

Q1:

$$f(n+1) = f(n) + f(n-1), 0 \leq c * g(n) \leq f(n)$$

$$c = 4/9, \text{ and } g(n) = (3/2)^n$$

$$n = 0 \text{ 代入 } \rightarrow 4/9 * (3/2)^n = 1 > f(0) = 0 \Rightarrow \text{Wrong}$$

$$n = 1 \text{ 代入 } \rightarrow 4/9 * (3/2)^n = 2/3 < f(1) = 1 \Rightarrow \text{成立}$$

$$\text{假設 } n = k \text{ 代入時 } f(n) \geq 4/9 * (3/2)^n \geq 0 \Rightarrow \text{成立}$$

$$n = k + 1 \text{ 代入}$$

$$f(k+1) = f(k) + f(k-1)$$

$$\geq (4/9) * (3/2)^k + (4/9) * (3/2)^{k-1}$$

$$= (4/9) * (5/2) * (3/2)^{k-1} > (4/9) * (3/2)^2 * (3/2)^{k-1}$$

$$= (4/9) * (3/2)^{k+1} \text{ 成立}$$

$$\therefore \text{根據數學歸納法可以得知 } f(n) \geq 4/9 * (3/2)^n \quad \forall n \geq 1 \text{ 都成立}$$

$$\therefore \text{可以得到 } n_0 = 1 \#$$