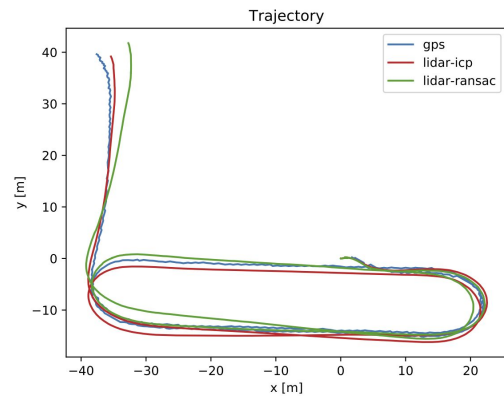




# Parameters Tuning

Feature Extraction			Tracking		
SuperPoint	nFeatures	300	BF Matcher	knnThreshold	0.7
	threshold	0.1		normType	L2/H
	nmsBlockSize	6		normThreshold	30
FAST	threshold	30	Registration		
ORB	nFeatures	300	IRLS	iterations	1
	scaleFactor	1.1		kernelThreshold	5e-5
	nLevels	8		damping	0.5
	edgeThreshold	15	RANSAC	iterations	30
	patchSize	15		inliersThreshold	20cm

# Results



# Comparison

## SuperPoint > ORB

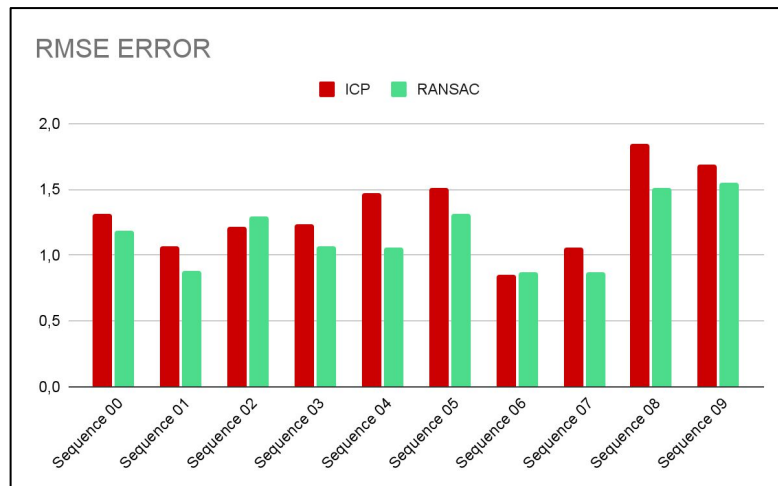
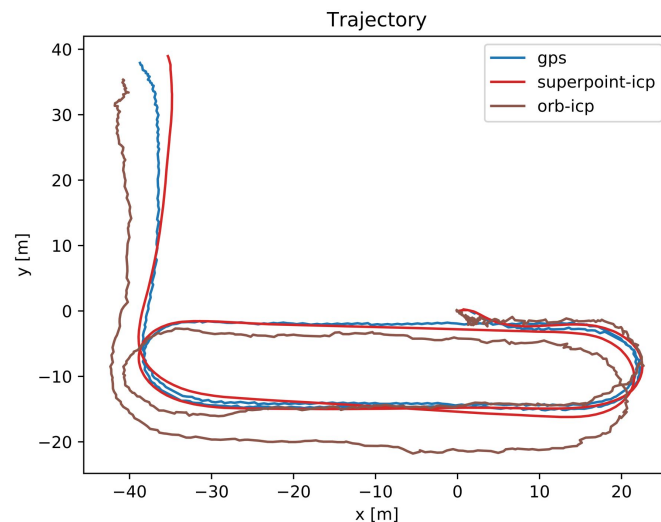
(with ICP)

- SuperPoint detections sparse and repeatable
- ORB detections poorly distributed
- ORB 110HZ >> SuperPoint 20Hz

## RANSAC > ICP

(with SuperPoint)

- RANSAC more accurate
- ICP 70 kHz >> RANSAC 20kHz
- ICP no longer valid in global optimization
- RANSAC suitable for loop closure



# Conclusions

## ➤ Feature extraction

Machine learning is overcoming traditional approaches

## ➤ Transform estimation

probabilistic framework more accurate than least-square optimization  
and more suitable for other task in SLAM frameworks

## ➤ Hardware requirements

machine learning technique feasible also without graphic card

## Future Work

- Use of LiDAR depth information in conjunction with intensity
- Registration in non-successive frame
- Loop closure detection and bundle adjustment



# Thanks

