# Fenwick Tree

A Fenwick Tree (also known as a Binary Indexed Tree) is a data structure on an array which enables fast ( $O(\log n)$ ) updates and prefix sum queries on the underlying data.

For this problem, implement a Fenwick Tree to support operations of two types: (a) increment an element in the array or (b) query the prefix sum of a portion of the array.

Problem ID: fenwick
CPU Time limit: 4 seconds
Memory limit: 1024 MB
Difficulty: 4.3

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### Input

The first line of input contains two integers N, Q, where  $1 \le N \le 5\,000\,000$  is the length of the array and  $0 \le Q \le 5\,000\,000$  is the number of operations. Then follow Q lines giving the operations. There are two types of operations:

- "+  $i \delta$ " indicates that a[i] is incremented by  $\delta$ , where  $0 \le i < N$  and  $-10^9 \le \delta \le 10^9$  (both are integers)
- "? i" is a query for the value of a[0] + a[1] + ... + a[i-1], where  $0 \le i \le N$  (for i = 0 this is interpreted as an empty sum)

You should assume that every array entry is initially 0.

# Output

For each query in the input, output one line giving the answer to that query.

#### Sample Input 1

## Sample Output 1

10 4		
+ 7 23		
? 8		
+ 3 17		
? 8		
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23 40

#### Sample Input 2

#### Sample Output 2

5 4		
+ 0 -43		
+ 4 1		
? 0		
? 5		

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