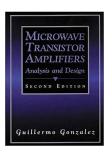
# EE5303 Microwave Electronics Part 2 Tutorial Q&As

Edited by En-Xiao Liu, 12 Oct 2022

This set of tutorial material should be used for the sole purpose of supplementing the study of Part 2 of EE5303. Questions are mainly taken or adapted from the 3 designated reference textbooks.

All copyrights belong to the original authors/publishers.

- Please study and grasp the key points covered in the four Lecture notes.
  - Please try all the examples in the lecture notes at least once.
- Do not hesitate to talk to your classmates, Prof. Guo, me, or our GAs, if you need help.



# Q1

### [Gonzalez, p.16] (adapted)

The propagation constants of the transmission lines in Fig. 1.3.6 is  $\beta$ .

Use the Transmission Line Equation to find out the expression (in terms of  $\beta$ , d, l,  $Z_0$  and/or  $Z_L$ ) for the input impedance  $\bf Z$  and reflection coefficient  $\Gamma$  for four cases: (a), (b), (c) and (d).

### Key Formulae

#### Lossless

When Z is normalized to the characteristic impedance Z<sub>0</sub>

$$egin{align} Z_{
m in}(\ell) &= Z_0 rac{Z_{
m L} + j\,Z_0\, an(eta\ell)}{Z_0 + j\,Z_{
m L}\, an(eta\ell)} & \Gamma_0 &= rac{z\,-\,1}{z\,+\,1} \ & \Gamma_{
m L} &= rac{Z_{
m L} - Z_0}{Z_{
m L} + Z_0} & \Gamma_{
m IN}(d) &= \Gamma_0 e^{-j2eta d} \ & z_{
m IN}(d) &= rac{1 + \Gamma_{
m IN}(d)}{1 - \Gamma_{
m IN}(d)} \ \end{aligned}$$

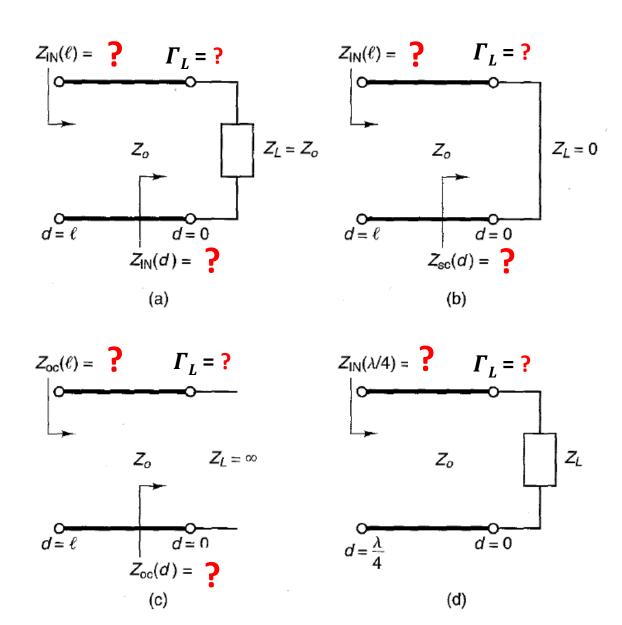


Figure 1.3.6 (a) The matched transmission line; (b) the short-circuited transmission line; (c) the open-circuited transmission line; (d) the quarter-wave transmission line.

### Q1-Ans

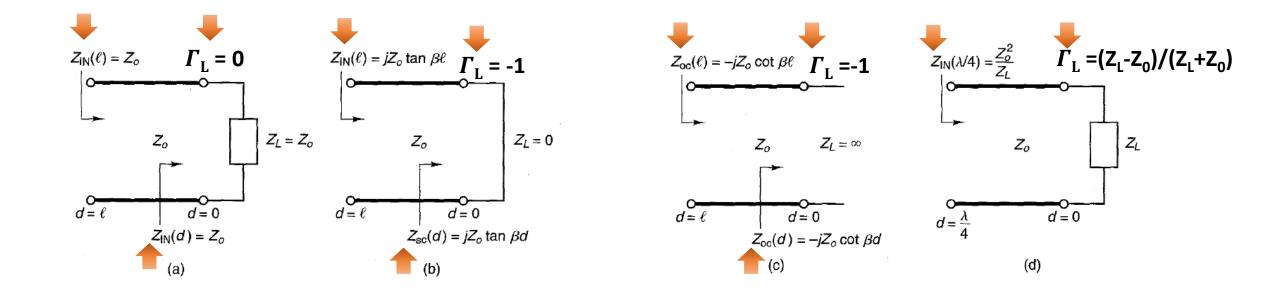
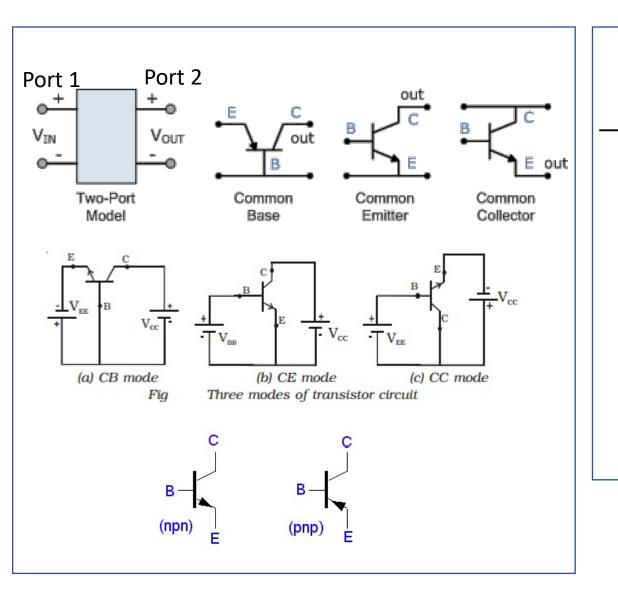


Figure 1.3.6 (a) The matched transmission line; (b) the short-circuited transmission line; (c) the open-circuited transmission line; (d) the quarter-wave transmission line.



\*\*\* Q2 & the info. below are for reference only, which is NOT in the EE5303 syllabus.

### Bipolar Transistors & Conversions of y parameters



CB, BE, CC
Conversion between Common-Base, Common-Emitter, and Common-Collector y Parameters

$$y_{11,e} = y_{11,b} + y_{12,b} + y_{21,b} + y_{22,b} = y_{11,c}$$

$$y_{12,e} = -(y_{12,b} + y_{22,b}) = -(y_{11,c} + y_{12,c})$$

$$y_{21,e} = -(y_{21,b} + y_{22,b}) = -(y_{11,c} + y_{21,c})$$

$$y_{22,e} = y_{22,b} = y_{11,c} + y_{12,c} + y_{21,c} + y_{22,c}$$

$$y_{11,b} = y_{11,e} + y_{12,e} + y_{21,e} + y_{22,e} = y_{22,c}$$

$$y_{12,b} = -(y_{12,e} + y_{22,e}) = -(y_{21,c} + y_{22,c})$$

$$y_{21,b} = -(y_{21,e} + y_{22,e}) = -(y_{12,c} + y_{22,c})$$

$$y_{22,b} = y_{22,e} = y_{11,c} + y_{12,c} + y_{21,c} + y_{22,c}$$

$$y_{11,c} = y_{11,e} = y_{11,b} + y_{12,b} + y_{21,b} + y_{22,b}$$

$$y_{12,c} = -(y_{11,e} + y_{12,e}) = -(y_{11,b} + y_{21,b})$$

$$y_{21,c} = -(y_{11,e} + y_{21,e}) = -(y_{11,b} + y_{12,b})$$

$$y_{22,c} = y_{11,e} + y_{12,e} + y_{21,e} + y_{22,e} = y_{11,b}$$

[Gonzalez, p.63]



#### [Gonzalez, p.91]

**1.27** The common-emitter S parameters of a GaAs FET at f = 10 GHz are

$$S_{11} = 0.73 \boxed{-128^{\circ}}$$

$$S_{21} = 1.73 \boxed{73^{\circ}}$$

$$S_{12} = 0.045 \boxed{114^{\circ}}$$

$$S_{22} = 0.75 \left[ -52^{\circ} \right]$$

Determine the common-base and common-collector S parameters.

### Q2-Ans

1.27) CONVERT THE CE SPARAMETERS TO CE & PARAMETERS (SEE FIG.1.8.1) THAT IS: y = 0.016+10.034 412e=0.00141-10.0272(103) y21,e=0.04-j0.036 y22,e=0.00363+j0.0079

USE THE RELATIONS IN FIG. 1.8.16 TO CALCULATE THE CB AND CC Y PARAMETERS. THAT IS,

CONVERT FROM CB AND CC & PARAMETERS TO CB AND CC S PARAMETERS. THAT IS,

$$[S] = \begin{bmatrix} 0.356 \left[ -173.6^{\circ} & 0.243 \left[ 35.41^{\circ} \right] \\ 1.348 \left[ -54.81^{\circ} & 1.198 \left[ -32.7^{\circ} \right] \end{bmatrix} & \text{AND} \quad [S] = \begin{bmatrix} 0.893 \left[ -62.03^{\circ} & 0.764 \left[ 29.68^{\circ} \right] \\ 1.12 \left[ -35.26^{\circ} & 0.176 \left[ 98.35^{\circ} \right] \end{bmatrix} \end{bmatrix}$$

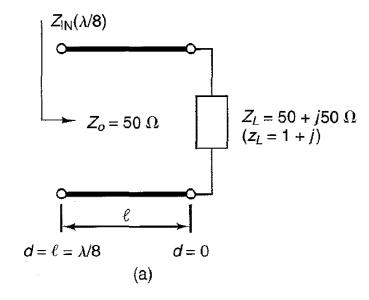


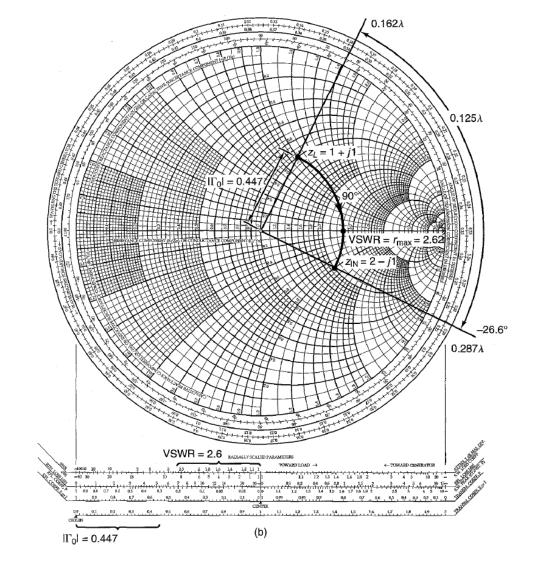
[Gonzalez, p.101-105]

### **Example 2.2.4**

Find the input impedance, the load reflection coefficient, in a transmission line having an electrical length of 45°, characteristic impedance of 50  $\Omega$ , and terminated in a load  $Z_L = 50 + j50 \Omega$ .

### Q3a-Ans







#### **Example 2.2.5**

[Gonzalez, p.101-105]

- (a) Determine the length l of the 50- $\Omega$  short-circuited transmission line shown in Fig. 2.2.8a so that the input impedance is  $Z_{\rm IN}(l) = j100~\Omega$ .
- (b) Determine the length l of the 50- $\Omega$  open-circuited transmission line shown in Fig. 2.2.8b so that the input impedance is  $Z_{\rm IN}(l) = j100~\Omega$ .

### Q3b-Ans

**Solution.** (a) In the short-circuited transmission line,  $z_L = 0$ . From Fig. 2.2.8a, the length l required to transform the load impedance  $z_L = 0$  to the input impedance  $z_{\text{IN}}(l) = j100/50 = j2 \Omega$  is  $l = 0.176 \lambda$ . Observe that in a short-circuited line the motion is along the edge of the chart (since  $|\Gamma| = 1$  in a short-circuited line).

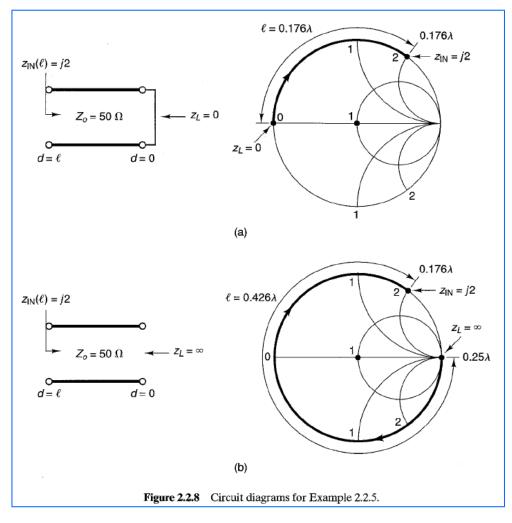
The length could have been calculated using (1.3.45). That is,

$$Z_{\rm IN}(l) = j100 = j50 \tan \beta l$$

which gives  $\tan \beta l = 2$  or  $\beta l = 63.43^{\circ} = 0.352\pi$ . Then

$$l = \frac{0.352\pi\lambda}{2\pi} = 0.176\lambda$$

(b) In the open-circuited transmission line,  $z_L = \infty$ . Therefore, from Fig. 2.2.8b the length l is  $0.426\lambda$  [i.e.,  $(0.5\lambda - 0.25\lambda) + 0.176\lambda = 0.426\lambda$ ].





[Gonzalez, p.101-105]

### **Example 2.2.6**

(a) Determine the input admittance of a short-circuited transmission line having a length of  $\lambda/8$  and  $Y_o = 1/Z_o = 20$  mS.

(b) Determine the input admittance of an open-circuited transmission line hav-

ing a length of  $\lambda/8$  and  $Y_o = 1/Z_o = 20$  mS.

### Q3c-Ans

**Solution.** (a) For the short-circuited line, the load admittance is  $y_L = \infty$ . Plotting  $y_L$  in the Y Smith chart shown in Fig. 2.2.9a and rotating along the constant gamma circle  $|\Gamma| = 1$  a distance  $l = \lambda/8$ , we obtain  $y_{IN}(l) = -j$  or

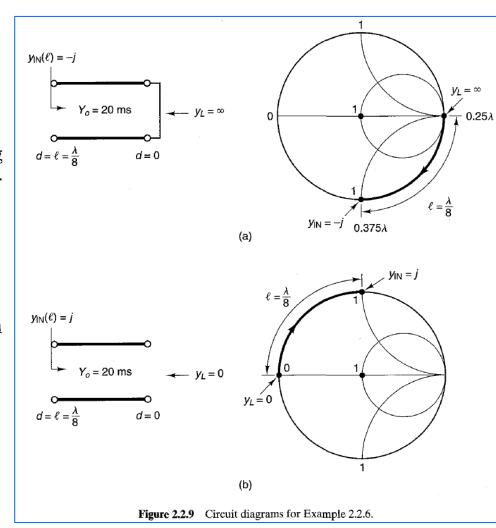
$$Y_{IN}(l) = y_{IN}(l)Y_o = -j(20 \times 10^{-3}) = -j20 \text{ mS}$$

The input impedance is  $Z_{IN}(l) = 1/Y_{IN}(l) = j50 \Omega$ .

(b) In the open-circuited line, the load admittance is  $y_L = 0$ . Therefore, as shown in Fig. 2.2.9b, at  $l = \lambda/8$  we obtain  $y_{IN}(l) = j$  or

$$Y_{IN}(l) = y_{IN}(l)Y_o = j(20 \times 10^{-3}) = j20 \text{ mS}$$

The input impedance is  $Z_{IN}(l) = 1/Y_{IN}(l) = -j50 \Omega$ .



3.18 A microwave amplifier is to be designed for  $G_{TU,max}$  using a transistor with

$$S_{11} = 0.5 \ \underline{140^{\circ}}$$
  $S_{12} = 0$   
 $S_{21} = 5 \ \underline{45^{\circ}}$   $S_{22} = 0.6 \ \underline{-95^{\circ}}$ 

The S parameters were measured in a 50- $\Omega$  system at f = 900 MHz,  $V_{CE} = 15$  V, and  $I_C = 15$  mA.

- (a) Determine  $G_{TU,\max}$ .
- (b) Design two different microstrip matching networks.
- (c) Draw the constant gain circle for  $G_L = 1$  dB.
- (d) If the S parameters at 1 GHz are

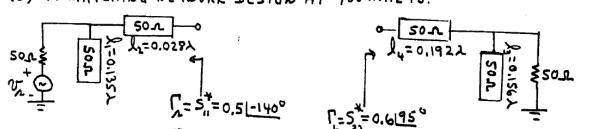
$$S_{11} = 0.48 \ \underline{137^{\circ}}$$
  $S_{12} = 0$   
 $S_{21} = 4.6 \ \underline{48^{\circ}}$   $S_{22} = 0.57 \ \underline{-99^{\circ}}$ 

calculate the gain  $G_T$  at 1 GHz for the designs in part (b).

# Q4-Ans

3.18)(a)  $G_{\text{n,max}} = \frac{1}{1 - (0.5)^2} = 1.33 \text{ or } 1.25 \text{ dB}$   $G_{\text{L,max}} = \frac{1}{1 - (0.6)^2} = 1.563 \text{ or } 1.94 \text{ dB}$  $G_0 = 15_{21}^2 = 25 \text{ or } 13.98 \text{ dB}$   $\therefore G_{\text{TU,max}} = 1.25 + 13.98 + 1.94 = 17.2 \text{ dB}$ 

(b) A MATCHING NETWORK DESIGN AT 900 MHZ 15:

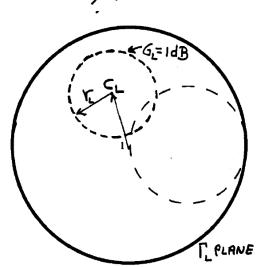


AT 900 MHZ:  $\lambda = \frac{310^{10}}{910^{8}} = 33.3 \text{ cm}$ ,  $l_1 = 0.135 \lambda = 4.496 \text{ cm}$ ,  $l_2 = 0.028 \lambda = 0.932 \text{ cm}$ ,  $l_3 = 0.156 \lambda = 5.195 \text{ cm}$ ,  $l_4 = 0.192 \lambda = 6.394 \text{ cm}$ 

(c) 
$$g_L = \frac{G_L}{G_{L/MRX}} = \frac{1.259}{1.563} = 0.805$$

FROM (3.4.11) AND (3.4.12):

r= 0.304



(d) LET x'= = where f'= 1 GHz, AND 2= WHERE f= 900 MHz. l=0.1352=0.135(1.112)=0.152, l2=0.028(1.112)=0.0312, 13=0.156(1.112)=0.1732 , 14=0.192(1.112)=0.2132 0.17421 12=0.0312 JO. 205 X まずれ 3/2= 1.79+51.58, [2=0.551-146° :. GTU= 1-(0.55)2 (4.6)2 1-(0.693)2=31.97 OR 15.05 dB **5.15 (a)** Johnson shows that the output power of an oscillator can be approximated with the equation

[Gonzalez, p.431]

$$P_{\text{OUT}} = P_{\text{sat}} (1 - e^{-G_0 P_{\text{IN}} / P_{\text{sat}}})$$

where  $P_{\text{sat}}$  is the saturated output power of the amplifier,  $P_{\text{IN}}$  is the input power, and  $G_o$  is the small-signal power gain. Show that the maximum oscillator power  $[P_{\text{osc}}(\text{max})]$  is given by

$$P_{\text{osc}}(\text{max}) = P_{\text{sat}} \left( 1 - \frac{1}{G_o} - \frac{\ln G_o}{G_o} \right)$$

Hint: The maximum oscillator power occurs at the point of maximum  $P_{\text{OUT}} - P_{\text{IN}}$ , or where

$$\frac{\partial P_{\text{OUT}}}{\partial P_{\text{IN}}} = 1$$

- (b) A GaAs FET has  $G_o = 7.5$  dB with  $P_{\text{sat}} = 1$  W. Calculate the maximum oscillator power.
- (c) Draw a typical  $P_{osc}/P_{sat}$  versus  $G_o$  plot.

MAXIMUM OSCILLATOR POWER OCCURS WHEN POUT - PIN 15 A

$$\frac{\partial P_{\text{out}}}{\partial P_{\text{IN}}} = P_{\text{sat}} \left( -\frac{G_0}{P_{\text{sat}}} \right) \left( e^{-G_0 P_{\text{IN}} / P_{\text{sat}}} \right) = G_0 e^{-G_0 P_{\text{IN}} / P_{\text{sat}}} = 1$$

$$P_{\text{out}} = P_{\text{sat}} \left( 1 - \frac{1}{G_0} \right) \tag{3}$$

FROM (3) AND (2), THE MAXIMUM OSCILLATOR POWER (P. (MAX)) IS

$$P_{osc}(max) = 1\left(1 - \frac{1}{5.623} - \frac{\ln 5.623}{5.623}\right) = 0.515 \text{ W}$$

[Gonzalez, p.428]

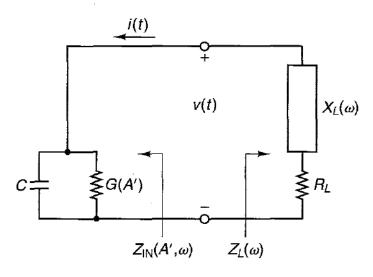


Figure P5.4

(a) Show that a stable oscillation at  $\omega = \omega_o$  occurs when

$$R_L = \frac{-G(A')}{G^2(A') + \omega^2 C^2}$$

$$X_L(\omega_o) = \frac{\omega C}{G^2(A') + \omega^2 C^2}$$

(b) Show that the oscillator power is a maximum when

$$G_L = \frac{G_0}{3}$$

where  $Y_L(\omega) = G_L + jB_L(\omega)$ .

## Q6-Ans

5.4)(a) 
$$Z_{IN}(A', \omega) = \frac{1}{G(A') + j\omega C} = \frac{G(A')}{G^2(A') + \omega^2 C^2} + j \cdot \frac{-\omega C}{G^2(A') + \omega^2 C^2}$$
  

$$\therefore R_{IN}(A', \omega) = \frac{G(A')}{G^2(A') + \omega^2 C^2} \quad \text{AND} \quad X_{IN}(A', \omega) = \frac{-\omega C}{G^2(A') + \omega^2 C^2}$$

Based on the oscillation conditions, A STABLE OSCILLATION OCCURS

$$R_{L} = -R_{IN}(A', \omega) = \frac{-G(A')}{G^{2}(A') + \omega^{2}C^{2}}$$

$$X_{L} = -X_{IN}(A', \omega) = \frac{\omega C}{G^{2}(A') + \omega^{2}C^{2}}$$

(b)  $P = \frac{1}{2} |V|^2 |G(A')| = \frac{1}{2} A'^2 G_0 (I - A'/A'_M), \frac{\partial P}{\partial A'} = \frac{G_0}{2} (2A' - \frac{3A'^2}{A'_M}) = 0$ or  $A' = A'_{0,Max} = \frac{2}{3} A'_M$ . At  $A' = A'_{0,Max}$  the value of  $G_{IN}(A')$  is:  $G_{IN}(A_{0,Max}) = -G_0/3$ . Therefore:  $G_L = G_0/3$ .



**4.13** Consider the LNB shown in Fig. P4.13. Calculate the total noise figure and the available gain.

[Gonzalez, p.377]

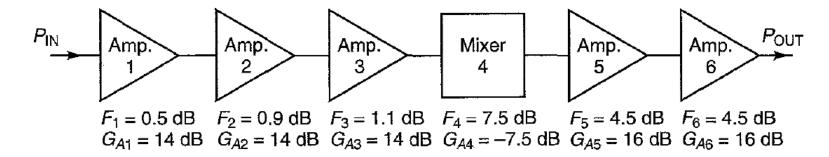


Figure P4.13

### Q7-Ans

4.13) G (dB)= 14+14+14-7.5+16+16=66.5 dB

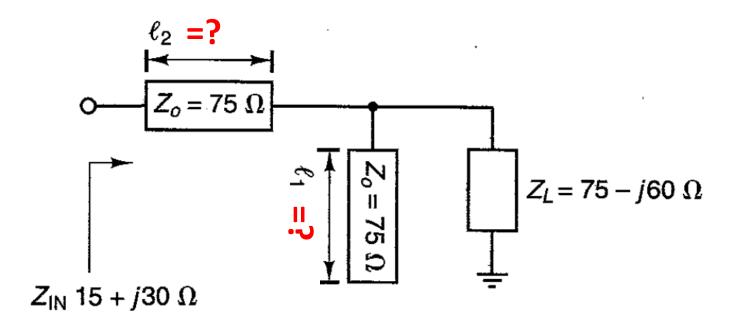
THE NOISE FIGURE OF THE LNB IS DETERMINED BY THE NOISE FIGURE OF THE LNA (C.R., THE FIRST 3 AMPLIFIERS).

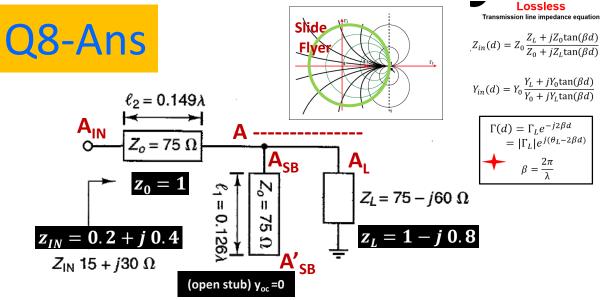
$$F = F_1 + \frac{F_2 - 1}{G_{A1}} + \frac{F_3 - 1}{G_{A1}G_{A2}} = 10^{0.05} + \frac{10^{0.09} - 1}{10^{1.4}} + \frac{10^{0.11} - 1}{10^{1.4} + 10^{1.4}} = 1.131 \text{ or } 0.54 \text{ dB}$$

THE CONTRIBUTION TO F FROM THE MIXER, AMP. 5, AND AMP. 6 IS NEGLIGIBLE.

# Q8

Design a microstrip matching network to transform the load  $Z_L = 75 - j60 \Omega$  to an input impedance of value  $Z_{\rm IN} = 15 + j30 \Omega$ . The characteristic impedance is  $Z_o = 75 \Omega$ 





**S0:** normalization (by  $Z_0$ )

#### **S1**: {ride on the $|\Gamma|$ flyers}

(i) draw the constant  $|\Gamma|$  circle, passing through  $z_L \frac{(!!!bye-bye)}{\text{the flyer & the slide}}$ 

$$y_L = 0.61 + j0.49 \text{ (at } A_L)$$

(ii) repeat (i) for z<sub>IN</sub> and we get

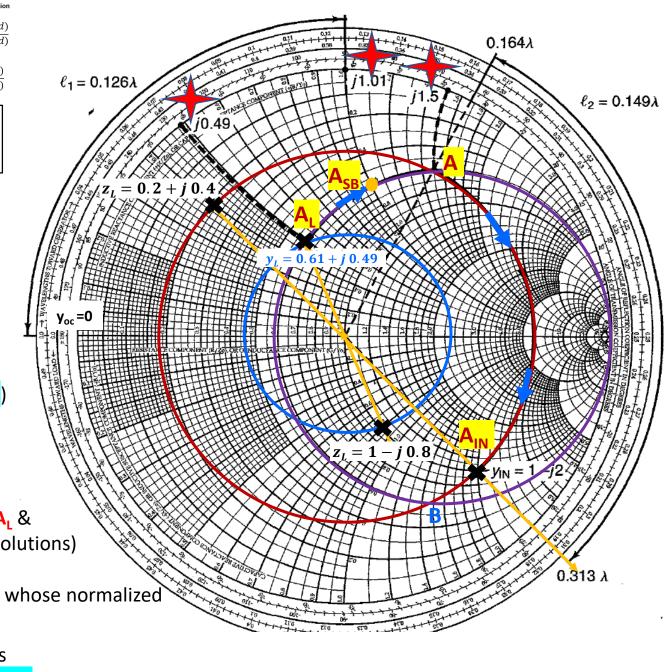
$$y_{IN} = 1.0 - j2.0 \text{ (at } A_{IN})$$

#### **S2**: {build the bridge to travel from A' to A''}

(i) draw the constant conductance  $g=Re(y_L)=\frac{0.61}{0.61}$  circle crossing  $A_L$  & intersecting with  $|\Gamma(y_{IN})|$  circle at two points A & B (two basic solutions) Read  $A \rightarrow y_A = 0.61 + j \cdot 1.5$  (see the flyer & the slide)

(ii) from  $A_L$  [  $\rightarrow$   $y_L$  = 0.61 +j 0.49] to A via  $A_{SB}$   $\rightarrow$  the shunt stub  $l_2$ , whose normalized admittance  $y_{SB}$ =j(1.50-0.49)=j 1.01

S3: Read, towards the generator, the length of the Transmission lines  $l_1$  (from A clockwise to  $A_{IN}$ ) and  $l_2$  (from  $A'_{SB}$  ( $y_{oc}$  =0) to  $A_{SB} \rightarrow it's$  a slide)





[Gonzalez, p.369-370]

#### **Example 4.7.3**

Design a 1-W (or 30-dBm) GaAs FET power amplifier for linear operation at 4 GHz. The input signal power is -5 dBm.

**Solution.** The required power gain of the power amplifier is

$$G_p(dB) = P_{OUT}(dBm) - P_{IN}(dBm) = 30 - (-5) = 35 dB$$

For this design we selected the transistors from the *Hewlett-Packard Communications Components—GaAs & Silicon Products Designer's Catalog*. The transistors selected, with some pertinent data at 4 GHz, are listed in Fig. 4.7.16a. Figure 4.7.16a shows that the ATF44101 transistor can provide linear amplification with  $G_p = 10$  dB and an output power of 1 W (or 30 dBm) at 4 GHz.

The required power gain of 35 dB can be obtained using three-stages, as shown in Fig. 4.7.16b. The gain and power levels of each stage are indicated in Fig. 4.7.16b.

The power gain of the three-stage amplifier in Fig. 4.7.16b is

$$G_p = G_{p1} + G_{p2} + G_{p3} = 14 + 11 + 10 = 35 \text{ dB}$$

Therefore, the output power is

$$P_{\text{out}}(\text{dBm}) = P_{\text{in}}(\text{dBm}) + G_p = -5 + 35 = 30 \text{ dBm (or 1 W)}$$



Transistor	Q point	$G_p$	$P_{1\mathrm{dB}}$	$G_{ m 1dB}$
ATF44101	9 V, 500 mA	10	32 dBm	9
ATF45101	9 V, 250 mA	11	29 dBm	10
ATF25570	5 V, 5 mA	14	20.5  dBm	13

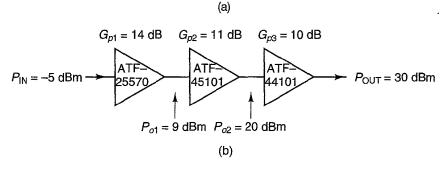


Figure 4.7.16 (a) Transistors selected and some pertinent data at 4 GHz; (b) a 1-W, three-stage, linear power amplifier at 4 GHz.

### 3.17 The scattering parameters of a GaAs FET in a 50- $\Omega$ system are

$$S_{11} = 2.3 \ | -135^{\circ}$$
 $S_{12} = 0$ 
 $S_{21} = 4 \ | 60^{\circ}$ 
 $S_{22} = 0.8 \ | -60^{\circ}$ 

- (a) Determine the unstable region in the Smith chart and construct the constant-gain circle for  $G_s = 4$  dB.
- (b) Design the input matching network for  $G_s = 4$  dB with the greatest degree of stability.
- (c) Draw the complete ac amplifier schematic.

### Q10-Ans

3.17) (a) THE INPUT RESISTANCE IS CALCULATED AS FOLLOWS:

[= 5, = 2.3 -135° , Z= 50(-0.45-j0.341)=-22.48-j17.04 1.

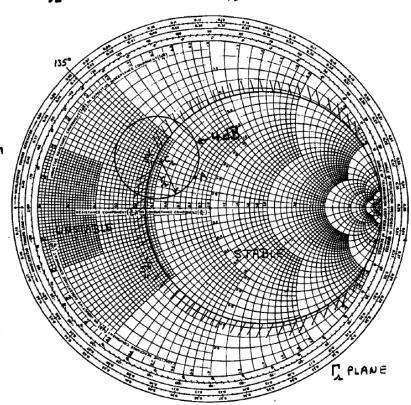
ZIN CAN ALSO BE CALCULATED USING THE SMITH CHART.

PLOT 1 = 0.435 1-135 AND READ ZIN 50(-0.45-30.34) =-22.5-317.

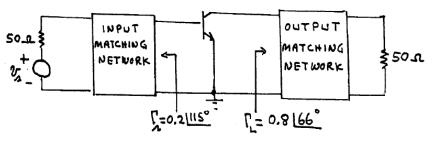
FOR G\_=4 dB , g\_=2.512[1-(2.3)2]=-10.78 FROM (3.4.11) AND (3.4.12): G=0.404[135° AND 7=0.24

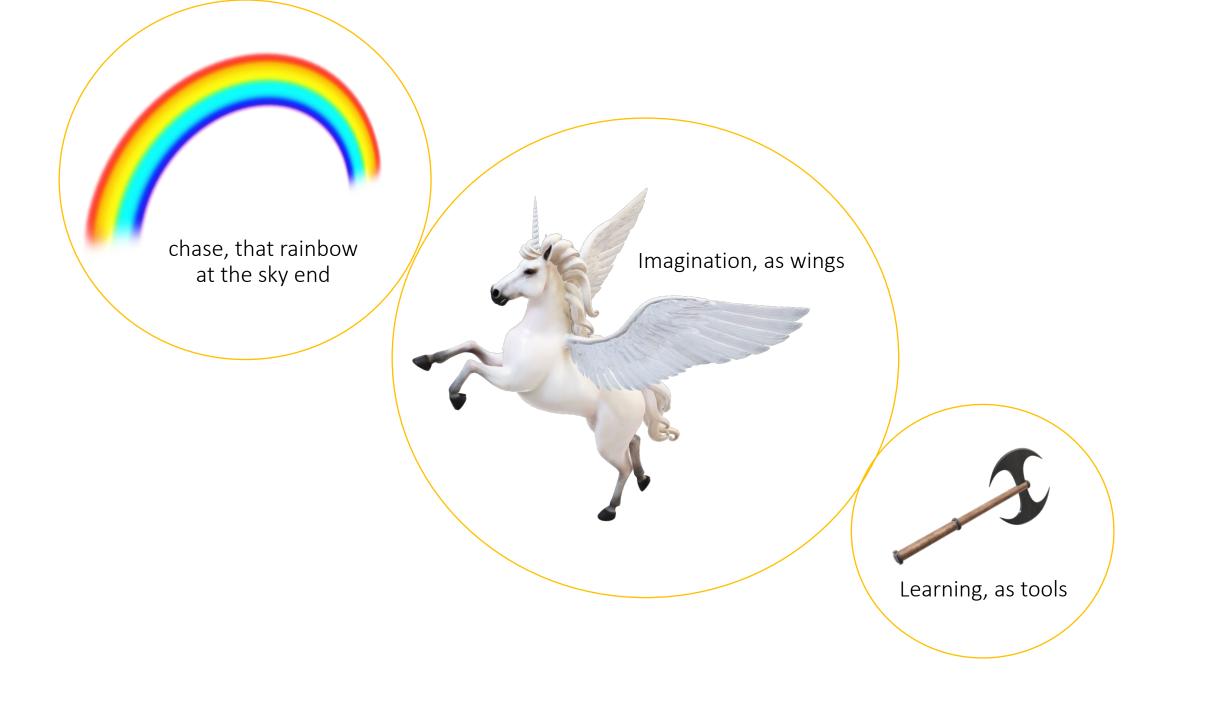
(b) AT POINT A, T, HAS
THE LARGEST REAL
PART ON THE G.= 4 dB
CIRCLE. THAT IS,
T.= 0.2 LII5°

THE INPUT MATCHING CIRCUIT MUST TRAUSFORM 50 1 TO \$\int\_{=0.2\langle 1150}^{\infty}.



(c) Design FOR  $\sqrt{100} = 0.2 \frac{115^{\circ}}{115^{\circ}}$  AND  $\sqrt{100} = \frac{5^{*}}{22} = 0.8 \frac{166^{\circ}}{100}$ . Then,  $G_{\lambda} = 4 \frac{dB}{dB}$ ,  $G_{0} = \frac{15_{21}}{216} \frac{1}{100} = \frac{1}{100} = \frac{1}{1000} = \frac{1}{1$ 







### **Summary of Topics Covered in Part II of the EE5303 Module**

- (a) Amplifiers
- (b) Oscillators
- (c) Mixers
- (d) Input/output matching network (continued from Part 1)

#### **Key words:**

- . Stability, circle, stable/unstable region
- II. Gain, noise figures
- III. Multistage devices (Amplifier/mixers)
- IV. Reflection coefficients and impedances (Output/input/source/load)

### **Sub-Topics:**

- (a) Amplifiers
  - I. Stability check, stability regions
  - II. Unilateral design: maximum power/gain
  - III. Power gain, power gain circle
  - IV. Constant gain circle
  - V. Noise Figure
  - VI. Impedance matching (input/output matching network); Single-stub matching; working principle of filters

- (b) Oscillators
- I. Un-Stability
- II. Oscillating conditions
- III. Max power
- (c) Mixers
- I. Conversion loss
- II. Up/down conversion, image frequency

