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# Laboratory

## DC Motor Speed Control

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Course: **ACA**

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## Abstract

The rotation speed of a DC motor will be closed-loop controlled in this laboratory. The setup used to test this closed-loop controller is described at section 1.

A reasonable dynamical model of the process is needed to develop a good controller. The model used in this laboratory is based on the differential equations described in section 3. Its parameters will be determined experimentally by exploiting a typical step answer (see section 5).

The controller development approach is depicted in section 6.

The developed controllers will be implemented in a Beckhoff PLC as described in section 6.

## 1 Introduction

DC Motors are being widely used in numerous applications (low-power mechatronic systems like mobile robots). A motor from the company Maxon Motor AG is being used in this laboratory.

The datasheet of the motor considered here can be found in appendix A.

A picture of the plant can be found in figure 1.

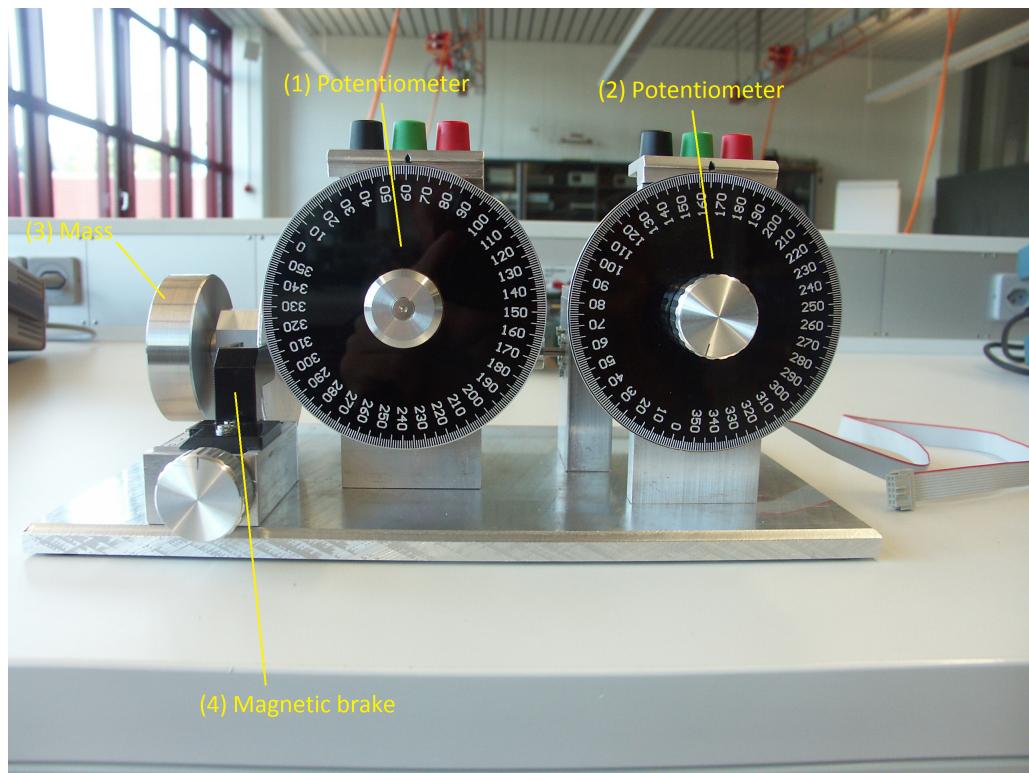


Figure 1: DC Motor experiment

Different masses (3) can be mounted on the plant. A magnetic brake (4) makes it possible to test different loads on the process.

## 2 Hardware

It's important to get familiar with the hardware of the experiment.

The DC motor being used is quite simple. Send it the enable signal, apply a positive or negative voltage and it rotates in the according direction. The motor voltage  $u(t)$  can take values between  $-24$  (V) and  $+24$  (V).

The incremental encoder is a bit more complicated. It is mounted directly on the motor axis and keeps track of the motor's position by incremental counting of pulses from its two sensors. The datasheet of this sensor can be found in the appendix B. This encoder has a resolution of 512 Impulses per turn.

The incremental encoder is nicely explained on Wikipedia:

An incremental rotary encoder provides cyclical outputs (only) when the encoder is rotated. They can be either mechanical or optical. ... The incremental rotary encoder is the most widely used of all rotary encoders due to its low cost and ability to provide signals that can be easily interpreted to provide motion related information such as velocity.

The fact that incremental encoders use only two sensors does not compromise their accuracy. One can find in the market incremental encoders with up to 10,000 counts per revolution, or more.

...

Incremental encoders are used to track motion and can be used to determine position and velocity. This can be either linear or rotary motion. Because the direction can be determined, very accurate measurements can be made.

They employ two outputs called A & B, which are called quadrature outputs, as they are 90 degrees out of phase.

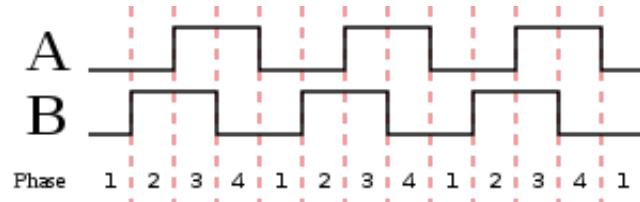


Figure 2: Sensor signals

The two output wave forms are 90 degrees out of phase, which is what quadrature means. These signals are decoded to produce a count up pulse or a count down pulse. For decoding in software, the A & B outputs are read by software, either via an interrupt on any edge or polling, and the above table is used to decode the direction. For example, if the last value was 00 and the current value is 01, the device has moved one half step in the clockwise direction.

A Beckhoff PLC will be used to program the different controllers and test them experimentally. The following terminals will be used:

Phase	A	B
1	0	0
2	0	1
3	1	1
4	1	0

Figure 3: Coding for clockwise rotation

Phase	A	B
1	1	0
2	1	1
3	0	1
4	0	0

Figure 4: Coding for counter-clockwise rotation

- EL5101: This terminal is used to read the encoder signal (differential). Take care, the step counter value of the channel is an UINT which at some point will overflow and start at 0 again.
- EL7342: This terminal is used to drive the motor. The enable signal is connected to DCM Control Channel 1. The DC supply voltage of the motor is provided by DCM Velocity Channel 1.

**Exercise 1:** Rotate the DC motor manually by one full revolution and check if you get the expected amount of steps from the encoder. You can observe this in the TwinCAT System Manager.



**Exercise 2:** Check if you can operate the motor manually (in free run mode) from the TwinCAT system manager. For this you first need to send it the enable signal, followed by the voltage to be applied. All these signals can be found in TwinCAT System Manager.



### 3 Model

A simple model of the DC Motor will be derived in this section

A schematic view of this motor can be seen in 5.

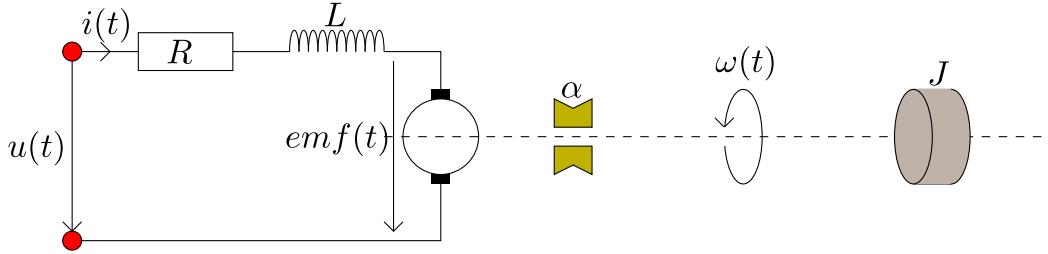


Figure 5: DC Motor Setup

The first differential equation links the current  $i(t)$  and the voltage  $u(t)$ .

$$u(t) = Ri(t) + L \frac{di(t)}{dt} + \text{emf}(t) \quad (1)$$

where  $\text{emf}(t)$  is the back-emf voltage expressed in (V).

Values for  $R$  and  $L$  can be found in appendix A.

It is assumed that  $\text{emf}(t)$  is proportional to the rotation speed  $\omega(t)$ :

$$\text{emf}(t) = K_\omega \omega(t) \quad (2)$$

$K_\omega$  can be found in appendix A.

$$J \frac{d\omega(t)}{dt} = K_M i(t) - M_l - \alpha \omega(t) \quad (3)$$

where  $M_l$  is the load.  $J$  is the inertia. The friction is approximated by  $\alpha \omega(t)$ .

$\alpha$  can be changed with the magnetic brake.

It is supposed that:

$$K_M = K_\omega \quad (4)$$

If we neglect  $L$ , the transfer function  $G(s) = \frac{\Omega(s)}{U(s)}$ , where

$$\begin{aligned} \omega(t) &\circlearrowleft \bullet \Omega(s) \\ u(t) &\circlearrowleft \bullet U(s) \end{aligned}$$

, can be derived as follows:

$$G(s) = \frac{K}{1 + \tau s}$$

## 4 Problem formulation

In this Laboratory, the rotation speed  $\omega(t)$  will be controlled.

**Exercise 3:** *Draw the block diagram of the process, uncontrolled. What is the control signal? The process output? What are possible disturbances?*

□

**Exercise 4:** *Draw the block diagram of the closed-loop controlled process.*

□

## 5 Parameter identification

Some of the parameters in  $G(s)$  are not well known. For this reason,  $K$  and  $\tau$  will be determined experimentally by applying a step signal to the motor voltage input from 5 [V] to 15 [V].

**Exercise 5:** In TwinCAT PLC Control (use the provided template project) and TwinCAT System Manager:

- connect the global variables (`globUint...`) in the template project with the hardware in- and outputs.
- in PROGRAM `WriteOutputs` convert the value of global variable `globVoltMotorVoltage` from volt to INT and save it in `globIntMotorVoltage`. Make sure the value does not exceed the INT value range! Use the constant `SCALE_VOLT_INT` for the conversion.
- use the provided visualization to control the motor voltage and create a step signal like described above. Use the TwinCAT scope to measure the step response of the velocity and export the acquired data.

□

**Exercise 6:** In Matlab display the acquired data of the motor voltage and velocity in the same plot and determine  $K$  and  $\tau$  graphically. Simulate the previously carried out experiment with the determined parameters in Matlab. Draw in the same plot the acquired data and the simulation results. Verify if the experiment and simulation match well.

Useful Matlab functions:

- Use `help <NAME_OF_FUNCTION>` to get the description of a function.
- Use `tf(...)` to create transfer functions.
- Use `lsim(...)` to simulate the output of a transfer function to a given input signal.

□

# 6 P Controller

In this section a P controller will be designed and experimentally tested. The controller design is normally done in three steps:

1. Create the specification (stability, stationary accuracy, rise time, oscillations)
2. Define the controller structure.
3. Calculate the parameters of the controller.

In this experiment we focus on points 2. and 3.

## 6.1 Controller structure

**Exercise 7:** For a P controller derive first the closed loop transfer function.

□

**Exercise 8:** Derive the reference tracking closed loop transfer function  $T_r(s)$  of the controlled process.

□

**Exercise 9:** Express the steady state error as a function of the controller gain  $K_p$ . Compute  $K_p$  for the following cases:

1. Case 1: A steady state error of 40 % is required.
2. Case 2: A steady state error of 5 % is required.

□

**Exercise 10:** In Matlab simulate the process output, when excited with a step from 0 RPM to 3000 RPM, of the closed loop transfer function of the controlled process with the above computed  $K_p$  for a steady state error of 5 % and 40 %. Also simulate the process output for the reference tracking closed loop transfer function  $T_r(s)$  with the same step signal. Compare the two simulations, are both of them sensible in a real world application?

□

## 6.2 Controller parameters

**Exercise 11:** Program and test the developed controller (with  $K_p$  for a steady state error of 40 %) experimentally and document the results (command signal, reference signal and process output). Test the controller with a reference value step from 1500 RPM to 2500 RPM. How does the DC supply voltage behave when you change the position of the magnetic brake? Is the controller stable? Compare the simulation results with the experimental results. Document these results.

□

## 7 PI Controller

In this section a PI controller will be first analyzed and experimentally tested.

### 7.1 Controller analysis

**Exercise 12:** *What is the transfer function of the PI Controller?*

□

**Exercise 13:** *Derive the closed loop transfer function for a PI Controller. How does this transfer function simplify if  $T_i$  is chosen such that  $T_i = \tau$ ?*

□

**Exercise 14:** *Derive the reference tracking closed loop transfer function  $T_r(s)$  of the controlled process for  $T_i \neq \tau$ . How does this transfer function simplify if  $T_i = \tau$ ?*

□

**Exercise 15:** *Prove that the steady state error is equal to zero for any value of  $K_p$  and  $T_i$ .*

□

### 7.2 PI controller parameters computation and experimental testing

**Exercise 16:** *Design a PI controller using the Kuhn approach.*

□

**Exercise 17:** *Test this controller in simulation using Matlab/Simulink. Realistic boundaries on the control signal should be taken into account in this simulation. A realistic reference signal should be programmed as well (for example a step of a few hundreds (rpm)). Test the controller with and without the anti-reset windup activated in the PID block (set  $K_D = 0$ ). Explain why it is important to have this option activated if an integral is present in the controller.*

□

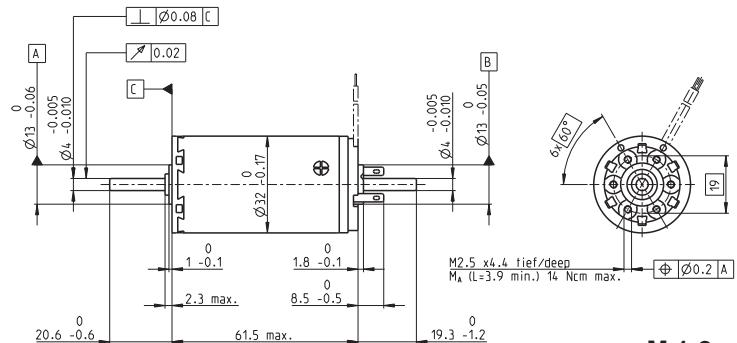
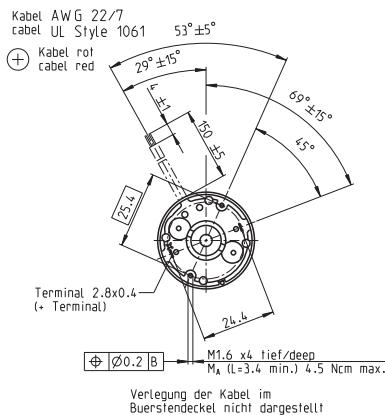
**Exercise 18:** *Program and test a PI controller experimentally.*

□

# A Maxon Motor 236655

## A-max 32 Ø32 mm, Graphite Brushes, 15 Watt

maxon A-max



Stock program  
Standard program  
Special program (on request)

### Order Number

with terminals	<b>236651</b>	236652	<b>236653</b>	236654	<b>236655</b>	236656	236657	236658
with cables	353220	353221	353222	353223	353224	353225	353226	353227

### Motor Data

#### Values at nominal voltage

1 Nominal voltage	V	6.0	9.0	12.0	18.0	24.0	30.0	36.0	48.0
2 No load speed	rpm	5830	4930	4670	5270	5930	5870	5830	3870
3 No load current	mA	153	83.2	58.4	44.8	38.6	30.5	25.2	11.7
4 Nominal speed	rpm	3800	2980	2860	3550	4180	4140	4090	2080
5 Nominal torque (max. continuous torque)	mNm	31.4	33.1	36.0	37.5	36.7	37.1	36.8	36.9
6 Nominal current (max. continuous current)	A	3.42	2.02	1.55	1.21	0.998	0.798	0.656	0.328
7 Stall torque	mNm	99.7	87.4	95.9	118	127	128	125	81.3
8 Starting current	A	10.4	5.12	3.98	3.66	3.34	2.66	2.15	0.698
9 Max. efficiency	%	75	75	77	79	80	80	80	76

#### Characteristics

10 Terminal resistance	Ω	0.577	1.76	3.02	4.92	7.19	11.3	16.7	68.8
11 Terminal inductance	mH	0.0657	0.209	0.416	0.739	1.04	1.66	2.43	9.71
12 Torque constant	mNm / A	9.58	17.1	24.1	32.2	38.2	48.2	58.3	117
13 Speed constant	rpm / V	996	559	396	297	250	198	164	81.9
14 Speed / torque gradient	rpm / mNm	59.9	57.6	49.5	45.5	47.1	46.3	47.1	48.4
15 Mechanical time constant	ms	27.6	23.5	22.4	21.8	21.7	21.5	21.5	21.5
16 Rotor inertia	gcm <sup>2</sup>	43.9	39.0	43.3	45.9	44.0	44.4	43.6	42.4

### Specifications

#### Thermal data

17 Thermal resistance housing-ambient	7.5 K / W
18 Thermal resistance winding-housing	2.1 K / W
19 Thermal time constant winding	17.7 s
20 Thermal time constant motor	791 s
21 Ambient temperature	-20 ... +85°C
22 Max. permissible winding temperature	+125°C

#### Mechanical data (ball bearings)

23 Max. permissible speed	6000 rpm
24 Axial play	0.12 - 0.22 mm
25 Radial play	0.025 mm
26 Max. axial load (dynamic)	7.6 N
27 Max. force for press fits (static)	110 N
(static, shaft supported)	2000 N
28 Max. radial loading, 5 mm from flange	32 N

#### Mechanical data (sleeve bearings)

23 Max. permissible speed	6000 rpm
24 Axial play	0.12 - 0.22 mm
25 Radial play	0.012 mm
26 Max. axial load (dynamic)	5.0 N
27 Max. force for press fits (static)	110 N
(static, shaft supported)	2000 N
28 Max. radial loading, 5 mm from flange	10.5 N

#### Other specifications

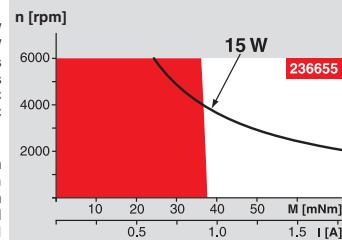
29 Number of pole pairs	1
30 Number of commutator segments	13
31 Weight of motor	211 g

Values listed in the table are nominal.  
Explanation of the figures on page 49.

#### Option

Sleeve bearings in place of ball bearings

### Operating Range



### Comments

#### Continuous operation

In observation of above listed thermal resistance (lines 17 and 18) the maximum permissible winding temperature will be reached during continuous operation at 25°C ambient.  
= Thermal limit.

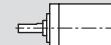
#### Short term operation

The motor may be briefly overloaded (recurring).

Assigned power rating

### maxon Modular System

#### Planetary Gearhead



#### Spur Gearhead



#### Spindle Drive



#### Recommended Electronics:

LSC 30/2 Page 282

ADS 50/5 282

ADS\_E 50/5 283

EPOS2 Module 36/2 304

EPOS2 24/5 305

EPOS2 50/5 305

EPOS2 P 24/5 308

Notes 18

### Overview on page 16 - 21

#### Encoder MR

256 - 1024 CPT,  
3 channels  
Page 263

#### Encoder HED\_5540

500 CPT,  
3 channels  
Page 267 / 268

# B Maxon Encoder 225785

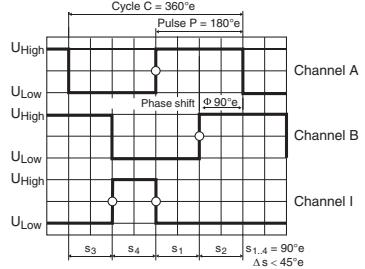
## Encoder MR Type L, 256 - 1024 CPT, 3 Channels, with Line Driver



**Stock program**

**Standard program**

**Special program (on request)**



Cycle C = 360°e  
Pulse P = 180°e  
Phase shift Φ 90°e  
S3 S4 S1 S2 S1,4 = 90°e Δs < 45°e  
Direction of rotation cw (definition cw p. 48)

maxon sensor
Order Number

	225783	228452	225785	228456	225787
<b>Type</b>					
Counts per turn	256	500	512	1000	1024
Number of channels	3	3	3	3	3
Max. operating frequency (kHz)	80	200	160	200	320
Max. speed (rpm)	18750	24000	18750	12000	18750

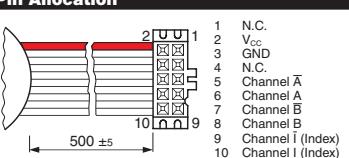
[overall length]
[overall length]

**maxon Modular System**

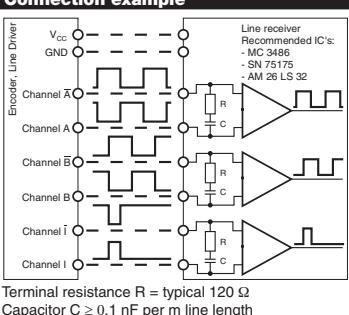
+ Motor	Page	+ Gearhead	Page	+ Brake	Page	Overall length [mm] / ● see Gearhead
RE 30, 60 W	80					79.4 79.4 79.4 79.4 79.4
RE 30, 60 W	80	GP 32, 0.75 - 4.5 Nm	229			● ● ● ● ●
RE 30, 60 W	80	GP 32, 0.75 - 6.0 Nm	231/232			● ● ● ● ●
RE 30, 60 W	80	GP 32 S	249-251			● ● ● ● ●
RE 35, 90 W	81					82.4 82.4 82.4 82.4 82.4
RE 35, 90 W	81	GP 32, 0.75 - 4.5 Nm	229			● ● ● ● ●
RE 35, 90 W	81	GP 32, 0.75 - 6.0 Nm	231/232			● ● ● ● ●
RE 35, 90 W	81	GP 32, 4.0 - 8.0 Nm	234			● ● ● ● ●
RE 35, 90 W	81	GP 42, 3 - 15 Nm	237			● ● ● ● ●
RE 35, 90 W	81	GP 32 S	249-251			● ● ● ● ●
RE 40, 150 W	82					82.4 82.4 82.4 82.4 82.4
RE 40, 150 W	82	GP 42, 3 - 15 Nm	237			● ● ● ● ●
RE 40, 150 W	82	GP 52, 4 - 30 Nm	240			● ● ● ● ●
A-max 32	110/112					72.7 72.7 72.7 72.7 72.7
A-max 32	110/112 GP 32, 0.75 - 6.0 Nm	231/233				● ● ● ● ●
A-max 32	110/112 GS 38, 0.1 - 0.6 Nm	236				● ● ● ● ●
A-max 32	110/112 GP 32 S	249-251				● ● ● ● ●
EC-max 40, 70 W	168					73.9 73.9 73.9 73.9 73.9
EC-max 40, 70 W	168	GP 42, 3 - 15 Nm	238			● ● ● ● ●
EC-max 40, 120 W	169					103.9 103.9 103.9 103.9 103.9
EC-max 40, 120 W	169	GP 52, 4 - 30 Nm	241			● ● ● ● ●
EC-i 40, 50 W	190					42.0 42.0 42.0 42.0 42.0
EC-i 40, 50 W	190	GP 32, 1 - 6 Nm	233			● ● ● ● ●
EC-i 40, 50 W	190	GP 32 S	249-251			● ● ● ● ●
EC-i 40, 70 W	191					52.0 52.0 52.0 52.0 52.0
EC-i 40, 70 W	191	GP 32, 1 - 6 Nm	233			● ● ● ● ●
EC-i 40, 70 W	191	GP 32 S	249-251			● ● ● ● ●

**Technical Data**

Supply voltage  $V_{CC}$  5 V ± 5%  
 Output signal TTL compatible  
 Phase shift  $\Phi$  90°e ± 45°e  
 Index pulse width 90°e ± 45°e  
 Operating temperature range -25 ... +85°C  
 Moment of inertia of code wheel ≤ 1.7 gcm²  
 Output current per channel max. 5 mA

**Pin Allocation**


DIN Connector 41651  
flat band cable AWG 28

**Connection example**


Line receiver  
Recommended IC's:  
- MC 3496  
- SN 75175  
- AM 26 LS 32

Terminal resistance R = typical 120 Ω  
Capacitor C ≥ 0.1 nF per m line length

The index signal I is synchronised with channel A or B.