

Class 21: Infinite Infinities, Exam 2

Schedule

Problem Set 9 is now due on **Wednesday, 23 November**.

See PDF Version for Notes.

Infinite Sets Recap

Definition. A set C is *countable* if and only if there exists a surjective function from \mathbb{N} to C . (That is, ≤ 1 arrow out from \mathbb{N} , ≥ 1 arrow in to C .)

Definition. A set C is *countably infinite* if and only if there exists a bijection between C and \mathbb{N} .

Cantor's Theorem

For **all** sets, S , $|\text{pow}(S)| > |S|$.

What does this mean for $|\mathbb{N}|$?

What is a *real number*?

Show there is a bijection between $[0, 1)$ and $\text{pow}(\mathbb{N})$.