

# CS1512

## Foundations of Computing Science 2

### Tutorial: Week 4

**Note:** In the lecture, I didn't manage to cover the probability of either of two mutually exclusive events occurring. However the material is there in the slides and your tutors will go over it with you.

**1.**

If someone tells you that the probability of event  $X$  happening is  $y$  (i.e.  $P(X) = y$ ), what are the possible sources of  $y$ ?

**2.**

A fair coin is tossed 4 times. How many possible outcomes are there for this experiment? List them, writing 'H' for heads and 'T' for tails. What is the probability of getting:

- (a) 4 heads?
- (b) no heads?
- (c) exactly 3 heads?
- (d) at least 3 heads?
- (e) a run of 3 or more heads (that is, 3 or more in a row)?
- (f) at least 2 tails?

Let  $X$  be the number of heads minus the number of tails. For each value  $k$  of the random variable  $X$  write down the probability  $P(X = k)$ .

**3.**

A bag contains 2 red balls, 3 white balls and 5 blue balls. A ball is withdrawn, its colour noted, replaced, and a second ball is drawn. What is the probability of a red ball being drawn followed by a blue ball? What is the probability of getting a red ball and a blue ball if the order in which they are drawn is not taken into account? What are the two probabilities if the first ball is **not** replaced?

**4.**

What is the probability of getting a total score of 3 from throwing two dice? Of getting 5? Of getting 7? 9? 11? What is the probability of getting a total score which is odd.

**5.**

Three cards are drawn at random without replacement from a well-shuffled pack of 52 cards. What is the probability that they are:

- all spades?
- all Aces?