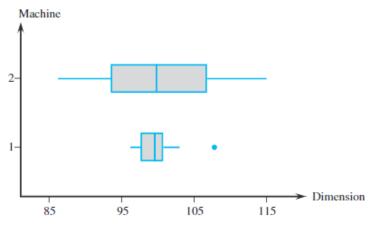
1. **Exercise 1.58:**

A company utilizes two different machines to manufacture parts of a certain type. During a single shift, a sample of n=20 parts produced by each machine is obtained, and the value of a particular critical dimension for each part is determined. The comparative boxplot at the bottom of this page is constructed from the resulting data. Compare and contrast the two samples.





Answer: Looking at the spread of the 2 boxplots we can make some assertions about the manufacturing quality of each machine. Firstly the machine 2 has a larger inter quartile range which means it will produce a less consistent product.

2. **Exercise 1.68:**

(a) For what value of c is the quantity $\sum (x_i - c)^2$ minimized? [Hint: Take the derivative with respect to c, set equal to 0, and solve.]

Answer: Taking the derivative of $f(x) = \sum (x_i - c)^2$, using chain-rule we get

that
$$f'(x) = \sum -2(x_i - c)$$
. Solving at $f'(x) = 0$,

$$0 = \sum_{i=1}^{n} -2(x_i - c)$$

$$0 = -2\sum_{i=1}^{n} (x_i - c)$$

$$0 = -nc + \sum_{i=1}^{n} (x_i)$$

$$nc = \sum_{i=1}^{n} (x_i)$$

$$c = \frac{\sum_{i=1}^{n} (x_i)}{n} = \overline{x}$$

Thus when $c = \overline{x}$, f(x) is minimized.

(b) Using the result of part (a), which of the two quantities $\sum (x_i - \overline{x})^2$ and $\sum (x_i - \mu)^2$ will be smaller than the other (assuming that $\overline{x} \neq \mu$)?

Answer: Recall that $f(x) = \sum (x_i - c)^2$ is minimized when $c = \overline{(x)}$ thus $\sum (x_i - \overline{x})^2$ must be smaller. Furthermore we know that x_i represent our sample, had they represented our population we would say that $\sum (x_i - \mu)^2$ is larger.

3. **Exercise 2.6:**

A college library has five copies of a certain text on reserve. Two copies (1 and 2) are first printings, and the other three (3, 4, and 5) are second printings. A student examines these books in random order, stopping only when a second printing has been selected. One possible outcome is 5, and another is 213.

(a) List the outcomes in S

Answer:

(b) Let A denote the event that exactly one book must be examined. What outcomes are in A?

Answer:

(c) Let *B* be the event that book 5 is the one selected. What outcomes are in *B*? **Answer:**

(d) Let C be the event that book 1 is not examined. What outcomes are in C? **Answer:**

4. **Exercise 2.12:**

Consider randomly selecting a student at a large university, and let A be the event that the selected student has a Visa card and B be the analogous event for Master-Card. Suppose that P(A) = .6 and P(B) = .4.

(a) Could it be the case that $P(A \cap B) = .5$? Why or why not? [Hint: See Exercise 24.]

Answer: It is not the case that that $P(A \cap B) = .5$, since by set theory we know that $P(A \cap B) \le min(P(A), P(B))$.

(b) From now on, suppose that $P(A \cap B) = .3$. What is the probability that the selected student has at least one of these two types of cards?

Answer: Through inclusion exclusion we know that $P(A \cup B) = P(A) + P(B) - P(A \cap B) = .6 + .4 - .3 = .7$.

(c) What is the probability that the selected student has neither type of card?

Answer: Note that $P(\overline{A \cap B}) = 1 - P(A \cup B) = 1 - .7 = .3$.

(d) Describe, in terms of *A* and *B*, the event that the selected student has a Visa card but not a MasterCard, and then calculate the probability of this event.

Answer: The event $P(A \setminus B) = P(A) - P(A \cap B) = .6 - .3 = .3$.

(e) Calculate the probability that the selected student has exactly one of the two types of cards.

Answer: The event $P((A \cup B) - (A \cap B)) = P(A \cup B) - P(A \cap B) = .7 - .3 = .4$.

5. **Exercise 2.16:**

An individual is presented with three different glasses of cola, labeled C, D, and P. He is asked to taste all three and then list them in order of preference. Suppose the same cola has actually been put into all three glasses.

(a) What are the simple events in this ranking experiment, and what probability would you assign to each one?

Answer:

Since its equally likely that the individual produces any of these rankings each event would have a probability of $\frac{1}{6}$

(b) What is the probability that *C* is ranked first?

Answer: the probability that C is ranked first is $\frac{1}{3}$

(c) What is the probability that C is ranked first and D is ranked last?

Answer: the probability that C is ranked first and D is ranked last is $\frac{1}{6}$.

6. **Exercise 2.24:**

Show that if one event A is contained in another event B (i.e., A is a subset of B), then $P(A) \le P(B)$. [Hint: For such A and B, A and $B \cap A'$ are disjoint and $B = A \cup (B \cap A')$, as can be seen from a Venn diagram.] For general A and B, what does this imply about the relationship among $P(A \cap B)$, P(A) and $P(A \cup B)$?

Answer: Recall that if two sets A and B are disjoint then $P(A \cup B) = P(A) + P(B)$. by set theory we know that,

$$P(B) = P(A \cup (B \cap \overline{A}))$$

$$= P(A) + P(B \cap \overline{A})$$

$$\geq P(A)$$

Thus we have shown that if $A \subseteq B$ then $P(B) \ge P(A)$. Furthermore since A is contained in B we know the following, $P(A \cap B) = P(A)$, $P(A \cup B) = P(B)$

7. **Exercise 2.32:**

An electronics store is offering a special price on a complete set of components (receiver, compact disc player, speakers, turntable). A purchaser is offered a choice of manufacturer for each component:

Receiver: Kenwood, Onkyo, Pioneer, Sony, Sherwood **Compact disc player:** Onkyo, Pioneer, Sony, Technics

Speakers: Boston, Infinity, Polk

Turntable: Onkyo, Sony, Teac, Technics

A switchboard display in the store allows a customer to hook together any selection of components (consisting of one of each type). Use the product rules to answer the following questions:

(a) In how many ways can one component of each type be selected?

Answer:

(b) In how many ways can components be selected if both the receiver and the compact disc player are to be Sony?

Answer:

(c) In how many ways can components be selected if none is to be Sony?

Answer:

(d) In how many ways can a selection be made if at least one Sony component is to be included?

Answer:

(e) If someone flips switches on the selection in a completely random fashion, what is the probability that the system selected contains at least one Sony component? Exactly one Sony component?

Answer:

8. **Exercise 2.38:**

A sonnet is a 14-line poem in which certain rhyming patterns are followed. The writer Raymond Queneau published a book containing just 10 sonnets, each on a different page. However, these were structured such that other sonnets could be created as follows: the first line of a sonnet could come from the first line on any of the 10 pages, the second line could come from the second line on any of the 10 pages, and so on (successive lines were perforated for this purpose).

(a) How many sonnets can be created from the 10 in the book?

Answer:

(b) If one of the sonnets counted in part (a) is selected at random, what is the probability that none of its lines came from either the first or the last sonnet in the book?

Answer:

9. **Exercise 2.40:**

Three molecules of type A, three of type B, three of type C, and three of type D are to be linked together to form a chain molecule. One such chain molecule is ABCDABCDABCD, and another is BCDDAAABDBCC.

(a) How many such chain molecules are there? [Hint: If the three A's were distinguishable from one another– A_1 , A_2 , A_3 – and the B's, C's, and D's were also, how many molecules would there be? How is this number reduced when the subscripts are removed from the A's?]

Answer:

(b) Suppose a chain molecule of the type described is randomly selected. What is the probability that all three molecules of each type end up next to one another (such as in *BBBAAADDDCCC*)?

Answer:

10. **Exercise 2.52:**

A system consists of two identical pumps, #1 and #2. If one pump fails, the system will still operate. However, because of the added strain, the remaining pump is now more likely to fail than was originally the case. That is, r = P(#2 fails|#1 fails) > P(#2 fails) = q. If at least one pump fails by the end of the pump design life in 7% of all systems and both pumps fail during that period in only 1%, what is the probability that pump #1 will fail during the pump design life?

Answer:

11. **Exercise 2.60:**

Seventy percent of the light aircraft that disappear while in flight in a certain country

are subsequently discovered. Of the aircraft that are discovered, 60% have an emergency locator, whereas 90% of the aircraft not discovered do not have such a locator. Suppose a light aircraft has disappeared.

(a) If it has an emergency locator, what is the probability that it will not be discovered?

Answer:

(b) If it does not have an emergency locator, what is the probability that it will be discovered?

Answer: