# Завдання

Nº	8			
0	5	10	19	14
10	0	3	11	20
12	15	0	13	3
19	20	6	0	12
19	9	5	12	0

# Розв'язок

Довільний маршрут:  $(1; 2) \rightarrow (2; 3) \rightarrow (3; 4) \rightarrow (4; 5) \rightarrow (5; 1)$ 

$$F(x) = 5 + 3 + 13 + 12 + 19 = 52$$

	1	2	3	4	5	$\mathbf{d}_{\mathbf{i}}$
1	$\infty$	5	10	19	14	5
2	10	$\infty$	3	11	20	3
3	12	15	$\infty$	13	3	3
4	19	20	6	$\infty$	12	6
5	19	9	5	12	$\infty$	5

	1	2	3	4	5	$\mathbf{d}_{\mathbf{i}}$
1	$\infty$	0	5	14	9	5
2	7	8	0	8	17	3
3	9	12	$\infty$	10	0	3
4	13	14	0	$\infty$	6	6
5	14	4	0	7	$\infty$	5
dj	7	0	0	7	0	36

$$H=\sum\! d_i+\sum\! d_j \qquad \quad H_0=22+14=36$$

# Редукована матриця:

	1	2	3	4	5
1	$\infty$	0	5	7	9
2	0	8	0	1	17
3	2	12	$\infty$	3	0
4	6	14	0	$\infty$	6
5	7	4	0	0	$\infty$

# Крок 1

	1	2	3	4	5	$\mathbf{d_{i}}$
1	$\infty$	0(9)	5	7	9	5
2	0(2)	$\infty$	0(0)	1	17	0
3	2	12	$\infty$	3	0(8)	2
4	6	14	0(6)	$\infty$	6	6
5	7	4	0(0)	0(1)	$\infty$	0
di	2	4	0	1	6	

	1	2	3	4	5	$\mathbf{d_i}$
1	8	8	5	7	9	5
2	0	$\infty$	0	1	17	0
3	2	12	$\infty$	3	0	0
4	6	14	0	$\infty$	6	0
5	7	4	0	0	$\infty$	0
dj	0	4	0	0	0	

$$H(1^*; 2^*) = 36 + 9 = \underline{45}$$
  $H(1; 2) = 36 + 2 = \underline{38} \le 45$  Включаємо (1; 2).

Виключаємо 5 рядок і 4 стовпець:

	1	3	4	5	$\mathbf{d_i}$
2	$\infty$	0	1	17	0
3	2	8	3	0	0
4	6	0	$\infty$	6	0
5	7	0	0	$\infty$	0
$\mathbf{d}_{\mathbf{j}}$	2	0	0	0	2

# Крок 2

	1	3	4	5	di
2	$\infty$	0(1)	1	17	1
3	0(4)	8	3	0(6)	0
4	4	0(4)	8	6	4
5	5	0(0)	0(1)	$\infty$	0
$\mathbf{d}_{\mathbf{j}}$	4	0	1	6	

$$H(3^*;5^*)=38+6=\underline{44}$$
  $H(3;5)=38+4=\underline{42}\leq 44$  Включаємо  $(3;5)$ .

	1	3	4	5	$\mathbf{d}_{\mathbf{i}}$
2	$\infty$	0	1	17	0
3	0	$\infty$	3	8	0
4	4	0	$\infty$	6	0
5	5	0	0	8	0
$\mathbf{d_{j}}$	0	0	0	6	

## Виключаємо 3 рядок і 5 стовпець:

	1	3	4	$\mathbf{d_{i}}$
2	8	0	1	0
4	4	0	8	0
5	5	8	0	0
dj	4	0	0	4

### Крок 3

	1	3	4	$\mathbf{d_i}$
2	$\infty$	0(1)	1	1
4	0(1)	0(0)	$\infty$	0
5	1	8	0(2)	1
$\mathbf{d}_{\mathbf{j}}$	1	0	1	

$$H(5^*;4^*)=42+2=\underline{44}$$
  $H(5;4)=42+0=\underline{42}\leq 44$  Включаємо  $(5;4)$ .

	1	3	4	di
2	$\infty$	0	1	0
4	0	0	8	0
5	1	8	8	1
$\mathbf{d}_{\mathbf{j}}$	0	0	1	2

## Виключаємо 5 рядок і 4 стовпець:

	1	3	$\mathbf{d_i}$
2	8	0	0
4	0	0	0
$\mathbf{d}_{\mathbf{j}}$	0	0	0

Відповідно до матриці включаємо в гамільтонів маршрут ребра (2; 3), (4; 1).

$$(1; 2) \rightarrow (2; 3) \rightarrow (3; 5) \rightarrow (5; 4) \rightarrow (4; 1)$$
  $F(x) = 5 + 3 + 3 + 12 + 19 = 42$ 

## Програмна реалізація

```
#AN INPUT OF DISTANCES
lc = input("How many localities do you have? ");
puts("\nEnter distances:\n");
for i = 1:1c
  inp = input(" ", "s");
  temp = cellfun("str2num", strsplit(inp, " "));
 for j = 1:lc
   distances(i, j) = temp(j);
  endfor
endfor
primary_lc = lc;
primary distances = distances;
#-----
#REDUCTION
min = inf;
H0 = 0;
min vect = [];
for k = 1:2
 #transpose matrix
 if (k == 2)
   distances = distances';
  endif
  for i = 1:1c
   for j = 1:lc
     if (distances(i, j) < min)</pre>
       min = distances(i, j);
     endif
    endfor
   min vect(end+1) = min;
   min = inf;
  endfor
  for i = 1:1c
    for j = 1:lc
     distances(i, j) -= min_vect(i);
    endfor
  endfor
  for i = 1:1c
   H0 += min vect(i);
  endfor
 min vect = [];
endfor
distances = distances';
```

```
puts("\nReduced matrix:\n");
disp(distances);
printf("\nH0 = %d", H0);
#-----
#ADD EXTRA NUMERATION OF ROWS AND COLS FOR MONITORING
#CHANGES INDEPENDENTLY FROM REDUCTION OF DIMENSIONS
for i = 1:lc
 row nums(i) = i;
 col nums(i) = i;
endfor
#-----
route = [];
for permanent = 1:100
 printf("\n\n-----\n\nStep %d\n", permanent);
 #REDUCTION CONSTANTS
 min = inf;
 min vect = [];
 zero check = 0;
 for k = 1:2
   #transpose matrix
   if (k == 2)
     distances = distances';
   endif
   for i = 1:lc
     for j = 1:lc
       if (distances(i, j) == 0)
        zero check++;
       endif
       if (zero check > 1)
        min = 0;
        break;
       elseif (distances(i, j) != 0 && distances(i, j) < min)</pre>
        min = distances(i, j);
       endif
     endfor
     min_vect(k, i) = min;
     min = inf;
     zero_check = 0;
   endfor
 endfor
 distances = distances';
```

```
#ZEROS CALCULATE
```

```
\max zero = 0;
temp = 0;
for i = 1:lc
  for j = 1:lc
    if (distances(i, j) == 0)
      temp = min vect(\mathbf{1}, i) + min vect(\mathbf{2}, j);
    endif
    if (temp > max_zero)
     max zero = temp;
     \max i = i;
      \max j = j;
    endif
  endfor
endfor
#SHOW MATRIX Nº1
puts("\n1.\n");
disp(distances);
printf("\ndi =");
disp(min_vect(1, :));
printf("\ndj =");
disp(min vect(2, :));
#infinite to node in next table at coords (i,j)
distances(max i, max j) = inf;
#SHOW MATRIX №2
puts("\n2.\n");
disp(distances);
#infinite to node in next table at reverse coords (j,i)
distances(max j, max i) = inf;
#DELETE i ROW & j COLUMN & INDEXES FIX
distances(max i, :) = [];
distances(:, max_j) = [];
fcoord_node = row_nums(max_i);
scoord node = col nums(max j);
row nums (max i) = [];
col_nums(max_j) = [];
lc--;
#LAST REDUCTION
sum_for_H2 = 0;
```

```
min = inf;
 #min_vect = [];
 for k = 1:2
   #transpose matrix
   if (k == 2)
     distances = distances';
    endif
    for i = 1:1c
      for j = 1:lc
        if (distances(i, j) < min)</pre>
          min = distances(i, j);
        endif
      endfor
      \#\min \operatorname{vect}(k, i) = \min;
      if (min > 0)
        for j = 1:lc
          distances(i, j) -= min;
        endfor
        sum_for_H2 += min;
      endif
      min = inf;
    endfor
  endfor
 distances = distances';
 #SHOW MATRIX №3
 puts("\n3.\n");
 disp(distances);
 #CHECK INCLUDE
 H1 = H0 + max zero;
 H2 = H0 + sum for H2;
 printf("\nH(%d*; %d*) = %d + %d = %d", max i, max j, H0, max zero, H1);
 if (H2 <= H1)
   printf("\nH(%d; %d) = %d + %d = %d <= %d\n", max i, max j, H0,
sum_for_H2, H2, H1);
   H0 = H2;
    #ADD NODE TO ROUTE
   route(end+1, 1) = fcoord node;
    route(end, 2) = scoord node;
 endif
  #CHECK STOP
 check\_stop = 0;
  for i = 1:1c
```

```
for j = 1:1c
      if (distances(i, j) == 0 || distances(i, j) == inf)
        check_stop++;
      endif
    endfor
  endfor
  if (check stop == lc*lc)
    break;
  endif
  check stop = 0;
endfor
#FINDING LAST TWO ROUTES
#last-1 route
for i = 1:1c
  if (isinf(distances(1, i)) == 0)
    route (end+1, 1) = row nums(1);
    route(end, 2) = col_nums(i);
  endif
endfor
#last route
for i = 1:1c
  if (col_nums(i) == route(1, 1))
    route(end+1, 1) = row_nums(2);
    route(end, 2) = col nums(i);
  endif
endfor
#SORTING ROUTES
sorted routes = [];
sorted routes(end+1, 1) = route(1, 1);
sorted routes(end, 2) = route(1, 2);
route(1, :) = [];
check fullsorted = 1;
while (check fullsorted < primary lc)</pre>
  for i = 1:primary_lc-check_fullsorted
    if (sorted_routes(end, 2) == route(i, 1))
      sorted routes(end+1, 1) = route(i, 1);
      sorted routes(end, 2) = route(i, 2);
      route(i, :) = [];
      check fullsorted++;
      break;
    endif
  endfor
```

```
endwhile
```

```
#DISPLAY ROUTE
puts("\nRoute: ");
for i = 1:primary lc
  if (i == primary lc)
    printf("(%d,%d)\n", sorted routes(i,1), sorted routes(i,2));
  else
    printf("(%d,%d)->", sorted routes(i,1), sorted routes(i,2));
  endif
endfor
F = 0;
for i = 1:primary lc
  F += primary distances(sorted routes(i,1), sorted routes(i,2));
endfor
printf("F = %d\n", F);
                    Результат роботи програми
Reduced matrix:
  Inf 0 5 7
0 Inf 0 1
                 1 1/
3 0
6
      12 Inf
    2
       14 0 Inf
        4
             0 0 Inf
H0 = 36
Step 1
1.
  Inf 0 5 7 9 0 Inf 0 1 17
           Inf 3
    2
       12
       14 0 Inf
    6
        4
             0 0 Inf
di = 5 0 2 6 0
dj = 2 \ 4 \ 0 \ 1 \ 6
2.
  Inf Inf 5 7
0 Inf 0 1
                       9
                  1 17
       12 Inf
                  3
       14 0 Inf
4 0 0
    6
                       6
                     Inf
з.
            1
                 17
  Inf
       0
                  0
       Inf
    0
    4
        0 Inf
        0
             0 Inf
H(1*; 2*) = 36 + 9 = 45
```

H(1; 2) = 36 + 2 = 38 <= 45

```
-----
```

### Step 2

1.

$$di = 1 0 4 0$$

$$dj = 4 \ 0 \ 1 \ 6$$

2.

3.

$$H(2*; 4*) = 38 + 6 = 44$$
  
 $H(2; 4) = 38 + 4 = 42 <= 44$ 

#### \_\_\_\_\_

### Step 3

1.

$$di = 1 0 1$$

$$dj = 1 0 1$$

2.

3.

$$H(3*; 3*) = 42 + 2 = 44$$
  
 $H(3; 3) = 42 + 0 = 42 <= 44$ 

Route: 
$$(1,2) \rightarrow (2,3) \rightarrow (3,5) \rightarrow (5,4) \rightarrow (4,1)$$
  
F = 42