

Security – Keys, Digital Signatures and Certificates I

CS3524 Distributed Systems and Security

Lecture 19

Modern Cryptography

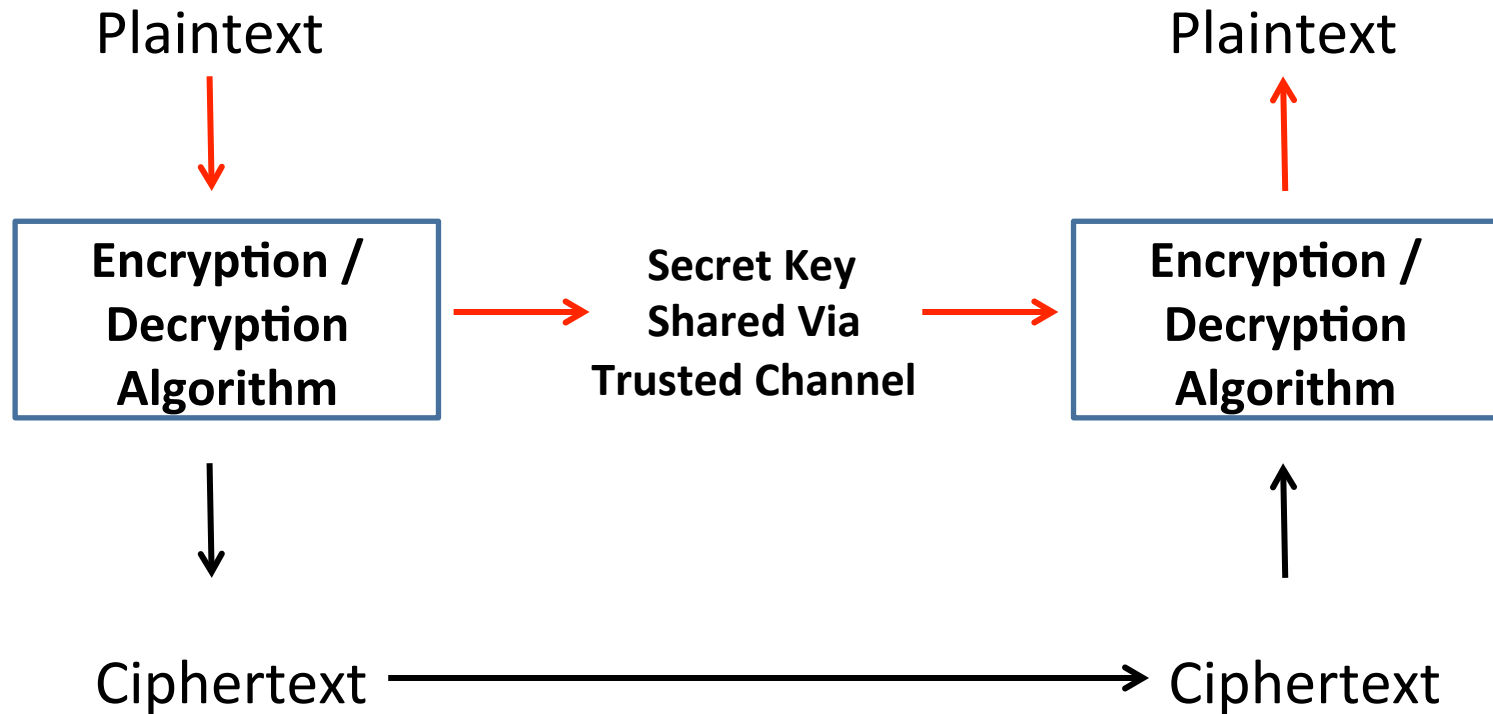
- Relates to
 - Communication: encrypt / decrypt with key
 - Symmetric: use a secret key for both encryption and decryption
 - Asymmetric: use different keys for encryption and decryption, usually a public key and a private key
 - Authentication, Data Integrity: encrypt for creating a unique “fingerprint” or “message digest” for a digital object (e.g. a message or files)
 - digital signatures, certificates

Modern Cryptography

- Classic ciphers encrypted written text messages
- Modern ciphers operate on the bit sequences representing digital objects to be transmitted (“plain text”) to produce an encoded result (“cipher text”)
 - Block ciphers: encoding the plain text (sequence of bits) takes place in a block-wise fashion
 - Stream ciphers: bit-wise encoding of a stream of plain text with a key
- Goal for a high-quality cipher
 - Fast and resource-efficient in encoding
 - Breaking the cipher would require an effort many magnitudes larger , making cryptanalysis impractical

Symmetric-Key Encryption

(Secret Key Encryption)



- Same key is used by sender and receiver, has to be shared via some trusted channel

Secret Key Encryption Concepts

- Plaintext:
 - Original message or data, input to encryption algorithm
- Encryption algorithm:
 - Performs **substitutions** and **transformations** on the plaintext
- Secret key:
 - The exact substitutions and transformations performed depend on the key, is also an input to the encryption algorithm
- Ciphertext:
 - Encrypted message produced as output, depends on the plaintext and the key
- Decryption algorithm
 - Encryption algorithm run in reverse, takes ciphertext and key as input, produces plaintext as output

Secret Key Cryptography

- Relies on a symmetric key for encryption and decryption
- Encryption algorithm should be hard to break
 - Attackers should be unable to decrypt ciphertext or discover the key (even if they have a set of corresponding cipher / plain texts)
- The larger the key size, the harder to attack
- Sender and receiver must obtain copies of the secret key in a secure fashion
- As long as the key is kept secret, the cryptographic procedure does not have to be secret

Block Ciphers

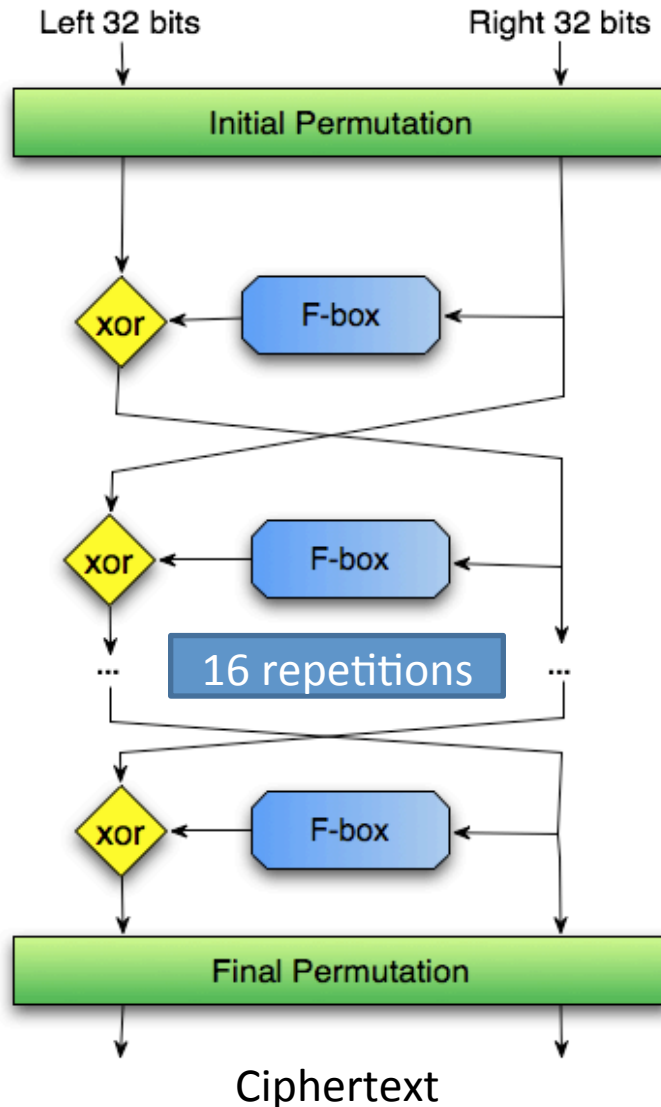
- Message is broken into blocks (usually 16 or 32bit words), each block is encrypted separately
- Operate with a fixed transformation procedure on large blocks of plaintext data
- Block Ciphers
 - Feistel Cipher
 - Is the first block cipher, which inspired subsequent cipher methods such as DES, etc.
 - Substitution-Permutation (SP) network

Symmetric-key Encryption

- Encryption methods
 - DES (Data Encryption Standard)
 - Was highly influential in modern cryptography
 - Developed by IBM
 - Is now considered unsecure due to its key size (56 bits)
 - 3DES
 - Is a form of DES that is regarded as secure, uses three keys and three executions of the DES algorithm
 - AES (Advanced Encryption Standard)
 - Has superseded DES
 - Cast-128
 - Uses fixed, carefully designed S-boxes for subkey generation
 - RC5
 - Fast, variable number of rounds, variable key length
 - IDEA
 - Uses a 128-bit key, does not use S-boxes, but a combination of three operations: XOR, binary addition of 16-bit integer, binary multiplication of 16-bit integers; IDEA is used in PGP (Pretty Good Privacy)
 - Blowfish
 - High execution speed, small footprint, variable keys up to 448 bits, uses S-boxes and XOR, S-boxes are not fixed but dynamically created from key
 - Very strong crypto-algorithm, no practical weaknesses found so far

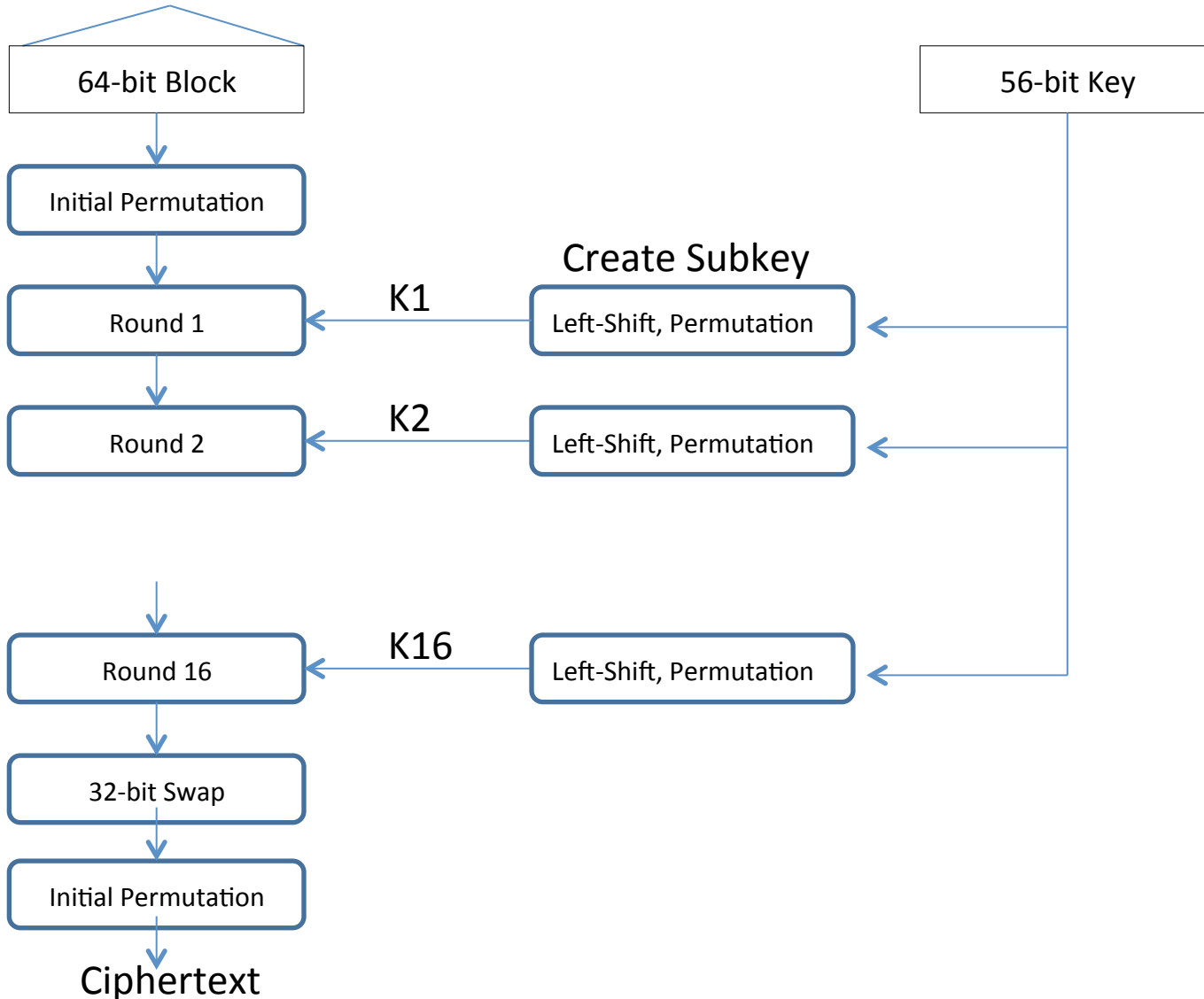
DES Data Encryption Standard

Plaintext 0100101100111010101000101110011001 ...



DES Data Encryption Standard

Plaintext 0100101100111010101000101110011001 ...



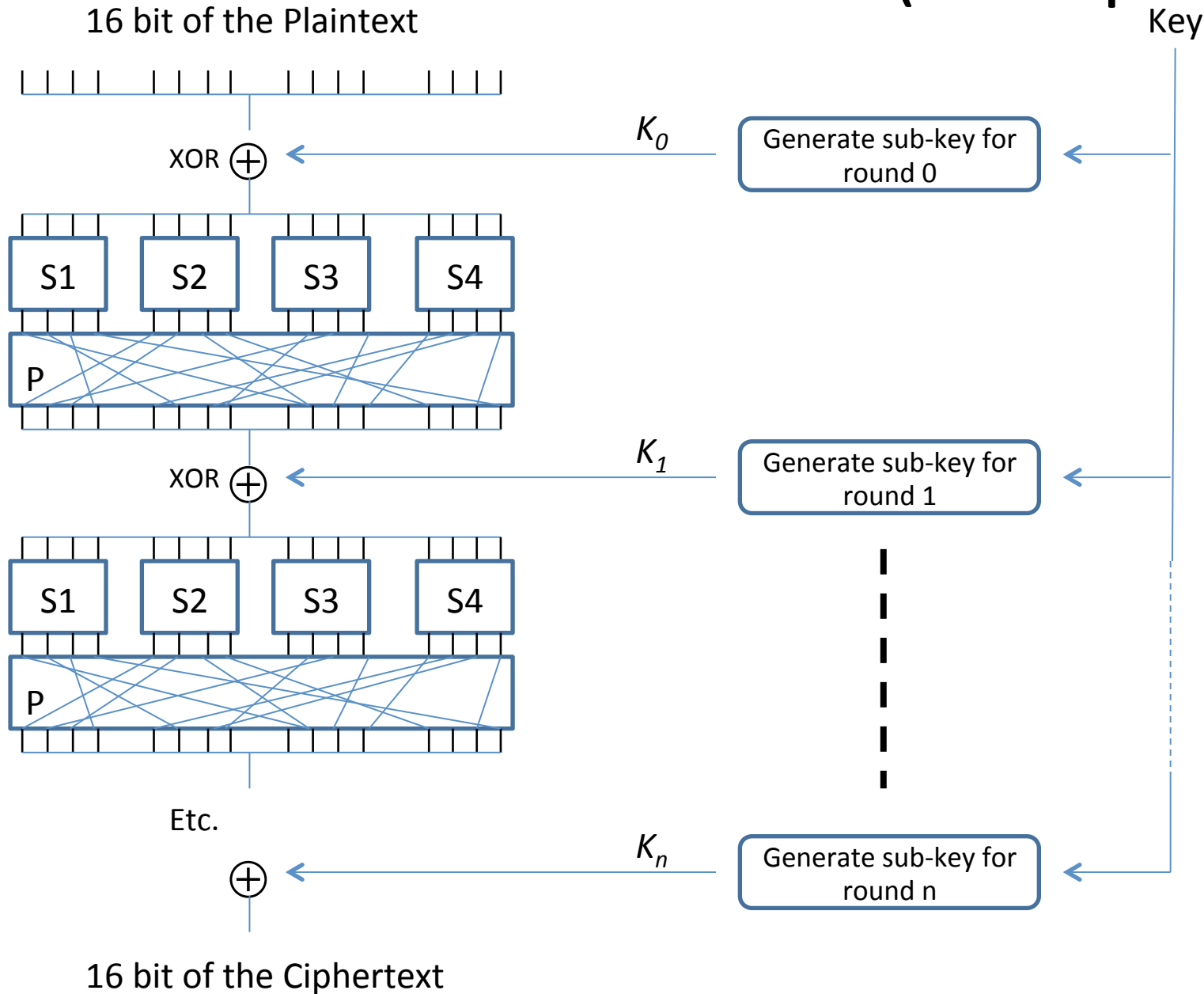
Shannon's Principles for Cryptography

- Shannon's principles of “confusion” and “diffusion”
 - Problems: non-uniformity of individual letters in plain text (e.g. Letter “E” occurs most often in English text) should not be reflected in ciphertext or hard to derive
- Confusion:
 - Make the relationship between plaintext and ciphertext (their statistical features in terms of non-uniformity) too complex to be exploited by an attacker
- Diffusion:
 - Output bits in ciphertext should depend on input bits in plaintext in a very complicated way – a change of one input bit should change at least half of all output bits in an unpredictable / pseudorandom manner , (and not just one bit of it)

Substitution-Permutation Network

- SP-Networks (SPN) describe a series of substitution and permutation operations to be applied on plain text
 - The plaintext is separated into blocks (16bit words)
- The encoding operates over a sequence of rounds (“layers”), reapplying substitution and permutation operations over and over again to the output of a previous round

SP-Network (Example)

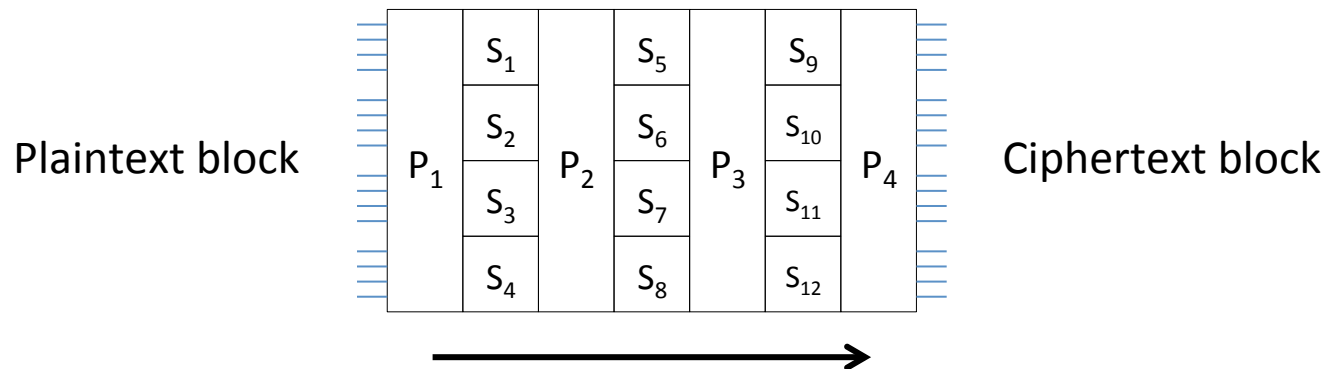


Substitution and Permutation

- Substitution in an SP-Network is performed with a so-called “substitution box” or S-box:
 - Are used to obscure or “confuse” the relationship between key and ciphertext
 - Takes as input m bits, produces a corresponding output of n bits
 - Implemented as an $m \times n$ lookup table
 - Substitution table is carefully designed to reduce vulnerability (Shannon: a change of one input bit should change at least half of all output bits)
- Permutation is performed with a so-called “permutation box” or P-box:
 - Takes the output of all substitution boxes as its input
 - Re-orders (permutes) bits to produce output

Substitution and Permutation

- Substitution and Permutation are called the “mixing transformations” by Shannon
 - S-box: provides “confusion” of input bits
 - P-box: provides “diffusion” across S-box inputs



AES Advanced Encryption Standard

- Based on the Rijndael algorithm
- Uses a SP-network
 - Fixed block size of 128 bits
 - Supports key sizes of 128, 192 and 256 bits
- Is fast in encryption / decryption both in software and hardware implementations
- Is the default encryption standard for the US government
- Probably cannot be cracked with current technology

Discussion of Secret-Key Cryptography

- Advantages
 - High rates of data throughput, with hardware solutions up to hundreds of megabytes per second
 - Key length is relatively short
 - Symmetric-key ciphers can also be combined to produce stronger ciphers
- Disadvantage
 - The key must remain secret at both ends
 - Cryptographic practice leads to frequent key change
 - In large networks, many key pairs have to be managed

Robustness

- Average time required for exhaustive key search:

Key Size (in bits)	Number of Alternative Keys	Time required at 10^6 Decryptions/ μ s
32	$2^{32} = 4.3 \times 10^9$	2.15 milliseconds
56	$2^{56} = 7.2 \times 10^{16}$	10 hours
128	$2^{128} = 3.4 \times 10^{38}$	5.4×10^{18} years
168	$2^{168} = 3.7 \times 10^{50}$	5.8×10^{30} years

Key Distribution

- With any symmetric algorithm, the key must be agreed upon by sender and receiver in a secure way
- Before 1976, key exchange was by far the biggest problem in secure communications
- Possible Strategies:
 - A key could be selected by A and physically delivered to B
 - A third party could select the key and physically deliver it to A and B
 - If A and B have previously used a key, one party could transmit the new key by encrypting it with the old key
 - If both A and B have an encrypted connection with a third party C, C could deliver a key on the encrypted links to A and B

Diffie-Hellman Key Exchange

- Developed in 1976, is a key exchange method where two parties exchange information that allows them to derive the same key, but never actually exchange the key
- Method:
 - Two parties, Alice and Bob, agree on a large prime number p and a small integer g ; these two numbers are public
 - Alice picks a secret large random integer a , and calculates a number A:

$$A = g^a \bmod p$$

- A becomes a public key, Alice transmits A to Bob
- Bob picks a secret large random integer b , and calculates a number B:

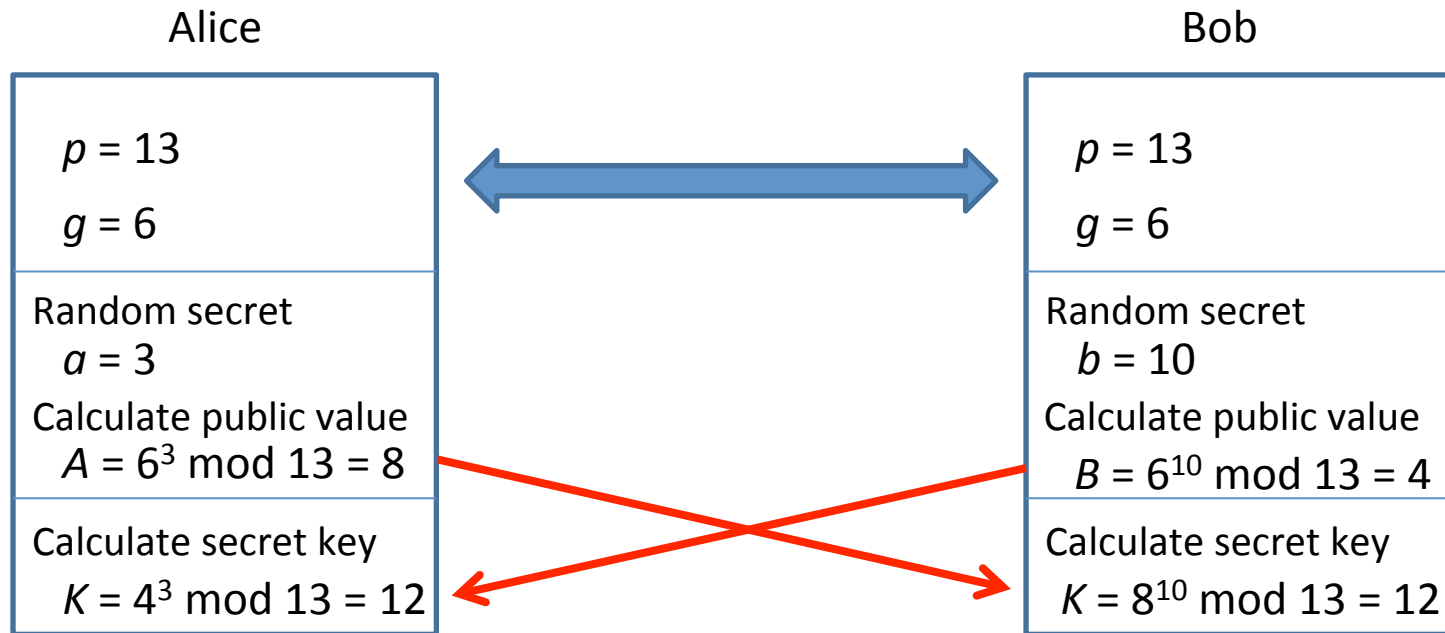
$$B = g^b \bmod p$$

- B becomes a public key, Bob transmits B to Alice
- Alice computes the secret key: $K_{Alice} = B^a \bmod p$
- Bob computes the secret key: $K_{Bob} = A^b \bmod p$

- Rules
 - p must be a prime number, $p > 2$
 - g must be a small integer, $g < p$
 - a and b are large random integers, $a < p-1$, $b < p-1$

Diffie-Hellman Key Exchange

- Example



Key Distribution

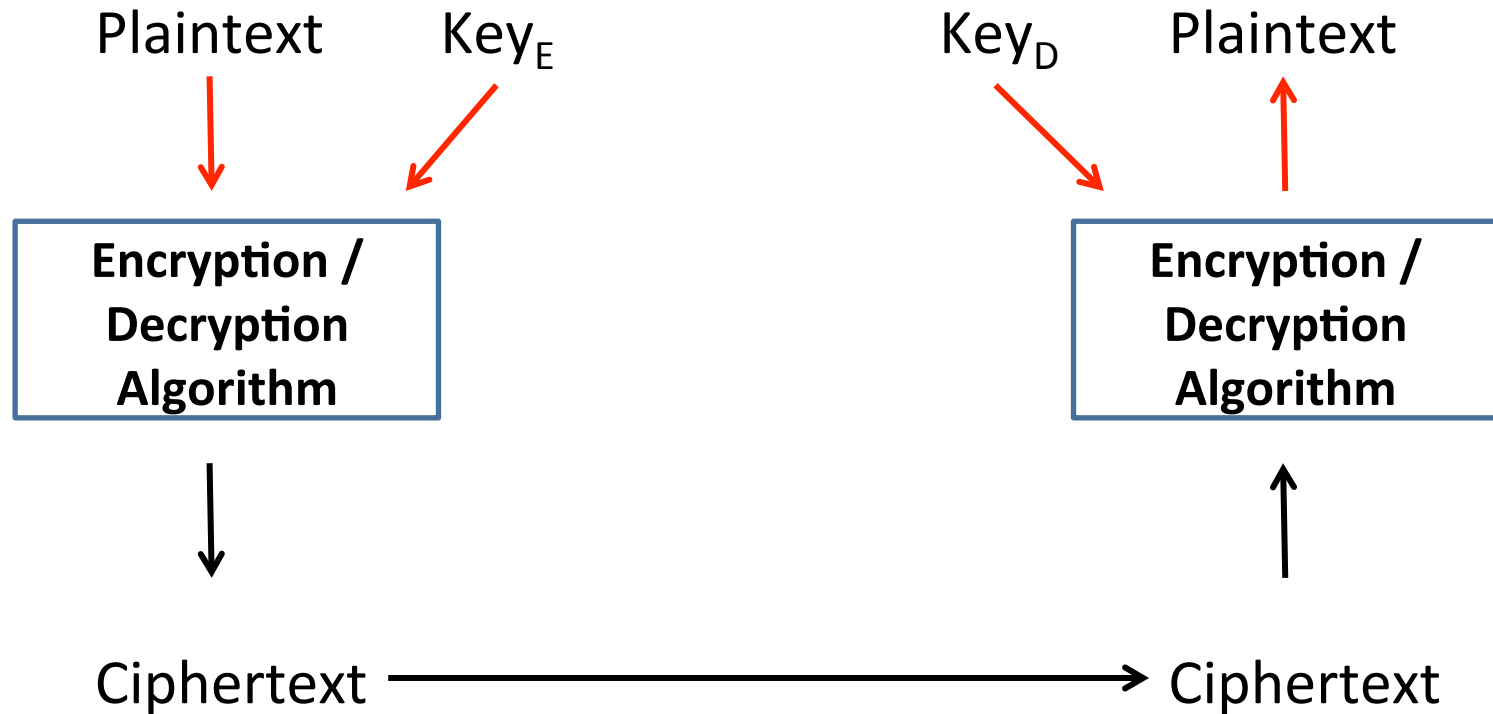
- Session key
 - Data encryption with a one-time session key, is destroyed at the conclusion of a session
- Permanent key
 - Used between entities for the purpose of distributing session keys

Public Key Cryptography

- Using one secret (private) key poses a security risk
- A solution to this problem is “Public Key Cryptography”
- Two keys: public and private (secret) key
- The keys are matched so that
 - A message encrypted with the public key can be decrypted using the private key
 - A message encrypted with the private key can be decrypted using the public key

Public-Key Encryption

(Asymmetric Key Encryption)



- Two different keys: public key, private key

Applications for Public Key Cryptography

- Encryption / Decryption
 - The sender encrypts the message with the recipients public key
- Digital Signature
 - The sender “signs” a message with its private key. For this, a cryptographic algorithm is applied to the whole message or to a small block of data that is a function of the message (a “fingerprint” of the message, called a message “digest”)
- Key Exchange
 - Exchange key information using the private key of one or both parties

Public-Key Cryptography

- Privacy:
 - Encryption with public key, decryption with private key
 - Anyone can send a message, using the public key of the receiver
 - no one else can read the message, because only the private key can decrypt the message
 - Only the owner of the private key can decrypt the message

Public-Key Cryptography

- Authenticity
 - Encryption with the private key, decryption with the public key
 - Receivers of a message can verify who sent the message with the sender's public key
 - Only the owner of the private key can have generated such an encrypted message

Public-Key Cryptography- Requirements

- Easy to generate a public key / private key pair
- Easy for a sender to generate ciphertext using the public key
- Easy for the receiver to decrypt ciphertext using the private key
- Computationally infeasible to determine the private key, knowing the public key
- Computationally infeasible to recover the message without the private key, knowing the public key and ciphertext
- Either of the two keys can be used for encryption, with the other used for decryption

RSA Public-Key Cryptosystem

- RSA (Rivest, Shamir, Adleman, 1977): best known, regarded as the most practical public-key scheme
 - Used for encrypting messages, key exchange and creating digital signatures
 - Is a block cipher
 - Plaintext and Ciphertext are represented as integers in the range of $[0 .. n-1]$ for some n

RSA

- Encryption:
 - A ciphertext block C is the result of encryption of a plaintext block M , using the publicly known numbers e and n

$$C = M^e \bmod n$$

- Decryption
 - A plaintext block M is the result of decryption of a ciphertext block C , using the secret number d

$$M = C^d \bmod n = (M^e)^d \bmod n = M^{ed} \bmod n$$

RSA Key Generation

- To do:
 - Public Key: both sender and receiver must know the values of n and e
 - Calculate number n (maximum possible value of a plaintext / ciphertext block)
 - Calculate number e (a value needed for encryption)
 - Private Key
 - Calculate number d (a value needed for decryption)
 - only the receiver knows the value of d

RSA Key Generation

- Calculate n
 - Select two large prime numbers p and q , these are secret
 - Calculate: $n = p \times q$
- Calculate the public e
 - e is “relatively prime” to the Euler Totient $\phi(n)$
 - $e < \phi(n)$
- *What is*
 - “relatively prime” ?
 - Euler Totient $\phi(n)$?

RSA

- Relatively prime numbers:
 - Two integers n and m are relatively prime, if their greatest common divisor is 1: $\gcd(n,m) = 1$
 - n and m do not share any common positive prime factors (divisors) except 1
- Euler Totient $\phi(n)$
 - Is the **number** of positive integers that are $\leq n$ and that are relatively prime to n
 - E.g.: $n = 10$, $\{1,3,7,9\}$ is the set of positive integers relative prime to 10, therefore: $\phi(n) = 4$
 - If n is the product of two prime numbers, p and q , then $\phi(n) = (p-1)(q-1)$
 - E.g.:
 - $p = 3$, $q = 5$, $n = p \times q = 3 \times 5 = 15$, therefore: $\phi(n) = (p-1)(q-1) = 2 \times 4 = 8$
 - $n = 15$, $\{1,2,4,6,7,8,11,13\}$

RSA Key Generation

- Calculate n
 - Calculate: $n = p \times q$, p and q are two large prime numbers
- Calculate the public e
 - We know:
 - If $n = p \times q$, p and q are prime numbers, then $\phi(n) = (p-1)(q-1)$
 - Choose e :
 - e is relatively prime to $(p-1)(q-1)$ and $1 < e < (p-1)(q-1)$
- Calculate the private key d
 - $d = e^{-1} \bmod (p-1)(q-1)$
- Result
 - Public key $K_{\text{PUB}} = \{e, n\}$
 - Private key $K_{\text{PRIV}} = \{d, n\}$
- *Encryption: encrypt a plaintext M to generate a ciphertext C via $\mathbf{C = M^e \bmod n}$*
- *Decryption: decrypt a ciphertext C to generate a plaintext M via $\mathbf{M = C^d \bmod n}$*

RSA Example

- Select two prime numbers, $p = 11$, $q = 3$
- Calculate $n = pq = 11 \times 3 = 33$
- Calculate $(p-1)(q-1) = 10 \times 2 = 20$
- Select e such that e is relatively prime to $(p-1)(q-1) = 20$ and $e < 20$
 - We select $e = 3$
- Calculate d such that $de = 1 \bmod 20$ and $d < 20$
 - That means: $3d \equiv 1 \bmod 20$
 - Result: $d = 7$, because $(7 \times 3)/20$ has the remainder 1 (that's the same as: $7 \times 3 = 21 = 2 \times 10 + 1$, or $21 \equiv 1 \bmod 20$)
- Keys
 - Public Key = $\{3, 33\}$
 - Private Key = $\{7, 33\}$
- Encrypt
 - Plaintext $M = 5$
 - Calculate ciphertext: $C = 5^3 \bmod 33 = 125 \bmod 33 = 26$
- Decrypt
 - Ciphertext = 26
 - Calculate plaintext $M = 26^7 \bmod 33 = 5$

RSA Cryptanalysis

- Brute force
 - Attack: try all possible private keys
 - Defence: the larger the number of bits for encoding e and d , the more secure this form of encoding will be
 - Problem: large keys slow down calculations
- Factoring n :
 - Vulnerability comes from the number n : If the number n is calculated from two large prime numbers p and q , finding these two secret prime factors by factoring n would allow us to calculate all elements of the RSA
 - Factoring n is a hard problem
 - We can factor a 512-bit number with 100s of CPU years (available to NSA, not random hacker)
 - We cannot factor 1024-bit numbers with present technology and math