# Spatial Prediction and Model Selection

The conditional distribution,  $p(\mathbf{Y_1}|\mathbf{Y_2},\boldsymbol{\beta},\sigma^2,\phi,\tau^2)$  is normal with:

## Posterior Predictive Distribution

The (posterior) predictive distribution  $p(Y(s_0)|y)$  can be written as

$$p(Y(s_0)|y) = \int p(Y(s_0)|y, \boldsymbol{\theta})p(\boldsymbol{\theta}|y)d\boldsymbol{\theta}$$

where

The posterior predictive distribution

## Prediction

We will use cross-validation or a test/training approach to compare predictive models.

Consider three data structures: continuous, count, and binary; how should we evaluate predictions in these situations?



The Continuous Rank Probability Score (CRPS) defined as

$$CRPS(F, y) = \int_{-\infty}^{\infty} (F(u) - 1(u \ge y))^2 du,$$

where F is the CDF of the predictive distribution, is a metric that measures distance between an observed value and a distribution.

```
crps_sample(y = 0, dat = 0)

## [1] 0

crps_sample(y = 0, dat = 2)

## [1] 2

crps_sample(y = 0, dat = c(2,-2))

## [1] 1

crps_sample(y = 0, dat = c(2,0,-2))

## [1] 0.4444444

crps_sample(y = 0, dat = c(2,0,0,0,0,-2))

## [1] 0.1111111
```

## **CRPS**

Consider four situations and sketch the predictive distribution and the resultant CRPS for each scenario. How does the MSE function in each setting?

1. Narrow predictive interval centered around outcome.

2. Wide predictive interval centered around outcome.

3. Narrow predictive interval with outcome in tail.

4. Wide predictive interval with outcome in tail.

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