# CIR310 Phase equilibrium project Part 1

Submission deadline: 22.03.2017 before 13:30

## 1 System description

A coupled reactor/column system is used for trioxane synthesis from formaldehyde to trioxane. The reversible liquid phase chemical reaction is given by the trimerization reaction:

$$3 \, \mathrm{CH_2O} \stackrel{\mathrm{[H^+]}}{\Longrightarrow} \mathrm{C_3H_3O_3}$$

The equilibrium concentration of trioxane is very low in this reaction. A common design solution to increase overall conversion of the process is by using azeotropic distillation with water. A simplified model of this process was developed by Hu et al. [1]. Figure 1 demonstrates this process.

The feed stream of the reactor contains an aqueous solution of formaldehyde and water. The goal of the process is to maximise the overall conversion of formaldehyde to trioxane.

#### 2 Model

The following assumptions have been made for the process.

- 1. The entire reactor/column system operates at a continuous steady state equilibrium.
- 2. The reactor is controlled at a set temperature and the heat transfer dynamics is negligible.
- 3. The system is adiabatic so that no heat is lost to the environment.
- 4. The catalytic reaction occurs in the liquid phase of the reactor only. No reaction occurs in the column equilibrium stages.
- 5. Side reactions and intermediate products are negligible so that the system is a tertiary formaldyhyde-trioxane-water system.

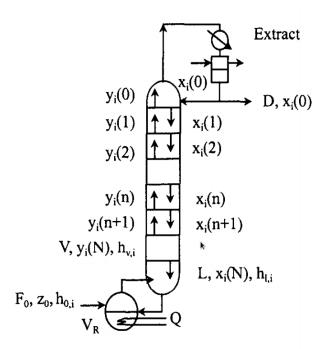


Figure 1: The coupled reactor/column system (adapted from Hu et al. [1]).

6. A constant relatively volatility is assumed at all stages of the reaction.

The system equations as developed by Hu et al. [1] are shown in Table 1.

Table 1: System equations. Here i is the chemical component index where i = 1 is formaldehyde, i = 2 is trioxane and i=3 is water. n represents an equilibrium stage  $n=0,1,2,\ldots N$ , the stage n=N is the reactor stage.

Equation	Parameters	Inputs	Outputs
Reactor mass balance			
$1  Fz_i + Lx_{i,N} - Vy_{i,N} + v_i r = 0$	$v_i$	$F z_i$	$x_{i,N} y_{i,N} L V r$
Column mass balance			
$2 Vy_{i,n} - (L + w_i D)x_{i,n} = 0$	$w_i$	D	$x_{i,n} y_{i,n}$
3  L = RD		R	
Component continuity			
$4  \sum_{i=1}^{3} z_{i} = 1$			
$5  \sum_{i=1}^{3} x_{i,n} = 1$			
$ \begin{array}{ll} 4 & \sum_{i}^{3} z_{i} = 1 \\ 5 & \sum_{i}^{3} x_{i,n} = 1 \\ 6 & \sum_{i}^{3} y_{i,n} = 1 \end{array} $			
Phase equilibrium			
$7  \alpha_i = \frac{y_{i,n}/y_{1,n}}{x_{i,n+1}/x_{1,n+1}}$			$lpha_i$
Reaction rate equation			
$8  r = V_r \left( k_1 C_1^2 - k_2 C_2 \right)$	$k_1 k_2$		r
Energy balance			
9 $\sum_{i=1}^{3} [Fz_{i}h_{F,i} + Lx_{i,N}h_{l,i} - Vy_{i,N}h_{v,i}] + Q = 0$		$h_{F,i} h_{l,i} h_{v,i} Q$	
Total: 21 =	4	+8	+9

#### 3 Instructions

Your company commissioned a reactor/column process based on a design using the described model. After startup however, a much lower yield than predicted by the design was was found. You and your colleagues have been assigned to investigate the process model, to improve its accuracy and to find solutions to improve the yield of the process.

- 1. Using only your background in thermodynamics and elementary chemistry, list the possible reasons why a lower steady state conversion than predicted by the model was obtained. For every possibility listed, suggest solutions and/or tests that can be performed on the system. Where relevant show the improvements to the model (write down these equations). Provide at least 4 possibilities relevant to the phase equilibria of the system, especially with regards to the assumptions made by the model. (40)
- 2. Prove that if an ideal gas model can be assumed, then increasing the reactor temperature will result in zero conversion of the reactant. Write down this temperature point. (10)
- 3. Describe how you would incorporate the following thermodynamic models into the system of equations. Write down the relevant supporting equations, but do not do any explicit symbolic computations. You may cite relevant algorithms from textbooks and other literature sources. Show that the degrees of freedom are zero.
  - Activity coefficient models (ex. NRTL, UNIQUAC). (20)
  - Cubic equation of state models (ex. Virial Van der Waals, Peng-Robinson, Redlich-Kwong). (20)
  - Virial equations of state (ex. Truncated compressibility equations with virial coefficient correlations). [5]
  - K-value correlations from VLE data. [5]

Total Marks: (100)

### References

[1] Hu, M., Zhou, X.-G., and Yuan, W.-K. (1999). Simulation and optimization of a coupled reactor/column system for trioxane synthesis. *Chemical Engineering Science*, 54(10):1353 – 1358.