

Uncertainty:

1. Find Δx for the following equation.

$$x = \frac{2M_{p+b}}{m_b} \sqrt{y \Delta h}$$

- First find partial derivative for every variable.

$$\frac{\partial x}{\partial y} = \frac{M_{p+b}}{m_b} (\Delta h)^{1/2} (y)^{-1/2}$$

$$\frac{\partial x}{\partial M_{p+b}} = \frac{2}{m_b} (\Delta h)^{1/2} (y)^{-1/2}$$

$$\frac{\partial x}{\partial \Delta h} = \frac{M_{p+b}}{m_b} (\Delta h)^{-1/2} (y)^{1/2}$$

$$\frac{\partial x}{\partial m_b} = -\frac{2 M_{p+b}}{m_b^2} (\Delta h)^{1/2} (y)^{1/2}$$

- Apply uncertainty formulae.

$$\Delta x = \left(\left(\frac{\partial x}{\partial y} y \right)^2 + \left(\frac{\partial x}{\partial \Delta h} \Delta h \right)^2 + \left(\frac{\partial x}{\partial M_{p+b}} M_{p+b} \right)^2 + \left(\frac{\partial x}{\partial m_b} m_b \right)^2 \right)^{1/2}$$

2. Find δL for the following equation.
with L_w having negligible uncertainty.

$$L_f = \frac{c_w m_h + c_d}{m_{ice}} (T_h - T_f) + c_w (T_{ice} - T_f)$$

- Find the necessary partial derivatives.

$$\frac{\partial L}{\partial m_h} = \frac{L_w + L_d}{m_{ice}} (T_h - T_f)$$

$$\frac{\partial L}{\partial m_{ice}} = - \frac{L_w m_h + L_d}{m_{ice}^2} (T_h - T_f)$$

$$\frac{\partial L}{\partial L_d} = \frac{L_w m_h + L_d}{m_{ice}} (T_h - T_f)$$

$$\frac{\partial L}{\partial T_h} = \frac{L_w m_h + L_d}{m_{ice}}$$

$$\frac{\partial L}{\partial T_f} = - \frac{L_w m_h + L_d}{m_{ice}} - L_w$$

$$\frac{\partial L}{\partial T_{ice}} = L_w$$

- Apply uncertainty formulae.

$$\begin{aligned} \delta L = & \left(\left(\frac{\partial L}{\partial m_h} m_h \right)^2 + \left(\frac{\partial L}{\partial L_d} L_d \right)^2 + \left(\frac{\partial L}{\partial T_f} T_f \right)^2 + \left(\frac{\partial L}{\partial m_{ice}} m_{ice} \right)^2 \right. \\ & \left. + \left(\frac{\partial L}{\partial T_h} T_h \right)^2 + \left(\frac{\partial L}{\partial T_{ice}} T_{ice} \right)^2 \right)^{1/2} \end{aligned}$$

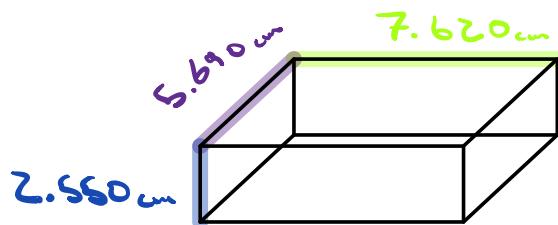
Part 2: Calipers.

3. Measure the outer dimensions of the 1-2-3 block with calipers.

Measurements:

Note that for all measurements

$$\Delta x = .0005 \text{ cm.}$$



4. Convert your measurements and uncertainty to inches and compare to the expected values.

	Measured	Converted	Expected
Length	7.620 cm	3.000 in	3 in
Width	5.690 cm	2.240 in	2 in
Height	2.550 cm	1.003 in	1 in
Δx	.0005 cm	.00019 in	.0002 in

Just from looking at the ruler both the length and height fit inside the tower. However the width doesn't at all.

Percent error calculation for width

$$12\% = \frac{|2.240 - 2.000|}{2.000} \cdot 100$$

Part 3: DMM

5.) Measure the voltages of the batteries and compare it to the accepted values.

	Measured Values	Accepted Values
Large Battery	4.47 Volts	6 Volts
Small Battery	1.36 Volts	1.5 Volts
Δx	.05 Volts	

With our given tolerance of .05 Volts neither battery reached the accepted value. The batteries are dead.

6.) Measure each resistor. Are the measurements within the tolerance of the accepted value.

Resistor #1	Measured	Accepted
	$4.12 \times 10^3 \Omega$ $\pm .05 \times 10^3 \Omega$	4.700Ω $\pm 470 \Omega$
Resistor #2		
	200Ω $\pm .05 \Omega$	220Ω $\pm 22 \Omega$
Resistor #3		
	$2.36 \times 10^6 \Omega$ $\pm .05 \times 10^6 \Omega$	$2,200,000 \Omega$ $\pm 220,000 \Omega$

At a quick glance we can see that resistors 2 and 3 fall within the manufacturer's tolerance. However resistor 1 does not fall into the manufacturing tolerance.

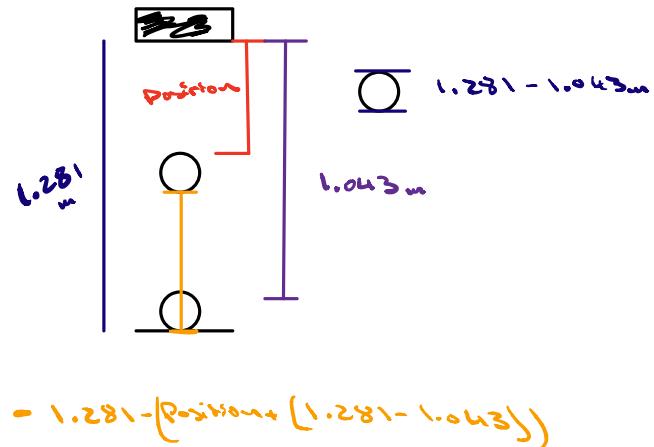
$$12.3\% = \frac{|4720 - 4700|}{4700} \cdot 100$$

Part 4: Lab Quest + Basketball.

7. Measure the mass of the basketball.

$$\text{Mass of B-ball} = 589.70 \text{ g} \pm .05 \text{ g}$$

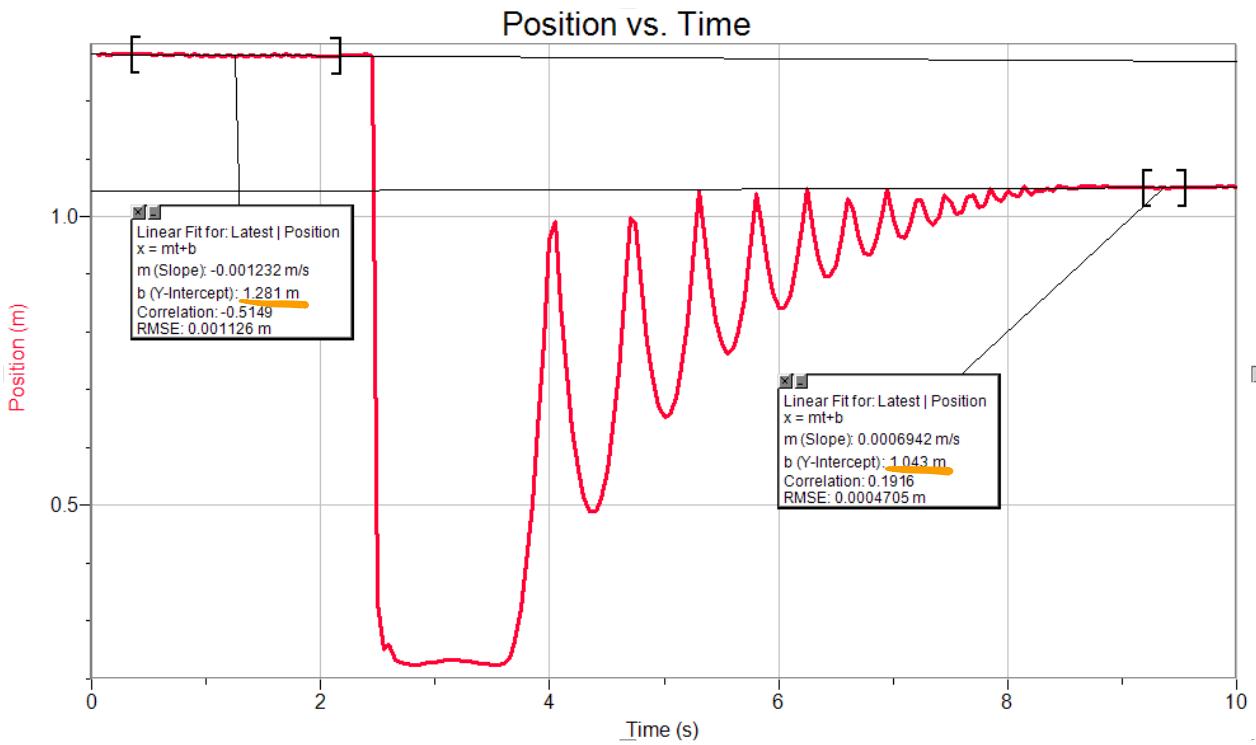
8. Experiment Results.



First note that the experiment data for positions results in a non-zero potential energy at the end of the experiment.
 $-1.281 - (\text{Position} - (1.281 - 1.043))$

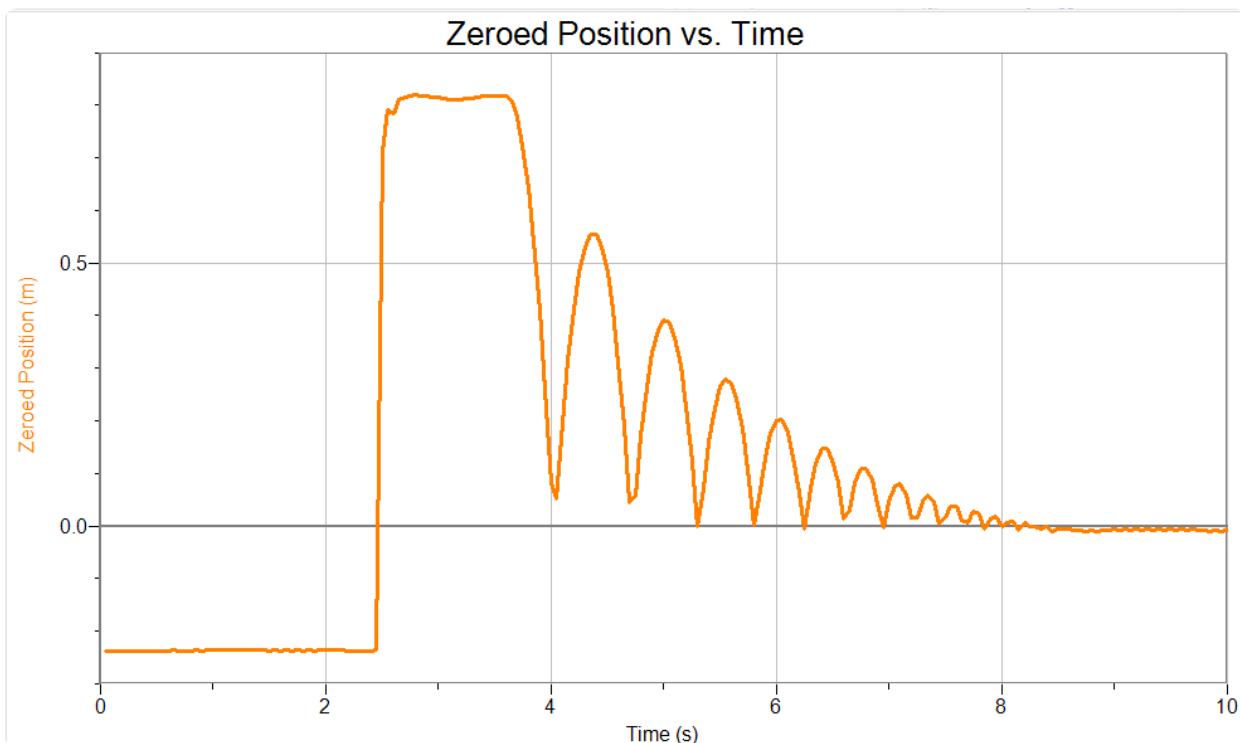
We measured Position, however we want the **orange Position** in order to zero the potential energy.

The following is the **Position vs time** data, using linear fit data to find the values needed to find **Zeroed Position**.

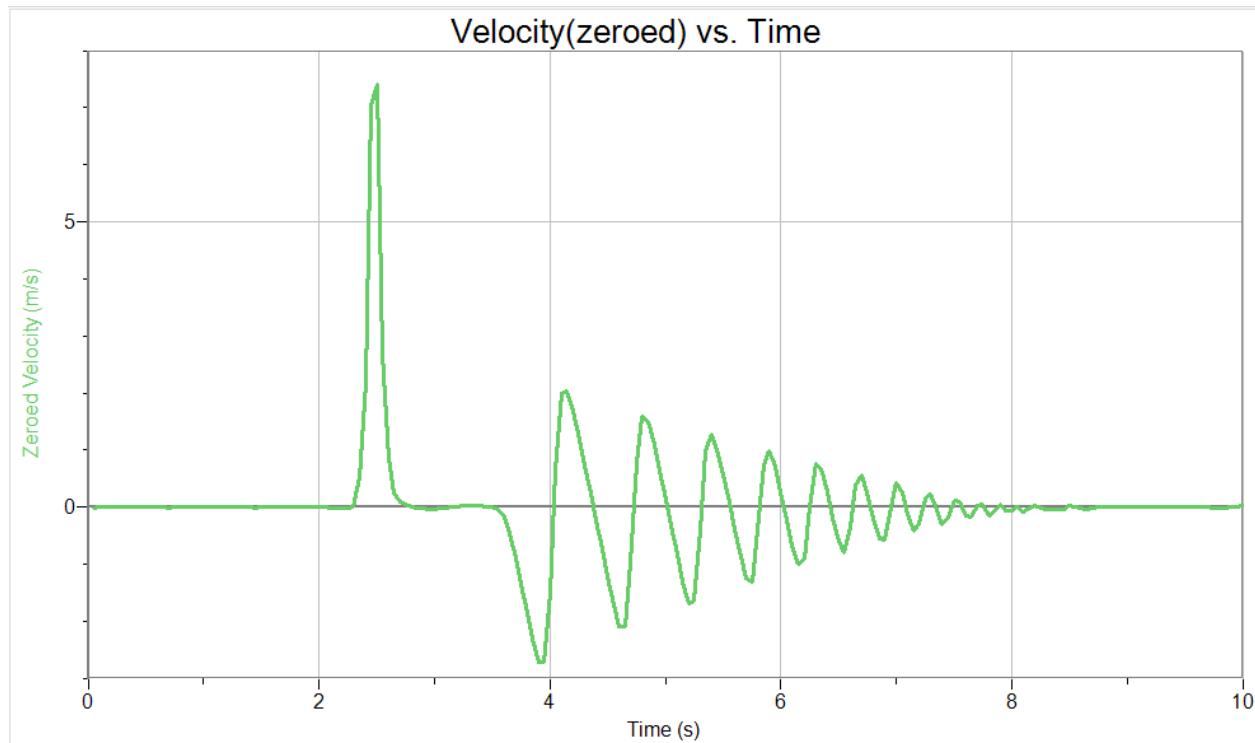


Using these values and the diagram shown above to calculate.

$$\text{Zeroed Position} = 1.281 - (\text{Position} \times (1.281 - 1.043))$$



Calculating the velocity by differentiating
the zeroed position.

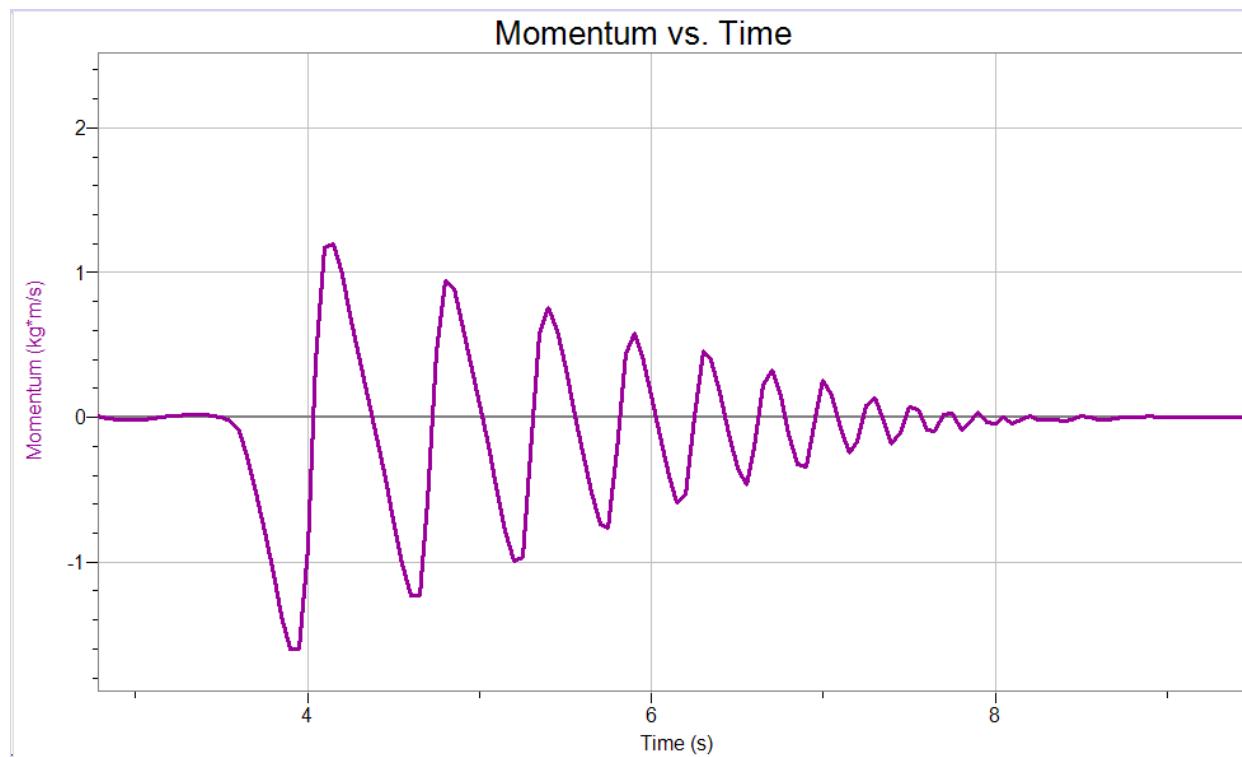
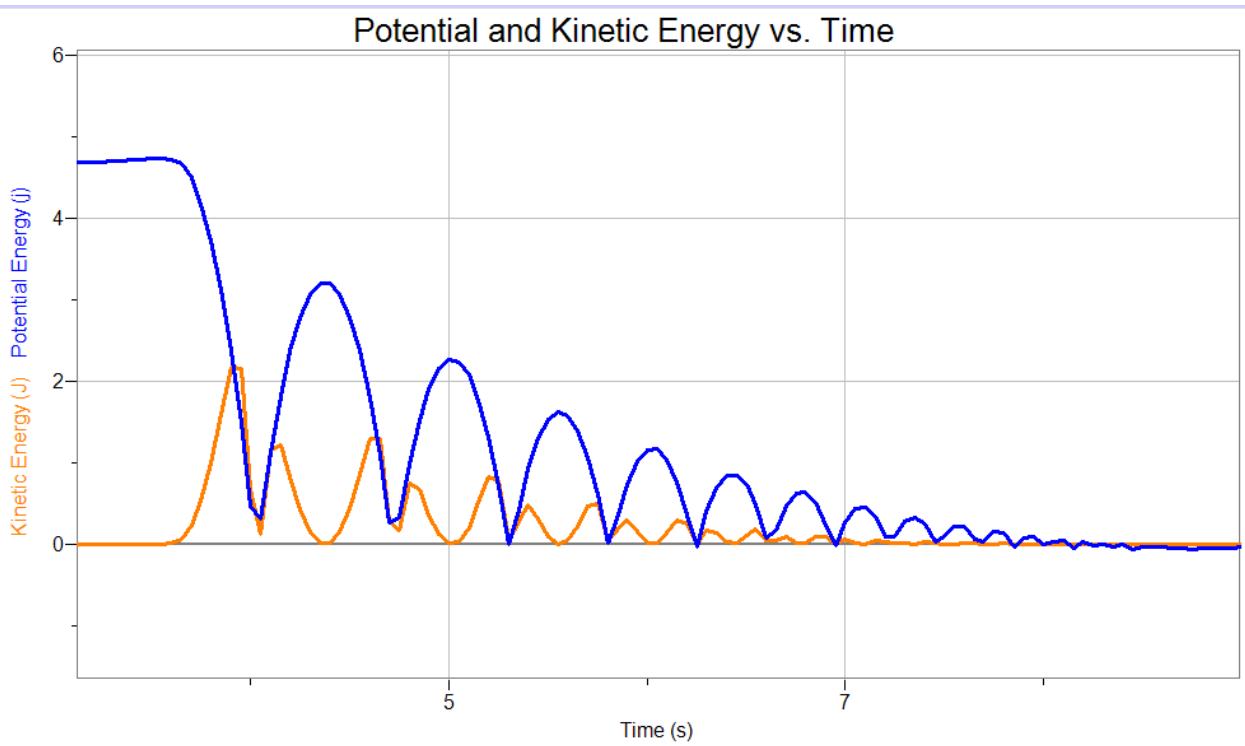


Finally with our velocity and position
we can calculate Potential energy, Kinetic
energy and momentum.

$$KE = \frac{1}{2}mv^2,$$

$$PE = mgh,$$

$$\text{Momentum} = mv.$$



Discussion:

The energy graph is exactly what we should expect. We see PE achieve a maximum where KE is a minimum. Slowly the total energy is decreasing since energy

is being lost on the board. The momentum
is also exactly what we should expect given
the power law nature of the velocity.