

# Spatial Prediction and Model Selection

## Conditional Multivariate Normal Theory

The conditional distribution,  $p(\mathbf{Y}_1|\mathbf{Y}_2, \beta, \sigma^2, \phi, \tau^2)$  is normal with:

## Posterior Predictive Distribution

The (posterior) predictive distribution  $p(Y(\mathbf{s}_0)|y)$  can be written as

$$p(Y(\mathbf{s}_0)|y) = \int p(Y(\mathbf{s}_0)|y, \boldsymbol{\theta})p(\boldsymbol{\theta}|y)d\boldsymbol{\theta}$$

where

The posterior predictive distribution

## Prediction

We will use cross-validation or a test/training approach to compare predictive models.

Consider three data structures: continuous, count, and binary; how should we evaluate predictions in these situations?

## Loss Functions

Loss functions penalize predictions that deviate from the true values.

For continuous or count data, squared error loss and absolute error loss are common.

With binary data, a zero-one loss is frequently used.

If we think about outcomes distributionally

The Continuous Rank Probability Score (CRPS) defined as

$$CRPS(F, y) = \int_{-\infty}^{\infty} (F(u) - 1(u \geq y))^2 du,$$

where  $F$  is the CDF of the predictive distribution, is a metric that measures distance between an observed value and a distribution.

## CRPS

Consider four situations and sketch the predictive distribution and the resultant CRPS for each scenario. How does the MSE function in each setting?

1. Narrow predictive interval centered around outcome.

2. Wide predictive interval centered around outcome.

3. Narrow predictive interval with outcome in tail.

4. Wide predictive interval with outcome in tail.