# Tiga TLA+ Specification

Time Range [Configurable]

EXTENDS Naturals, TLC, FiniteSets, Sequences

# Bounds for Model Check [Configurable]

```
MaxTime \triangleq 3
 In Tiga, we assume client and coordinator are co-located
 In this spec, we use "coordinator" to represent them
 Each coordinator is only allowed to submit MaxReqNum requests [Configurable]
 In the specification, we will only consider two roles, client and replicas
 (i.e. it can be considered as co-locating one proxy with one client)
 For the proxy-based design, we just need to replace client with proxy,
 and then the specification describes the interaction between proxy and replicas
MaxRegNum \triangleq 1
 The leader is only allowed to crash when the view < MaxViews [Configurable]
MaxViews \triangleq 3
 The set of replicas and an ordering of them [Can be configured in TLA+\ Toolbox]
Replicas \stackrel{\triangle}{=} 0 \dots 2
ReplicaOrder \triangleq \langle 0, 1, 2 \rangle
Shards \stackrel{\triangle}{=} 0 \dots 2
Coords \triangleq 0...1
LatencyBounds \triangleq [c \in Coords \mapsto 1]
ASSUME IsFiniteSet(Replicas)
ASSUME IsFiniteSet(Shards)
Assume ReplicaOrder \in Seq(Replicas)
Servers \stackrel{\triangle}{=} \{
         replicaId \mapsto e[1],
         shardId \mapsto e[2]
    ]: e \in Replicas \times Shards
```

These variables are used to implment at-most-once primitives

#### Constants

 $F \triangleq (Cardinality(Replicas) - 1) \div 2$ 

### Server Status

 $StNormal \triangleq 1$   $StViewChange \triangleq 2$   $StCrossShardSyncing \triangleq 3$   $StRecovering \triangleq 4$  $StFailing \triangleq 5$ 

## Message Types

 $MTxn \triangleq 1$ 

 $MLogEntry \stackrel{\triangle}{=} 2$  Log entry, different from index, it includes command field, which can be large in practice  $MTimestampNotification \stackrel{\triangle}{=} 3$  Leaders send the message to other leaders for timestamp agreement  $MInterReplicaSync \stackrel{\triangle}{=} 4$  Synchronize within shard group (across replicas) to ensure strict serializability  $MFastReply \stackrel{\triangle}{=} 5$  Fast Reply Message  $MSlowReply \stackrel{\triangle}{=} 6$  Slow Reply Message

The following messages are mainly for view change within each sharding group

 $MViewChangeReq \stackrel{\triangle}{=} 7$  Sent by config manager when leader/sequencer failure detected  $MViewChange \stackrel{\triangle}{=} 8$  Sent to ACK view change  $MStartView \stackrel{\triangle}{=} 9$  Sent by new leader to start view

The following messages are mainly used for periodic sync

Just as described in NOPaxos, it is an optional optimization to enable fast recovery after failure

 $MLocalSyncStatus \stackrel{\Delta}{=} 10$  Sent by the leader to ensure log durability

 $MLocalCommit \stackrel{\triangle}{=} 11$  Sent by followers as ACK

The following messages are used for periodic sync across sharding groups

This is an optional optimization to enable fast recovery

 $MPeerShardCommitStatus \stackrel{\Delta}{=} 12$ 

The following messages are mainly used for server recovery

 $MCrashVectorReq \stackrel{\triangle}{=} 13$   $MCrashVectorRep \stackrel{\triangle}{=} 14$   $MRecoveryReq \stackrel{\triangle}{=} 15$   $MRecoveryRep \stackrel{\triangle}{=} 16$  $MStartViewReq \stackrel{\triangle}{=} 17$ 

```
MCrossShardVerifyReq \stackrel{\triangle}{=} 18
MCrossShardVerifyRep \stackrel{\triangle}{=} 19
```

Config Manager (CM)'s Operations. Since CM is supported by typical viewstamped replication (VR), in this spec, we do not repeat the VR's failure recovery spec for CM

```
MCMPrepare \stackrel{\triangle}{=} 20

MCMPrepareReply \stackrel{\triangle}{=} 21

MCMCommit \stackrel{\triangle}{=} 22
```

## Message Schemas

Each server is identified by a combination of < replicald, shardId > TxnID uniquely identifies one request on one server But across replicas, the same TxnID may have different timestamps (the leader may modify the timestamp to make the request eligible to enter the early-buffer) so  $< timestamp, \ txnId >$  uniquely identifies one request across replicas

```
TxnID = [
   coordId \mapsto i \text{ in } (1 \dots),
   rId \mapsto i \text{ in } (1 \dots)
Txn = [
   mtype \mapsto MTxn
   txnId \mapsto TxnID,
   shards \mapsto Shards,
   command \mapsto command,
       \mapsto sendTime,
   bound \mapsto latencyBound
LogEntry = [
   mtype \mapsto MLogEntry
   txnId \mapsto TxnID,
   shards \mapsto Shards,
   command \mapsto command,
   timestamp \mapsto timestamp
```

After the request arrives at the *shards* and is placed into its early buffer (either with timestamp modified or not), the server will broadcast TimestampNotification to all the other servers in the same replica group to tell them the timestamp of the request on its own server

```
\begin{split} & \textit{TimestampNotification} = \left[ \\ & \textit{mtype} \mapsto \textit{MTimestampNotification}, \\ & \textit{gView} \mapsto 0 \dots x \\ & \textit{lView} \mapsto 0 \dots y \\ & \textit{sender} \mapsto \textit{src} \in \textit{Servers}, \\ & \textit{dest} \mapsto \textit{dst} \in \textit{Servers}, \\ & \textit{entry} \mapsto \textit{LogEntry} \\ \right] \end{split}
```

After leader has released the txn, it synchronizes the log with its followers. If followers are inconsistent, they will rectify their logs to keep consistent with leader

```
InterReplicaSync = [
   mtype
                \mapsto MInterReplicaSync,
   lView
                \mapsto 0 \dots y
               \mapsto src \in Servers,
   sender
              \mapsto dst \in Servers,
   dest
              \mapsto [LogEntry...]
   entries
logId (i.e., the position index of the log entry in the log list) is not necessary and it is not
described in the paper. Here we include logSlotNum in FastReply and SlowReply messages to
facilitate the check of Linearizability invariant
FastReply = [
                \mapsto \mathit{MFastReply},
   mtype
                \mapsto src \in Servers,
   sender
   dest
              \mapsto dst \in Coords,
   gView
                \mapsto 0 \dots x
   lView
                \mapsto 0 \dots x
   txnId
               \mapsto txnId
   In real implementation, we use SHA1 + Incremental Hash
               \mapsto [ entries \mapsto log entries so far cv \mapsto crashVector ]
   timestamp \mapsto i \in (1 ... MaxTime + MaxBound), logId
                                                                        \mapsto n \in (1..)
SlowReply = [
   mtype
               \mapsto MSlowReply,
   sender
            \mapsto src \in Servers,
             \mapsto c \in Coords,
   dest
   gView \mapsto 0 \dots x
   lView
            \mapsto 0 \dots x
   txnId
              \mapsto txnId
   logId
              \mapsto n \in (1..)
ViewChangeReq = [
   mtype \mapsto MViewChangeReq,
   sender \mapsto src \in Replicas, \, (by \, \mathit{configManager})
   dest \mapsto dst \in Servers,
   gView \mapsto 0 \dots x
   gVec \mapsto \text{ the } lViews \text{ for each shard}
ViewChange = [
   mtype
                \mapsto MViewChange,
   sender
              \mapsto src \in Servers,
   dest
              \mapsto dst \in Servers,
   qView
                \mapsto 0 \dots x
   gVec
               \mapsto the lViews for each shard
   lView
               \mapsto 0 \dots x
   lastNormal \mapsto v \in \mathit{ViewIDs},
   lSyncPoint \mapsto 0 . .
```

```
\mapsto l \in vLogs[1 \dots n],
   entries
             \mapsto crash vector
  cv
Tell the leaders in other sharding groups my syncPoint
MCrossShardVerifyReq = [
              \mapsto MCrossShardVerifyReq,
   mtype
   sender
             \mapsto src \in Servers,
   dest
             \mapsto dst \in Servers,
   lView
             \mapsto 0 \dots x
   gView
              \mapsto 0 \dots x
   syncedDdl \mapsto The largest timestamp of the synced entries
Reply the entries to the other leaders. These entries' log positions are beyond the syncPoint
of the receiving leader, so that the receiving leader can verify whether it needs timestamp
agreement for the txn, or even misses the txn
MCrossShardVerifyRep = [
   mtype
              \mapsto MCrossShardVerifyRep,
   sender
              \mapsto src \in Servers,
   dest
             \mapsto dst \in Servers,
   lView
              \mapsto 0 \dots x
   gView
              \mapsto 0 \dots x
   entries \mapsto l \in vLogs[1 \dots n]
StartView = [
  mtype
             \mapsto MStartView,
   sender \qquad \mapsto src \in Servers,
   dest
            \mapsto dst \in Servers,
   lView \mapsto 0 \dots x
   gView \mapsto 0 \dots x
   gVec
             \mapsto the lViews for each shard
   entries \mapsto l \in vLogs[1 \dots n],
            \mapsto \ {\rm crash \ vector}
   cv
CrashVectorReq = [
               \mapsto MCrashVectorReq,
   mtype
   sender
               \mapsto src \in Servers,
   dest
             \mapsto dst \in Servers,
   nonce
            \mapsto nonce
CrashVectorRep = [
   mtype
              \mapsto MCrashVectorRep,
   sender
                \mapsto src \in Servers,
   dest
               \mapsto dst \in Servers,
   nonce
                \mapsto nonce,
               \mapsto vector of counters
   cv
```

```
RecoveryReq = [
  mtype
                 \mapsto MRecoveryReq,
               \mapsto src \in Servers,
   sender
   dest
               \mapsto dst \in Servers,
               \mapsto\, vector of counters
   cv
RecoveryRep = [
   mtype \mapsto MRecoveryRep,
   sender \mapsto src \in Servers,
  dest \mapsto dst \in Servers,
   gView \mapsto 0 \dots x
  lView\mapsto 0\mathrel{.\,.} x
   cv \qquad \mapsto vector \ of \ counters
StartViewReq = [
              \mapsto MStartViewReq,
  mtype
   sender
              \mapsto src \in Servers,
   dest
              \mapsto dst \in Servers,
   lView
              \mapsto 0 \dots x
             \mapsto vector\ of\ counters
Follower reports to its leader
LocalSyncStatus = [
  mtype
               \mapsto MLocalSyncStatus,
   sender
               \mapsto src \in Servers,
   dest
              \mapsto dst \in Servers,
   lView
               \mapsto 0 \dots x
   lSyncPoint \mapsto 1..
              \mapsto vector of counters
Leader notifies its followers
LocalCommit = [
            \mapsto MLocalCommit,
  mtype
   sender
              \mapsto src \in Servers,
   dest
              \mapsto dst \in \mathit{Servers},
   lView
               \mapsto 0 \dots x
              \mapsto log \text{ entries}
   entries
   lCommitPoint \mapsto n \in (1...)
Each server tells its neighbors (the servers in the same region but belong to different shards)
its local commit status. This is optional optimization (only for checkpoint and failure recovery
acceleration)
\ * [Optional Optimization]
PeerShardCommitStatus = [
   mtype
               \mapsto MPeerShardCommitStatus,
```

```
sender
                 \mapsto src \in Servers,
   dest
               \mapsto dst \in Servers,
   gView
                \mapsto 0 \dots x
   timestamp \mapsto the\ largest\ committed\ timestamp
Configuration Manager (CM)'s message to prepare global information (including gView and
gVec)
In our implementation, CM is co-located on Shard -0, but from design perspective, CM is
completed standal
one and decoupled from \it Tiga~Servers
CMPrepare = [
   mtype \mapsto MCMPrepare,
   sender \mapsto src \in Servers,
   dest \mapsto dst \in Servers,
   c\mathit{View} \mapsto 0 \mathrel{.\,.} x
   gView \mapsto 0 \dots x
   gVec \mapsto [shardId \mapsto lView]
CMPrepareReply = [
   mtype \mapsto MCMPrepareReply,
   sender \mapsto src \in Servers,
   dest \mapsto dst \in Servers,
   cView\mapsto 0\mathrel{.\,.} x
   gView\mapsto 0\mathrel{.\,.} x
CMCommit = [
   mtype \mapsto MCMPrepareReply,
   sender \mapsto src \in Servers,
   \textit{dest} \mapsto \textit{dst} \in \textit{Servers},
   \mathit{cView} \mapsto 0 \mathrel{.\,.} x
   gView \mapsto 0 \dots x
```

### Network State

VARIABLES messages Set of all messages sent

### Server State

VARIABLES

```
Messages that have been processed by servers vServerProcessed\,, Log \ \text{list of entries} vLog\,, The sequencer to hold txns and release it after clock passes its timestamp (s+l)
```

vEarlyBuffer,

The buffer to hold txns on followers because these txns come too late and cannot enter early-buffer

vLateBuffer,

Each leader server has a data structure of  $\mathit{TimestampQuroum}$  to collect the timestamps from other servers for agreement

vTimestampQuorum,

One of StNormal, StViewChange, StFailing, StCrossShardSyncing, StRecovering

vServerStatus.

Global views of each server

vGView,

The g-vecs of each server

vGVec,

Local views of each server

vLView,

Current Time of the server

vServerClock.

Last lView in which this server had StNormal status

vLastNormView,

Used for collecting view change votes

vViewChange,

Used for collecting CrossShardVerify replies. After the leader have recovered their logs for its own shard, they need verify from the other shards to ensure the recovered logs satisfy strict serializability, i.e., every log has commonly-agreed timestamps across sharding groups.

vCrossShardVerifyReps,

vLSyncPoint indicates to which the server state (vLog) is consistent with the leader.

vLSyncPoint,

vLCommitPoint indicates that the log entries before this point has been locally committed, i.e., replicated to majority in this sharding groups. So followers can safely execute the logged txns

vLCommitPoint,

vLSyncQuorum is used by each leader to collect the LocalSyncStatus messages from servers in the same sharding group

vLSyncQuorum,

Locally unique string (for CrashVectorReq)

vUUIDCounter,

Crash Vector, initialized as all-zero vector

vCrashVector,

 $vCrash\,VectorReps,$ 

vRecoveryReps

### Coordinator State

 $InitServerState \triangleq$ 

```
Current Clock Time of the coordinator
VARIABLES
               vCoordClock,
         The txns that have been sent by this coordinator. This variable makes it easy to derive
         the Invariants
            vCoordTxns,
         Messages that have been processed by coordinators
            vCoordProcessed
 Configuration Manager (CM) State
VARIABLES
         Since CM is supported by traditional VR, here we do not want to repeat VR's failure
         recovery in this spec, so we make CMStatus always StNormal
            vCMStatus,
            vCMView,
         Config Manager: the latest global info the manager maintains (gView \text{ and } gVec)
            vCMGInfo,
            vCMPrepareGInfo,
         Config Manager: quorum of CMPrepareReplies
            vCMPrepareReps,
            vCMProcessed
VARIABLES ActionName
networkVars \triangleq \langle messages \rangle
serverStateVars \triangleq
    \langle vLog, vEarlyBuffer, vLateBuffer,
    vTimestampQuorum, vCrossShardVerifyReps, vServerStatus,
    vGView, vGVec, vLView, vServerClock, vLastNormView,
    vViewChange, vLSyncPoint, vLCommitPoint,
    vLSyncQuorum, vUUIDCounter, vCrashVector,
    vCrashVectorReps, vRecoveryReps, vServerProcessed
coordStateVars \triangleq \langle vCoordClock, vCoordTxns, vCoordProcessed \rangle
configManagerStateVars \triangleq \langle vCMStatus, vCMView, vCMGInfo, \rangle
                                 vCMPrepareGInfo, vCMPrepareReps,
                                vCMProcessed
InitNetworkState \stackrel{\triangle}{=} messages = \{\}
```

```
\land vServerProcessed = [serverId \in Servers \mapsto \{\}]
     \land vLog = [serverId \in Servers \mapsto \langle \rangle]
     \land vEarlyBuffer = [serverId \in Servers \mapsto \{\}]
     \land vLateBuf\!f\!er = [serverId \in Servers \mapsto \{\}]
     \land vTimestampQuorum = [serverId \in Servers \mapsto \{\}]
     \land \ \ vCrossShardVerifyReps = [serverId \in Servers \mapsto \{\}]
     \land vServerStatus
                           = [serverId \in Servers \mapsto StNormal]
     \land vGView = [serverId \in Servers \mapsto 0]
     \wedge vGVec = [
             serverId \in Servers \mapsto [
                  shardId \in Shards \mapsto 0
     \land vLView = [serverId \in Servers \mapsto 0]
     \land vServerClock = [serverId \in Servers \mapsto 1]
     \land vLastNormView
                               = [serverId \in Servers \mapsto 0]
     \land vViewChange = [serverId \in Servers \mapsto \{\}]
     \land vLSyncPoint = [serverId \in Servers \mapsto 0]
     \land vLCommitPoint = [serverId \in Servers \mapsto 0]
     \land vLSyncQuorum = [serverId \in Servers \mapsto \{\}]
     \land vUUIDCounter = [serverId \in Servers \mapsto 0]
     \land vCrashVector =
             serverId
                           \in Servers \mapsto [
                 rr \in Replicas \mapsto 0
     \land vCrashVectorReps = [serverId \in Servers \mapsto \{\}]
     \land vRecoveryReps
                            = [serverId \in Servers \mapsto \{\}]
InitCoordState \triangleq
     \land vCoordProcessed = [c \in Coords \mapsto \{\}]
     \land vCoordClock = [c \in Coords \mapsto 1]
     \land vCoordTxns = [c \in Coords \mapsto \{\}]
InitConfigManagerState \stackrel{\Delta}{=}
     \land vCMStatus = [
             replicaId \in Replicas \mapsto StNormal
     \land vCMView = [
             replicaId \in Replicas \mapsto 0
     \land vCMGInfo = [
             replicaId \in Replicas \mapsto [
                 gView \mapsto 0,
```

```
gVec \mapsto [shardId \in Shards \mapsto 0]
     \land vCMPrepareGInfo = [
              replicaId \in Replicas \mapsto \lceil
                    gView \mapsto 0,
                    gVec \mapsto [shardId \in Shards \mapsto 0]
     \land vCMPrepareReps = [
              replicaId \in Replicas \mapsto \{\}
     \land vCMProcessed = [
              replicaId \in Replicas \mapsto \{\}
PickMax(S) \stackrel{\triangle}{=} CHOOSE \quad x \in S : \forall y \in S : y \leq x
PickMin(S) \triangleq CHOOSE \quad x \in S : \forall y \in S : y > x
Min(a, b) \stackrel{\triangle}{=} \text{ if } a < b \text{ Then } a \text{ else } b
Max(a, b) \stackrel{\triangle}{=} \text{ if } a < b \text{ Then } b \text{ else } a
Send(ms) \stackrel{\triangle}{=} messages' = messages \cup ms
SeqToSet(s) \triangleq
  \{s[i]: i \in \text{DOMAIN } s\}
IsInjective(s) \stackrel{\triangle}{=}
  TRUE iff the sequence s contains no duplicates where two elements a, b of s are defined to be
  duplicates iff a = b. In other words,
  Cardinality(ToSet(s)) = Len(s)
  This definition is overridden by TLC in the Java class SequencesExt. The operator is overridden
  by the Java method with the same name.
  Also see Functions!Injective operator.
  \forall i, j \in \text{DOMAIN } s : (s[i] = s[j]) \Rightarrow (i = j)
SetToSeq(S) \triangleq
  Convert a set to some sequence that contains all the elements of the set exactly once, and
  contains no other elements.
  CHOOSE f \in [1 ... Cardinality(S) \rightarrow S] : IsInjective(f)
Remove(s, e) \triangleq
    The sequence s with e removed or s iff e \notin Range(s)
```

```
SelectSeq(s, LAMBDA \ t : t \neq e) SetToSortSeq(S, op(\_, \_)) \stackrel{\triangle}{=}
```

Convert a set to a sorted sequence that contains all the elements of the set exactly once, and contains no other elements. Not defined via CHOOSE like SetToSeq but with an additional conjunct, because this variant works efficiently without a dedicated TLC override.

```
SortSeq(SetToSeq(S), op)
```

## View ID Helpers

```
LeaderID(viewId) \triangleq ReplicaOrder[(viewId\%Len(ReplicaOrder)) + 1] \quad \text{remember } \langle \rangle \text{ are 1-indexed} isLeader(replicaId, viewId) \triangleq (replicaId = LeaderID(viewId)) PrintVal(id, exp) \triangleq Print(\langle id, exp \rangle, \text{TRUE}) ViewGreater(gv1, lv1, gv2, lv2) \triangleq \text{IF } gv1 > gv2 \text{ THEN TRUE} \text{ELSE} \text{IF } \wedge gv1 = gv2 \\ \wedge lv1 > lv2 \text{THEN TRUE} \text{ELSE} \text{ELSE} \text{FALSE}
```

Coordinator c submits a txn. We assume Coordinator can only send one txn in one tick of time. If time has reached the bound, this client cannot send request any more

```
LastAppendedTimestamp(Log) \triangleq \text{IF } Len(Log) = 0 \text{ THEN } 0
ELSE Tail(Log).timestamp
```

```
CoordSubmitTxn(c) \triangleq
    \land vCoordClock[c] < MaxTime
    \land Cardinality(vCoordTxns[c]) < MaxReqNum
    \wedge LET
            txnId \stackrel{\triangle}{=} [
                 coordId \mapsto c,
                         \mapsto Cardinality(vCoordTxns[c]) + 1
                 rId
        IN
        \land Send(\{[mtype \mapsto MTxn,
                  txnId
                             \mapsto txnId,
                  command \mapsto "",
                   Here we assume involves all shards
                  shards \mapsto Shards,
                           \mapsto vCoordClock[c],
                  bound \mapsto LatencyBounds[c],
```

```
sender \mapsto c,
                 dest
                        \mapsto serverId
           : serverId \in Servers\})
        \land vCoordClock' = [vCoordClock \ EXCEPT \ ![c] = vCoordClock[c] + 1]
        \land vCoordTxns' = [vCoordTxns \ EXCEPT \ ![c] = vCoordTxns[c] \cup \{txnId\}]
Handle Txn(m) \triangleq
   LET
        myServerId \stackrel{\triangle}{=} m.dest
        newLog \triangleq [
                        \mapsto MLogEntry,
            mtype
            txnId
                        \mapsto m.txnId,
            command \mapsto m.command,
            shards
                       \mapsto m.shards,
            timestamp \mapsto Max(LastAppendedTimestamp(vLog[myServerId]), m.st + m.bound)
        serversInOneReplica \stackrel{\Delta}{=} \{s \in Servers : s.replicaId = myServerId.replicaId\}
   IN
        \land isLeader(myServerId.replicaId, vLView[myServerId])
        \land vEarlyBuffer' = [
            vEarlyBuffer \ except \ ![myServerId]
                 = vEarlyBuffer[myServerId] \cup \{newLog\}]
         Broadcast timestamp notifications to other shards
        \land Send(\{[
                    \mapsto MTimestampNotification,
            mtype
            gView \mapsto vGView[myServerId],
           lView \mapsto vLView[myServerId],
            sender \mapsto myServerId,
                     \mapsto dstServerId,
            dest
                     \mapsto newLog
           ]: dstServerId \in serversInOneReplica\})
        \land UNCHANGED \langle vLateBuffer \rangle
       \land \neg isLeader(myServerId.replicaId, vLView[myServerId])
        \land \lor \land newLog.timestamp = (m.st + m.bound)
                \land vEarlyBuffer' = [
                        vEarlyBuffer except ![myServerId]
                            = vEarlyBuffer[myServerId] \cup \{newLog\}
                \land UNCHANGED \langle vLateBuffer \rangle
            \vee \land \neg (newLog.timestamp = (m.st + m.bound))
                \land vLateBuffer' = [
                        vLateBuffer except ![myServerId]
                             = vLateBuffer[myServerId] \cup \{newLog\}
```

```
\land UNCHANGED \langle vEarlyBuffer \rangle
        \land UNCHANGED \langle network Vars \rangle
HandleTimestampNotification(m) \stackrel{\Delta}{=}
   LET
        myServerId \triangleq m.dest
        quorum \stackrel{\triangle}{=} \{
           msq \in vTimestampQuorum[myServerId]
                : \land msg.entry.txnId = m.entry.txnId
                    \land msg.gView = m.gView
                    \land m.gView = vGView[myServerId]
           \} \cup \{m\}
   IN
     Only leader does timestamp agreement
    \land vGView[myServerId] = m.qView
    \land vGVec[myServerId][m.sender.shardId] = m.lView
    \land isLeader(myServerId.replicaId, vLView[myServerId])
    \land vTimestampQuorum' = [
           vTimestampQuorum \ EXCEPT \ ![myServerId]]
                = vTimestampQuorum[myServerId] \cup \{m\}
    \land IF Cardinality(quorum) = Cardinality(m.entry.shards)
        Timestamp quorum established: Update the timestamp of the txn in Sequencer
               maxTimestampTxn \triangleq
                   CHOOSE x \in quorum:
                               \in quorum:
                          y.entry.timestamp \le x.entry.timestamp
               sequencingTxn \triangleq
                   CHOOSE x \in vEarlyBuffer[myServerId]:
                       x.txnId = m.entry.txnId
           IF maxTimestampTxn.entry.timestamp > sequencingTxn.timestamp
            THEN
               vEarlyBuffer' = [vEarlyBuffer \ Except \ ![myServerId]]
                    = (vEarlyBuffer[myServerId] \setminus \{sequencingTxn\}) \cup \{maxTimestampTxn.entry\}]
            ELSE UNCHANGED \langle vEarlyBuffer \rangle
        ELSE
        Timestamp quorum not sufficient so far: do not take further actions
           UNCHANGED \langle vEarlyBuffer \rangle
```

```
HandleInterReplicaSync(m) \stackrel{\Delta}{=}
    \land m.lView = vLView[m.dest]
    Even if m's crash Vector is newer (larger value), we do not accept it. The consistency of
    crashVector will finally be solved during viewchange
    \land m.crashVector[m.sender] = vCrashVector[m.sender]
    \land \neg isLeader(m.dest.replicaId, vLView[m.dest])
        myServerId \stackrel{\triangle}{=} m.dest
       syncedTxnIds \stackrel{\triangle}{=} \{m.entries[i].txnId : i \in 1 ... Len(m.entries)\}
        currentSyncPoint \stackrel{\triangle}{=} Len(vLSyncPoint[myServerId])
            \land currentSyncPoint < Len(m.entries)
            \land vLog' = [vLog \ EXCEPT \ ![myServerId] = m.entries]
         Kick synced entries out of earlyBuffer
             \land vEarlyBuffer' = [
                    vEarlyBuffer except ![myServerId]
                         = \{msg \in vEarlyBuffer[myServerId] :
                              msg.txnId \notin syncedTxnIds
         Kick synced entries out of late buffer. In actual implementation, InterReplicaSync only
         carries log indices, and the entries are fetched from Late Buffer first, if still missing,
         then it will go to ask leader. Such a design can save much unnessary transmission in
         practice.
             \land vLateBuffer' = [
                    vLateBuffer \ except \ ![myServerId]]
                         = \{msg \in vLateBuffer[myServerId] :
                              msg.txnId \notin syncedTxnIds
         Kick synced entries out of timestamp quorum. These txns have been synced, no need
         to record in TimestampQuorum
             \land vTimestampQuorum' = [
                    vTimestampQuorum \ EXCEPT \ ![myServerId]]
                         = \{ msg \in vTimestampQuorum[myServerId] : 
                              msq.txnId \notin syncedTxnIds
             \land vLSyncPoint' = [
                    vLSyncPoint \ \text{EXCEPT} \ ![myServerId] = Len(m.entries)]
         Send slow-replies to coordinators
             \land Send({[
                      mtype \mapsto MSlowReply,
                      sender \mapsto myServerId,
                               \mapsto m.entries[i].txnId.coordId,
                      gView \mapsto vGView[myServerId],
                      lView \mapsto vLView[myServerId],
```

```
txnId
                                 \mapsto m.entries[i].txnId,
                       logId
                                 \mapsto i
                 : i \in (currentSyncPoint + 1) .. Len(m.entries)\})
         \lor \land currentSyncPoint \ge Len(m.entries)
              Noting new to sync
             \land UNCHANGED \langle network Vars, vLog, vEarly Buffer,
                                    vLateBuffer, vTimestampQuorum, vLSyncPoint \rangle
StartLeaderFail(serverId) \stackrel{\Delta}{=}
     This leader fails
    LET
         serversInOneShard \stackrel{\Delta}{=} \{
             s \in Servers : s.shardId = serverId.shardId
         aliveReplicas \triangleq \{
             s \in serversInOneShard:
                                               \land vServerStatus[s] = StNormal
                                               \land s \neq serverId
         }
    IN
     if the current alive replicas are less than QuorumSize
     Then no more replicas in this sharding group can fail (by assumption of consensus)
    If Cardinality(aliveReplicas) > QuorumSize then
         vServerStatus' = [vServerStatus \ Except \ ![serverId] = StFailing]
                UNCHANGED \langle vServerStatus \rangle
     ELSE
DetectLeaderFail(cmReplicaId) \stackrel{\Delta}{=}
    \exists shardId \in Shards:
       LET
            lView \stackrel{\triangle}{=} vCMGInfo[cmReplicaId].gVec[shardId]
            leaderId \triangleq LeaderID(lView)
            serverId \triangleq [
                replicaId \mapsto leaderId,
                shardId
                             \mapsto shardId
       vServerStatus[serverId] = StFailing
SelectProperLView(currentView, shardId) \stackrel{\Delta}{=}
    LET
         aliveReplicaId \stackrel{\Delta}{=} CHOOSE \ replicaId \in Replicas :
                                 vServerStatus[shardId][replicaId] = StNormal
    IN
       Ensure 1 the new view is larger than currentView
     * (2) its corresponding leader happens to be the selected aliveReplicaId
```

```
(currentView \div Cardinality(Replicas) + 1) * Cardinality(Replicas) + aliveReplicaId)
PrepareViewChange(cmReplicaId) \stackrel{\Delta}{=}
   LET
       newGVec \triangleq [
           shardId \in Shards \mapsto
               SelectProperLView(vCMGInfo[cmReplicaId].gVec[shardId], shardId)
   IN
    \land vCMPrepareGInfo' = [vCMPrepareGInfo \ EXCEPT \ ! [cmReplicaId] =
              gView \mapsto vCMGInfo[cmReplicaId].gView + 1,
                     \mapsto newGVec
              gVec
    \land Send({[
            mtype \mapsto MCMPrepare,
            sender \mapsto cmReplicaId,
                     \mapsto dstRid,
            dest
            cView \mapsto vCMView[cmReplicaId],
            gView \mapsto vCMPrepareGInfo'[cmReplicaId].gView,
            gVec
                   \mapsto newGVec
      ]: dstRid \in Replicas\})
Launch View Change (cmReplicaId) \stackrel{\Delta}{=}
   IF \land is Leader (cmReplicaId, vCMView[cmReplicaId])
       \land DetectLeaderFail(cmReplicaId)
    THEN
       Prepare View Change (cmReplicaId)
    ELSE
       UNCHANGED \langle network Vars \rangle
HandleCMPrepare(m) \stackrel{\Delta}{=}
    \land m.cView = vCMView[m.dest]
    \land \quad m.gView > vCMGInfo[m.dest].gView
    gView \mapsto m.gView,
              gVec \mapsto m.gVec
    \land Send(\{[
```

```
mtype \mapsto MCMPrepareReply,
             sender \mapsto m.dest,
             dest
                      \mapsto m.src,
             cView \mapsto m.cView,
             gView \mapsto m.gView
       ]})
HandleCMPrepareReply(m) \stackrel{\Delta}{=}
    \land m.cView = vCMView[m.dest]
    \land isLeader(m.dest, vCMView[m.dest])
    \land m.gView = vCMPrepareGInfo[m.dest].gView
    \land vCMPrepareReps' = [vCMPrepareReps \ EXCEPT \ ! [m.dest] =
           vCMPrepareReps[m.dest] \cup \{m\}
    \land LET
           quorum \stackrel{\triangle}{=} \{mm \in vCMPrepareReps[m.dest] : mm.gView = m.gView\}
       IN
       IF Cardinality(quorum) = QuorumSize THEN
             Quorum sufficient, the prepared GInfo is persisted and can be safely used
            \land vCMGInfo' = [vCMGInfo \ EXCEPT \ ! [m.dest] =
                   vCMPrepareGInfo[m.dest]
            notify other follower CM, so that they can catch up with the leader
            \land Send(\{[
                     mtype \mapsto MCMCommit,
                     sender \mapsto m.dest,
                     dest
                              \mapsto rid.
                     cView \mapsto m.cView,
                     gView \mapsto m.gView
               ]: rid \in \{r \in Replicas : r \neq m.dest\}\})
            start view change, broadcast view change request to every server
            \land Send(\{[
                     mtype \mapsto MViewChangeReg,
                     sender \mapsto m.dest,
                              \mapsto serverId,
                              \mapsto vCMGInfo'[m.dest].gView,
                     gVec
                              \mapsto vCMGInfo'[m.dest].gVec
               ]: serverId \in Servers\})
        ELSE
           UNCHANGED (network Vars, vCMGInfo)
HandleCMCommit(m) \triangleq
    \land m.cView = vCMView[m.dest]
    \land \neg isLeader(m.dest, vCMView[m.dest])
    \land m.gView = vCMPrepareGInfo[m.dest].gView
```

```
\land vCMGInfo' = [vCMGInfo \text{ except } ![m.dest] =
                      vCMPrepareGInfo[m.dest]
Handle View Change Req(m) \triangleq
   LET
       myServerId \stackrel{\triangle}{=} m.dest
       myLeader \stackrel{\triangle}{=} \text{CHOOSE } s \in Servers :
                      \land s.replicaId = LeaderID(m.gVec[myServerId.shardId])
                      \land s.shardId = myServerId.shardId
   IN
    If the msg's view is lower, ignore
    \land vGView[myServerId] < m.qView
    \land IF vServerStatus[myServerId] = StNormal Then
           \land vServerStatus' = [vServerStatus \ EXCEPT \ ![myServerId] = StViewChange]
           UNCHANGED \langle vServerStatus, vLastNormView \rangle
    \land vGView' = [
           vGView \ \text{EXCEPT} \ ![myServerId] = m.vGView
    \wedge vGVec' = [
           vGVec \ \text{EXCEPT} \ ![myServerId] = m.gVec
    \land vLView' = [
           vLView \ \text{EXCEPT} \ ![myServerId] = m.qVec[myServerId.shardId]
    Clear ealry buffer,
    \land vEarlyBuffer' = [
           vEarlyBuffer \ except \ ![myServerId] = \{\}
    Clear late buffer
    \land vLateBuffer' = [
           vLateBuffer \ Except \ ![myServerId] = \{\}
    Clear timestamp quorum
    \land vTimestampQuorum' = [
           vTimestampQuorum \ EXCEPT \ ![myServerId] = \{\}
    {\bf Clear}\ vCrossShardVerifyReps
    \land vCrossShardVerifyReps' = [
           serverId \in Servers \mapsto \{\}
    Send ViewChange to the myLeader
    \land Send(\{[
```

```
gView
                                  \mapsto m.vGView,
                   gVec
                                  \mapsto m.qVec,
                   lView
                                  \mapsto vLView'[myServerId],
                   lastNormal \mapsto vLastNormView'[myServerId],
                   lSyncPoint \mapsto vLSyncPoint[myServerId],
                   entries
                                  \mapsto vLog[myServerId],
                                  \mapsto vCrashVector[myServerId]
                   cv
              ]})
  Define a comparison function based on the key
Compare(a, b) \triangleq
          a.timestamp < b.timestamp
    \lor \land a.timestamp = b.timestamp
         \land \ a.txnId.coordId < b.txnId.coordId
        \land a.timestamp = b.timestamp
         \land a.txnId.coordId = b.txnId.coordId
         \land a.txnId.rId < b.txnId.rId
isCrashVectorValid(m) \stackrel{\Delta}{=}
     \land \forall rr \in Replicas : vCrashVector[m.dest][rr] \leq m.cv[rr]
     \land vCrashVector' = [
             vCrashVector \ \text{EXCEPT } ![m.dest] = [
                 rr \in Replicas \mapsto Max(m.cv[rr], vCrashVector[m.dest][rr])
CountVotes(entry, logSets) \triangleq
    LET
         validCandidates \stackrel{\triangle}{=} \{s \in logSets : \exists e \in s :
                                     \land e.timestamp = entry.timestamp
                                     \land e.txnId = entry.txnId
    IN
         Cardinality(validCandidates)
ReBuildLogs(vcQuorum) \triangleq
    LET
         refinedQuorum \stackrel{\triangle}{=} \{m \in vcQuorum :
                                      \forall msg \in vcQuorum : msg.lastNormal \leq m.lastNormal \}
        lSyncPoints \triangleq \{m.lSyncPoint : m \in refinedQuorum\}
        largestLSyncPointVC \stackrel{\Delta}{=} CHOOSE \ vc \in refinedQuorum :
                                        \forall sp \in lSyncPoints : sp \leq vc.lSyncPoint
```

mtype

sender

dest

 $\mapsto MViewChange$ ,

 $\mapsto myServerId$ ,

 $\mapsto myLeader$ ,

```
syncedLogSeq \triangleq SubSeq(largestLSyncPointVC.entries, 1, largestLSyncPointVC.lSyncPoint)
        timestampBoundary \stackrel{\Delta}{=} \text{ if } largestLSyncPointVC.lSyncPoint = 0 \text{ then } 0
                                ELSE syncedLogSeq[largestLSyncPointVC.lSyncPoint].timestamp
        logSets \triangleq \{SeqToSet(m.entries) : m \in refinedQuorum\}
        allLogs \triangleq \text{UNION } logSets
        allUnSyncedLogs \triangleq \{entry \in allLogs : entry.timestamp > timestampBoundary\}
        unSyncedLogs \triangleq \{entry \in allUnSyncedLogs : 
            CountVotes(entry, logSets) \ge RecoveryQuorumSize
        unSyncedLogSeq \triangleq SetToSortSeq(unSyncedLogs, Compare)
   IN
   syncedLogSeg \circ unSyncedLogSeg
SelectEntriesBeyondCommitPoint(entries, timestamp) \stackrel{\Delta}{=}
   LET
        validLogIndices \triangleq \{
            i \in 1 ... Len(entries) : entries[i].timestamp > timestamp
        startIndex \stackrel{\triangle}{=} PickMin(validLogIndices)
   SubSeq(entries, startIndex, Len(entries))
Handle View Change(m) \triangleq
   LET
        myServerId \triangleq m.dest
        serversInOneShard \stackrel{\triangle}{=} \{s \in Servers : s.shardId = myServerId.shardId\}
        leadersInAllShard \triangleq 
                s \in Servers : s.replicaId = isLeader(s.replicaId, m.gVec[s.shardId])
        }
   IN
       \lor ViewGreater(m.qView, m.lView, vGView[myServerId], vLView[myServerId])
        \lor \land m.gView = vGView[myServerId]
            \land m.lView = vLView[myServerId]
            \land vServerStatus[myServerId] = StViewChange
    \land isLeader(myServerId.replicaId, m.lView)
    \land vGView' = [vGView \ EXCEPT \ ! [myServerId] = m.qView]
    \land vLView' = [vLView \ EXCEPT \ ! [myServerId] = m.lView]
    \land vGVec' = [vGVec \ EXCEPT \ ![myServerId] = m.gVec]
    \land vViewChange' = [
            vViewChange \ \text{EXCEPT } ![myServerId] = {
                vc \in vViewChange[myServerId]:
                   vc.lView = m.lView
           \} \cup \{m\}
    \land IF Cardinality(vViewChange'[myServerId]) = QuorumSize Then
            \land vLog' = [vLog \ EXCEPT \ ![myServerId] = ReBuildLogs(vViewChange'[myServerId])]
```

```
\land vServerStatus' = [vServerStatus \ Except \ ! [myServerId] = StCrossShardSyncing]
         Even after the log is recovered within one shard,
           * The newly elected leader cannot StartView
           * It needs to verify with other shards' leaders to ensure strict serializability
             \land vViewChange' = [vViewChange \ Except \ ![myServerId] = \{\}]
             \land Send({[
                                    \mapsto MCrossShardVerifyReg,
                       mtype
                       sender
                                    \mapsto myServerId,
                       dest
                                    \mapsto dst,
                       lView
                                    \mapsto vLView'[myServerId],
                                    \mapsto vGView'[myServerId],
                       gView
                       syncedDdl \mapsto vLog[myServerId][vLSyncPoint[myServerId]].timestamp
                 ]: dst \in leadersInAllShard\})
         ELSE
             \land vServerStatus' = [vServerStatus \ EXCEPT \ ! [myServerId] = StViewChange]
             \land UNCHANGED \langle network Vars, vLog \rangle
Handle CrossShard VerifyReq(m) \triangleq
    LET
        myServerId \stackrel{\Delta}{=} m.dest
        myLog \triangleq vLog[myServerId]
logSet \triangleq SeqToSet(myLog)
        unVerifiedLogs \triangleq \{
             e \in logSet: \land e.timestamp > m.syncedDdl
                              \land \quad m.sender \in e.shards
        }
        unVerifiedLogList \triangleq SetToSortSeq(unVerifiedLogs, Compare)
    ΙN
    \land m.gView = vGView[myServerId]
    \land m.lView = vGVec[myServerId][m.sender.shardId]
    \land Send(\{[
              mtype
                           \mapsto MCrossShardVerifyRep,
                           \mapsto myServerId,
              sender
              dest
                           \mapsto m.sender,
              lView
                           \mapsto vLView[myServerId],
              qView
                           \mapsto vGView[myServerId],
              entries
                           \mapsto unVerifiedLogList
        ]})
Handle CrossShard VerifyRep(m) \stackrel{\Delta}{=}
    LET
        myServerId \stackrel{\Delta}{=} m.dest
        myLog \triangleq vLog[myServerId]
        myLogSet \triangleq SeqToSet(myLog)
    IN
```

```
\land m.gView = vGView[myServerId]
    \land m.lView = vGVec[myServerId][m.sender.shardId]
    \land vCrossShardVerifyReps' = [
            vCrossShardVerifyReps except ![myServerId] =
                vCrossShardVerifyReps[myServerId] \cup \{m\}]
    \land IF Cardinality(vCrossShardVerifyReps'[myServerId]) = Cardinality(Shards)
         THEN
            LET
                unVerifiedLogs \stackrel{\triangle}{=} UNION \{SeqToSet(mm.entries) :
                     mm \in vCrossShardVerifyReps'[myServerId]
                maxTimestampLogs \triangleq \{
                     e \in unVerifiedLogs:
                        \forall x \in unVerifiedLogs:
                            \forall x.txnId \neq e.txnId
                            \forall x.timestamp \leq e.timestamp
                agreedLogs \triangleq \{
                     e \in maxTimestampLogs:
                         the reciving shard is missing this txn
                         \forall x \in myLogSet : x.txnId \neq e.txnId
                         \forall \exists x \in myLogSet : x.timestamp < e.timestamp
                goodLogs \triangleq \{
                     e \in myLogSet : \forall x \in agreedLogs : x.txnId \neq e.txnId
                completeLogs \triangleq goodLogs \cup agreedLogs
                newLogList \stackrel{\triangle}{=} SetToSortSeq(completeLogs, Compare)
            IN
                vLog' = [vLog \ EXCEPT \ ![myServerId] = newLogList]
         ELSE
            UNCHANGED \langle vLoq \rangle
BuildGlobalConsistentLog(serverId, entries) \stackrel{\Delta}{=}
   LET
        myEntries \triangleq \{
             entry \in entries : \land serverId \in entry.shards
                                \land \forall e \in entries:
                                    If e.txnId = entry.txnId then
                                         e.timestamp \leq entry.timestamp
                                     ELSE TRUE
        }
   IN
    SetToSortSeq(myEntries, Compare)
```

```
HandleStartView(m) \triangleq
   LET
       myServerId \triangleq m.dest
   IN
       \lor ViewGreater(m.qView, m.lView, vGView[myServerId], vLView[myServerId])
        \lor \land m.gView = vGView[myServerId]
           \land m.lView = vLView[myServerId]
           \land \lor vServerStatus[myServerId] = StViewChange
               \lor vServerStatus[myServerId] = StRecovering
    \land vGView' = [vGView \ EXCEPT \ ! [myServerId] = m.gView]
    \land vLView' = [vLView \ EXCEPT \ ! [myServerId] = m.gLView]
    \land vGVec' = [vGVec \ EXCEPT \ ! [myServerId] = m.vGVec]
    \land vServerStatus' = [vServerStatus \ Except \ ![myServerId] = StNormal]
    \wedge vLoq' = [vLoq \text{ EXCEPT } ! [myServerId] = m.entries]
    \land vEarlyBuffer' = [vEarlyBuffer \ EXCEPT \ ![myServerId] = \{\}]
    \land vLateBuffer' = [vLateBuffer \ EXCEPT \ ! [myServerId] = \{\}]
    \land vTimestampQuorum' = [vTimestampQuorum \ EXCEPT \ ![myServerId] = \{\}]
       vCrossShardVerifyReps' = [
           vCrossShardVerifyReps Except ![myServerId] = \{\}
    \land vLSyncPoint' = [vLSyncPoint \ EXCEPT \ ![myServerId] = Len(vLog'[myServerId])]
    \land vLastNormView' = [vLastNormView \ Except \ ![myServerId] = m.lView]
    \land vViewChange' = [vViewChange \ EXCEPT \ ![myServerId] = \{\}]
    \land vLSyncQuorum' = [vLSyncQuorum \ EXCEPT \ ![myServerId] = \{\}]
    \land vCrashVectorReps' = [vCrashVectorReps \ EXCEPT \ ![myServerId] = \{\}]
    \land vRecoveryReps' = [vRecoveryReps \ EXCEPT \ ![myServerId] = \{\}]
ResetServerState(serverId) \stackrel{\Delta}{=}
    \land vLog' = [vLog \ EXCEPT \ ![serverId] = \langle \rangle]
    \land vEarlyBuffer' = [vEarlyBuffer \ EXCEPT \ ![serverId] = \{\}]
    \land vLateBuffer' = [vLateBuffer \ except \ ![serverId] = \{\}]
    \land vTimestampQuorum' = [vTimestampQuorum \ EXCEPT \ ! [serverId] = \{\}]
    \land vCrossShardVerifyReps' = [
           vCrossShardVerifyReps Except ![serverId] = \{\}
    \land vGView' = [vGView \ EXCEPT \ ![serverId] = 0]
    \land vGVec' = [vGVec \ EXCEPT \ ![serverId] = [s \in Shards \mapsto 0]]
    \land vLView' = [vLView \ EXCEPT \ ![serverId] = 0]
    \land vLastNormView' = [vLastNormView \ EXCEPT \ ! [serverId] = 0]
    \land vViewChange' = [vViewChange \ EXCEPT \ ![serverId] = \{\}]
    \land vLSyncPoint' = [vLSyncPoint except ![serverId] = 0]
    \land vLCommitPoint' = [vLCommitPoint EXCEPT ! [serverId] = 0]
    \land vLSyncQuorum' = [vLSyncQuorum \ EXCEPT \ ![serverId] = \{\}]
    \land vCrashVector' = [vCrashVector except ! [serverId] = [
```

```
rr \in Replicas \mapsto 0
    \land vCrashVectorReps' = [vCrashVectorReps \ EXCEPT \ ![serverId] = \{\}]
    \land vRecoveryReps' = [vRecoveryReps \ EXCEPT \ ![serverId] = \{\}]
    \land vServerProcessed' = [vServerProcessed \ EXCEPT \ ![serverId] = \{\}]
StartServerRecovery(serverId) \triangleq
    LET
        serversInOneShard \triangleq \{
             s \in Servers : s.shardId = serverId.shardId
        nonce \triangleq vUUIDCounter[serverId] + 1
    IN
    \land vServerStatus' = [vServerStatus \ EXCEPT \ ! [serverId] = StRecovering]
    \land vUUIDCounter' = [vUUIDCounter \ EXCEPT \ ![serverId] = vUUIDCounter[serverId] + 1]
    \land Send({[
                            \mapsto MCrashVectorReq,
              mtype
              sender
                            \mapsto serverId,
                            \mapsto dst.
              dest
              nonce
                            \mapsto nonce
       : dst \in serversInOneShard\})
HandleCrashVectorReq(m) \triangleq
    LET
        myServerId \stackrel{\triangle}{=} m.dest
    IN
    \land \ \ vServerStatus[myServerId] = StNormal
    \land Send({[
                            \mapsto MCrashVectorRep,
              mtype
                            \mapsto myServerId,
              sender
              dest
                            \mapsto m.sender,
              nonce
                            \mapsto m.nonce,
                            \mapsto vCrashVector[myServerId]
       ]})
AggregateCV(serverId) \triangleq
    LET
        cvQuorum \stackrel{\triangle}{=} \{m.cv : m \in vCrashVectorReps[serverId]\}
        cvValQuorum \stackrel{\Delta}{=} [rr \in Replicas \mapsto \{cv[rr] : cv \in cvQuorum\}]
    IN
        [rr \in Replicas \mapsto PickMax(cvValQuorum[rr])]
Handle Crash Vector Rep(m) \triangleq
    LET
        myServerId \triangleq m.dest
```

```
IN
       vServerStatus[myServerId] = StRecovering
    \land vUUIDCounter[myServerId] = m.nonce
    \land vCrashVectorReps' = [
            vCrashVectorReps except ![myServerId] = vCrashVectorReps \cup \{m\}
    \land IF Cardinality(vCrashVectorReps'[myServerId]) = QuorumSize Then
                acv \triangleq AggregateCV(myServerId)
                myCV \triangleq [acv \ EXCEPT \ ![myServerId] = acv[myServerId] + 1]
            IN
            \land vCrashVector' = [
                    vCrashVector \ \text{except } ![myServerId] = myCV
            \wedge \ Send(\{[
                                     \mapsto MRecoveryReq,
                     mtype
                                     \mapsto myServerId,
                     sender
                     dest
                                     \mapsto dst,
                                     \mapsto myCV
               ]: dst \in serversInOneShard\})
                  UNCHANGED \langle network Vars, vCrash Vector \rangle
        ELSE
HandleRecoveryReq(m) \triangleq
   LET
        myServerId \stackrel{\triangle}{=} m.dest
   IN
    \land vServerStatus[myServerId] = StNormal
    \land Send(\{[
             mtype \mapsto MRecoveryRep,
             sender \mapsto myServerId,
                      \mapsto m.sender,
             gView \mapsto vGView[myServerId],
             lView \mapsto vLView[myServerId],
                      \mapsto vCrashVector'[myServerId]
       ]})
HandleRecoveryRep(m) \triangleq
   LET
        myServerId \triangleq m.dest
   IN
    \land vServerStatus[myServerId] = StRecovering
    \land vRecoveryReps' = [
```

 $serversInOneShard \stackrel{\triangle}{=} \{s \in Servers : s.shardId = myServerId.shardId\}$ 

```
vRecoveryReps Except ![myServerId]
                 = vRecoveryReps[myServerId] \cup \{m\}
    \land IF Cardinality(vRecoveryReps[myServerId]) = QuorumSize THEN
                lViewQuorum \stackrel{\triangle}{=} \{mm.lView : mm \in vRecoveryReps[myServerId]\}
                gViewQuorum \stackrel{\Delta}{=} \{mm.gView : mm \in vRecoveryReps[myServerId]\}
            IN
            \land vLView' = [vLView \ EXCEPT \ ! [myServerId] = PickMax(lViewQuorum)]
            \land vGView' = [vLView \ EXCEPT \ ! [myServerId] = PickMax(gViewQuorum)]
             \land Send(\{[
                                   \mapsto MStartViewReq,
                      mtype
                                   \mapsto \mathit{myServerId},
                      sender
                      dest
                                           replicaId \mapsto LeaderID(vLView[myServerId]),
                                           shardId \mapsto myServerId.shardId
                      lView
                                   \mapsto vLView'[myServerId],
                                   \mapsto vCrashVector'[myServerId]
                      cv
                ]})
         ELSE UNCHANGED \langle networkVars, vLView, vGView \rangle
HandleStartViewReq(m) \stackrel{\Delta}{=}
    LET
        myServerId \stackrel{\triangle}{=} m.dest
    IN
    \land vServerStatus[myServerId] = StNormal
    \land vLView[myServerId] = m.lView
    \land isLeader(myServerId.replicaId, vLView[myServerId])
    \land Send({[
             mtype
                          \mapsto MStartView,
                          \mapsto myServerId,
             sender
             dest
                          \mapsto m.sender,
             lView
                          \mapsto vLView[myServerId],
             gView
                          \mapsto vGView[myServerId],
             gVec
                          \mapsto vGVec[myServerId],
                          \mapsto vLog[myServerId],
             entries
                          \mapsto vCrashVector[myServerId]
              cv
       ]})
StartLocalSync(serverId) \triangleq
    LET
        leaderServerId \triangleq [
```

```
replicaId \mapsto LeaderID(vLView[serverId]),
            shardId \mapsto serverId.shardId
   IN
    \land vServerStatus[serverId] = StNormal
    \land Send({[
                           \mapsto MLocalSyncStatus,
             mtype
                           \mapsto serverId,
             sender
             dest
                           \mapsto leaderServerId,
                           \mapsto vLView[serverId],
             lView
             lSyncPoint \mapsto vLSyncPoint[serverId],
                           \mapsto vCrashVector[serverId]
       ]})
HandleLocalSyncStatus(m) \stackrel{\Delta}{=}
   LET
        myServerId \stackrel{\triangle}{=} m.dest
        lSyncQuorum \stackrel{\triangle}{=} vLSyncQuorum[myServerId]
    \land vServerStatus[myServerId] = StNormal
    \land vLView[myServerId] = m.lView
    ∧ isLeader(myServerId.replicaId, vLView[myServerId])
    \land \forall mm \in lSyncQuorum :
        \lor mm.sender \neq m.sender
        \lor mm.lSyncPoint < m.lSyncPoint
    \land vLSyncQuorum' = [
            vLSyncQuorum \ EXCEPT \ ![myServerId] =
                \{mm \in lSyncQuorum : mm.sender \neq m.sender\} \cup \{m\}
    \land IF Cardinality(vLSyncQuorum'[myServerId]) <math>\ge QuorumSize THEN
                candidateQuorum \triangleq \{
                    R \in \text{SUBSET} (vLSyncQuorum'[myServerId]):
                        Cardinality(R) = QuorumSize
                quorumSyncPoints \triangleq \{
                    \{x.lSyncPoint : x \in R\} : R \in candidateQuorum
                validCommitPoints \triangleq \{PickMax(Q) : Q \in quorumSyncPoints\}
                maxCommitPoint \triangleq PickMax(validCommitPoints)
            IN
            \land vLCommitPoint' = [vLCommitPoint \ EXCEPT \ ! [myServerId] = maxCommitPoint]
            \land Send(\{[
                                     \mapsto MLocalCommit,
                     mtype
```

```
sender
                                      \mapsto myServerId,
                      dest
                                      \mapsto m.sender,
                                      \mapsto vLView[myServerId],
                      lView
                      lCommitPoint \mapsto vLCommitPoint'[myServerId],
                                      \mapsto vCrashVector'[myServerId]
                ]})
                   UNCHANGED \langle vLCommitPoint, networkVars \rangle
         ELSE
HandleLocalCommit(m) \triangleq
    LET
        myServerId \triangleq m.dest
    IN
    \land vServerStatus[myServerId] = StNormal
    \land \ \ vLView[myServerId] = m.lView
    \land \neg isLeader(myServerId.replicaId, vLView[myServerId])
     Make sure the syncPoint is large enough before updating CommitPoint
            \land vLSyncPoint[myServerId] \ge m.lCommitPoint
             \land vLCommitPoint[myServerId] < m.lCommitPoint
         THEN
            vLCommitPoint' = [
                 vLCommitPoint \ EXCEPT \ ![myServerId] = m.lCommitPoint
         ELSE UNCHANGED \langle vLCommitPoint \rangle
isCommitting(txn, timestampQ) \stackrel{\Delta}{=}
    LET quorum \stackrel{\triangle}{=} \{ msg \in timestampQ : msg.entry.txnId = txn.txnId \}
        Cardinality(quorum) = Cardinality(txn.shards)
ReleaseSequencer(serverId, currentTime) \stackrel{\Delta}{=}
        serversInOneShard \stackrel{\triangle}{=} \{s \in Servers : s.shardId = serverId.shardId\}
        expire Txns \triangleq
            \{msg \in vEarlyBuffer[serverId]:
                 \land msg.timestamp \leq currentTime
        sortedTxnList \triangleq SetToSortSeq(expireTxns, Compare)
        committingStatus \triangleq
            [i \in 1 ... Len(sortedTxnList)]
               \mapsto isCommitting(sortedTxnList[i], vTimestampQuorum[serverId])
        canReleaseTxnIndices \stackrel{\triangle}{=} \{
            i \in 1 \dots Len(sortedTxnList):
               \forall j \in 1 ... i : committingStatus[j] = TRUE
```

```
Here we consider all txns are not commutative,
      Therefore, At most one txn can be speculatively executed with risk
      Refer to Section 3.6 of Tiga paper
    spec TxnIndex \triangleq \{
         i \in 1 \dots Len(sortedTxnList):
            \land \ \forall j \in 1 ... (i-1) : \textit{committingStatus}[j] = \texttt{true}
            \land committingStatus[i] = FALSE
    }
IN
    Cardinality(canReleaseTxnIndices) = 0 Nothing to release
_{
m IF}
 THEN
     \land UNCHANGED \langle vLog, vEarlyBuffer, vLateBuffer, vTimestampQuorum \rangle
     While there is nothing to release, some txns might be speculatively executed (Section 3.6 of Tiga paper)
     \wedge IF Cardinality(specTxnIndex) > 0 THEN
             Send(\{[
                   mtype \mapsto MFastReply,
                   sender \mapsto serverId,
                             \mapsto sortedTxnList[i].txnId.coordId,
                   gView \mapsto vGView[serverId],
                   lView \mapsto vLView[serverId],
                   txnId
                             \mapsto sortedTxnList[i].txnId,
                   hash
                                log \mapsto vLog'[serverId],
                                cv \mapsto vCrashVector
                                ],
                             \mapsto sortedTxnList[i].timestamp,
                   logId
                             \mapsto 0 logId = 0 indicates this is a speculative txn with rollback risk,
                                   we need to compare the timestamps from different shards to decide
                                   whether the execution results are serializable
            ]: i \in specTxnIndex\})
         ELSE
             UNCHANGED \langle network Vars \rangle
 ELSE
    LET
         releaseUpTo \stackrel{\triangle}{=} CHOOSE \ i \in canReleaseTxnIndices :
                             \forall j \in canReleaseTxnIndices: j \leq i
         releaseSeq \triangleq SubSeq(sortedTxnList, 1, releaseUpTo)
         releaseTxns \stackrel{\Delta}{=} \{releaseSeq[i] : i \in 1 .. Len(releaseSeq)\}
    IN
     \land vEarlyBuffer' = [
         vEarlyBuffer except ![serverId]
             = vEarlyBuffer[serverId] \setminus releaseTxns]
     \land vTimestampQuorum' = [
         vTimestampQuorum \ \ \text{EXCEPT} \ ![serverId]
```

```
= \{ msg \in vTimestampQuorum[serverId] :
             \forall txn \in releaseTxns : txn.txnId \neq msg.entry.txnId \}
 Append to log
\land vLog' = [vLog \ EXCEPT \ ! [serverId] = vLog[serverId] \circ releaseSeq]
\land IF isLeader(serverId.replicaId, vLView[serverId]) THEN
        \land vLSyncPoint' = [vLSyncPoint \ EXCEPT \ ![serverId] = Len(vLog'[serverId])]
               UNCHANGED \langle vLSyncPoint \rangle
    ELSE
 Send fast-replies to coordinators
\land Send(\{[
            \mapsto MFastReply,
   mtype
   sender \mapsto serverId,
   dest
             \mapsto sortedTxnList[i].txnId.coordId,
   qView \mapsto vGView[serverId],
   lView
            \mapsto vLView[serverId],
   txnId
             \mapsto sortedTxnList[i].txnId,
   hash
             \mapsto
                 log \mapsto vLog'[serverId],
                 cv \ \mapsto v\mathit{Crash}\mathit{Vector}
            ],
   t
            \mapsto 0, timestamp = 0 indicates this is not a speculative txn with rollback risk
   logId \mapsto i
   : i \in (1 + Len(vLog[serverId])) ... Len(vLog'[serverId]))
 Send InterReplicaSync to the other servers in the same sharding group
 In real implementation, we send the log indices incrementally (i.e., consider it as an optimization)
 Here for clarity and simplicity, we always send the whole log list
\land Send(\{[
         mtype \mapsto MInterReplicaSync,
         lView \mapsto vLView[serverId],
         sender \mapsto serverId,
         dest
                   \mapsto dstServerId,
         entries \mapsto vLog'[serverId]
   ]: dstServerId \in serversInOneShard\})
\land IF Cardinality(specTxnIndex) > 0 THEN
        Send(\{[
              mtype \mapsto MFastReply,
              sender \mapsto serverId,
                       \mapsto sortedTxnList[i].txnId.coordId,
              gView \mapsto vGView[serverId],
              lView \mapsto vLView[serverId],
              txnId
                       \mapsto sortedTxnList[i].txnId,
              hash
                           log \mapsto vLog'[serverId],
                           cv \mapsto vCrashVector
                           ],
```

```
\mapsto sortedTxnList[i].timestamp,
                                \mapsto 0 logId = 0 indicates this is a speculative txn with rollback risk
                      logId
                ]: i \in specTxnIndex\})
             ELSE
                TRUE
ServerClockMove(serverId) \stackrel{\Delta}{=}
    IF vServerClock[serverId] \ge MaxTime
        UNCHANGED (network Vars, server State Vars)
     ELSE
         \land vServerClock' = [
                 vServerClock \ Except \ ![serverId] = vServerClock[serverId] + 1]
         \land IF vServerStatus[serverId] = StNormal THEN
                 \land ReleaseSequencer(serverId, vServerClock[serverId] + 1)
             ELSE
                 UNCHANGED \langle network Vars, vLog, vEarlyBuffer, \rangle
                     vLateBuffer, vTimestampQuorum \rangle
         \land UNCHANGED \langle vCrossShardVerifyReps,
                 vServerStatus, vGView, vGVec, vLView, vLastNormView,
                 vViewChange, vLSyncPoint, vLCommitPoint,
                 vLSyncQuorum, vUUIDCounter, vCrashVector,
                 vCrashVectorReps, vRecoveryReps, vServerProcessed \rangle
CoordClockMove(coordId) \stackrel{\Delta}{=}
    \lor \land vCoordClock[coordId] \ge MaxTime
         \land UNCHANGED \langle vCoordClock \rangle
        \land vCoordClock[coordId] < MaxTime
         \land vCoordClock' = [
            vCoordClock \ EXCEPT \ ![coordId] = vCoordClock[coordId] + 1]
Init \triangleq
    \land InitNetworkState
    \land InitServerState
    \land \ InitCoordState
    \land \ InitConfigManagerState
    \wedge ActionName = \langle \text{"Init"} \rangle
Next \triangleq
       \land ActionName' = \langle \text{``Next''} \rangle
        \land UNCHANGED \langle network Vars, server State Vars,
                           coordStateVars, configManagerStateVars \rangle
    \lor \exists c \in Coords:
         \land Cardinality(vCoordTxns[c]) < MaxRegNum
```

```
\land CoordSubmitTxn(c)
   \land UNCHANGED \langle serverStateVars, configManagerStateVars,
               vCoordProcessed
   \land ActionName' = \langle \text{``CoordSubmitTxn''} \rangle
\vee \exists m \in messages :
   \wedge m.mtype = MTxn
   \land vServerStatus[m.dest] = StNormal
   \land m \notin vServerProcessed[m.dest]
   \land vServerProcessed' = [vServerProcessed \ EXCEPT \ ![m.dest] =
       vServerProcessed[m.dest] \cup \{m\}]
   \wedge Handle Txn(m)
   \land UNCHANGED \langle coordStateVars, configManagerStateVars,
       vLog, vTimestampQuorum, vCrossShardVerifyReps,
       vServerStatus, vGView, vGVec,
       vLView, vServerClock, vLastNormView,
       vViewChange, vLSyncPoint, vLCommitPoint,
       vLSyncQuorum, vUUIDCounter, vCrashVector,
       vCrashVectorReps, vRecoveryReps
   \land ActionName' = \langle \text{"HandleTxn"} \rangle
\vee \exists m \in messages :
   \land m.mtype = MTimestampNotification
   \land vServerStatus[m.dest] = StNormal
   \land m \notin vServerProcessed[m.dest]
   \land vServerProcessed' = [vServerProcessed \ EXCEPT \ ![m.dest] =
       vServerProcessed[m.dest] \cup \{m\}]
   \land Handle TimestampNotification(m)
   \land UNCHANGED \langle network Vars, coordState Vars, configManagerState Vars,
           vLog, vCrossShardVerifyReps, vLateBuffer, vServerStatus,
           vGView, vGVec, vLView, vServerClock, vLastNormView,
          vViewChange, vLSyncPoint, vLCommitPoint, vLSyncQuorum,
           vUUIDCounter, vCrashVector, vCrashVectorReps, vRecoveryReps \rangle
   \land ActionName' = \langle \text{"HandleTimestampNotification"} \rangle
\vee \exists m \in messages :
   \land m.mtype = MInterReplicaSync
   \land vServerStatus[m.dest] = StNormal
   \land m \notin vServerProcessed[m.dest]
   \land vServerProcessed' = [vServerProcessed \ EXCEPT \ ![m.dest] =
       vServerProcessed[m.dest] \cup \{m\}]
   \wedge HandleInterReplicaSync(m)
   \land UNCHANGED \langle coordStateVars, configManagerStateVars,
           vLoq, vCrossShardVerifyReps, vLateBuffer,
           vServerStatus, vGView, vGVec, vLView,
           vServerClock, vLastNormView,
```

```
vViewChange, vLCommitPoint,
           vLSyncQuorum, \ vUUIDCounter, \ vCrashVector,
           vCrashVectorReps, vRecoveryReps
   \land ActionName' = \langle \text{"HandleInterReplicaSync"} \rangle
Some Leader(s) fail
\vee \exists serverId \in Servers :
   \land vLView[serverId] < MaxViews
   \land isLeader(serverId.replicaId, vLView[serverId])
   \land vServerStatus[serverId] = StNormal
   \land StartLeaderFail(serverId)
   \land UNCHANGED \langle network Vars, coordState Vars, configManagerState Vars,
       vLog, vEarlyBuffer, vLateBuffer, vTimestampQuorum,
       vCrossShardVerifyReps, vGView, vGVec, vLView, vServerClock,
       vLastNormView, vViewChange, vLSyncPoint, vLCommitPoint,
       vLSyncQuorum, vUUIDCounter, vCrashVector, vCrashVectorReps,
       vRecoveryReps, vServerProcessed
   \land ActionName' = \langle \text{"StartLeaderFail"} \rangle
Config Manager notices some leader(s) fail and launch view change
  \exists cmReplicaId \in Replicas:
   \land LaunchViewChange(cmReplicaId)
   ∧ UNCHANGED ⟨coordStateVars, serverStateVars, configManagerStateVars⟩
   \land \ \ ActionName' = \langle \text{``LaunchViewChange''} \rangle
\vee \exists m \in messages :
   \land m.mtype = MCMPrepare
   \land m \notin vCMProcessed[m.dest]
   \land vCMProcessed' = [vCMProcessed \ EXCEPT \ ![m.dest] =
           vCMProcessed[m.dest] \cup \{m\}]
   \land vCMStatus[m.dest] = StNormal
   \land HandleCMPrepare(m)
   \land UNCHANGED \langle coordStateVars, serverStateVars \rangle
   \land ActionName' = \langle \text{"HandleCMPrepare"} \rangle
\lor \exists m \in messages :
   \land m.mtype = MCMPrepareReply
   \land m \notin vCMProcessed[m.dest]
   \land vCMProcessed' = [vCMProcessed \ EXCEPT \ ![m.dest] =
           vCMProcessed[m.dest] \cup \{m\}]
   \land vCMStatus[m.dest] = StNormal
   \land HandleCMPrepareReply(m)
   \land UNCHANGED \langle coordStateVars, serverStateVars,
                       vCMStatus, vCMView, vCMPrepareGInfo
   \land ActionName' = \langle \text{"HandleCMPrepareReply"} \rangle
```

```
\vee \exists m \in messages :
   \land m.mtype = MCMCommit
   \land m \notin vCMProcessed[m.dest]
   \land vCMProcessed' = [vCMProcessed \ EXCEPT \ ![m.dest] =
           vCMProcessed[m.dest] \cup \{m\}]
   \land vCMStatus[m.dest] = StNormal
   \land HandleCMCommit(m)
      UNCHANGED \(\langle network Vars, \) coordState Vars, serverState Vars,
                       vCMStatus, vCMView, vCMPrepareGInfo, vCMPrepareReps
   \land ActionName' = \langle \text{"HandleCMCommit"} \rangle
\vee \exists m \in messages :
   \land m.mtype = MViewChangeReq
   \land m \notin vServerProcessed[m.dest]
   \land vServerProcessed' = [vServerProcessed \ Except \ ![m.dest] =
           vServerProcessed[m.dest] \cup \{m\}]
       \lor vServerStatus[m.dest] = StNormal
       \lor vServerStatus[m.dest] = StViewChange
   \land Handle View Change Req(m)
   \land UNCHANGED \langle coordStateVars, configManagerStateVars,
           vLog, vServerClock, vViewChange, vLSyncPoint,
           vLCommitPoint, vLSyncQuorum, vUUIDCounter,
           vCrashVector, vCrashVectorReps, vRecoveryReps \rangle
   \land ActionName' = \langle \text{"HandleViewChangeReq"} \rangle
\vee \exists m \in messages :
   \land m.mtype = MViewChange
   \land is Crash Vector Valid(m)
   \land m \notin vServerProcessed[m.dest]
   \land vServerProcessed' = [vServerProcessed \ Except \ ![m.dest] =
           vServerProcessed[m.dest] \cup \{m\}]
      \lor vServerStatus[m.dest] = StNormal
       \lor vServerStatus[m.dest] = StViewChange
   \land Handle View Change (m)
   \land UNCHANGED \land coordStateVars, configManagerStateVars,
           vGVec, vServerClock, vLSyncPoint, vLastNormView,
           vLCommitPoint, vLSyncQuorum, vUUIDCounter,
           vCrashVector, vCrashVectorReps, vRecoveryReps\rangle
   \land ActionName' = \langle \text{"HandleViewChange"} \rangle
\vee \exists m \in messages :
   \land m.mtype = MCrossShardVerifyReq
   \land m \notin vServerProcessed[m.dest]
   \land vServerProcessed' = [vServerProcessed \ EXCEPT \ ! [m.dest] =
```

```
vServerProcessed[m.dest] \cup \{m\}]
   \land vServerStatus[m.dest] = StCrossShardSyncing
   \land Handle Cross Shard Verify Reg(m)
   \land UNCHANGED \langle coordStateVars, configManagerStateVars,
           vLog, vEarlyBuffer, vLateBuffer, vTimestampQuorum,
           vCrossShardVerifyReps, vServerStatus,
           vGView, vGVec, vLView, vServerClock, vLastNormView,
          vViewChange, vLSyncPoint, vLCommitPoint, vLSyncQuorum,
           vUUIDCounter, vCrashVector, vCrashVectorReps,
           vRecoveryReps\rangle
   \land ActionName' = \langle \text{"HandleCrossShardVerifyReg"} \rangle
\vee \exists m \in messages :
   \land m.mtype = MCrossShardVerifyRep
   \land m \notin vServerProcessed[m.dest]
   \land vServerProcessed' = [vServerProcessed \ EXCEPT \ ![m.dest] =
           vServerProcessed[m.dest] \cup \{m\}]
   \land vServerStatus[m.dest] = StCrossShardSyncing
   \land HandleCrossShardVerifyRep(m)
   \land UNCHANGED \langle coordStateVars, configManagerStateVars,
           vEarlyBuffer, vLateBuffer, vTimestampQuorum, vServerStatus,
           vGView, vGVec, vLView, vServerClock, vLastNormView,
           vViewChange, vLSyncPoint, vLCommitPoint,
          vLSyncQuorum, vUUIDCounter, vCrashVector,
           vCrashVectorReps, vRecoveryReps
   \land ActionName' = \langle \text{"HandleCrossShardVerifyRep"} \rangle
\vee \exists m \in messages :
   \land m.mtype = MStartView
   \land isCrashVectorValid(m)
   \land m \notin vServerProcessed[m.dest]
   \land vServerProcessed' = [vServerProcessed \ Except \ ![m.dest] =
           vServerProcessed[m.dest] \cup \{m\}]
   \land \ \ vServerStatus[m.dest] \neq StFailing
   \land HandleStartView(m)
   \land UNCHANGED \langle coordStateVars, configManagerStateVars,
              vServerClock, vLCommitPoint,
              vUUIDCounter, vCrashVector
   \land ActionName' = \langle \text{"HandleStartView"} \rangle
Failed server rejoin
\vee \exists serverId \in Servers :
   \land vServerStatus[serverId] = StFailing
   \land vServerStatus' = [vServerStatus \ Except \ ![serverId] = StRecovering]
   \land ResetServerState(serverId)
```

```
\land StartServerRecovery(serverId)
   \land UNCHANGED \langle network Vars, coord State Vars, configManager State Vars \rangle
   \land ActionName' = \langle \text{"StartReplicaRecovery"} \rangle
\lor \exists m \in messages :
   \land m.mtype = MCrashVectorReq
   \land m \notin vServerProcessed[m.dest]
      vServerProcessed' = [vServerProcessed \ Except \ ![m.dest] =
           vServerProcessed[m.dest] \cup \{m\}]
   \land vServerStatus[m.dest] = StNormal
   \land HandleCrashVectorReq(m)
   \land UNCHANGED \langle coordStateVars, configManagerStateVars,
           vLog, vEarlyBuffer, vLateBuffer, vTimestampQuorum,
           vCrossShardVerifyReps, vServerStatus, vGView, vGVec,
           vLView, vServerClock, vLastNormView, vViewChange,
           vLSyncPoint, vLCommitPoint, vLSyncQuorum, vUUIDCounter,
           vCrashVector, vCrashVectorReps, vRecoveryReps \rangle
   \land ActionName' = \langle \text{"HandleCrashVectorReq"} \rangle
\vee \exists m \in messages :
   \land m.mtype = MCrashVectorRep
   \land m \notin vServerProcessed[m.dest]
   \land vServerProcessed' = [vServerProcessed \ Except \ ![m.dest] =
           vServerProcessed[m.dest] \cup \{m\}]
   \land vServerStatus[m.dest] = StRecovering
   \land HandleCrashVectorRep(m)
   \land UNCHANGED \langle coordStateVars, configManagerStateVars,
           vLog, vEarlyBuffer, vLateBuffer,
           vTimestampQuorum, vCrossShardVerifyReps, vServerStatus,
           vGView, vGVec, vLView, vServerClock, vLastNormView,
           vViewChange, vLSyncPoint, vLCommitPoint, vLSyncQuorum,
           vUUIDCounter, vCrashVectorReps, vRecoveryReps\rangle
   \land ActionName' = \langle \text{"HandleCrashVectorRep"} \rangle
\vee \exists m \in messages :
   \land m.mtype = MRecoveryReq
   \land m \notin vServerProcessed[m.dest]
   \land vServerProcessed' = [vServerProcessed \ Except \ ![m.dest] =
           vServerProcessed[m.dest] \cup \{m\}]
   \land vServerStatus[m.dest] = StNormal
   \land isCrashVectorValid(m)
   \land HandleRecoveryReq(m)
   \land UNCHANGED \langle coordStateVars, configManagerStateVars,
           vLog, vEarlyBuffer, vLateBuffer,
           vTimestampQuorum, vCrossShardVerifyReps, vServerStatus,
           vGView, vGVec, vLView, vServerClock, vLastNormView,
```

```
vViewChange, vLSyncPoint, vLCommitPoint, vLSyncQuorum,
           vUUIDCounter, vCrashVectorReps, vRecoveryReps\rangle
   \land ActionName' = \langle \text{"HandleRecoveryReq"} \rangle
\lor \exists m \in messages :
   \land m.mtype = MRecoveryRep
   \land m \notin vServerProcessed[m.dest]
      vServerProcessed' = [vServerProcessed \ EXCEPT \ ![m.dest] =
           vServerProcessed[m.dest] \cup \{m\}]
   \land vServerStatus[m.dest] = StRecovering
   \land isCrashVectorValid(m)
   \land HandleRecoveryRep(m)
   \land UNCHANGED \langle coordStateVars, configManagerStateVars,
           vLog,\ vEarlyBuffer,\ vLateBuffer,
           vTimestampQuorum, vCrossShardVerifyReps, vServerStatus,
           vGVec,\ vServerClock,\ vLastNormView,\ vViewChange,
           vLSyncPoint, vLCommitPoint, vLSyncQuorum,
           vUUIDCounter, vCrashVectorReps, vRecoveryReps \rangle
   \land ActionName' = \langle \text{"HandleRecoveryRep"} \rangle
\lor \exists m \in messages :
   \land m.mtype = MStartViewReq
   \land m \notin vServerProcessed[m.dest]
   \land vServerProcessed' = [vServerProcessed \ Except \ ![m.dest] =
           vServerProcessed[m.dest] \cup \{m\}]
   \land vServerStatus[m.dest] = StCrossShardSyncing
   \land isCrashVectorValid(m)
   \land HandleStartViewReg(m)
   \land UNCHANGED \langle coordStateVars, configManagerStateVars,
           vLog, vEarlyBuffer, vLateBuffer, vTimestampQuorum,
           vCrossShardVerifyReps, vServerStatus,
           vGView, vGVec, vLView, vServerClock,
          vLastNormView, vViewChange, vLSyncPoint,
           vLCommitPoint, vLSyncQuorum,
          vUUIDCounter, vCrashVector,
           vCrashVectorReps, vRecoveryReps
   \land ActionName' = \langle \text{"HandleStartViewReq"} \rangle
Periodic Sync
\lor \exists serverId \in Servers :
   \land vServerStatus[serverId] = StNormal
   \land StartLocalSync(serverId)
   \land UNCHANGED \langle coordStateVars,
           serverStateVars, configManagerStateVars
   \land \ \ ActionName' = \langle \text{"StartLocalSync"} \rangle
```

```
\vee \exists m \in messages :
        \land m.mtype = MLocalSyncStatus
        \land m \notin vServerProcessed[m.dest]
        \land vServerProcessed' = [vServerProcessed \ Except \ ![m.dest] =
                vServerProcessed[m.dest] \cup \{m\}]
        \land vServerStatus[m.dest] = StNormal
        \land is Crash Vector Valid(m)
        \land HandleLocalSyncStatus(m)
        \land UNCHANGED \langle coordStateVars, configManagerStateVars,
                vLog, vEarlyBuffer, vLateBuffer, vTimestampQuorum,
                vCrossShardVerifyReps, vServerClock, vViewChange,
               vGVec, vGView, vLSyncPoint, vLView, vLastNormView,
                vServerStatus, vUUIDCounter, vCrashVectorReps,
                vRecoveryReps
        \land ActionName' = \langle \text{"HandleLocalSyncStatus"} \rangle
    \vee \exists m \in messages :
        \land m.mtype = MLocalCommit
        \land m \notin vServerProcessed[m.dest]
        \land vServerProcessed' = [vServerProcessed \ Except \ ![m.dest] =
                vServerProcessed[m.dest] \cup \{m\}]
        \land vServerStatus[m.dest] = StNormal
        \land isCrashVectorValid(m)
        \land HandleLocalCommit(m)
        \land UNCHANGED \langle coordStateVars, configManagerStateVars,
                networkVars, vLog, vEarlyBuffer, vLateBuffer,
                vTimestampQuorum, vCrossShardVerifyReps,
                vServerStatus, vServerClock, vGView, vGVec,
                vLView, vLastNormView, vViewChange, vLSyncPoint,
                vLSyncQuorum, vUUIDCounter, vCrashVectorReps, vRecoveryReps
        \land ActionName' = \langle \text{"HandleLocalCommit"} \rangle
     Clock Move
    \forall \exists serverId \in Servers :
        \land ServerClockMove(serverId)
        \land UNCHANGED \langle coordStateVars, configManagerStateVars \rangle
        \land ActionName' = \langle \text{"ServerClockMove"} \rangle
    \vee \exists coordId \in Coords:
        \land CoordClockMove(coordId)
        \land UNCHANGED \langle network Vars, serverState Vars, configManagerState Vars,
           vCoordTxns, vCoordProcessed
        \land ActionName' = \langle \text{``CoordClockMove''} \rangle
Spec \triangleq Init \land \Box [Next] \land network Vars, server State Vars, coord State Vars,
```

## $configManagerStateVars,\ ActionName \rangle$

```
ShardRecovered(shardId, lViewID) \stackrel{\Delta}{=}
         serversInOneShard \stackrel{\triangle}{=} \{s \in Servers : s.shardId = shardId\}
        leaderServer \stackrel{\Delta}{=} [
             replicaId \mapsto LeaderID(lViewID),
             shardId \mapsto shardId
    IN
    \land \exists RM \in SUBSET (serversInOneShard) :
         \land Cardinality(RM) \ge QuorumSize
         \land leaderServer \in RM
         \land \forall r \in RM : vServerStatus[r] = StNormal
         \land \forall r \in RM : vLastNormView[r] \ge lViewID
CommittedInView(v, shardId, txnId) \stackrel{\Delta}{=}
         serversInOneShard \triangleq \{s \in Servers : s.shardId = shardId\}
        leaderServer \triangleq [
             replicaId \mapsto LeaderID(v),
             shardId \mapsto shardId
        replySet \triangleq \{
             m \in messages: \land \lor m.mtype = MFastReply
                                     \vee m.mtype = MSlowReply
                                 \wedge m.txnId = txnId
                                 \land m.sender \in serversInOneShard
                                 \land m.lView = v
         }
    If \forall reply \in replySet:
         \lor reply.mtype \neq MFastReply
         \lor reply.sender \neq leaderServer
     THEN No leader's fast reply \rightarrow This txn is not committed
        FALSE
     ELSE
        LET
             leaderReply \stackrel{\triangle}{=} CHOOSE \ reply \in replySet :
                                      \land reply.mtype = MFastReply
                                      \land reply.sender = leaderServer
        IN
          Committed in Fast Path
```

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```
 \begin{tabular}{ll} $ & \exists fastQuorum \in {\tt SUBSET} \ replySet: \\ & \land \ leaderReply \in fastQuorum \\ & \land \ Cardinality(fastQuorum) = FastQuorumSize \\ & \verb{All replies have the same hash (or it is a slow reply)} \\ & \land \ \forall reply \in fastQuorum: \\ & \lor \land \ reply.mtype = MFastReply \\ & \land \ reply.mtype = MFastReply.hash \\ & \verb{Slow Reply can be used as fast reply} \\ & \lor \ reply.mtype = MSlowReply \\ \\ & \verb{Committed in Slow Path} \\ & \lor \ \exists \ slowQuorum \in \verb{SUBSET} \ replySet: \\ & \land \ leaderReply \in slowQuorum \\ & \land \ Cardinality(slowQuorum) = QuorumSize \\ & \land \ \forall \ reply \in slowQuorum \setminus \{leaderReply\}: \\ & reply.mtype = MSlowReply \\ \end{tabular}
```

### **Invariants**

Durability [In-Shard-Property]: Committed txns always survive failure i.e. If a txn is committed (to be more precise, locally committed) in one view, then it will remain committed in the higher views.

One thing to note, the check of "committed" only happens when the system is still "normal". While the system is under recovery (i.e. less than f+1 replicas are normal), the check of committed does not make sense

```
\begin{array}{l} Durability \stackrel{\triangle}{=} \\ \forall \, shardId \in Shards: \\ \forall \, v1, \, v2 \in 0 \dots MaxViews: \\ \text{If a } txn \text{ is committed in lower view } (v1,), \\ \text{it is impossible to make this request uncommited in higher vie} \\ \neg ( \, \land \, v1 < v2 \\ \quad \land \, ShardRecovered(shardId, \, v2) \\ \quad \land \, \exists \, c \in Coords: \\ \quad \exists \, txnId \in \, vCoordTxns[c]: \\ \quad \land \, \, CommittedInView(v1, \, shardId, \, txnId) \\ \quad \land \, \, \neg CommittedInView(v2, \, shardId, \, txnId) \\ ) \end{array}
```

Consistency [In-Shard-Property]: Committed txns have the same history even after view changes, i.e. If a request is committed in a lower view (v1), then (based on *Durability* Property), then it remains committed in higher view (v2)

Consistency requires the history of the txns (i.e. all the txs before this txn) remain the same

```
Consistency \triangleq

\forall shardId \in Shards:

\forall v1, v2 \in 1.. MaxViews:

\neg (\land v1 < v2)
```

```
To check Consistency of txns in higher views,
               the shard should have entered the higher views
              \land ShardRecovered(shardId, v2)
              \land \exists c \in Coords:
                 \exists txnId \in vCoordTxns[c]:
                     Durability has been checked in another invariant
                        \land CommittedInView(v1, shardId, txnId)
                         \land CommittedInView(v2, shardId, txnId)
                     THEN
                        LET
                             v1LeaderReply \stackrel{\triangle}{=} CHOOSE \ m \in messages :
                                                           m.mtype = MFastReply
                                                           m.txnId = txnId
                                                           m.lView = v1
                                                           m.sender.shardId = shardId
                                                           m.sender.replicaId = LeaderID(v1)
                            v2LeaderReply \triangleq \text{CHOOSE } m \in messages:
                                                           m.mtype = MFastReply
                                                           m.txnId = txnId
                                                           m.lView = v2
                                                           m.sender.shardId = shardId
                                                           m.sender.replicaId = LeaderID(v2)
                        IN
                             v1LeaderReply.hash \neq v2LeaderReply.hash
                     ELSE FALSE
Linearizability [In-Shard-Property]: Only one txn can be committed for a given position, i.e. If
one txn has committed at position i, then no contrary observation can be made
i.e. there cannot be a second txn committed at the same position
Linearizability \triangleq
    LET
        allTxns \stackrel{\triangle}{=} UNION \{vCoordTxns[c] : c \in Coords\}
    IN
    \forall shardId \in Shards:
       \forall txnId1, txnId2 \in allTxns:
         If txnId1 = txnId2 then true
          ELSE
              \forall v1, v2 \in 1 \dots MaxViews:
                 IF \land CommittedInView(v1, shardId, txnId1)
                        CommittedInView(v1, shardId, txnId2)
                 THEN
                     LET
                         v1LeaderReply \stackrel{\triangle}{=} CHOOSE \ m \in messages :
                                                        m.mtype = MFastReply
```

```
m.lView = v1
                                                       m.sender.shardId = shardId
                                                       m.sender.replicaId = LeaderID(v1)
                         v2LeaderReply \stackrel{\triangle}{=} CHOOSE \ m \in messages :
                                                       m.mtype = MFastReply
                                                       m.txnId = txnId2
                                                       m.lView = v2
                                                       m.sender.shardId = shardId
                                                       m.sender.replicaId = LeaderID(v2)
                    IN
                          They cannot be committed in the same log position, regardless of the view
                         v1LeaderReply.logId \neq v2LeaderReply.logId
                         Not both are committed, so no need to check
                    TRUE
Serializability [Cross-Shard-Property]: Given two txns and two shards: If they are both committed
in both shards, then they should be committed in the same order, i.e., if txn-1 committed before
txn-2 on Shard -1, then txn-1 is also committed before txn-2 on Shard -2
Serializability \triangleq
   LET
        allTxns \stackrel{\triangle}{=} UNION \{vCoordTxns[c] : c \in Coords\}
   IN
   \forall txnId1, txnId2 \in allTxns:
       IF txnId1 = txnId2 THEN TRUE
       ELSE
           \forall v \in 1 \dots Max Views:
             \forall shardId1, shardId2 \in Shards:
                IF shardId1 = shardId2 THEN TRUE
                    IF \land CommittedInView(v, shardId1, txnId1)
                         \land CommittedInView(v, shardId1, txnId2)
                         \land CommittedInView(v, shardId2, txnId1)
                         \land CommittedInView(v, shardId2, txnId2)
                     THEN
                        LET
                             txn1\_LeaderReplyOnShard1 \triangleq CHOOSE m \in messages:
                                                  \land m.mtype = MFastReply
                                                  \land m.txnId = txnId1
                                                  \land m.lView = v
                                                  \land m.sender.shardId = shardId1
                                                  \land m.sender.replicaId = LeaderID(v)
                             txn2\_LeaderReplyOnShard1 \stackrel{\Delta}{=} CHOOSE \ m \in messages:
                                                  \land m.mtype = MFastReply
                                                  \land m.txnId = txnId2
```

m.txnId = txnId1

```
\land m.lView = v
                           \land \quad m.sender.shardId = shardId1
                           \land m.sender.replicaId = LeaderID(v)
       txn1\_LeaderReplyOnShard2 \stackrel{\Delta}{=} CHOOSE \ m \in messages:
                           \land m.mtype = MFastReply
                           \land m.txnId = txnId1
                           \land m.lView = v
                           \land m.sender.shardId = shardId2
                           \land m.sender.replicaId = LeaderID(v)
       txn2\_LeaderReplyOnShard2 \stackrel{\triangle}{=} CHOOSE \ m \in messages:
                           \land m.mtype = MFastReply
                           \land m.txnId = txnId2
                           \land m.lView = v
                           \land m.sender.shardId = shardId2
                           \land m.sender.replicaId = LeaderID(v)
       \land txn1\_LeaderReplyOnShard1.t = txn1\_LeaderReplyOnShard2.t
       \land \ \ txn2\_LeaderReplyOnShard1.t = txn2\_LeaderReplyOnShard2.t
   THEN
           \land txn1\_LeaderReplyOnShard1.logId > txn2\_LeaderReplyOnShard1.logId
           \land \ \ txn1\_LeaderReplyOnShard2.logId > txn2\_LeaderReplyOnShard2.logId
       \lor \land txn1\_LeaderReplyOnShard1.logId < txn2\_LeaderReplyOnShard1.logId
           \land \ txn1\_LeaderReplyOnShard2.logId < txn2\_LeaderReplyOnShard2.logId
    ELSE
        if their timestamps are not equal, our coordinator will not consider them as committed,
        We do not need to check such cases
      TRUE
ELSE TRUE
```