



*Conservatorio di Musica Alfredo Casella*  
*Istituto Superiore di Studi Musicali*

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**BIENNIO DI II LIVELLO IN NUOVE TECNOLOGIE E LINGUAGGI MUSICALI**  
**MUSICA ELETTRONICA**

**INDIRIZZO REGIA E TECNOLOGIA DEL SUONO**

**Vowel phonemes Analysis & Classification**  
**by means of**  
***OCN rectifiers* Deep Learning Architectures**

**Appendix A**  
Python code

RELATORE

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## REPOSITORIES

### **Google Drive** (*temporary repository*)

Vowel phonemes Analysis & Classification by means of OCON Deep Learning Architectures

[https://drive.google.com/drive/folders/1QNY3n0IT1dNtwUUJ0We-vCC64Gm5kXuN?usp=drive link](https://drive.google.com/drive/folders/1QNY3n0IT1dNtwUUJ0We-vCC64Gm5kXuN?usp=drive_link)

### **GitHub** (*permanent repository*)

Vowel phonemes Analysis & Classification by means of OCON Deep Learning Architectures

[https://github.com/StefanoGiacomelli/Vowel\\_phonemes\\_Analysis\\_and\\_Classification\\_by\\_means\\_of\\_OCON\\_rectifiers\\_Deep\\_Learning\\_Architectures](https://github.com/StefanoGiacomelli/Vowel_phonemes_Analysis_and_Classification_by_means_of_OCON_rectifiers_Deep_Learning_Architectures)

### **GitLab**

ASAP repository

<https://gitlab.com/stefano.giacomelli/asap/>

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## GOOGLE COLAB NOTEBOOKS LIST

*Vowel phonemes Analysis & Classification by means of OCON Deep Learning Architectures*

### **Preliminary Analysis**

- *HGCW\_Dataset\_Analysis.ipynb*
- *One-Class\_Sub-Network\_Analysis.ipynb*

### **Phoneme Recognition**

- *1\_OCON\_Model\_Analysis\_(3\_features\_all\_speakers).ipynb*
- *2\_OCON\_Model\_Analysis\_(4\_features\_all\_speakers).ipynb*
- *3\_OCON\_Model\_Analysis\_(3\_features\_no-children).ipynb*
- *4\_OCON\_Model\_Analysis\_(12\_features\_all\_speakers).ipynb*

### **Speaker Recognition**

- *5\_OCON\_Model\_Analysis\_(13\_features\_all\_speakers)\_Speaker\_Recognition.ipynb*



## ▼ Dataset Analysis & Pre-Processing

**Author:** S. Giacomelli

**Year:** 2023

**Affiliation:** A.Casella Conservatory (student)

**Master Degree Thesis:** "Vowel phonemes Analysis & Classification by means of OCON rectifiers Deep Learning Architectures"

**Description:** Python scripts for HGCW Dataset analysis, features extraction and pre-processing

```
# Numerical computations packages/modules
import numpy as np

# Graphic visualization modules
import matplotlib.pyplot as plt
import matplotlib_inline
matplotlib_inline.backend_inline.set_matplotlib_formats('svg')

# Common Seed initialization
SEED = 42 # ... the answer to the ultimate question of Life, the Universe, and Everything... (cit.)
```

## ▼ HGCW (Hillenbrand-Getty-Clark-Wheeler) Dataset

Download link: ["Vowel Data" - Western Michigan University](#) (...no longer maintained)

### References

1. L.A. Getty, 1990 - [Acoustic Characteristics of Vowels Produced by Men, Women and and Children](#), Master Degree Thesis, Western Michigan University
2. J. Hillenbrand, R.T. Gayvert, 1993 - [Vowel Classification Based on Fundamental Frequency and Formant Frequencies](#), in Journal of Speech and Hearing Research, vol. 36, pp. 694 - 700
3. J. Hillenbrand, L.A. Getty, M.J. Clark, K. Wheeler, 1995 - [Acoustic characteristics of American English vowels](#), in The Journal of the Acoustical Society of America, 97, pp. 3099 - 3111

### Filenames Structure

1	2-3	4-5	Example
m = man	nn = speaker n° (50 each)	xx = vocal label	m10ae
b = boy	nn = speaker n° (29 each)	xx = vocal label	b11ei
w = woman	nn = speaker n° (50 each)	xx = vocal label	w49ih
g = girl	nn = speaker n° (21 each)	xx = vocal label	g20oo

### Audio files features:

- Duration: 1 sec.
- Sample Rate: 16 KHz
- Resolution depth: 16 bit
- File extension: .wav (*wave audio*)

### Analysis File Structure

```
***Formant_Fine_Sampling.csv" Columns**
0) filename
1) duration (in ms)
2) "f0" (fundamental frequency) at steady state
3) "F1" (1st formant frequency) at steady state
4) "F2" (2nd formant frequency) at steady state
5) "F3" (3rd formant frequency) at steady state
6) "F1" at 10% of vowel utterance duration
7) "F2" at 10% of vowel utterance duration
8) "F3" at 10% of vowel utterance duration
18) "F1" at 50% of vowel utterance duration
19) "F2" at 50% of vowel utterance duration
20) "F3" at 50% of vowel utterance duration
27) "F1" at 80% of vowel utterance duration
28) "F2" at 80% of vowel utterance duration
29) "F3" at 80% of vowel utterance duration
```

**IMP:** *Os feature values = formant analysis errors*

...for more information (steady state times etc.) see "*Time\_Measurements.dat*" and "*Descriptive\_Statistics.dat*".

```
# Database (.DAT file) Features Reading (converted to NumPy array)
formant_analysis_data = np.loadtxt("./HGCW_LPC_formants_fine.dat", usecols=(2, 3, 4, 5))
formant_analysis_filenames = np.loadtxt("./HGCW_LPC_formants_fine.dat", usecols=0, dtype=str)

# Useful Parameters
vowels = ['ae', 'ah', 'aw', 'eh', 'er', 'ei', 'ih', 'iy', 'oa', 'oo', 'uh', 'uw'] # Vowels list
colors = ['red', 'saddlebrown', 'darkorange', 'darkgoldenrod', 'gold', 'darkkhaki', 'olive', 'darkgreen', 'steelblue', 'fuchsia']
speakers = ['m', 'b', 'w', 'g'] # Speakers list
print(f"Dataset: {formant_analysis_data.shape[0]} samples (for {len(vowels)} labels) & {formant_analysis_data.shape[1]} features")
```

## ▼ Filtering Functions

- Speaker-based dataset filtering
- Vowel-based dataset filtering
- Null elements dataset filtering

```
# Speaker filter
def speaker_filter(data_array, filenames_array, speaker: str = 'm'):
    """
    Return a list of indices and a filtered data array for a defined speaker string
    """
    assert len(data_array) == len(filenames_array)
    indices = []

    for i in range(len(filenames_array)): # For each filename...
        if filenames_array[i].lower()[0] == speaker:
            indices.append(i) # If filename contains speaker sub-string, append actual index to indices array

    return data_array[indices], indices

# -----

# Vowels filter
def vowel_filter(data_array, filenames_array, vowel: str = 'ae'):
    """
    Return a list of indices and a filtered data array for a defined vowel string
    """
    assert len(data_array) == len(filenames_array)
    indices = []

    for i in range(len(filenames_array)): # For each filename...
        if vowel in filenames_array[i].lower()[3:]:
            indices.append(i) # If filename contains vowel sub-string, append actual index to indices array

    return data_array[indices], indices

# -----

# Null elements filter
def null_filter(data_array, filenames_array):
    """
    Return a list of "null-elements" indices and a filtered data and labels array, without null elements
    """
    assert len(data_array) == len(filenames_array)
    null_indices = []

    for i in range(len(filenames_array)): # For each filename...
        for j in range(data_array.shape[1]): # For each feature column...
            if (data_array[i, j] == 0): # If any formant frequency is null...
                null_indices.append(i) # Append actual index to indices array

    filtered_filenames = np.delete(filenames_array, null_indices, axis=0) # Create output deleting null indices from filename
    filtered_data = np.delete(data_array, null_indices, axis=0) # Create output deleting null indices from data array

    return filtered_data, filtered_filenames, null_indices

# Remove Null elements
nonnull_data, nonnull_filenames, _ = null_filter(formant_analysis_data, formant_analysis_filenames)
print(f"NON NULL Dataset: {nonnull_data.shape[0]} samples (for {len(vowels)} labels) & {nonnull_data.shape[1]} features each")
print('-----')
print()

# Outputs initialization
x_data_raw_np = np.zeros((len(nonnull_data), 4), dtype=float) # Same Database n° of elements, 4 float features (columns)
y_labels_raw_np = np.zeros((len(nonnull_data), 1), dtype=int) # Same Database n° of elements, integer label single column array
```

```

# Subgroups extraction & analysis
end_idx = [0] # Indices list initialization (0 and size values comprised)
vow_size = [] # Vowel groups size list initialization

for vowel_idx, vowel in enumerate(vowels):
    vow_data, _ = vowel_filter(nonnull_data, nonnull_filenames, vowel=vowel) # Vowel sub-set extraction
    end_idx.append(end_idx[vowel_idx] + len(vow_data)) # Actual sub-group End-Index appending
    vow_size.append(len(vow_data)) # Actual sub-group length appending
    print(f'Vowel "{vowel}" sub-set : {len(vow_data)} samples')

    start_idx = end_idx[vowel_idx] # Previous sub-set end-index
    print('1st element Idx :', start_idx)
    stop_idx = end_idx[vowel_idx] + len(vow_data) # Actual stop index = previous End + actual Size
    print('Last element Idx :', stop_idx - 1)
    x_data_raw_np[start_idx: stop_idx, :] = vow_data[:, :] # Output data sub-set ordered writing (Fundamental, 1st, 2nd & 3r

    vow_labels = np.full((len(vow_data), 1), vowel_idx, dtype=int) # Actual integer labels array creation
    print(f'Vowel LABEL : {vowel} - {vowel_idx}')
    y_labels_raw_np[start_idx: stop_idx, :] = vow_labels # Output labels sub-set ordered writing

    print('-----')

# Different labels counter
diff_labels = len(np.unique(y_labels_raw_np))

print()
print(f'--> RAW DATASET shape: {x_data_raw_np.shape}, w. {diff_labels} Labels')

# Raw Dataset Plot
plt.figure(figsize=(12, 15))
plt.suptitle('Dataset "2-Features" separation')

for index, vowel in enumerate(vowels):

    first_coords = x_data_raw_np[end_idx[index]: end_idx[index + 1], 1]
    second_coords = x_data_raw_np[end_idx[index]: end_idx[index + 1], 2]
    third_coords = x_data_raw_np[end_idx[index]: end_idx[index + 1], 3]

    plt.subplot(3, 1, 1)
    plt.title('$1_{st}$ VS $2_{nd}$')
    plt.scatter(first_coords, second_coords, marker='o', color=colors[index], label=f'Vowel "{vowel}"')
    plt.xlabel('$1_{st}$ Formant Frequency (in Hz)')
    plt.ylabel('$2_{nd}$ Formant Frequency (in Hz)')
    plt.legend(loc='best')
    plt.grid(True)

    plt.subplot(3, 1, 2)
    plt.title('$1_{st}$ VS $3_{rd}$')
    plt.scatter(first_coords, third_coords, marker='o', color=colors[index], label=f'Vowel "{vowel}"')
    plt.xlabel('$1_{st}$ Formant Frequency (in Hz)')
    plt.ylabel('$3_{rd}$ Formant Frequency (in Hz)')
    plt.legend(loc='best')
    plt.grid(True)

    plt.subplot(3, 1, 3)
    plt.title('$2_{nd}$ VS $3_{rd}$')
    plt.scatter(second_coords, third_coords, marker='o', color=colors[index], label=f'Vowel "{vowel}"')
    plt.xlabel('$2_{nd}$ Formant Frequency (in Hz)')
    plt.ylabel('$3_{rd}$ Formant Frequency (in Hz)')
    plt.legend(loc='best')
    plt.grid(True)

plt.tight_layout()
plt.savefig("raw_dataset_plot")
plt.show()

# Class Occurences Plot (Sample Balancing Analysis)
plt.figure(figsize=(12, 5))
plt.suptitle("Dataset Samples Balance")

for i in range(len(colors)):
    plt.bar(i, vow_size[i], color=colors[i])
    plt.xlabel('Vowels')
    plt.ylabel('Samples')

plt.xticks(ticks=[n for n in range(12)], labels=vowels)

plt.axhline(np.min(vow_size), color='grey', linestyle='--', label=f'Min: {np.min(vow_size)} samples')
plt.axhline(np.max(vow_size), color='red', linestyle='--', label=f'Max: {np.max(vow_size)} samples')
plt.legend(loc='best')
plt.grid()

```

```
plt.savefig('dataset_class_occurences')
plt.show()
```

## ▼ "Formant to Fundamental" Normalization

Formant frequency ratio

$$formant_{ratio(i)} = \frac{freq_{formant(i)}}{freq_{fund}}$$

```
# Fundamental Frequency (ratio) Normalization
x_data_fund_norm = np.zeros(x_data_raw_np.shape) # Output initialization

for i in range(x_data_raw_np.shape[1]): # For each feature...
    if i >= 1: # For each formant column...
        x_data_fund_norm[:, i] = x_data_raw_np[:, i] / x_data_raw_np[:, 0] # i-Formant value / i-Fundamental value
    else: # Exception for Fundamental freq column
        x_data_fund_norm[:, i] = x_data_raw_np[:, i]

print(f'Fundamental Normalized' Dataset: {x_data_fund_norm.shape[0]} elements (w. {diff_labels} labels) & {x_data_fund_norm.s

# Fundamental Normalized dataset Plot
plt.figure(figsize=(12, 15))
plt.suptitle('Raw VS Normalized Datasets\n')

for index, vowel in enumerate(vowels):

    first_coords = x_data_fund_norm[end_idx[index]: end_idx[index + 1], 1]
    second_coords = x_data_fund_norm[end_idx[index]: end_idx[index + 1], 2]
    third_coords = x_data_fund_norm[end_idx[index]: end_idx[index + 1], 3]

    plt.subplot(3, 2, 2)
    plt.title('Fund. Normalized $1_{st}$ VS $2_{nd}$')
    plt.scatter(first_coords, second_coords, marker='o', color=colors[index], label=f'Vowel "{vowel}"')
    plt.xlabel('$1_{st}$ Formant Ratio')
    plt.ylabel('$2_{nd}$ Formant Ratio')
    plt.legend(loc='best')
    plt.grid(True)

    plt.subplot(3, 2, 4)
    plt.title('Fund. Normalized $1_{st}$ VS $3_{rd}$')
    plt.scatter(first_coords, third_coords, marker='o', color=colors[index], label=f'Vowel "{vowel}"')
    plt.xlabel('$1_{st}$ Formant Ratio')
    plt.ylabel('$3_{rd}$ Formant Ratio')
    plt.legend(loc='best')
    plt.grid(True)

    plt.subplot(3, 2, 6)
    plt.title('Fund. Normalized $2_{nd}$ VS $3_{rd}$')
    plt.scatter(second_coords, third_coords, marker='o', color=colors[index], label=f'Vowel "{vowel}"')
    plt.xlabel('$2_{nd}$ Formant Ratio')
    plt.ylabel('$3_{rd}$ FFormant Ratio')
    plt.legend(loc='best')
    plt.grid(True)

for index, vowel in enumerate(vowels):

    first_coords = x_data_raw_np[end_idx[index]: end_idx[index + 1], 1]
    second_coords = x_data_raw_np[end_idx[index]: end_idx[index + 1], 2]
    third_coords = x_data_raw_np[end_idx[index]: end_idx[index + 1], 3]

    plt.subplot(3, 2, 1)
    plt.title('Raw $1_{st}$ VS $2_{nd}$')
    plt.scatter(first_coords, second_coords, marker='o', color=colors[index], label=f'Vowel "{vowel}"')
    plt.xlabel('$1_{st}$ Formant Frequency (in Hz)')
    plt.ylabel('$2_{nd}$ Formant Frequency (in Hz)')
    plt.legend(loc='best')
    plt.grid(True)

    plt.subplot(3, 2, 3)
    plt.title('Raw $1_{st}$ VS $3_{rd}$')
    plt.scatter(first_coords, third_coords, marker='o', color=colors[index], label=f'Vowel "{vowel}"')
    plt.xlabel('$1_{st}$ Formant Frequency (in Hz)')
    plt.ylabel('$3_{rd}$ Formant Frequency (in Hz)')
    plt.legend(loc='best')
    plt.grid(True)

    plt.subplot(3, 2, 5)
    plt.title('Raw $2_{nd}$ VS $3_{rd}$')
```



```
plt.scatter(second_coords, third_coords, marker='o', color=colors[index], label=f'Vowel "{vowel}"')
plt.xlabel('$2_{nd}$ Formant Frequency (in Hz)')
plt.ylabel('$3_{rd}$ Formant Frequency (in Hz)')
plt.legend(loc='best')
plt.grid(True)

plt.tight_layout()
plt.savefig("raw_vs_fund_norm_datasets_plot")
plt.show()
```

## ▼ Min-Max Scaling

$$\hat{x} = \frac{x_i - \min(x)}{\max(x) - \min(x)}$$

and eventually

$$x^* = a + \hat{x}(b - a)$$

with  $a$  &  $b$  respectively, lower and upper bounds of the destination range.

**IMP:** in this case Min-Max scaling is commonly applied to entire features space (*are measured on the same axis and represents samples of same spectral domain properties*)

```
a = 0. # Lower bound
b = 1. # Upper bound
x_data_minmax = np.zeros((x_data_fund_norm.shape))
print(f'Fundamental Ratios STATS: Min. = {x_data_fund_norm[:, 1:].min()} Max. = {x_data_fund_norm[:, 1:].max()}')

x_data_minmax[:, 1:] = a + ((x_data_fund_norm[:, 1:] - x_data_fund_norm[:, 1:].min()) / (x_data_fund_norm[:, 1:].max() - x_data_fund_norm[:, 1:].min()))
x_data_minmax[:, 0] = x_data_fund_norm[:, 0] # Fundamental column exception

print(f'Min-Max Ratios STATS: Min. = {x_data_minmax[:, 1:].min()} Max. = {x_data_minmax[:, 1:].max()}')
print('-----')
print(f'"Fundamental & Min-Max Normalized" Dataset: {x_data_minmax.shape[0]} elements (w. {diff_labels} labels) & {x_data_minmax.shape[0]} elements (w. {diff_labels} labels)')
print('-----')
```

## ▼ Statistical Analysis

- Features **Probability Mass Distribution** (on the entire Dataset)
- Features **Probability Mass Distribution** (for each class sub-set)

```
# Dataset Plot
dataset = x_data_minmax # x_data_fund_norm

plt.figure(figsize=(12, 15))
plt.suptitle('Normalized Dataset "2-Features" separation')

for index, vowel in enumerate(vowels):

    first_coords = dataset[end_idx[index]: end_idx[index + 1], 1]
    second_coords = dataset[end_idx[index]: end_idx[index + 1], 2]
    third_coords = dataset[end_idx[index]: end_idx[index + 1], 3]

    plt.subplot(3, 1, 1)
    plt.title('$1_{st}$ VS $2_{nd}$')
    plt.scatter(first_coords, second_coords, marker='o', color=colors[index], label=f'Vowel "{vowel}"')
    plt.xlabel('$1_{st}$ Formant Frequency ratio')
    plt.ylabel('$2_{nd}$ Formant Frequency ratio')
    plt.legend(loc='best')
    plt.grid(True)

    plt.subplot(3, 1, 2)
    plt.title('$1_{st}$ VS $3_{rd}$')
    plt.scatter(first_coords, third_coords, marker='o', color=colors[index], label=f'Vowel "{vowel}"')
    plt.xlabel('$1_{st}$ Formant Frequency ratio')
    plt.ylabel('$3_{rd}$ Formant Frequency ratio')
    plt.legend(loc='best')
    plt.grid(True)

    plt.subplot(3, 1, 3)
    plt.title('$2_{nd}$ VS $3_{rd}$')
    plt.scatter(second_coords, third_coords, marker='o', color=colors[index], label=f'Vowel "{vowel}"')
    plt.xlabel('$2_{nd}$ Formant Frequency ratio')
    plt.ylabel('$3_{rd}$ Formant Frequency ratio')
    plt.legend(loc='best')
    plt.grid(True)

plt.tight_layout()
plt.savefig("normalized_dataset_plot")
```

```
plt.show()

# Formants Probability Distribution plot
plt.figure(figsize=(12, 5))
plt.suptitle('Features Probability Mass Distribution\n(entire Dataset)')

for i in range(dataset.shape[1] - 1):
    plt.subplot(1, 3, i + 1)
    plt.hist(dataset[:, i + 1], bins=30, rwidth=0.9)
    plt.title(f'PMD $Formant_{i + 1}$ ratio')
    plt.xlabel('Normalized Formant Ratio')
    plt.ylabel('Frequency (occurrences)')
    plt.ylim([0, 350])
    plt.grid()

plt.tight_layout()
plt.savefig("normalized_dataset_stats")
plt.show()
```

Examining features data distribution (per class), we evaluate *Z-Scoring* (standardization) usefulness/availability.

```
# Probability distribution (for each feature, in each class)
plt.figure(figsize=(12, 50))

for i in range(len(vowels)):
    vow_group = dataset[end_idx[i]: end_idx[i + 1], :] # Vowel group Extraction
    for n in range(vow_group.shape[1] - 1):
        plt.subplot(12, 3, (n + 1) + i * 3)
        plt.hist(vow_group[:, n + 1], bins=30, rwidth=0.9, color=colors[i])
        plt.title(f"{vowels[i]} Group, $Formant_{n + 1}$ ratio")
        plt.xlabel('Normalized Formant Ratio')
        plt.ylabel('Frequency')
        plt.ylim([0, 50])
        plt.grid()

plt.tight_layout()
plt.savefig('normalized_dataset_stats_(per_class)')
plt.show()
```

## ▼ OUTPUT Datasets

Reference: [NPZ - NumPy Binary File Compression](#)

```
# HGCW Dataset: 3 Formants (steady state) + Fundamental Normalization + MinMax Scaling
classes_size = np.array(vow_size) # Phoneme classes sizes array
classes_indices = np.array(end_idx) # Phoneme classes indices (start/end included)
np.savez_compressed(file='./HGCW_dataset_utils',
                    HGCW_raw = x_data_raw_np,
                    HGCW_fund_norm = x_data_fund_norm,
                    HGCW_minmax = x_data_minmax,
                    HGCW_labels = y_labels_raw_np,
                    classes_size = classes_size,
                    classes_idx = classes_indices)

# HGCW MEN Dataset: 3 Formants (steady state) + Fundamental Normalization + MinMax Scaling
import numpy as np

# Database (.DAT file) Features Reading (converted to NumPy array)
formant_analysis_data = np.loadtxt("./HGCW_LPC_formants_fine.dat", usecols=(2, 3, 4, 5))
formant_analysis_filenames = np.loadtxt("./HGCW_LPC_formants_fine.dat", usecols=0, dtype=str)

# Useful Parameters
vowels = ['ae', 'ah', 'aw', 'eh', 'er', 'ei', 'ih', 'iy', 'oa', 'oo', 'uh', 'uw'] # Vowels list
speakers = ['m', 'b', 'w', 'g'] # Speakers list
print(f"Dataset: {formant_analysis_data.shape[0]} samples (for {len(vowels)} labels) & {formant_analysis_data.shape[1]} featur
# -----

# Gender Filtering (Male)
male_data, male_indices = speaker_filter(formant_analysis_data, formant_analysis_filenames, speaker = 'm')
male_filenames = formant_analysis_filenames[male_indices]

# Remove Null elements
nonnull_data, nonnull_filenames, _ = null_filter(male_data, male_filenames)
print(f"NON NULL Dataset: {nonnull_data.shape[0]} samples (for {len(vowels)} labels) & {nonnull_data.shape[1]} features each")
print('-----')
print()

# Outputs initialization
```

```

x_data_raw_np = np.zeros((len(nonnull_data), 4), dtype=float) # Same Database n° of elements, 4 float features (columns)
y_labels_raw_np = np.zeros((len(nonnull_data), 1), dtype=int) # Same Database n° of elements, integer label single column arr

# Subgroups extraction & analysis
end_idx = [0] # Indices list initialization (0 and size values comprised)
vow_size = [] # Vowel groups size list initialization

for vowel_idx, vowel in enumerate(vowels):
    vow_data, _ = vowel_filter(nonnull_data, nonnull_filenames, vowel=vowel) # Vowel sub-set extraction
    end_idx.append(end_idx[vowel_idx] + len(vow_data)) # Actual sub-group End-Index appending
    vow_size.append(len(vow_data)) # Actual sub-group length appending
    print(f'Vowel "{vowel}" sub-set : {len(vow_data)} samples')

    start_idx = end_idx[vowel_idx] # Previous sub-set end-index
    print('1st element Idx :', start_idx)
    stop_idx = end_idx[vowel_idx] + len(vow_data) # Actual stop index = previous End + actual Size
    print('Last element Idx :', stop_idx - 1)
    x_data_raw_np[start_idx: stop_idx, :] = vow_data[:, :] # Output data sub-set ordered writing (Fundamental, 1st, 2nd & 3r

    vow_labels = np.full((len(vow_data), 1), vowel_idx, dtype=int) # Actual integer labels array creation
    print(f'Vowel LABEL : {vowel} - {vowel_idx}')
    y_labels_raw_np[start_idx: stop_idx, :] = vow_labels # Output labels sub-set ordered writing

    print('-----')

# Different labels counter
diff_labels = len(np.unique(y_labels_raw_np))
print()
print(f'--> RAW DATASET shape: {x_data_raw_np.shape}, w. {diff_labels} Labels')
print('-----')
# -----

# Fundamental Frequency (ratio) Normalization
x_data_fund_norm = np.zeros(x_data_raw_np.shape) # Output initialization

for i in range(x_data_raw_np.shape[1]): # For each feature...
    if i >= 1: # For each formant column...
        x_data_fund_norm[:, i] = x_data_raw_np[:, i] / x_data_raw_np[:, 0] # i-Formant value / i-Fundamental value
    else: # Exception for Fundamental freq column
        x_data_fund_norm[:, i] = x_data_raw_np[:, i]

print(f'"Fundamental Normalized" Dataset: {x_data_fund_norm.shape[0]} elements (w. {diff_labels} labels) & {x_data_fund_norm.s
print('-----')
# -----

a = 0. # Lower bound
b = 1. # Upper bound
x_data_minmax = np.zeros((x_data_fund_norm.shape))
print(f'Fundamental Ratios STATS: Min. = {x_data_fund_norm[:, 1:].min()} Max. = {x_data_fund_norm[:, 1:].max()}')

x_data_minmax[:, 1:] = a + ((x_data_fund_norm[:, 1:] - x_data_fund_norm[:, 1:].min()) / (x_data_fund_norm[:, 1:].max() - x_dat
x_data_minmax[:, 0] = x_data_fund_norm[:, 0] # Fundamental column exception

print(f'Min-Max Ratios STATS: Min. = {x_data_minmax[:, 1:].min()} Max. = {x_data_minmax[:, 1:].max()}')
print('-----')
print(f'"Fundamental & Min-Max Normalized" Dataset: {x_data_minmax.shape[0]} elements (w. {diff_labels} labels) & {x_data_minr
# -----

# Output Store
classes_size = np.array(vow_size) # Phoneme classes sizes array
classes_indices = np.array(end_idx) # Phoneme classes indices (start/end included)
np.savez_compressed(file='./HGCW_dataset_utils',
                    HGCW_raw = x_data_raw_np,
                    HGCW_fund_norm = x_data_fund_norm,
                    HGCW_minmax = x_data_minmax,
                    HGCW_labels = y_labels_raw_np,
                    classes_size = classes_size,
                    classes_idx = classes_indices)

# HGCW WOMEN Dataset: 3 Formants (steady state) + Fundamental Normalization + MinMax Scaling
import numpy as np

# Database (.DAT file) Features Reading (converted to NumPy array)
formant_analysis_data = np.loadtxt("./HGCW_LPC_formants_fine.dat", usecols=(2, 3, 4, 5))
formant_analysis_filenames = np.loadtxt("./HGCW_LPC_formants_fine.dat", usecols=0, dtype=str)

# Useful Parameters
vowels = ['ae', 'ah', 'aw', 'eh', 'er', 'ei', 'ih', 'iy', 'oa', 'oo', 'uh', 'uw'] # Vowels list
speakers = ['m', 'b', 'w', 'g'] # Speakers list
print(f"Dataset: {formant_analysis_data.shape[0]} samples (for {len(vowels)} labels) & {formant_analysis_data.shape[1]} featur
# -----

```

```

# Gender Filtering (Male)
male_data, male_indices = speaker_filter(formant_analysis_data, formant_analysis_filenames, speaker = 'w')
male_filenames = formant_analysis_filenames[male_indices]

# Remove Null elements
nonnull_data, nonnull_filenames, _ = null_filter(male_data, male_filenames)
print(f'NON NULL Dataset: {nonnull_data.shape[0]} samples (for {len(vowels)} labels) & {nonnull_data.shape[1]} features each")
print('-----')
print()

# Outputs initialization
x_data_raw_np = np.zeros((len(nonnull_data), 4), dtype=float) # Same Database n° of elements, 4 float features (columns)
y_labels_raw_np = np.zeros((len(nonnull_data), 1), dtype=int) # Same Database n° of elements, integer label single column arr

# Subgroups extraction & analysis
end_idx = [0] # Indices list initialization (0 and size values comprised)
vow_size = [] # Vowel groups size list initialization

for vowel_idx, vowel in enumerate(vowels):
    vow_data, _ = vowel_filter(nonnull_data, nonnull_filenames, vowel=vowel) # Vowel sub-set extraction
    end_idx.append(end_idx[vowel_idx] + len(vow_data)) # Actual sub-group End-Index appending
    vow_size.append(len(vow_data)) # Actual sub-group length appending
    print(f'Vowel "{vowel}" sub-set : {len(vow_data)} samples')

    start_idx = end_idx[vowel_idx] # Previous sub-set end-index
    print('1st element Idx :', start_idx)
    stop_idx = end_idx[vowel_idx] + len(vow_data) # Actual stop index = previous End + actual Size
    print('Last element Idx :', stop_idx - 1)
    x_data_raw_np[start_idx: stop_idx, :] = vow_data[:, :] # Output data sub-set ordered writing (Fundamental, 1st, 2nd & 3r

    vow_labels = np.full((len(vow_data), 1), vowel_idx, dtype=int) # Actual integer labels array creation
    print(f'Vowel LABEL : {vowel} - {vowel_idx}')
    y_labels_raw_np[start_idx: stop_idx, :] = vow_labels # Output labels sub-set ordered writing

    print('-----')

# Different labels counter
diff_labels = len(np.unique(y_labels_raw_np))
print()
print(f'--> RAW DATASET shape: {x_data_raw_np.shape}, w. {diff_labels} Labels')
print('-----')
# -----

# Fundamental Frequency (ratio) Normalization
x_data_fund_norm = np.zeros(x_data_raw_np.shape) # Output initialization

for i in range(x_data_raw_np.shape[1]): # For each feature...
    if i >= 1: # For each formant column...
        x_data_fund_norm[:, i] = x_data_raw_np[:, i] / x_data_raw_np[:, 0] # i-Formant value / i-Fundamental value
    else: # Exception for Fundamental freq column
        x_data_fund_norm[:, i] = x_data_raw_np[:, i]

print(f'Fundamental Normalized' Dataset: {x_data_fund_norm.shape[0]} elements (w. {diff_labels} labels) & {x_data_fund_norm.s
print('-----')
# -----

a = 0. # Lower bound
b = 1. # Upper bound
x_data_minmax = np.zeros((x_data_fund_norm.shape))
print(f'Fundamental Ratios STATS: Min. = {x_data_fund_norm[:, 1:].min()} Max. = {x_data_fund_norm[:, 1:].max()}')

x_data_minmax[:, 1:] = a + ((x_data_fund_norm[:, 1:] - x_data_fund_norm[:, 1:].min()) / (x_data_fund_norm[:, 1:].max() - x_dat
x_data_minmax[:, 0] = x_data_fund_norm[:, 0] # Fundamental column exception

print(f'Min-Max Ratios STATS: Min. = {x_data_minmax[:, 1:].min()} Max. = {x_data_minmax[:, 1:].max()}')
print('-----')
print(f'Fundamental & Min-Max Normalized' Dataset: {x_data_minmax.shape[0]} elements (w. {diff_labels} labels) & {x_data_minm
# -----

# Output Store
classes_size = np.array(vow_size) # Phoneme classes sizes array
classes_indices = np.array(end_idx) # Phoneme classes indices (start/end included)
np.savez_compressed(file='./HGCW_dataset_utils',
                    HGCW_raw = x_data_raw_np,
                    HGCW_fund_norm = x_data_fund_norm,
                    HGCW_minmax = x_data_minmax,
                    HGCW_labels = y_labels_raw_np,
                    classes_size = classes_size,
                    classes_idx = classes_indices)

# HGCW Dataset (3 x 4 Formants: 3- steady state, 3 - 10%, 3 - 50%, 3 - 80%) + Transform

```

```
# Database (.DAT file) Features Reading (converted to NumPy array)
import numpy as np

formant_analysis_data = np.loadtxt("./HGCW_LPC_formants_fine.dat", usecols=(2, 3, 4, 5, 6, 7, 8, 18, 19, 20, 27, 28, 29))
formant_analysis_filenames = np.loadtxt("./HGCW_LPC_formants_fine.dat", usecols=0, dtype=str)
# Useful Parameters
vowels = ['ae', 'ah', 'aw', 'eh', 'er', 'ei', 'ih', 'iy', 'oa', 'oo', 'uh', 'uw'] # Vowels list
speakers = ['m', 'b', 'w', 'g'] # Speakers list
print(f'Dataset: {formant_analysis_data.shape[0]} samples (for {len(vowels)} labels) & {formant_analysis_data.shape[1]} features each')
# -----

# Remove Null elements
nonnull_data, nonnull_filenames, _ = null_filter(formant_analysis_data, formant_analysis_filenames)
print(f'NON NULL Dataset: {nonnull_data.shape[0]} samples (for {len(vowels)} labels) & {nonnull_data.shape[1]} features each')
print('-----')
print()

# Outputs initialization
x_data_raw_np = np.zeros((len(nonnull_data), 13), dtype=float) # Same Database n° of elements, fund + 12 formants features (c
y_labels_raw_np = np.zeros((len(nonnull_data), 1), dtype=int) # Same Database n° of elements, integer label single column arr

# Subgroups extraction & analysis
end_idx = [0] # Indices list initialization (0 and size values comprised)
vow_size = [] # Vowel groups size list initialization

for vowel_idx, vowel in enumerate(vowels):
    vow_data, _ = vowel_filter(nonnull_data, nonnull_filenames, vowel=vowel) # Vowel sub-set extraction
    end_idx.append(end_idx[vowel_idx] + len(vow_data)) # Actual sub-group End-Index appending
    vow_size.append(len(vow_data)) # Actual sub-group length appending
    print(f'Vowel "{vowel}" sub-set : {len(vow_data)} samples')

    start_idx = end_idx[vowel_idx] # Previous sub-set end-index
    print('1st element Idx :', start_idx)
    stop_idx = end_idx[vowel_idx] + len(vow_data) # Actual stop index = previous End + actual Size
    print('Last element Idx :', stop_idx - 1)
    x_data_raw_np[start_idx: stop_idx, :] = vow_data[:, :] # Output data sub-set ordered writing (Fundamental, 1st, 2nd & 3rd)

    vow_labels = np.full((len(vow_data), 1), vowel_idx, dtype=int) # Actual integer labels array creation
    print(f'Vowel LABEL : {vowel} - {vowel_idx}')
    y_labels_raw_np[start_idx: stop_idx, :] = vow_labels # Output labels sub-set ordered writing

    print('-----')

# Different labels counter
diff_labels = len(np.unique(y_labels_raw_np))
print()
print(f'--> RAW DATASET shape: {x_data_raw_np.shape}, w. {diff_labels} Labels')
print('-----')
# -----

# Fundamental Frequency (ratio) Normalization
x_data_fund_norm = np.zeros(x_data_raw_np.shape) # Output initialization

for i in range(x_data_raw_np.shape[1]): # For each feature...
    if i >= 1: # For each formant column...
        x_data_fund_norm[:, i] = x_data_raw_np[:, i] / x_data_raw_np[:, 0] # i-Formant value / i-Fundamental value
    else: # Exception for Fundamental freq column
        x_data_fund_norm[:, i] = x_data_raw_np[:, i]

print(f'Fundamental Normalized' Dataset: {x_data_fund_norm.shape[0]} elements (w. {diff_labels} labels) & {x_data_fund_norm.shape[1]} features each')
print('-----')
# -----

a = 0. # Lower bound
b = 1. # Upper bound
x_data_minmax = np.zeros((x_data_fund_norm.shape))
print(f'Fundamental Ratios STATS: Min. = {x_data_fund_norm[:, 1:].min()} Max. = {x_data_fund_norm[:, 1:].max()}')

x_data_minmax[:, 1:] = a + ((x_data_fund_norm[:, 1:] - x_data_fund_norm[:, 1:].min()) / (x_data_fund_norm[:, 1:].max() - x_data_fund_norm[:, 1:].min()))
x_data_minmax[:, 0] = x_data_fund_norm[:, 0] # Fundamental column exception

print(f'Min-Max Ratios STATS: Min. = {x_data_minmax[:, 1:].min()} Max. = {x_data_minmax[:, 1:].max()}')
print('-----')
print(f'Fundamental & Min-Max Normalized' Dataset: {x_data_minmax.shape[0]} elements (w. {diff_labels} labels) & {x_data_minmax.shape[1]} features each')
# -----

# Output Store
classes_size = np.array(vow_size) # Phoneme classes sizes array
classes_indices = np.array(end_idx) # Phoneme classes indices (start/end included)
np.savez_compressed(file='./HGCW_dataset_utils',
                    HGCW_raw = x_data_raw_np,
                    HGCW_fund_norm = x_data_fund_norm,
```

```

        HGCW_minmax = x_data_minmax,
        HGCW_labels = y_labels_raw_np,
        classes_size = classes_size,
        classes_idx = classes_indices)

# HGCW Dataset (3 x 4 Formants: 3- steady state, 3 - 10%, 3 - 50%, 3 - 80%) + SPEAKER Label

# Database (.DAT file) Features Reading (converted to NumPy array)
import numpy as np

formant_analysis_data = np.loadtxt("./HGCW_LPC_formants_fine.dat", usecols=(2, 3, 4, 5, 6, 7, 8, 18, 19, 20, 27, 28, 29))
formant_analysis_filenames = np.loadtxt("./HGCW_LPC_formants_fine.dat", usecols=0, dtype=str)
# Useful Parameters
vowels = ['ae', 'ah', 'aw', 'eh', 'er', 'ei', 'ih', 'iy', 'oa', 'oo', 'uh', 'uw'] # Vowels list
speakers = ['b', 'g', 'm', 'w'] # Speakers list
print(f"Dataset: {formant_analysis_data.shape[0]} samples (for {len(vowels)} labels) & {formant_analysis_data.shape[1]} features")
# -----

# Remove Null elements
nonnull_data, nonnull_filenames, _ = null_filter(formant_analysis_data, formant_analysis_filenames)
print(f"NON NULL Dataset: {nonnull_data.shape[0]} samples (for {len(vowels)} labels) & {nonnull_data.shape[1]} features each")
print('-----')
print()

# Outputs initialization
x_data_raw_np = np.zeros((len(nonnull_data), 13), dtype=float) # Same Database n° of elements, fund + 12 formants features (c
y_labels_raw_np = np.zeros((len(nonnull_data), 1), dtype=int) # Same Database n° of elements, integer phoneme labels single c
z_labels_raw_np = np.zeros((len(nonnull_data), 1), dtype=int) # Same Database n° of elements, integer speaker labels single c

# Subgroups extraction & analysis
end_idx = [0] # Indices list initialization (0 value comprised)
vow_size = [] # Vowel groups size list initialization
spk_coords = [] # Will be a list of 12 lists: each sub-list will contain 4 speaker tuples (start_idx, speaker-phoneme size)

for vowel_idx, vowel in enumerate(vowels):
    vow_data, vow_indices = vowel_filter(nonnull_data, nonnull_filenames, vowel=vowel) # Vowel sub-set extraction
    end_idx.append(end_idx[vowel_idx] + len(vow_data)) # Actual sub-group End-Index appending
    vow_size.append(len(vow_data)) # Actual sub-group length appending
    print(f'Vowel "{vowel}" sub-set : {len(vow_data)} samples')

    start_idx = end_idx[vowel_idx] # Previous sub-set end-index
    print('1st element Idx :', start_idx)
    stop_idx = end_idx[vowel_idx] + len(vow_data) # Actual stop index = previous End + actual Size
    print('Last element Idx :', stop_idx - 1)
    x_data_raw_np[start_idx: stop_idx, :] = vow_data[:, :] # Output data sub-set ordered writing (Fundamental, 1st, 2nd & 3r

    vow_labels = np.full((len(vow_data), 1), vowel_idx, dtype=int) # Actual integer labels array creation
    print(f'Vowel LABEL : {vowel} - {vowel_idx}')
    y_labels_raw_np[start_idx: stop_idx, :] = vow_labels # Output labels sub-set ordered writing
    print()
    # -----

    # Subset speaker analysis
    vow_data_spk = np.zeros((len(vow_data), 1), dtype=int)
    vow_data_idx = []

    for speaker_idx, speaker in enumerate(speakers):
        _, spk_indices = speaker_filter(vow_data, nonnull_filenames[vow_indices], speaker=speaker) # Extract n-speaker indice
        vow_data_idx.append((spk_indices[0], len(spk_indices)))
        vow_data_spk[spk_indices] = speaker_idx # Set actual speaker label to actual vowel-speaker array
        print(f'"{speaker.upper()}"-speakers : {len(spk_indices)} (w. label "{speaker_idx}")')

    z_labels_raw_np[start_idx: stop_idx, :] = vow_data_spk # Append vowel-speaker to Output Speakers label
    spk_coords.append(vow_data_idx)
    print('-----')
    # -----

# Different labels counter
diff_phoneme_labels = len(np.unique(y_labels_raw_np))
diff_speaker_labels = len(np.unique(z_labels_raw_np))
print()
print(f'--> RAW DATASET shape: {x_data_raw_np.shape}, w. {diff_phoneme_labels} PHONEME Labels & {diff_speaker_labels} SPEAKER')
print('-----')
# -----

# Fundamental Frequency (ratio) Normalization
x_data_fund_norm = np.zeros(x_data_raw_np.shape) # Output initialization

for i in range(x_data_raw_np.shape[1]): # For each feature...
    if i >= 1: # For each formant column...
        x_data_fund_norm[:, i] = x_data_raw_np[:, i] / x_data_raw_np[:, 0] # i-Formant value / i-Fundamental value

```

```

else: # Exception for Fundamental freq column
    x_data_fund_norm[:, i] = x_data_raw_np[:, i]

print(f'Fundamental Normalized' Dataset: {x_data_fund_norm.shape[0]} elements & {x_data_fund_norm.shape[1]} features each")
print('-----')
# -----

a = 0. # Lower bound
b = 1. # Upper bound
x_data_minmax = np.zeros((x_data_fund_norm.shape))
print(f'Fundamental Ratios STATS: Min. = {x_data_fund_norm[:, 1:].min()} Max. = {x_data_fund_norm[:, 1:].max()}')

x_data_minmax[:, 1:] = a + ((x_data_fund_norm[:, 1:] - x_data_fund_norm[:, 1:].min()) / (x_data_fund_norm[:, 1:].max() - x_data_fund_norm[:, 1:].min()))
x_data_minmax[:, 0] = x_data_fund_norm[:, 0] # Fundamental column exception

print(f'Min-Max Ratios STATS: Min. = {x_data_minmax[:, 1:].min()} Max. = {x_data_minmax[:, 1:].max()}')
print('-----')
print(f'Fundamental & Min-Max Normalized' Dataset: {x_data_minmax.shape[0]} elements & {x_data_minmax.shape[1]} features each")
# -----

# Output Store
phon_classes_size = np.array(vow_size) # Phoneme classes sizes array
phon_classes_indices = np.array(end_idx) # Phoneme classes indices (start/end included)
phoneme_speaker_coordinates = np.array(sp_k_coords) # Each couple is (vow_spk sub-group start idx, vow-spk sub-group size)
np.savez_compressed(file='./HGCW_dataset_utils',
                    HGCW_raw = x_data_raw_np,
                    HGCW_fund_norm = x_data_fund_norm,
                    HGCW_minmax = x_data_minmax,
                    HGCW_phon_labels = y_labels_raw_np,
                    HGCW_spk_labels = z_labels_raw_np,
                    phon_size = phon_classes_size,
                    phon_idx = phon_classes_indices,
                    phon_spk_coords = phoneme_speaker_coordinates)

# HGCW Dataset (3 x 4 Formants: 3- steady state, 3 - 10%, 3 - 50%, 3 - 80%) + SPEAKER Label

# Database (.DAT file) Features Reading (converted to NumPy array)
import numpy as np

formant_analysis_data = np.loadtxt("./HGCW_LPC_formants_fine.dat", usecols=(2, 3, 4, 5, 6, 7, 8, 18, 19, 20, 27, 28, 29))
formant_analysis_filenames = np.loadtxt("./HGCW_LPC_formants_fine.dat", usecols=0, dtype=str)
# Useful Parameters
vowels = ['ae', 'ah', 'aw', 'eh', 'er', 'ei', 'ih', 'iy', 'oa', 'oo', 'uh', 'uw'] # Vowels list
speakers = ['b', 'g', 'm', 'w'] # Speakers list
print(f'Dataset: {formant_analysis_data.shape[0]} samples (for {len(vowels)} labels) & {formant_analysis_data.shape[1]} features each")
# -----

# Remove Null elements
nonnull_data, nonnull_filenames, _ = null_filter(formant_analysis_data, formant_analysis_filenames)
print(f'NON NULL Dataset: {nonnull_data.shape[0]} samples (for {len(vowels)} labels) & {nonnull_data.shape[1]} features each")
print('-----')
print()

```

## Future Works

- Extract an HGCW output with formant tracks only (No Steady States): test the minimum amount of time-points required for a correct evaluation;
- Repeat Analysis & feature extraction on:
  - PB Dataset
  - TIMIT Dataset
  - Bernard Dataset (Australian English)
  - VTRFormants Dataset
  - IRCAM VocalSet





## ▼ One-Class Sub-Network Analysis

(Vowel Phonemes Binary Classifier)

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**Year:** 2023

**Affiliation:** A.Casella Conservatory (student)

**Master Degree Thesis:** "Vowel phonemes Analysis & Classification by means of OCON rectifiers Deep Learning Architectures"

**Description:** Python scripts for "One-Class" neural network binary classifier analysis and optimization

```
# Numerical computations packages/modules
import numpy as np
import torch
import torch.nn as nn
import torch.nn.functional as F

# Dataset processing modules
from torch.utils.data import DataLoader
from sklearn.model_selection import train_test_split

# Graphic visualization modules
import matplotlib.pyplot as plt
import matplotlib_inline
matplotlib_inline.backend_inline.set_matplotlib_formats('svg')

# Common Seed initialization
SEED = 42 # ... the answer to the ultimate question of Life, the Universe, and Everything... (cit.)
```

## ▼ HGCW Dataset One-Hot Encoding

(class binarization)

```
# Load Dataset
HGCW_dataset_utils = np.load(file='./HGCW_dataset_utils.npz')
print('Raw features Data shape:', HGCW_dataset_utils['HGCW_raw'].shape)
print('Fundamental Normalized features Data shape:', HGCW_dataset_utils['HGCW_fund_norm'].shape)
print('MinMax features Data shape:', HGCW_dataset_utils['HGCW_minmax'].shape)
print('Labels Data shape:', HGCW_dataset_utils['HGCW_labels'].shape)
print('Classes size Data shape:', HGCW_dataset_utils['classes_size'].shape)
print('Classes indices Data shape:', HGCW_dataset_utils['classes_idx'].shape)

x_data_raw_np = HGCW_dataset_utils['HGCW_raw']
x_data_fund_norm = HGCW_dataset_utils['HGCW_fund_norm']
x_data_minmax = HGCW_dataset_utils['HGCW_minmax']
y_labels_raw_np = HGCW_dataset_utils['HGCW_labels']
vow_size = HGCW_dataset_utils['classes_size']
end_idx = HGCW_dataset_utils['classes_idx']

# Auxiliary lists
vowels = ['ae', 'ah', 'aw', 'eh', 'er', 'ei', 'ih', 'iy', 'oa', 'oo', 'uh', 'uw'] # Vowels list
colors = ['red', 'saddlebrown', 'darkorange', 'darkgoldenrod', 'gold', 'darkkhaki', 'olive', 'darkgreen', 'steelblue', 'fuchsia']

# Class-specific One-hot encoding (Binarization)
def one_hot_encoder(sel_class_number: int = 3, dataset: np.ndarray = x_data_minmax, orig_labels: int = len(vowels), classes_size: int = len(classes_size)):
    classes = [n for n in range(orig_labels)] # Class Labels list initialization

    # Auxiliary Parameters Initialization
    if sel_class_number < len(classes):
        classes.remove(sel_class_number) # REST Classes list
        if debug is True:
            print(f'Selected Class "{vowels[sel_class_number]}" : {classes_size[sel_class_number]} samples')
        sub_classes_size = classes_size[sel_class_number] // len(classes)
        if debug is True:
            print(f'Rest Classes size (...each): {sub_classes_size} samples')

    # 1-Subset processing
    sub_data = dataset[classes_idx[sel_class_number]: classes_idx[sel_class_number + 1], :] # Selected Class feature slice
    sub_data_labels_bin = np.ones((classes_size[sel_class_number], 1), dtype='int') # Selected Class labels (1) creation
    sub_data_labels = np.ones((classes_size[sel_class_number], 1), dtype='int') * sel_class_number

    # 0-Subset processing
    for i in classes:
```

```

class_i_indices = np.random.choice(np.arange(classes_idx[i], classes_idx[i + 1], 1), size=sub_classes_size, replac
sub_class_i_array = dataset[class_i_indices, :]
sub_class_labels_bin_array = np.zeros((sub_class_i_array.shape[0], 1), dtype='int') # Rest I-esimal Class labels
sub_class_labels_array = np.ones((sub_class_i_array.shape[0], 1), dtype='int') * i

# Outputs append
sub_data = np.vstack((sub_data, sub_class_i_array))
sub_data_labels_bin = np.vstack((sub_data_labels_bin, sub_class_labels_bin_array))
sub_data_labels = np.vstack((sub_data_labels, sub_class_labels_array))
else:
    raise ValueError(f'Invalid Class ID: "{sel_class_number}" --> It must be less than {len(classes)}!')

return sub_data, sub_data_labels_bin, sub_data_labels

# Test Call
dataset = x_data_minmax
sel_class_number = 0
sub_data, sub_data_labels_bin, sub_data_labels = one_hot_encoder(sel_class_number=sel_class_number, dataset=dataset, debug=True)
diff_labels_bin = len(np.unique(sub_data_labels_bin))
print('-----')
print(f"SUB 'Min-Max' Normalized Dataset: {sub_data.shape[0]} elements (w. {diff_labels_bin} BINARIZED labels) & {sub_data.shape[0]} samples (w. {len(np.unique(sub_data_labels))} labels)")
print(f"Also AVAILABLE Standard Labels: {sub_data_labels.shape[0]} samples (w. {len(np.unique(sub_data_labels))} labels)")

# Sub-Dataset Plot (previous example)
classes = [n for n in range(len(vowels))]
sub_classes_size = vow_size[sel_class_number] // (len(classes) - 1)

plt.figure(figsize=(12, 15))
plt.suptitle(f'Sub-Dataset ({vowels[sel_class_number]} - example) One-Hot Encoding')

counter = 0
for index in classes:
    if index == sel_class_number: # Selected Class exception (non increment counter variable)
        first_coords = sub_data[0: vow_size[sel_class_number], 1]
        second_coords = sub_data[0: vow_size[sel_class_number], 2]
        third_coords = sub_data[0: vow_size[sel_class_number], 3]
    else:
        start = vow_size[sel_class_number] + (counter * sub_classes_size)
        end = start + sub_classes_size

        first_coords = sub_data[start : end, 1]
        second_coords = sub_data[start : end, 2]
        third_coords = sub_data[start : end, 3]

    counter += 1

    plt.subplot(3, 2, 1)
    plt.title(f'$1_{st}$ VS $2_{nd}$')
    plt.scatter(first_coords, second_coords, marker='o', color=colors[index], label=f'Vowel "{vowels[index]}"')
    plt.xlabel(f'$1_{st}$ Formant Ratio')
    plt.ylabel(f'$2_{nd}$ Formant Ratio')
    plt.legend(loc='best')
    plt.grid(True)

    plt.subplot(3, 2, 3)
    plt.title(f'$1_{st}$ VS $3_{rd}$')
    plt.scatter(first_coords, third_coords, marker='o', color=colors[index], label=f'Vowel "{vowels[index]}"')
    plt.xlabel(f'$1_{st}$ Formant Ratio')
    plt.ylabel(f'$3_{rd}$ Formant Ratio')
    plt.legend(loc='best')
    plt.grid(True)

    plt.subplot(3, 2, 5)
    plt.title(f'$2_{nd}$ VS $3_{rd}$')
    plt.scatter(second_coords, third_coords, marker='o', color=colors[index], label=f'Vowel "{vowels[index]}"')
    plt.xlabel(f'$2_{nd}$ Formant Ratio')
    plt.ylabel(f'$3_{rd}$ Formant Ratio')
    plt.legend(loc='best')
    plt.grid(True)

plt.subplot(3, 2, 2)
plt.title(f'$1_{st}$ VS $2_{nd}$ Binarized')
plt.scatter(sub_data[0: vow_size[sel_class_number], 1], sub_data[0: vow_size[sel_class_number], 2], color=colors[sel_class_number], label=f'Vowel "{vowels[sel_class_number]}"')
plt.scatter(sub_data[vow_size[sel_class_number]:, 1], sub_data[vow_size[sel_class_number]:, 2], color='grey', label=f'Rest')
plt.xlabel(f'$1_{st}$ Formant Ratio')
plt.ylabel(f'$2_{nd}$ Formant Ratio')
plt.legend(loc='best')
plt.grid(True)

plt.subplot(3, 2, 4)
plt.title(f'$1_{st}$ VS $3_{rd}$ Binarized')
plt.scatter(sub_data[0: vow_size[sel_class_number], 1], sub_data[0: vow_size[sel_class_number], 3], color=colors[sel_class_number], label=f'Vowel "{vowels[sel_class_number]}"')
plt.scatter(sub_data[vow_size[sel_class_number]:, 1], sub_data[vow_size[sel_class_number]:, 3], color='grey', label=f'Rest')
plt.xlabel(f'$1_{st}$ Formant Ratio')
plt.ylabel(f'$3_{rd}$ Formant Ratio')
plt.legend(loc='best')
plt.grid(True)

```

```

plt.scatter(sub_data[vow_size[sel_class_number]:, 1], sub_data[vow_size[sel_class_number]:, 3], color='grey', label=f'Rest')
plt.xlabel('$1_{st}$ Formant Ratio')
plt.ylabel('$3_{rd}$ Formant Ratio')
plt.legend(loc='best')
plt.grid(True)

plt.subplot(3, 2, 6)
plt.title('$2_{nd}$ VS $3_{rd}$ Binarized')
plt.scatter(sub_data[0: vow_size[sel_class_number], 2], sub_data[0: vow_size[sel_class_number], 3], color=colors[sel_class_num
plt.scatter(sub_data[vow_size[sel_class_number]:, 2], sub_data[vow_size[sel_class_number]:, 3], color='grey', label=f'Rest')
plt.xlabel('$2_{nd}$ Formant Ratio')
plt.ylabel('$3_{rd}$ Formant Ratio')
plt.legend(loc='best')
plt.grid(True)

plt.tight_layout()
plt.savefig(f'{vowels[sel_class_number]}_class_one_hot_encoding')
plt.show()

# Train/Test split (auxiliary function)
def train_test_split_aux(features_dataset, labels_dataset, test_perc, tolerance):
    """
    An auxiliary Train_Test_split function (based on Scikit Learn implementation) w. balance tolerance specification
    """
    test_size = int(test_perc / 100 * len(features_dataset))
    train_balance = 0 # Output Training set balance value initialization
    test_balance = 0 # Output Testing set balance value initialization

    min_tol = np.mean(labels_dataset) - tolerance
    max_tol = np.mean(labels_dataset) + tolerance
    print(f'Data Balancing (TARGET = {np.mean(labels_dataset)} +- {tolerance}): ', end='')

    while (min_tol >= train_balance or train_balance >= max_tol) or (min_tol >= test_balance or test_balance >= max_tol):
        train_data, test_data, train_labels, test_labels = train_test_split(features_dataset, labels_dataset, test_size=test_s
        train_balance = np.mean(train_labels)
        test_balance = np.mean(test_labels)
        print('.', end='')
    else:
        print('OK')

    return train_data, test_data, train_labels, test_labels, train_balance, test_balance

# Train-Dev-Test split function
def train_dev_test_split(x_data, y_labels, split_list, tolerance=0.1, output='Loaders', debug=False):
    """
    Compute a Train, Development (Hold-Out) and a Test set split w. PyTorch Dataset conversion (and eventual Loaders initializ
    """
    if len(split_list) == 3:
        # Train - Dev+Test separation
        print('Training --- Devel/Test SPLIT')
        train_data, testTMP_data, train_labels, testTMP_labels, _, _ = train_test_split_aux(x_data, y_labels, (split_list[1] *
        print('-----')

        # Dev - Test separation
        print('Devel --- Test SPLIT')

        split = ((split_list[1] * 100) / np.sum(split_list[1:] * 100)) * 100 # Split in %
        dev_data, test_data, dev_labels, test_labels, _, _ = train_test_split_aux(testTMP_data, testTMP_labels, split, toleran
        print('-----')

        # Tensor Conversion
        train_data_tensor = torch.tensor(train_data).float()
        train_labels_tensor = torch.tensor(train_labels, dtype=torch.int64).squeeze()
        dev_data_tensor = torch.tensor(dev_data).float()
        dev_labels_tensor = torch.tensor(dev_labels, dtype=torch.int64).squeeze()
        test_data_tensor = torch.tensor(test_data).float()
        test_labels_tensor = torch.tensor(test_labels, dtype=torch.int64).squeeze()
        if debug is True:
            print(f'Training Data Shape: {train_data.shape}')
            print(f'Development Data Shape: {dev_data.shape}')
            print(f'Testing Data Shape: {test_data.shape}')

            # Balance Evaluation
            print(f'Training Set Balance: {np.mean(train_labels)}')
            print(f'Development Set Balance: {np.mean(dev_labels)}')
            print(f'Testing Set Balance: {np.mean(test_labels)}')

        if output != 'Loaders':
            return train_data_tensor, train_labels_tensor, dev_data_tensor, dev_labels_tensor, test_data_tensor, test_labels_t
        else:
            # PyTorch Dataset Conversion
            train_dataset = torch.utils.data.TensorDataset(torch.tensor(train_data).float(), torch.tensor(train_labels, dtype=

```

```

dev_dataset = torch.utils.data.TensorDataset(torch.tensor(dev_data).float(), torch.tensor(dev_labels, dtype=torch.
test_dataset = torch.utils.data.TensorDataset(torch.tensor(test_data).float(), torch.tensor(test_labels, dtype=torch.

# DataLoader (Batches) --> Drop-Last control to optimize training
trainLoader = DataLoader(train_dataset, shuffle=False, batch_size = 32, drop_last=True)
devLoader = DataLoader(dev_dataset, shuffle=False, batch_size = dev_dataset.tensors[0].shape[0])
testLoader = DataLoader(test_dataset, shuffle=False, batch_size = test_dataset.tensors[0].shape[0])
if debug is True:
    print(f'Training Set      Batch Size: {trainLoader.batch_size}')
    print(f'Development Set  Batch Size: {devLoader.batch_size}')
    print(f'Testing Set      Batch Size: {testLoader.batch_size}')

    return trainLoader, devLoader, testLoader
else:
    # Train - Test separation
    print('Training --- Test      SPLIT')
    train_data, test_data, train_labels, test_labels, _, _ = train_test_split_aux(x_data, y_labels, split_list[1] * 100, t
    print('-----')

    # Tensor Conversion
    train_data_tensor = torch.tensor(train_data).float()
    train_labels_tensor = torch.tensor(train_labels, dtype=torch.int64).squeeze()
    test_data_tensor = torch.tensor(test_data).float()
    test_labels_tensor = torch.tensor(test_labels, dtype=torch.int64).squeeze()
    if debug is True:
        print(f'Training Data      Shape: {train_data.shape}')
        print(f'Testing Data       Shape: {test_data.shape}')

    # Balance Evaluation
    print(f'Training Set      Balance: {np.mean(train_labels)}')
    print(f'Testing Set       Balance: {np.mean(test_labels)}')

if output != 'Loaders':
    return train_data_tensor, train_labels_tensor, test_data_tensor, test_labels_tensor
else:
    # PyTorch Dataset Conversion
    train_dataset = torch.utils.data.TensorDataset(torch.tensor(train_data).float(), torch.tensor(train_labels, dtype=
    test_dataset = torch.utils.data.TensorDataset(torch.tensor(test_data).float(), torch.tensor(test_labels, dtype=torch.

    # DataLoader (Batches) --> Drop-Last control to optimize training
    trainLoader = DataLoader(train_dataset, shuffle=False, batch_size = 32, drop_last=True)
    testLoader = DataLoader(test_dataset, shuffle=False, batch_size = test_dataset.tensors[0].shape[0])
    if debug is True:
        print(f'Training Set      Batch Size: {trainLoader.batch_size}')
        print(f'Testing Set       Batch Size: {testLoader.batch_size}')

    return trainLoader, testLoader

```

## ▼ Multi-Layer Perceptron Binary Classifier

```

# Dynamic Multi-Layer Architecture Class (w. units and activation function specification)
class binaryClassifier(nn.Module):
    def __init__(self, n_layers, n_units, act_fun):
        super().__init__()

        self.layers = nn.ModuleDict()
        self.nLayers = n_layers

        # Input Layer
        if n_layers == 1:
            self.layers['input'] = nn.Linear(3, n_units)

        else:
            self.layers['input'] = nn.Linear(3, n_units[0])

        # Hidden Layers
        if n_layers == 1:
            self.layers['hidden0'] = nn.Linear(n_units, n_units)
        else:
            for i in range(n_layers):
                if i == (n_layers - 1):
                    self.layers[f'hidden{i}'] = nn.Linear(n_units[i], n_units[i])
                else:
                    self.layers[f'hidden{i}'] = nn.Linear(n_units[i], n_units[i + 1])

        # Output Layer
        if n_layers == 1:
            self.layers['output'] = nn.Linear(n_units, 1)
        else:

```

```

        self.layers['output'] = nn.Linear(n_units[n_layers - 1], 1)

# Activation Function
self.actfun = act_fun # Function string-name attribute association

# Weights initialization (Kaiming He - Normal Distributed)
for layer in self.layers.keys():
    nn.init.kaiming_normal_(self.layers[layer].weight, mode='fan_in')

# Forward Pass Method
def forward(self, x):

    # Activation function object computation
    actfun = getattr(torch.nn, self.actfun)

    # Input Layer pass --> Weightening (Dot Product) "Linear transfor
    x = actfun()(self.layers['input'](x))

    # Hidden Layers sequential pass --> Weightening (Dot Product) "Linear transfor
    for i in range(self.nLayers):
        x = actfun()(self.layers[f'hidden{i}'](x))

    # Output Layer pass --> Output Weightening (Dot Product) "Linear t
    x = self.layers['output'](x)
    x = nn.Sigmoid()(x)

    return x

# Train/Test function (w. variable Backpropagation Optimizer Algorithm definition)
def cross_val_train_test(model, optim: str, epochs: int, learning_rate, train_data: torch.Tensor, train_labels: torch.Tensor,
    """
    Train & Test an ANN Classifier w. Binary Cross Entropy Loss computation and the specified Backpropagation Optimizer algori
    """
    # Loss Function initialization
    loss_function = nn.BCELoss()

    # Optimizer Algorithm initialization
    optimizer_function = getattr(torch.optim, optim) # Optimizer function retrieving
    optimizer = optimizer_function(model.parameters(), lr=learning_rate) # Parameters application (rest are standard initiali

    # TRAINING Phase
    train_losses = []
    train_accuracies = []

    model.train() # TRAINING Switch ON

    for i in range(epochs):
        train_predictions = model(train_data)
        train_loss = loss_function(train_predictions.squeeze(), train_labels.squeeze().to(torch.float))
        train_losses.append(train_loss.detach())

        # Backpropagation
        optimizer.zero_grad()
        train_loss.backward()
        optimizer.step()

        train_accuracy = 100 * torch.mean(((train_predictions.squeeze() > 0.5) == train_labels.squeeze()).float())
        train_accuracies.append(train_accuracy.detach())

        if debug is True:
            if i % 100 == 0:
                print(f'Epoch {i} --> Train Accuracy: {train_accuracy.detach()}%')
                print('-----')

    # TESTING Phase
    model.eval() # EVALUATION Switch ON (TRAINING Switch OFF)
    with torch.no_grad(): # Gradient (and Batch Normalization) deactivation
        test_predictions = model(test_data)
        test_accuracy = 100 * torch.mean(((test_predictions.squeeze() > 0.5) == test_labels.squeeze()).float())

        if debug is True:
            print(f'TEST ACCURACY: {test_accuracy.detach()} %')
            print('-----')

    return test_predictions.detach(), test_accuracy.detach(), train_losses, train_accuracies

# Batch Training function
def mini_batch_train_test(model, optim: str, epochs: int, learning_rate, train_loader, dev_loader, test_loader, debug=False):
    """
    Train & Test an ANN Architecture via Mini-Batch Training (w. Train/Dev/Test PyTorch Loaders) and same params of cross_vali
    """
    # Loss Function initialization

```

```

loss_function = nn.BCELoss()

# Optimizer Algorithm initialization
optimizer_function = getattr(torch.optim, optim)
optimizer = optimizer_function(model.parameters(), lr=learning_rate)

# Output list initialization
train_accuracies = []
train_losses = []
dev_accuracies = []

# TRAINING Phase
for epoch in range(epochs):
    model.train() # TRAINING Switch ON

    batch_accuracies = []
    batch_losses = []

    # Training BATCHES Loop
    for data_batch, labels_batch in train_loader:
        train_predictions = model(data_batch)
        train_loss = loss_function(train_predictions.squeeze(), labels_batch.type(torch.int64).float())
        batch_losses.append(train_loss.detach())

        # Backpropagation
        optimizer.zero_grad()
        train_loss.backward()
        optimizer.step()

        # Accuracy
        train_accuracy = 100 * torch.mean(((train_predictions.squeeze() > 0.5) == labels_batch.type(torch.int64).squeeze()))

        # Batch Stats appending
        batch_accuracies.append(train_accuracy.detach())
        batch_losses.append(train_loss.detach())

    # Training Stats appending
    train_accuracies.append(np.mean(batch_accuracies)) # Average of Batch Accuracies = Training step accuracy
    train_losses.append(np.mean(batch_losses)) # Average of Batch Losses = Training step Losses

# EVALUATION (Dev) Phase
model.eval()
with torch.no_grad():
    dev_data_batch, dev_labels_batch = next(iter(dev_loader))
    dev_predictions = model(dev_data_batch)

    dev_accuracy = 100 * torch.mean(((dev_predictions.squeeze() > 0.5) == dev_labels_batch.type(torch.int64).squeeze()))

    if debug is True:
        if epoch % 100 == 0:
            print(f'Epoch {epoch} --> DEV ACCURACY: {dev_accuracy.detach():.3f} %')
            print('-----')

    # Evaluation accuracy appending
    dev_accuracies.append(dev_accuracy.detach())

# TEST Phase
model.eval()
with torch.no_grad():
    test_data_batch, test_labels_batch = next(iter(test_loader))
    test_predictions = model(test_data_batch)
    test_accuracy = 100 * torch.mean(((test_predictions.squeeze() > 0.5) == test_labels_batch.type(torch.int64).squeeze()))

    if debug is True:
        print(f'TEST ACCURACY: {test_accuracy.detach():.2f} %')
        print('-----')

return train_accuracies, train_losses, dev_accuracies, test_accuracy.detach()

```

## ▼ Architecture optimal hyper-parameters estimate

Grid-Search (orders of magnitude)

- **Hidden Layers:** 1
- **Hidden Nodes:** (10, 50, 100)
- **Activation Function:** ReLU (*He standard distribution initialization*)

K. He, X. Zhang, S. Ren, J. Sun (2015) - [Delving Deep into Rectifiers: Surpassing Human-Level Performance on ImageNet Classification](#)

- **Learning Rates:** (0.001, 0.0001, 0.00001)
- **Optimizers:** Adam, RMSprop

---

## Root Mean Square Propagation (RMSprop)

$$w_t \leftarrow w_{t-1} - \frac{\eta}{\sqrt{v_t + \epsilon}} \nabla L$$

with

$$v_t = (1 - \beta)(\nabla L)^2 + \beta v_{t-1}$$

Similar to *Momentum* conditioning, but applied to Learning Rate coefficient (instead to Loss function) according to Gradient magnitudes. For this reason we speak about *Dynamic Learning Rate*, where:

- large gradients: implies small LR and smaller steps of minimization
- small gradients ( $0 < x < 1$ ): implies very large steps of minimization

$\epsilon$  is a standard positive coefficient added to denominator to avoid division by 0: usually  $10^{-8}$

---

## Adaptive Momentum (Adam)

Probably nowadays best gradient optimizer:

$$w_t \leftarrow w_{t-1} - \frac{\eta}{\sqrt{s_t + \epsilon}} v_t$$

with

$$v_t = \frac{(1 - \beta_1)\nabla L + \beta_1 v_{t-1}}{1 - \beta_1^t}$$
$$s_t = \frac{(1 - \beta_2)(\nabla L)^2 + \beta_2 s_{t-1}}{1 - \beta_2^t}$$

A combined form of **Momentum** and **RMSprop** with a dampening normalization factor, learning epoch dependent.

---

Reference: [PyTorch Reference - torch.optim Algorithms](#)

```
# Experiment Parameters
epochs = 1000 # For each "Batch-Set"
iterations = 3 # A total of 3000 Epochs of Training (3x Batch-Sub-Dataset shuffling)
min_tolerance = 0.1 # ...for sub-dataset balancing

# Architecture Hyper-Parameters
hidden_layers = 1
hidden_nodes = [10, 50, 100]
act_fun = 'ReLU'
learning_rates = [0.001, 0.0001, 0.00001] # [10^-3, 10^-4, 10^-5]
optimizers = ['Adam', 'RMSprop']

# AVG. Time 2h
from time import perf_counter
debug=False
experiment_results = np.zeros((len(hidden_nodes), len(learning_rates), len(optimizers), 2)) # Output Matrix initialization (1

exp_counter = 0
for i in range(len(hidden_nodes)):
    for j in range(len(learning_rates)):
        for k in range(len(optimizers)):

            exp_counter += 1 # Aux variable increment
            print(f'Experiment {exp_counter}: Units (HL): {hidden_nodes[i]}, LR: {learning_rates[j]}, Optimizer: {optimizers[k]}

            test accuracies = [] # List of Classes Test Accuracies (Re-initialized for each experiment)
            training_times = [] # List of Classes Training Times (Re-initialized for each experiment)

            # Experiment Routine
            for w in range(len(vowels)):

                # Reset Seed
                torch.manual_seed(SEED)

                # Create Classifier
                binary_classifier = binaryClassifier(1, hidden_nodes[i], act_fun)

                # Iterated (w. Batch-Sets shuffling) Training
                start_timer = perf_counter()
                for iteration in range(iterations):

                    # Dataset processing
                    sub_data, sub_data_labels_bin, _ = one_hot_encoder(sel_class_number=w, dataset=x_data_minmax, debug=debug)
                    print('-----')
                    trainLoader, devLoader, testLoader = train_dev_test_split(sub_data[:, 1:], sub_data_labels_bin, [0.7, 0.15
```

```

        # Train/Test Architecture
        _, _, _, test_accuracy = mini_batch_train_test(binary_classifier, optimizers[k], epochs, learning_rates[j])
        print(f'Sub-Net "{vowels[w]}" Partial-{iteration + 1} TEST ACCURACY: {test_accuracy:.2f}%')

    stop_timer = perf_counter()

    # Class Outputs append
    test accuracies.append(test_accuracy) # in %
    training_times.append(stop_timer - start_timer) # in sec.
    print('-----')

    print(f'Classes MEAN ACCURACY: {np.mean(test accuracies)}%')
    print(f'Classes Mean Training Runtime: {np.mean(training_times)}sec.')

    experiment_results[i, j, k, 0] = np.mean(test accuracies) # Average of 12 classes Accuracies
    experiment_results[i, j, k, 1] = np.mean(training_times) # Average of 12 classes Training Times

    print('-----')

# Outputs Save
np.savez_compressed(file='./architecture_grid_search',
                    avg_test accuracies=experiment_results[:, :, :, 0],
                    avg_training_times=experiment_results[:, :, :, 1])

# Architecture Grid-Search Experiment Plot
experiment_data = np.load(file='./architecture_grid_search.npz')

plt.figure(figsize=(12, 12))
plt.suptitle('Architecture Hyper-Parameters Experiment\n(average results across all classes)\n')

plt.subplot(2, 1, 1)
counter = 1
for i in range(experiment_data['avg_test accuracies'].shape[0]):
    for j in range(experiment_data['avg_test accuracies'].shape[1]):
        for k in range(experiment_data['avg_test accuracies'].shape[2]):
            if k == 1:
                plt.bar(counter, experiment_data['avg_test accuracies'][i, j, k], color='k', label=f'HN: {hidden_nodes[i]}, LR')
            else:
                plt.bar(counter, experiment_data['avg_test accuracies'][i, j, k], color='r', label=f'HN: {hidden_nodes[i]}, LR')

            counter += 1

max_accuracy = np.max(experiment_data['avg_test accuracies'])
plt.axhline(max_accuracy, color='grey', linestyle='--')
plt.title(f'Test Accuracies (RMSprop = Black, Adam = Red), Max.: {max_accuracy:.2f}%')
plt.xlabel('Experiment Run (index)')
plt.xticks([(n + 1) for n in range(18)], [(n + 1) for n in range(18)])
plt.ylabel('Accuracy (in %)')
plt.ylim([50, 100])
plt.grid()
plt.legend(loc='lower center', bbox_to_anchor=(0.5, -0.3), fancybox=True, shadow=True, ncol=6)

plt.subplot(2, 1, 2)
counter = 1
for i in range(experiment_data['avg_training_times'].shape[0]):
    for j in range(experiment_data['avg_training_times'].shape[1]):
        for k in range(experiment_data['avg_training_times'].shape[2]):
            if k == 1:
                plt.bar(counter, experiment_data['avg_training_times'][i, j, k], color='k', label=f'HN: {hidden_nodes[i]}, LR: ')
            else:
                plt.bar(counter, experiment_data['avg_training_times'][i, j, k], color='pink', label=f'HN: {hidden_nodes[i]}, LR: ')

            counter += 1

plt.title('Training Times (RMSprop = Black, Adam = Pink)')
plt.xlabel('Experiment Run (index)')
plt.xticks([(n + 1) for n in range(18)], [(n + 1) for n in range(18)])
plt.ylabel('Time (in sec.)')
plt.ylim([20, 40])
plt.grid()
plt.legend(loc='lower center', bbox_to_anchor=(0.5, -0.3), fancybox=True, shadow=True, ncol=6)

plt.tight_layout()
plt.savefig('architecture_grid_search')
plt.show()

# Best Test Accuracy inspection
best_run_acc = experiment_data['avg_test accuracies'][2, 1, 0]

```



```
best_run_time = experiment_data['avg_training_times'][2, 1, 0]
print(f'Run 15 (Adam Optimizer): {best_run_acc:.2f}% in {best_run_time:.2f}sec. (per class)')
```

## ▼ Architecture Optimization

Multi-Layer Perceptron

- Input Layer: 3 features [formant ratios, min-max normalized]
- Hidden Layer: 100 units
- Output Layer: 1 normalized probability
- Learning Rate: 0.0001 ( $10^{-4}$ )
- Optimizer : Adam (Adaptive Momentum)

- Mini-Batch Training:

- . Re-iterated Sub-Dataset Shuffling
- . Batch size = 32

- **Bias Initialization:** 0
- **Regularization:** Dropout, Batch-Normalization, L2 Loss Regularization

## ▼ Dropout

Probabilistic method to "mute" (sparsing) learning inference of arbitrary nodes during each epoch. It aims to uniform learning patterns and avoid mnemonic recognition/association of data examples.

- N. Srivastava, G. Hinton, A. Krizhevsky, I. Sutskever, R. Salakhutdinov (2014) - [Dropout: A Simple Way to Prevent Neural Networks from Overfitting](#)

```

# Dynamic Multi-Layer Architecture Class (w. units, activation function and DropOut Rate specification)
class binaryClassifier_dropout(nn.Module):
    def __init__(self, n_layers, n_units, act_fun, rate_in, rate_hidden):
        super().__init__()

        self.layers = nn.ModuleDict()
        self.nLayers = n_layers

        # Input Layer
        self.layers['input'] = nn.Linear(3, n_units)

        # Hidden Layers
        self.layers[f'hidden'] = nn.Linear(n_units, n_units)

        # Output Layer
        self.layers['output'] = nn.Linear(n_units, 1)

        # Activation Function
        self.actfun = act_fun

        # Dropout Parameter
        self.dr_in = rate_in
        self.dr_hidden = rate_hidden

        # Weights & Bias initialization
        for layer in self.layers.keys():
            nn.init.kaiming_normal_(self.layers[layer].weight, mode='fan_in')
        for layer in self.layers.keys():
            self.layers[layer].bias.data.fill_(0.)

    # Forward Pass Method
    def forward(self, x):

        # Activation function object computation
        actfun = getattr(torch.nn, self.actfun)

        # Input Layer pass
        x = actfun()(self.layers['input'](x))
        x = F.dropout(x, p=self.dr_in, training=self.training)

        # Hidden Layers sequential pass
        x = actfun()(self.layers[f'hidden'](x))
        x = F.dropout(x, p=self.dr_hidden, training=self.training)

        # Output Layer pass
        x = self.layers['output'](x)
        x = nn.Sigmoid()(x)

        return x

# Experiment Parameters
epochs = 1000 # For each "Batch-Set"
iterations = 6 # A total of 6000 Epochs of Training (6x Batch-Sub-Dataset shuffling) --> w. Early Stopping
min_tolerance = 0.1 # ...for sub-dataset balancing

# Architecture Hyper-Parameters
hidden_layer = 1
hidden_nodes = 100
act_fun = 'ReLU'
learning_rate = 0.0001 # 10^-4
optimizer = 'Adam'

# DropOut Regularization Parameters
dropout_rates_in = [0.8, 0.9]
dropout_rates_hidden = (np.arange(5) / 10.) + 0.5

# AVG. Time 1h 30min
from time import perf_counter
debug=False
experiment_results = np.zeros((len(dropout_rates_in), len(dropout_rates_hidden), 2))

exp_counter = 0
for i in range(len(dropout_rates_in)):
    for j in range(len(dropout_rates_hidden)):
        exp_counter += 1
        print(f'Experiment {exp_counter}: DropOut Input: {dropout_rates_in[i]}, DropOut Hidden: {dropout_rates_hidden[j]}')

        test accuracies = [] # List of Classes Test Accuracies (Re-initialized for each experiment)
        training_times = [] # List of Classes Training Times (Re-initialized for each experiment)

    # Experiment Routine

```

```

for k in range(len(vowels)):

    # Reset Seed
    torch.manual_seed(SEED)

    # Create Classifier
    binary_classifier = binaryClassifier_dropout(1, hidden_nodes, act_fun, dropout_rates_in[i], dropout_rates_hidden[j])

    # Iterated (w. Batch-Sets shuffling) Training
    iteration = 0

    start_timer = perf_counter()
    while iteration < iterations:

        # Dataset processing
        sub_data, sub_data_labels_bin, _ = one_hot_encoder(sel_class_number=k, dataset=x_data_minmax, debug=debug)
        print('-----')
        trainLoader, devLoader, testLoader = train_dev_test_split(sub_data[:, 1:], sub_data_labels_bin, [0.7, 0.15, 0.15])

        # Train/Test Architecture
        _, _, _, test_accuracy = mini_batch_train_test(binary_classifier, optimizer, epochs, learning_rate, trainLoader, devLoader, testLoader)
        print(f'Sub-Net "{vowels[k]}" Partial-{iteration + 1} TEST ACCURACY: {test_accuracy:.2f}%')

        if test_accuracy > 93.67: # If specific class instance overshoot class mean accuracy
            iteration += 1
            print(f'Training STOP {iteration}-----')
            break # Early stop

        iteration += 1 # Go to next Batch training iteration

    stop_timer = perf_counter()

    # Class Outputs append
    test accuracies.append(test_accuracy) # in %
    training_times.append(stop_timer - start_timer) # in sec.
    print('-----')

    print(f'Classes MEAN ACCURACY: {np.mean(test accuracies)}%')
    print(f'Classes Mean Training Runtime: {np.mean(training_times)}sec.')

    experiment_results[i, j, 0] = np.mean(test accuracies) # Average of 12 classes Accuracies
    experiment_results[i, j, 1] = np.mean(training_times) # Average of 12 classes Training Times

    print('-----')

# Outputs Save
np.savez_compressed(file='./dropout_grid_search',
                    avg_test accuracies=experiment_results[:, :, 0],
                    avg_training_times=experiment_results[:, :, 1])

# DropOut Grid-Search Experiment Plot
experiment_data = np.load(file='./dropout_grid_search.npz')

plt.figure(figsize=(12, 8))
plt.suptitle('Dropout Regularization Experiment\n(average results across all classes)\n')

counter = 0
plt.subplot(2, 1, 1)
for i in range(experiment_data['avg_test accuracies'].shape[0]):
    for j in range(experiment_data['avg_test accuracies'].shape[1]):
        plt.bar(counter + 1, experiment_data['avg_test accuracies'][i, j], label=f'DR_in: {dropout_rates_in[i]}, DR_hidden: {dropout_rates_hidden[j]}')
        counter += 1

max_accuracy = np.max(experiment_data['avg_test accuracies'])
plt.axhline(max_accuracy, color='grey', linestyle='--')
plt.title(f'Test Accuracies, Max.: {max_accuracy:.2f}%')
plt.xlabel('Experiment Run (indices)')
plt.xticks([(n + 1) for n in range(10)], [(n + 1) for n in range(10)])
plt.ylabel('Accuracy (in %)')
plt.ylim([70, 100])
plt.grid()
plt.legend(loc='center right', bbox_to_anchor=(1.3, 0.5), fancybox=True, shadow=True, ncol=1)

counter = 0
plt.subplot(2, 1, 2)
for i in range(experiment_data['avg_training_times'].shape[0]):
    for j in range(experiment_data['avg_training_times'].shape[1]):
        plt.bar(counter + 1, experiment_data['avg_training_times'][i, j], label=f'DR_in: {dropout_rates_in[i]}, DR_hidden: {dropout_rates_hidden[j]}')
        counter += 1

plt.title(f'Training Times')
plt.xlabel('Experiment Run (indices)')

```

```
plt.xticks([(n + 1) for n in range(10)], [(n + 1) for n in range(10)])
plt.ylabel('Time (in sec.)')
plt.ylim([20, 60])
plt.grid()
plt.legend(loc='center right', bbox_to_anchor=(1.3, 0.5), fancybox=True, shadow=True, ncol=1)

plt.tight_layout()
plt.savefig('dropout_grid_search')
plt.show()

# Best Test Accuracy inspection
best_run_acc = experiment_data['avg_test_accuracies'][0, 0]
best_run_time = experiment_data['avg_training_times'][0, 0]
print(f'Adam + Dropout: {best_run_acc:.2f}% in {best_run_time:.2f}sec. (per class)')
```

## ▼ Batch Normalization

A form of regularization applied to layers inputs, in order to avoid covariance shift, vanishing or exploding gradients.

$$\hat{y} = \sigma(\tilde{x}^T w)$$

with

$$\tilde{x} = \gamma x + \beta$$

with  $\gamma$  and  $\beta$  respectively a scaling and shifting coefficient, learned by the model itself during training phase, while  $\tilde{x}$  is a normalized "raw input" to the n-Layer.

- S. Ioffe, C. Szegedy (2015) - [Batch Normalization: Accelerating Deep Network Training by Reducing Internal Covariate Shift](#)

```
# Dynamic Multi-Layer Architecture Class (w. units, activation function, Dropout Rate specification)
class binaryClassifier_batchnorm(nn.Module):
    def __init__(self, n_layers, n_units, act_fun, rate_in, rate_hidden):
        super().__init__()

        self.layers = nn.ModuleDict()
        self.nLayers = n_layers

        # Input Layer
        self.layers['input'] = nn.Linear(3, n_units)

        # Hidden Layers
        self.layers[f'hidden'] = nn.Linear(n_units, n_units)
        self.layers[f'batch_norm'] = nn.BatchNorm1d(n_units)

        # Output Layer
        self.layers['output'] = nn.Linear(n_units, 1)

        # Activation Function
        self.actfun = act_fun

        # Dropout Parameter
        self.dr_in = rate_in
        self.dr_hidden = rate_hidden

        # Weights & Bias initialization
        for layer in self.layers.keys():
            try:
                nn.init.kaiming_normal_(self.layers[layer].weight, mode='fan_in')
            except:
                pass
        for layer in self.layers.keys():
            self.layers[layer].bias.data.fill_(0.)

# Forward Pass Method
def forward(self, x):

    # Activation function object computation
    actfun = getattr(torch.nn, self.actfun)

    # Input Layer pass
    x = actfun()(self.layers['input'](x))
    x = F.dropout(x, p=self.dr_in, training=self.training)

    # Hidden Layers sequential pass
    x = self.layers[f'batch_norm'](x)
    x = actfun()(self.layers[f'hidden'](x))
    x = F.dropout(x, p=self.dr_hidden, training=self.training)

    # Output Layer pass
    x = self.layers['output'](x)
```

```

x = nn.Sigmoid()(x)

return x

# Experiment Parameters
epochs = 1000 # For each "Batch-Set"
iterations = 10 # A total of 10000 Epochs of Training (10x Batch-Sub-Dataset shuffling) --> w. Early Stopping
min_tolerance = 0.1 # ...for sub-dataset balancing

# Architecture Hyper-Parameters
hidden_layer = 1
hidden_nodes = 100
act_fun = 'ReLU'
learning_rates = [0.001, 0.0001, 0.00001] # Try increasing and reducing actual LR
optimizer = 'Adam'

# Regularization Hyper-Parameters
dropout_rate_in = 0.8
dropout_rate_hidden = 0.5

# AVG. Time 40min.
from time import perf_counter
debug=False
experiment_results = np.zeros((len(learning_rates), 2))

for i in range(len(learning_rates)):
    print(f'Experiment {i + 1}: LR: {learning_rates[i]}')

    test_accuracies = [] # List of Classes Test Accuracies (Re-initialized for each experiment)
    training_times = [] # List of Classes Training Times (Re-initialized for each experiment)

    # Experiment Routine
    for k in range(len(vowels)):

        # Reset Seed
        torch.manual_seed(SEED)

        # Create Classifier
        binary_classifier = binaryClassifier_batchnorm(1, hidden_nodes, act_fun, dropout_rate_in, dropout_rate_hidden)

        # Iterated (w. Batch-Sets shuffling) Training
        iteration = 0

        start_timer = perf_counter()
        while iteration < iterations:

            # Dataset processing
            sub_data, sub_data_labels_bin, _ = one_hot_encoder(sel_class_number=k, dataset=x_data_minmax, debug=debug)
            print('-----')
            trainLoader, devLoader, testLoader = train_dev_test_split(sub_data[:, 1:], sub_data_labels_bin, [0.7, 0.15, 0.15],

            # Train/Test Architecture
            _, _, _, test_accuracy = mini_batch_train_test(binary_classifier, optimizer, epochs, learning_rates[i], trainLoade
            print(f'Sub-Net "{vowels[k]}" Partial-{iteration + 1} TEST ACCURACY: {test_accuracy:.2f}%')

            if test_accuracy > 93.86: # If specific class instance overshoot previous class mean accuracy
                iteration += 1
                print(f'Training STOP {iteration}-----')
                break # Early stop

            iteration += 1 # Go to next Batch training iteration

        stop_timer = perf_counter()

        # Class Outputs append
        test_accuracies.append(test_accuracy) # in %
        training_times.append(stop_timer - start_timer) # in sec.
        print('-----')

    print(f'Classes MEAN ACCURACY: {np.mean(test_accuracies)}%')
    print(f'Classes Mean Training Runtime: {np.mean(training_times)}sec.')

    experiment_results[i, 0] = np.mean(test_accuracies) # Average of 12 classes Accuracies
    experiment_results[i, 1] = np.mean(training_times) # Average of 12 classes Training Times

    print('-----')

# Outputs Save
np.savez_compressed(file='./batch_norm_lr',

```

```

        avg_test accuracies=experiment_results[:, 0],
        avg_training_times=experiment_results[:, 1])

# Batch Normalization Experiment Plot
experiment_data = np.load(file='./batch_norm_lr.npz')

plt.figure(figsize=(12, 5))
plt.suptitle('Dropout + Batch-Norm Regularization Experiment\n(average results across all classes)\n')

counter = 0
plt.subplot(1, 2, 1)
for i in range(experiment_data['avg_test accuracies'].shape[0]):
    plt.bar(i + 1, experiment_data['avg_test accuracies'][i], label=f'LR: {learning_rates[i]}')
    counter += 1

max_accuracy = np.max(experiment_data['avg_test accuracies'])
plt.axhline(max_accuracy, color='grey', linestyle='--')
plt.title(f'Test Accuracies, Max.: {max_accuracy:.2f}%')
plt.xlabel('Experiment Run (indices)')
plt.xticks([(n + 1) for n in range(3)], [(n + 1) for n in range(3)])
plt.ylabel('Accuracy (in %)')
plt.ylim([85, 97])
plt.grid()
plt.legend(loc='best')

plt.subplot(1, 2, 2)
for i in range(experiment_data['avg_training_times'].shape[0]):
    plt.bar(i + 1, experiment_data['avg_training_times'][i], label=f'LR: {learning_rates[i]}')

plt.title(f'Training Times')
plt.xlabel('Experiment Run (indices)')
plt.xticks([(n + 1) for n in range(3)], [(n + 1) for n in range(3)])
plt.ylabel('Time (in sec.)')
plt.ylim([40, 85])
plt.grid()
plt.legend(loc='best')

plt.tight_layout()
plt.savefig('batch_norm_lr')
plt.show()

# Best Test Accuracy inspection
best_run_acc = experiment_data['avg_test accuracies'][1]
best_run_time = experiment_data['avg_training_times'][1]
print(f'Adam + DropOut + Batch-Norm: {best_run_acc:.2f}% in {best_run_time:.2f}sec. (per class)')

```

## ▼ L2 (Ridge) Penalty

*L2*, also called "*Ridge regression*" or "*weight decay*" regularization it's expressed as:

$$J = \frac{1}{n} \sum_{i=1}^n L(\hat{y}_i, y_i) + \lambda ||w_i||_2^2$$

where:  $||w_i||_2^2 = w^T w$

$\lambda$  is a scalar coefficient, also called "regularization parameter/coefficient" and is usually expressed as:

$$\lambda = \frac{\alpha}{2m}$$

where  $m$  is the number of weights and  $||w||$  represent the vector magnitude (norm) of weights.

Generally, we tend to prefer a relatively large value from the left term (the summation) and a relatively small value from the regularization term in order to minimize cost function adding weights features itself.

[Wikipedia](#)

```

# Batch Training function (w. Adam Optimizer & L2 penalty term) Re-Definition
def mini_batch_train_test(model, weight_decay, epochs: int, learning_rate, train_loader, dev_loader, test_loader, debug=False)
    """
    Train & Test an ANN Architecture via Mini-Batch Training (w. Train/Dev/Test PyTorch Loaders) and Adam Backpropagation Opti
    """
    # Loss Function initialization
    loss_function = nn.BCELoss()

    # Optimizer Algorithm initialization
    optimizer = torch.optim.Adam(model.parameters(), lr=learning_rate, weight_decay=weight_decay)

    # Output list initialization
    train accuracies = []

```

```

train_losses = []
dev_accuracies = []

# TRAINING Phase
for epoch in range(epochs):
    model.train() # TRAINING Switch ON

    batch_accuracies = []
    batch_losses = []

    # Training BATCHES Loop
    for data_batch, labels_batch in train_loader:
        train_predictions = model(data_batch)
        train_loss = loss_function(train_predictions.squeeze(), labels_batch.type(torch.int64).float())
        batch_losses.append(train_loss.detach())

        # Backpropagation
        optimizer.zero_grad()
        train_loss.backward()
        optimizer.step()

        # Accuracy
        train_accuracy = 100 * torch.mean(((train_predictions.squeeze() > 0.5) == labels_batch.type(torch.int64).squeeze()))

        # Batch Stats appending
        batch_accuracies.append(train_accuracy.detach())
        batch_losses.append(train_loss.detach())

    # Training Stats appending
    train_accuracies.append(np.mean(batch_accuracies)) # Average of Batch Accuracies = Training step accuracy
    train_losses.append(np.mean(batch_losses)) # Average of Batch Losses = Training step Losses

# EVALUATION (Dev) Phase
model.eval()
with torch.no_grad():
    dev_data_batch, dev_labels_batch = next(iter(dev_loader))
    dev_predictions = model(dev_data_batch)

    dev_accuracy = 100 * torch.mean(((dev_predictions.squeeze() > 0.5) == dev_labels_batch.type(torch.int64).squeeze()))

    if debug is True:
        if epoch % 100 == 0:
            print(f'Epoch {epoch} --> DEV ACCURACY: {dev_accuracy.detach():.3f} %')
            print('-----')

        # Evaluation accuracy appending
        dev_accuracies.append(dev_accuracy.detach())

# TEST Phase
model.eval()
with torch.no_grad():
    test_data_batch, test_labels_batch = next(iter(test_loader))
    test_predictions = model(test_data_batch)
    test_accuracy = 100 * torch.mean(((test_predictions.squeeze() > 0.5) == test_labels_batch.type(torch.int64).squeeze()))

    if debug is True:
        print(f'TEST ACCURACY: {test_accuracy.detach():.2f} %')
        print('-----')

return train_accuracies, train_losses, dev_accuracies, test_accuracy.detach()

# Experiment Parameters
epochs = 1000 # For each "Batch-Set"
iterations = 10 # A total of 10000 Epochs of Training (10x Batch-Sub-Dataset shuffling) --> w. Early Stopping
min_tolerance = 0.1 # ...for sub-dataset balancing

# Architecture Hyper-Parameters
hidden_layer = 1
hidden_nodes = 100
act_fun = 'ReLU'
learning_rate = 0.0001
optimizer = 'Adam'

# Regularization Hyper-Parameters
dropout_rate_in = 0.8
dropout_rate_hidden = 0.5
l2_lambda = np.logspace(-2, -4, num=3, base=10) # [10^-2, 10^-3, 10^-4]

# AVG. Time 30min.
from time import perf_counter
debug=False

```

```

experiment_results = np.zeros((len(l2_lambda), 2))

for i in range(len(l2_lambda)):
    print(f'Experiment {i + 1}: L2_Lambda (Weight Decay): {l2_lambda[i]}')

    test_accuracies = [] # List of Classes Test Accuracies (Re-initialized for each experiment)
    training_times = [] # List of Classes Training Times (Re-initialized for each experiment)

    # Experiment Routine
    for k in range(len(vowels)):

        # Reset Seed
        torch.manual_seed(SEED)

        # Create Classifier
        binary_classifier = binaryClassifier_batchnorm(1, hidden_nodes, act_fun, dropout_rate_in, dropout_rate_hidden)

        # Iterated (w. Batch-Sets shuffling) Training
        iteration = 0

        start_timer = perf_counter()
        while iteration < iterations:

            # Dataset processing
            sub_data, sub_data_labels_bin, _ = one_hot_encoder(sel_class_number=k, dataset=x_data_minmax, debug=debug)
            print('-----')
            trainLoader, devLoader, testLoader = train_dev_test_split(sub_data[:, 1:], sub_data_labels_bin, [0.7, 0.15, 0.15],

            # Train/Test Architecture
            _, _, _, test_accuracy = mini_batch_train_test(binary_classifier, l2_lambda[i], epochs, learning_rate, trainLoader)
            print(f'Sub-Net "{vowels[k]}" Partial-{iteration + 1} TEST ACCURACY: {test_accuracy:.2f}%')

            if test_accuracy > 94.96: # If specific class instance overshoot previous class mean accuracy
                iteration += 1
                print(f'Training STOP {iteration}------')
                break # Early stop

            iteration += 1 # Go to next Batch training iteration

        stop_timer = perf_counter()

        # Class Outputs append
        test_accuracies.append(test_accuracy) # in %
        training_times.append(stop_timer - start_timer) # in sec.
        print('-----')

    print(f'Classes MEAN ACCURACY: {np.mean(test_accuracies)}%')
    print(f'Classes Mean Training Runtime: {np.mean(training_times)}sec.')

    experiment_results[i, 0] = np.mean(test_accuracies) # Average of 12 classes Accuracies
    experiment_results[i, 1] = np.mean(training_times) # Average of 12 classes Training Times

    print('-----')

# Outputs Save
np.savez_compressed(file='./L2_grid_search',
                    avg_test_accuracies=experiment_results[:, 0],
                    avg_training_times=experiment_results[:, 1])

# L2 Normalization Experiment Plot
experiment_data = np.load(file='./L2_grid_search.npz')

plt.figure(figsize=(12, 5))
plt.suptitle('Dropout + Batch-Norm + L2 Norm Experiment\n(average results across all classes)\n')

counter = 0
plt.subplot(1, 2, 1)
for i in range(experiment_data['avg_test_accuracies'].shape[0]):
    plt.bar(i + 1, experiment_data['avg_test_accuracies'][i], label=f'$\lambda$: {l2_lambda[i]}')
    counter += 1

max_accuracy = np.max(experiment_data['avg_test_accuracies'])
plt.axhline(max_accuracy, color='grey', linestyle='--')
plt.title(f'Test Accuracies, Max.: {max_accuracy:.2f}%')
plt.xlabel('Experiment Run (indices)')
plt.xticks([(n + 1) for n in range(3)], [(n + 1) for n in range(3)])
plt.ylabel('Accuracy (in %)')
plt.ylim([80, 100])
plt.grid()
plt.legend(loc='best')

```



```

plt.subplot(1, 2, 2)
for i in range(experiment_data['avg_training_times'].shape[0]):
    plt.bar(i + 1, experiment_data['avg_training_times'][i], label=f'$\lambda$: {l2_lambda[i]}')

plt.title(f'Training Times')
plt.xlabel('Experiment Run (indices)')
plt.xticks([(n + 1) for n in range(3)], [(n + 1) for n in range(3)])
plt.ylabel('Time (in sec.)')
plt.ylim([40, 70])
plt.grid()
plt.legend(loc='best')

plt.tight_layout()
plt.savefig('L2_grid_search')
plt.show()

# Best Test Accuracy inspection
best_run_acc = experiment_data['avg_test accuracies'][2]
best_run_time = experiment_data['avg_training_times'][2]
rint(f'Adam + DropOut + Batch-Norm + L2: {best_run_acc:.2f}% in {best_run_time:.2f}sec. (per class)')

```



## ▼ *OCON Model Analysis*

(3-features all\_speakers Dataset)

**Author:** S. Giacomelli

**Year:** 2023

**Affiliation:** A.Casella Conservatory (student)

**Master Degree Thesis:** "Vowel phonemes Analysis & Classification by means of OCON rectifiers Deep Learning Architectures"

**Description:** Python scripts for One-Class-One-Network (OCON) Model analysis and optimization

```
# Numerical computations packages/modules
import numpy as np
import torch
import torch.nn as nn
import torch.nn.functional as F

# Dataset processing modules
from torch.utils.data import DataLoader
from sklearn.model_selection import train_test_split

# Graphic visualization modules
import matplotlib.pyplot as plt
import matplotlib_inline
matplotlib_inline.backend_inline.set_matplotlib_formats('svg')

# Common Seed initialization
SEED = 42 # ... the answer to the ultimate question of Life, the Universe, and Everything... (cit.)

# PyTorch Processing Units evaluation
device = 'cuda' if torch.cuda.is_available() else 'cpu'
print(f'AVAILABLE Processing Unit: {device.upper()}')
!nvidia-smi
```

## ▼ *HGCW Dataset*

- *Dataset\_utils.npz* file read
- *One-Hot encoding* definition
- *Train/Dev/Test split* definition

```
# Load HGCW 4_features_all Dataset
HGCW_dataset_utils = np.load(file='./HGCW_dataset_utils.npz')
print('Raw features Data shape:', HGCW_dataset_utils['HGCW_raw'].shape)
print('Fundamental Normalized features Data shape:', HGCW_dataset_utils['HGCW_fund_norm'].shape)
print('MinMax features Data shape:', HGCW_dataset_utils['HGCW_minmax'].shape)
print('Labels Data shape:', HGCW_dataset_utils['HGCW_labels'].shape)
print('Classes size Data shape:', HGCW_dataset_utils['classes_size'].shape)
print('Classes indices Data shape:', HGCW_dataset_utils['classes_idx'].shape)

x_data_raw_np = HGCW_dataset_utils['HGCW_raw']
x_data_fund_norm = HGCW_dataset_utils['HGCW_fund_norm']
x_data_minmax = HGCW_dataset_utils['HGCW_minmax']
y_labels_raw_np = HGCW_dataset_utils['HGCW_labels']
vow_size = HGCW_dataset_utils['classes_size']
end_idx = HGCW_dataset_utils['classes_idx']

# Auxiliary lists
vowels = ['ae', 'ah', 'aw', 'eh', 'er', 'ei', 'ih', 'iy', 'oa', 'oo', 'uh', 'uw'] # Vowels list
colors = ['red', 'saddlebrown', 'darkorange', 'darkgoldenrod', 'gold', 'darkkhaki', 'olive', 'darkgreen', 'steelblue', 'fuchsia']

# Class-specific One-hot encoding (Binarization)
def one_hot_encoder(sel_class_number: int = 3, dataset: np.ndarray = x_data_minmax, orig_labels: int = len(vowels), classes_size: int = len(classes_size)):
    classes = [n for n in range(orig_labels)] # Class Labels list initialization

    # Auxiliary Parameters Initialization
    if sel_class_number < len(classes):
        classes.remove(sel_class_number) # REST Classes list
        if debug is True:
            print(f'Selected Class "{vowels[sel_class_number]}" : {classes_size[sel_class_number]} samples')
        sub_classes_size = classes_size[sel_class_number] // len(classes)
        if debug is True:
            print(f'Rest Classes size (...each): {sub_classes_size} samples')
```

```

# 1-Subset processing
sub_data = dataset[classes_idx[sel_class_number]: classes_idx[sel_class_number + 1], :] # Selected Class feature slice
sub_data_labels_bin = np.ones((classes_size[sel_class_number], 1), dtype='int') # Selected Class labels (1) creation
sub_data_labels = np.ones((classes_size[sel_class_number], 1), dtype='int') * sel_class_number

# 0-Subset processing
for i in classes:
    class_i_indices = np.random.choice(np.arange(classes_idx[i], classes_idx[i + 1], 1), size=sub_classes_size, replace=True)
    sub_class_i_array = dataset[class_i_indices, :]
    sub_class_labels_bin_array = np.zeros((sub_class_i_array.shape[0], 1), dtype='int') # Rest I-esimal Class labels
    sub_class_labels_array = np.ones((sub_class_i_array.shape[0], 1), dtype='int') * i

    # Outputs append
    sub_data = np.vstack((sub_data, sub_class_i_array))
    sub_data_labels_bin = np.vstack((sub_data_labels_bin, sub_class_labels_bin_array))
    sub_data_labels = np.vstack((sub_data_labels, sub_class_labels_array))
else:
    raise ValueError(f'Invalid Class ID: "{sel_class_number}" --> It must be less than {len(classes)}!')

return sub_data, sub_data_labels_bin, sub_data_labels

# Train/Test split (auxiliary function)
def train_test_split_aux(features_dataset, labels_dataset, test_perc, tolerance):
    """
    An auxiliary Train_Test_split function (based on Scikit Learn implementation) w. balance tolerance specification
    """
    test_size = int(test_perc / 100 * len(features_dataset))
    train_balance = 0 # Output Training set balance value initialization
    test_balance = 0 # Output Testing set balance value initialization

    min_tol = np.mean(labels_dataset) - tolerance
    max_tol = np.mean(labels_dataset) + tolerance
    print(f'Data Balancing (TARGET = {np.mean(labels_dataset)} +- {tolerance}): ', end='')

    while (min_tol >= train_balance or train_balance >= max_tol) or (min_tol >= test_balance or test_balance >= max_tol):
        train_data, test_data, train_labels, test_labels = train_test_split(features_dataset, labels_dataset, test_size=test_size, random_state=None)
        train_balance = np.mean(train_labels)
        test_balance = np.mean(test_labels)
        print('.', end='')
    else:
        print('OK')

    return train_data, test_data, train_labels, test_labels, train_balance, test_balance

# Train-Dev-Test split function
def train_dev_test_split(x_data, y_labels, split_list, tolerance=0.1, output='Loaders', debug=False):
    """
    Compute a Train, Development (Hold-Out) and a Test set split w. PyTorch Dataset conversion (and eventual Loaders initialization)
    """
    if len(split_list) == 3:
        # Train - Dev+Test separation
        print('Training --- Devel/Test SPLIT')
        train_data, testTMP_data, train_labels, testTMP_labels, _, _ = train_test_split_aux(x_data, y_labels, (split_list[1] * 100))
        print('-----')

        # Dev - Test separation
        print('Devel --- Test SPLIT')

        split = ((split_list[1] * 100) / np.sum(split_list[1:] * 100)) * 100 # Split in %
        dev_data, test_data, dev_labels, test_labels, _, _ = train_test_split_aux(testTMP_data, testTMP_labels, split, tolerance=tolerance)
        print('-----')

        # Tensor Conversion
        train_data_tensor = torch.tensor(train_data).float()
        train_labels_tensor = torch.tensor(train_labels, dtype=torch.int64).squeeze()
        dev_data_tensor = torch.tensor(dev_data).float()
        dev_labels_tensor = torch.tensor(dev_labels, dtype=torch.int64).squeeze()
        test_data_tensor = torch.tensor(test_data).float()
        test_labels_tensor = torch.tensor(test_labels, dtype=torch.int64).squeeze()
        if debug is True:
            print(f'Training Data Shape: {train_data.shape}')
            print(f'Development Data Shape: {dev_data.shape}')
            print(f'Testing Data Shape: {test_data.shape}')

        # Balance Evaluation
        print(f'Training Set Balance: {np.mean(train_labels)}')
        print(f'Development Set Balance: {np.mean(dev_labels)}')
        print(f'Testing Set Balance: {np.mean(test_labels)}')

    if output != 'Loaders':
        return train_data_tensor, train_labels_tensor, dev_data_tensor, dev_labels_tensor, test_data_tensor, test_labels_tensor

```

```

else:
    # PyTorch Dataset Conversion
    train_dataset = torch.utils.data.TensorDataset(torch.tensor(train_data).float(), torch.tensor(train_labels, dtype=
dev_dataset = torch.utils.data.TensorDataset(torch.tensor(dev_data).float(), torch.tensor(dev_labels, dtype=torch.
test_dataset = torch.utils.data.TensorDataset(torch.tensor(test_data).float(), torch.tensor(test_labels, dtype=torch.

    # DataLoader (Batches) --> Drop-Last control to optimize training
    trainLoader = DataLoader(train_dataset, shuffle=False, batch_size = 32, drop_last=True)
    devLoader = DataLoader(dev_dataset, shuffle=False, batch_size = dev_dataset.tensors[0].shape[0])
    testLoader = DataLoader(test_dataset, shuffle=False, batch_size = test_dataset.tensors[0].shape[0])
    if debug is True:
        print(f'Training Set      Batch Size: {trainLoader.batch_size}')
        print(f'Development Set Batch Size: {devLoader.batch_size}')
        print(f'Testing Set      Batch Size: {testLoader.batch_size}')

    return trainLoader, devLoader, testLoader
else:
    # Train - Test separation
    print('Training --- Test      SPLIT')
    train_data, test_data, train_labels, test_labels, _, _ = train_test_split_aux(x_data, y_labels, split_list[1] * 100, t
    print('-----')

    # Tensor Conversion
    train_data_tensor = torch.tensor(train_data).float()
    train_labels_tensor = torch.tensor(train_labels, dtype=torch.int64).squeeze()
    test_data_tensor = torch.tensor(test_data).float()
    test_labels_tensor = torch.tensor(test_labels, dtype=torch.int64).squeeze()
    if debug is True:
        print(f'Training Data      Shape: {train_data.shape}')
        print(f'Testing Data      Shape: {test_data.shape}')

    # Balance Evaluation
    print(f'Training Set      Balance: {np.mean(train_labels)}')
    print(f'Testing Set      Balance: {np.mean(test_labels)}')

    if output != 'Loaders':
        return train_data_tensor, train_labels_tensor, test_data_tensor, test_labels_tensor
    else:
        # PyTorch Dataset Conversion
        train_dataset = torch.utils.data.TensorDataset(torch.tensor(train_data).float(), torch.tensor(train_labels, dtype=
        test_dataset = torch.utils.data.TensorDataset(torch.tensor(test_data).float(), torch.tensor(test_labels, dtype=torch.

        # DataLoader (Batches) --> Drop-Last control to optimize training
        trainLoader = DataLoader(train_dataset, shuffle=False, batch_size = 32, drop_last=True)
        testLoader = DataLoader(test_dataset, shuffle=False, batch_size = test_dataset.tensors[0].shape[0])
        if debug is True:
            print(f'Training Set      Batch Size: {trainLoader.batch_size}')
            print(f'Testing Set      Batch Size: {testLoader.batch_size}')

        return trainLoader, testLoader

```

## ▼ One-Class Architecture (Binary Classifier)

(see "One-Class\_Sub-Network\_Analysis.ipynb")

Multi-Layer Perceptron

- Input Layer: 3 features [formant ratios, min-max normalized]
- Hidden Layer: 100 units
- Output Layer: 1 normalized probability
- Learning Rate: 0.0001 ( $10^{-4}$ )
- Optimizer: Adam (Adaptive Momentum)

- Mini-Batch Training:

- . Re-iterated Sub-Dataset Shuffling
- . Early Stopping (Test Accuracy driven)
- . Batch size = 32

- Regularization:

- . Weight Decay (L2 Penalty): 0.0001 ( $10^{-4}$ )
- . Dropout:
  - \* Input Layer Drop Rate: 0.8
  - \* Hidden Layer Drop Rate: 0.5.
- . Batch Normalization

- *MLP Classifier Architecture* class definition
- *Mini-Batch Training* function definition

```

# Dynamic Multi-Layer Architecture Class (w. units, activation function, batch normalization and dropOut rate specification)
class binaryClassifier(nn.Module):
    def __init__(self, n_units, act_fun, rate_in, rate_hidden, model_name):
        super().__init__()

        self.layers = nn.ModuleDict()
        self.name = model_name

        # Input Layer
        self.layers['input'] = nn.Linear(3, n_units)

        # Hidden Layer
        self.layers[f'hidden'] = nn.Linear(n_units, n_units)
        self.layers[f'batch_norm'] = nn.BatchNorm1d(n_units)

        # Output Layer
        self.layers['output'] = nn.Linear(n_units, 1)

        # Activation Function
        self.actfun = act_fun

        # Dropout Parameter
        self.dr_in = rate_in
        self.dr_hidden = rate_hidden

        # Weights & Bias initialization
        for layer in self.layers.keys():
            try:
                nn.init.kaiming_normal_(self.layers[layer].weight, mode='fan_in')
            except:
                pass
            self.layers[layer].bias.data.fill_(0.)

# Forward Pass Method
def forward(self, x):

    # Activation function object computation
    actfun = getattr(torch.nn, self.actfun)

    # Input Layer pass
    x = actfun()(self.layers['input'](x))
    x = F.dropout(x, p=self.dr_in, training=self.training)

    # Single Hidden Layer pass
    x = self.layers[f'batch_norm'](x)
    x = actfun()(self.layers[f'hidden'](x))
    x = F.dropout(x, p=self.dr_hidden, training=self.training)

    # Output Layer pass
    x = self.layers['output'](x)
    x = nn.Sigmoid()(x)

    return x

# Batch Training function (w. Adam Optimizer & L2 penalty term) Re-Definition
def mini_batch_train_test(model, weight_decay, epochs: int, learning_rate, train_loader, dev_loader, test_loader, debug=False)
    """
    Train & Test an ANN Architecture via Mini-Batch Training (w. Train/Dev/Test PyTorch Loaders) and Adam Backpropagation Opti
    """
    # Loss Function initialization
    loss_function = nn.BCELoss()

    # Optimizer Algorithm initialization
    optimizer = torch.optim.Adam(model.parameters(), lr=learning_rate, weight_decay=weight_decay)

    # Output list initialization
    train_accuracies = []
    train_losses = []
    dev_accuracies = []

    # TRAINING Phase
    for epoch in range(epochs):
        model.train() # TRAINING Switch ON

        batch_accuracies = []
        batch_losses = []

        # Training BATCHES Loop
        for data_batch, labels_batch in train_loader:
            train_predictions = model(data_batch)
            train_loss = loss_function(train_predictions.squeeze(), labels_batch.type(torch.int64).float())

```

```

        batch_losses.append(train_loss.detach())

    # Backpropagation
    optimizer.zero_grad()
    train_loss.backward()
    optimizer.step()

    # Accuracy
    train_accuracy = 100 * torch.mean(((train_predictions.squeeze() > 0.5) == labels_batch.type(torch.int64).squeeze()))

    # Batch Stats appending
    batch_accuracies.append(train_accuracy.detach())
    batch_losses.append(train_loss.detach())

# Training Stats appending
train_accuracies.append(np.mean(batch_accuracies)) # Average of Batch Accuracies = Training step accuracy
train_losses.append(np.mean(batch_losses)) # Average of Batch Losses = Training step Losses

# EVALUATION (Dev) Phase
model.eval()
with torch.no_grad():
    dev_data_batch, dev_labels_batch = next(iter(dev_loader))
    dev_predictions = model(dev_data_batch)

    dev_accuracy = 100 * torch.mean(((dev_predictions.squeeze() > 0.5) == dev_labels_batch.type(torch.int64).squeeze()))

    if debug is True:
        if epoch % 100 == 0:
            print(f'Epoch {epoch} --> DEV ACCURACY: {dev_accuracy.detach():.3f} %')
            print('-----')

    # Evaluation accuracy appending
    dev_accuracies.append(dev_accuracy.detach())

# TEST Phase
model.eval()
with torch.no_grad():
    test_data_batch, test_labels_batch = next(iter(test_loader))
    test_predictions = model(test_data_batch)
    test_accuracy = 100 * torch.mean(((test_predictions.squeeze() > 0.5) == test_labels_batch.type(torch.int64).squeeze()))

    if debug is True:
        print(f'TEST ACCURACY: {test_accuracy.detach():.2f} %')
        print('-----')

return train_accuracies, train_losses, dev_accuracies, test_accuracy.detach()

```

## ▼ OCON (One-Class-One-Net) Model

### Binary classifiers **Parallelization**

- *Classifiers-Bank* function definition
  - *Models Parameters* inspection
- Classifiers **Sequential** Training & Evaluation
- *Models Parameters State Save/Load* function definition

- 
- MaxNet output algorithm
  - Argmax output algorithm

```

def OCON_bank(one_class_function, hidden_units, act_fun, dr_in, dr_hidden, classes_list):
    """
    Create a One-Class-One-Network parallelization bank of an input Sub-Network definition
    """
    # Sub-Net names creation
    models_name_list = []
    for i in range(len(classes_list)):
        models_name_list.append("{}_{}".format(classes_list[i], "subnet")) # Class name + _subnet

    # Sub-Networks instances creation
    sub_nets = [] # Sub Network list initialization

    for i in range(len(models_name_list)):

        torch.manual_seed(SEED) # Seed re-initialization

        # Sub-Net instance creation
        locals()[models_name_list[i]] = one_class_function(hidden_units, act_fun, dr_in, dr_hidden, models_name_list[i])
        sub_nets.append(locals()[models_name_list[i]])

```

```

    return sub_nets

# Load Architecture Parameters State function
def load_model_state(model, state_dict_path):
    """
    Load an existent State Dictionary in a defined model
    """

    model.load_state_dict(torch.load(state_dict_path))
    print(f'Loaded Parameters (from "{state_dict_path}") into: {model.name}')

    return model

# Build The OCON Model
ocon_vowels = OCON_bank(binaryClassifier, 100, 'ReLU', 0.8, 0.5, vowels) # Best MLP (see "One-Class_Binary_Classifier_Analysi

# Load Pre-Trained Architectures in a fresh Model instance:
#ocon_vowels = OCON_bank(binaryClassifier, 100, 'ReLU', 0.8, 0.5, vowels) # Best MLP (see "One-Class_Binary_Classifier_Analysi
#states_path = ["Trained_models_state/ae_subnet_Params.pth",
#               "Trained_models_state/ah_subnet_Params.pth",
#               "Trained_models_state/aw_subnet_Params.pth",
#               "Trained_models_state/eh_subnet_Params.pth",
#               "Trained_models_state/er_subnet_Params.pth",
#               "Trained_models_state/ei_subnet_Params.pth",
#               "Trained_models_state/ih_subnet_Params.pth",
#               "Trained_models_state/iy_subnet_Params.pth",
#               "Trained_models_state/oa_subnet_Params.pth",
#               "Trained_models_state/oo_subnet_Params.pth",
#               "Trained_models_state/uh_subnet_Params.pth",
#               "Trained_models_state/uw_subnet_Params.pth"]
#
#for i in range(len(ocon_vowels)):
#    load_model_state(ocon_vowels[i], states_path[i])

# OCON Evaluation function
def OCON_eval(ocon_models_bank, features_dataset: np.ndarray = x_data_minmax[:, 1:], labels: np.ndarray = y_labels_raw_np):
    """
    Evaluate OCON models-bank over an entire dataset
    """
    # Output lists initialization
    predictions = []
    dist_errors = []
    eval_accuracies = []
    g_truths = [] # For plotting purposes

    # Evaluate each Sub-Network...
    for i in range(len(ocon_models_bank)):
        ocon_models_bank[i].eval() # Put j-esimal Sub-Network in Evaluation Mode
        print(f'{ocon_models_bank[i].name.upper()} Evaluation -', end=' ')

        with torch.no_grad():

            # Make predictions
            features_data_tensor = torch.tensor(features_dataset).float()
            raw_eval_predictions = ocon_models_bank[i](features_data_tensor)

            # Create Ground Truths
            ground_truth = np.where(labels == i, 1, 0)
            ground_truth_tensor = torch.tensor(ground_truth, dtype=torch.int64).squeeze()

            # Compute Errors
            dist_error = ground_truth_tensor - raw_eval_predictions.detach().squeeze() # Distances
            eval_accuracy = 100 * torch.mean(((raw_eval_predictions.detach().squeeze() > 0.5) == ground_truth_tensor).float())
            print(f'Accuracy: {eval_accuracy:.2f}%')

            # Outputs append
            predictions.append(raw_eval_predictions.detach())
            dist_errors.append(dist_error.detach())
            eval_accuracies.append(eval_accuracy.detach())

        g_truths.append(ground_truth)

    return predictions, dist_errors, eval_accuracies, g_truths

# For Pre-Trained Models
#ocon_predictions, ocon_dist_errors, ocon_eval_accuracies, ocon_g_truths = OCON_eval(ocon_vowels)

# Model Parameters State function
def model_desc(model):

```



```

"""
Print a Console report of Neural Network Model parameters
"""
# Parameters Description
print('Params Description:')
trainable_params = 0

for parameter in model.named_parameters():
    print(f'Parameter Name      : {parameter[0]}')
    print(f'Parameter Weights   : {parameter[1][:]}')
    if parameter[1].requires_grad:
        print(f'...with {parameter[1].numel()} TRAINABLE parameters')
        trainable_params += parameter[1].numel()

    print('.....')

print('-----')

# Nodes Count
nodes = 0
for param_name, param_tensor in model.named_parameters():
    if 'bias' in param_name:
        nodes += len(param_tensor)

print(f'Total Nodes          : {nodes}')
print('-----')

# OCON-Model Description
for i in range(len(ocon_vowels)):
    print(f'OCON "{ocon_vowels[i].name}" Classifier STATE')
    model_desc(ocon_vowels[i])
    print()

# Training/Eval/Testing Parameters
epochs = 1000 # For each "Data Batch-Set"
loss_break = 0.20 # loss (for Early Stopping)
acc_break = 90. # % accuracy (for Early Stopping)
min_tolerance = 0.01 # ...for sub-dataset balancing

# Outputs Initialization
loss_functions = [[] for _ in range(len(ocon_vowels))]
training_accuracies = [[] for _ in range(len(ocon_vowels))]
evaluation_accuracies = [[] for _ in range(len(ocon_vowels))]
test_accuracies = [[] for _ in range(len(ocon_vowels))]
training_times = []

# OCON Sub-Networks Training
from time import perf_counter
debug = False

for i, vowel in enumerate(vowels):
    print(f'Architecture "{ocon_vowels[i].name}" TRAINING PHASE')

    start_timer = perf_counter()
    # Iterated (w. Batch-Sets shuffling) Mini-Batch Training
    iteration = 0 # Batch Training iteration counter
    mean_loss = 1.
    test_accuracy = 0.

    while (mean_loss > loss_break) or (test_accuracy < acc_break):
        # Dataset processing
        sub_data, sub_data_labels_bin, _ = one_hot_encoder(sel_class_number=i, dataset=x_data_minmax, debug=debug)
        print('-----')
        trainLoader, devLoader, testLoader = train_dev_test_split(sub_data[:, 1:], sub_data_labels_bin, [0.5, 0.25, 0.25], tol

        # Train/Test Architecture
        train_accuracies, train_losses, dev_accuracies, test_accuracy = mini_batch_train_test(ocon_vowels[i], weight_decay=0.0
        print(f'Sub-Net "{vowel.upper()}" Epoch {(iteration + 1) * epochs} - TEST ACCURACY: {test_accuracy:.2f}%', end=' ')

        # Outputs append
        loss_functions[i].append(train_losses)
        training_accuracies[i].append(train_accuracies)
        evaluation_accuracies[i].append(dev_accuracies)
        test_accuracies[i].append(test_accuracy)

        # Repeating condition evaluation
        mean_loss = np.mean(train_losses[-50: ]) # Last 100 losses mean
        print(f'- MEAN LOSS: {mean_loss}')

    iteration += 1 # Go to next Batch training iteration

```

```

print(f'Training STOPPED at iteration {iteration}')
print('-----')
stop_timer = perf_counter()

print(f'"{ocon_vowels[i].name}" Training COMPLETED in {float(stop_timer - start_timer)}sec.')
training_times.append(stop_timer - start_timer)
print('-----')

# Graphical smoothing filter
def smooth(data, k=100):
    """
    A Convolution LP filter w. interval definition
    """
    return np.convolve(data, np.ones(k) / k, mode='same')

# Training Phase Plots
plt.figure(figsize=(12, 5 * 12))

# loss_functions, training_accuracies, evaluation_accuracies, test_accuracies, training_times
classes = len(ocon_vowels)

for i in range(classes):
    plt.subplot(classes, 2, (i * 2) + 1)
    flat_loss_function = [item for sublist in loss_functions[i] for item in sublist]

    plt.plot(smooth(flat_loss_function), 'k-')
    plt.axhline(loss_break, color='r', linestyle='--')
    plt.title(f'{ocon_vowels[i].name.upper()} Training Loss')
    plt.xlabel('Epochs')
    plt.xlim([100, len(flat_loss_function) - 100])
    plt.ylabel('GT - Predicted diff. (probability)')
    plt.grid()

    plt.subplot(classes, 2, (i * 2) + 2)
    flat_training_accuracy = [item for sublist in training_accuracies[i] for item in sublist]
    flat_dev_accuracy = [item for sublist in evaluation_accuracies[i] for item in sublist]
    flat_test_accuracy = test_accuracies[i]

    plt.plot(smooth(flat_training_accuracy), 'k-', label='Training')
    plt.plot(smooth(flat_dev_accuracy), color='grey', label='Development')
    if len(flat_test_accuracy) > 1:
        plt.plot([(n + 1) * epochs for n in range(len(flat_test_accuracy))], flat_test_accuracy, 'r-', label=f'Test')
    else:
        plt.axhline(test_accuracy, color='r', linestyle='-', label=f'Test')
    plt.title(f'{ocon_vowels[i].name.upper()} Accuracy (after {training_times[i]:.2f}sec.)')
    plt.xlabel('Epochs')
    plt.xlim([100, len(flat_training_accuracy) - 100])
    plt.ylabel('Accuracy (in %)')
    plt.ylim([40, 101])
    plt.grid()
    plt.legend(loc='best')

plt.tight_layout()
plt.savefig('OCON_training_phase')
plt.show()

# OCON Evaluation
ocon_predictions, ocon_dist_errors, ocon_eval_accuracies, ocon_g_truths = OCON_eval(ocon_vowels)

# Dataset Evaluation Analysis Plot
plt.figure(figsize=(22, 5 * len(ocon_vowels)))
plot_ticks = end_idx[:]
plot_ticks = np.delete(plot_ticks, -1)

for i in range(len(ocon_vowels)):
    plt.subplot(len(ocon_vowels), 3, (i * 3) + 1)
    plt.plot(ocon_predictions[i], 'k.', label='Raw Predictions')
    plt.plot(ocon_g_truths[i], 'rx', label='Ground Truths')
    plt.axhline(0.5, linestyle='--', color='grey')
    plt.title(f'{ocon_vowels[i].name.upper()} Predictions Accuracy: {ocon_eval_accuracies[i]:.2f}%')
    plt.xlabel('Data (Indices)')
    plt.xticks(ticks=plot_ticks, labels=vowels)
    plt.ylabel('Normalized Probability')
    plt.grid()
    plt.legend(loc='best')

    plt.subplot(len(ocon_vowels), 3, (i * 3) + 2)
    plt.plot(ocon_dist_errors[i], 'k')
    plt.title(f'Predicted to Measured Error')
    plt.xlabel('Data (Indices)')

```

```

plt.xticks(ticks=plot_ticks, labels=vowels)
plt.ylabel('Normalized Probability Error')
plt.ylim([-1.1, 1.1])
plt.grid()

plt.subplot(len(ocon_vowels), 3, (i * 3) + 3)

# Predictions list processing
predictions_temp = ocon_predictions[i]
class_predictions = [item for sublist in predictions_temp for item in sublist] # Turn a list of lists in a single list (c
for j in range(len(class_predictions)): # Turn a list of tensors of one variable in a list of scalars (item() method)
    class_predictions[j] = class_predictions[j].item()

# Positives & False-Positives extraction
positives = []
for w in range(len(vowels)):
    num = (np.array(class_predictions[end_idx[w]: end_idx[w + 1]]) > 0.5).sum()
    positives.append(num)

plt.bar(np.arange(len(vowels)), positives, color='k')
plt.title(f'"{vowels[i]}" Positive Probabilities Distribution')
plt.xlabel('Normalized Probabilities')
plt.ylabel('Occurences')
plt.xticks([n for n in range(12)], vowels)
plt.grid()

plt.tight_layout()
plt.savefig('OCON_bank_evaluation')
plt.show()

# Model Parameters Save/Load functions
from pathlib import Path

def save_model_state(model, folder_name: str = "Trained_models_state"):
    """
    Save Pre-Trained model parameters in a State Dictionary
    """

    MODEL_PATH = Path(folder_name) # Placed in root
    MODEL_PATH.mkdir(parents=True, exist_ok=True) # Pre-existing folder (w. same name) monitoring
    MODEL_NAME = '{}_{}'.format(model.name, "Params.pth")
    MODEL_SAVE_PATH = MODEL_PATH / MODEL_NAME

    print(f"Saving {model.name} Parameters in: {MODEL_SAVE_PATH}")
    torch.save(obj=model.state_dict(), f=MODEL_SAVE_PATH)

    return MODEL_SAVE_PATH

# Save Pre-Trained Models-bank
states_path = [] # Path for each model parameters state
for i in range(len(ocon_vowels)):
    state_path = save_model_state(ocon_vowels[i])
    states_path.append(state_path)
print()

```

## ▼ Output Maxnet Algorithm

```

# OCON "MaxNet" Architecture (Weightening + Non Linearity apply)
class OCON_MaxNet(nn.Module):
    def __init__(self, n_units, act_fun, eps):
        super().__init__()

        self.layers = nn.ModuleDict() # Dictionary to store Model layers
        self.eps_weight = eps

        # MaxNet Layer
        self.layers['MAXNET'] = nn.Linear(n_units, n_units) # Key 'MaxNet' layer specification

        # Weights & Bias initialization
        self.layers['MAXNET'].weight.data.fill_(self.eps_weight)
        for i in range(n_units):
            self.layers['MAXNET'].weight[i][i].data.fill_(1.) # Self Weight = 1

        self.layers['MAXNET'].bias.data.fill_(0.)

        # Activation Function
        self.actfun = act_fun # Function string-name attribute association

# Forward Pass Method

```

```

def forward(self, x):

    # Activation function object computation
    actfun = getattr(torch.nn, self.actfun)

    # Maxnet Layer pass                                     --> Output Weightening (Dot Product) "Linear transfo
    x = actfun()(self.layers['MAXNET'](x.squeeze().float()))

    # Self

    return x

# Build OCON MaxNetwork Architecture
torch.manual_seed(SEED)
ocon_maxnet = OCON_MaxNet(n_units=12, act_fun='ReLU', eps=0.25)

# MaxNet & Sub-Networks Parameters
print('OCON MaxNet STATE')
model_desc(ocon_maxnet)

def maxnet_algo(maxnet_function, n_units, act_fun, eps, input_array):
    """
    MaxNet Re-iteration algorithm for Maximum Value retrieving from an input array
    """
    non_zero_outs = np.count_nonzero(input_array) # Non Zero Values initialization
    maxnet_in = torch.from_numpy(input_array) # MaxNet Input Tensor initialization

    results = [] # Results initialization

    counter = 0
    while non_zero_outs != 1:
        counter += 1

        # Create the MaxNet
        torch.manual_seed(SEED) # Redundant
        maxnet = maxnet_function(n_units = n_units, act_fun = act_fun, eps = eps)

        # Compute Forward Pass
        results = maxnet(maxnet_in)

        # Non_zero outputs & Maxnet Input Update
        non_zero_outs = np.count_nonzero(results.detach().numpy())
        maxnet_in = results.detach() # Save results for next iteration

    print(f'Maximum Value found in {counter} iterations')
    return np.argmax(results.detach().numpy())

# MaxNet on Sub-Networks predictions
ocon_predictions_prob = np.zeros((len(ocon_predictions), x_data_minmax.shape[0])) # NumPy predictions matrix (12 * 1617)

# Convert from List of Tensors to 2D NumPy Array
for i in range(len(ocon_predictions)):
    ocon_predictions_prob[i, :] = ocon_predictions[i].detach().squeeze().numpy()

maxnet_class_predictions = [] # Classes Outputs list initialization
# MaxNet application
for i in range(x_data_minmax.shape[0]):
    print(f'Dataset Sample({i + 1}) Class Evaluation')

    samp_predictions = ocon_predictions_prob[:, i] # Array of 12 predictions for each Dataset sample (OCON outputs)
    class_prediction = maxnet_algo(OCON_MaxNet, n_units=12, act_fun='ReLU', eps=-0.1, input_array=samp_predictions) # MaxNet
    maxnet_class_predictions.append(class_prediction) # Result appending
    print('-----')

maxnet_accuracy = 100 * np.mean((np.array(maxnet_class_predictions).reshape(1617, 1) == y_labels_raw_np)) # Accuracy computat
print(f'Maxnet Output --> Phoneme ACCURACY: {maxnet_accuracy}%')

# Argmax on Sub-Networks predictions (...for multiple 1s probabilities MaxNet infinite loops)
#ocon_predictions_prob = np.zeros((len(new_ocon_predictions), x_data_minmax.shape[0])) # NumPy predictions matrix (12 * 1617)
#
# Convert from List of Tensors to 2D NumPy Array
#for i in range(len(new_ocon_predictions)):
#    ocon_predictions_prob[i, :] = new_ocon_predictions[i].detach().squeeze().numpy()
#
#maxnet_class_predictions = np.argmax(ocon_predictions_prob, axis=0)
#maxnet_accuracy = 100 * np.mean((np.array(maxnet_class_predictions).reshape(1617, 1) == y_labels_raw_np)) # Accuracy computa
#print(f'Maxnet Output ACCURACY: {maxnet_accuracy}%')

```

```

# Evaluation Analysis Plot
plt.figure(figsize=(30, 5))
plt.suptitle(f'OCON Bank + MaxNet Evaluation: {maxnet_accuracy:.0f}%')

plot_x_ticks = end_idx[:]
plot_x_ticks = np.delete(plot_x_ticks, len(end_idx) - 1)
plot_y_ticks = [n for n in range(len(vowels))]

plt.plot(y_labels_raw_np, 'rs', label='Ground Truths')
plt.plot(maxnet_class_predictions, 'k.', label='MAXNET Outputs')
plt.xlabel('Dataset samples')
plt.xticks(ticks=plot_x_ticks, labels=vowels)
plt.xlim([-10, len(y_labels_raw_np) + 10])
plt.ylabel('Labels')
plt.yticks(ticks=plot_y_ticks, labels=vowels)
plt.legend(loc='best')
plt.grid()

plt.tight_layout()
plt.savefig('OCON_model_evaluation')
plt.show()

```

## Further improvements

- 1) Repeat Training Cycle in order to increase Loss minimization ( $< 0.1$ ,  $< 0.05$ )
- 2) Other Datasets Evaluation
- 3) Ratios multi-resolution transform (Bark, ERB, Mel)
- 4) Dataset Augmentation via Pitch Shifting: mean fund, mean ratios + artificial randomness (variance)

- 
- 1) Spectral features (HGCW dataset)



## ▼ OCON Model Analysis

(4-features Complete Dataset)

**Author:** S. Giacomelli

**Year:** 2023

**Affiliation:** A.Casella Conservatory (student)

**Master Degree Thesis:** "Vowel phonemes Analysis & Classification by means of OCON rectifiers Deep Learning Architectures"

**Description:** Python scripts for One-Class-One-Network (OCON) Model analysis and optimization

```
# Numerical computations packages/modules
import numpy as np
import torch
import torch.nn as nn
import torch.nn.functional as F

# Dataset processing modules
from torch.utils.data import DataLoader
from sklearn.model_selection import train_test_split

# Graphic visualization modules
import matplotlib.pyplot as plt
import matplotlib_inline
matplotlib_inline.backend_inline.set_matplotlib_formats('svg')

# Common Seed initialization
SEED = 42 # ... the answer to the ultimate question of Life, the Universe, and Everything... (cit.)

# PyTorch Processing Units evaluation
device = 'cuda' if torch.cuda.is_available() else 'cpu'
print(f'AVAILABLE Processing Unit: {device.upper()}')
!nvidia-smi
```

## ▼ HGCW Dataset

- *Dataset\_utils.npz* file read
- *One-Hot encoding* definition
- *Train/Dev/Test split* definition

```
# Load HGCW 4_features_all Dataset
HGCW_dataset_utils = np.load(file='./HGCW_dataset_utils.npz')
print('Raw features Data shape:', HGCW_dataset_utils['HGCW_raw'].shape)
print('Fundamental Normalized features Data shape:', HGCW_dataset_utils['HGCW_fund_norm'].shape)
print('MinMax features Data shape:', HGCW_dataset_utils['HGCW_minmax'].shape)
print('Labels Data shape:', HGCW_dataset_utils['HGCW_labels'].shape)
print('Classes size Data shape:', HGCW_dataset_utils['classes_size'].shape)
print('Classes indices Data shape:', HGCW_dataset_utils['classes_idx'].shape)

x_data_raw_np = HGCW_dataset_utils['HGCW_raw']
x_data_fund_norm = HGCW_dataset_utils['HGCW_fund_norm']
x_data_minmax = HGCW_dataset_utils['HGCW_minmax']
y_labels_raw_np = HGCW_dataset_utils['HGCW_labels']
vow_size = HGCW_dataset_utils['classes_size']
end_idx = HGCW_dataset_utils['classes_idx']

# Auxiliary lists
vowels = ['ae', 'ah', 'aw', 'eh', 'er', 'ei', 'ih', 'iy', 'oa', 'oo', 'uh', 'uw'] # Vowels list
colors = ['red', 'saddlebrown', 'darkorange', 'darkgoldenrod', 'gold', 'darkkhaki', 'olive', 'darkgreen', 'steelblue', 'fuchsia']

# Fundamental Frequencies Min-Max Normalization
a = 0
b = 1
x_data_minmax[:, 0] = a + ((x_data_minmax[:, 0] - x_data_minmax[:, 0].min()) / (x_data_minmax[:, 0].max() - x_data_minmax[:, 0].min()))
x_data_minmax[:, 1:] = x_data_minmax[:, 1:] # Fundamental column exception

# Class-specific One-hot encoding (Binarization)
def one_hot_encoder(sel_class_number: int = 3, dataset: np.ndarray = x_data_minmax, orig_labels: int = len(vowels), classes_size: int = len(colors)):
    classes = [n for n in range(orig_labels)] # Class Labels list initialization

    # Auxiliary Parameters Initialization
    if sel_class_number < len(classes):
```

```

classes.remove(sel_class_number) # REST Classes list
if debug is True:
    print(f'Selected Class "{vowels[sel_class_number]}" : {classes_size[sel_class_number]} samples')
sub_classes_size = classes_size[sel_class_number] // len(classes)
if debug is True:
    print(f'Rest Classes size (...each): {sub_classes_size} samples')

# 1-Subset processing
sub_data = dataset[classes_idx[sel_class_number]: classes_idx[sel_class_number + 1], :] # Selected Class feature slice
sub_data_labels_bin = np.ones((classes_size[sel_class_number], 1), dtype='int') # Selected Class labels (1) creation
sub_data_labels = np.ones((classes_size[sel_class_number], 1), dtype='int') * sel_class_number

# 0-Subset processing
for i in classes:
    class_i_indices = np.random.choice(np.arange(classes_idx[i], classes_idx[i + 1], 1), size=sub_classes_size, replace=True)
    sub_class_i_array = dataset[class_i_indices, :]
    sub_class_labels_bin_array = np.zeros((sub_class_i_array.shape[0], 1), dtype='int') # Rest I-esimal Class labels
    sub_class_labels_array = np.ones((sub_class_i_array.shape[0], 1), dtype='int') * i

    # Outputs append
    sub_data = np.vstack((sub_data, sub_class_i_array))
    sub_data_labels_bin = np.vstack((sub_data_labels_bin, sub_class_labels_bin_array))
    sub_data_labels = np.vstack((sub_data_labels, sub_class_labels_array))
else:
    raise ValueError(f'Invalid Class ID: "{sel_class_number}" --> It must be less than {len(classes)}!')

return sub_data, sub_data_labels_bin, sub_data_labels

# Train/Test split (auxiliary function)
def train_test_split_aux(features_dataset, labels_dataset, test_perc, tolerance):
    """
    An auxiliary Train_Test_split function (based on Scikit Learn implementation) w. balance tolerance specification
    """
    test_size = int(test_perc / 100 * len(features_dataset))
    train_balance = 0 # Output Training set balance value initialization
    test_balance = 0 # Output Testing set balance value initialization

    min_tol = np.mean(labels_dataset) - tolerance
    max_tol = np.mean(labels_dataset) + tolerance
    print(f'Data Balancing (TARGET = {np.mean(labels_dataset)} +- {tolerance}): ', end='')

    while (min_tol >= train_balance or train_balance >= max_tol) or (min_tol >= test_balance or test_balance >= max_tol):
        train_data, test_data, train_labels, test_labels = train_test_split(features_dataset, labels_dataset, test_size=test_size, random_state=None)
        train_balance = np.mean(train_labels)
        test_balance = np.mean(test_labels)
        print('.', end='')
    else:
        print('OK')

    return train_data, test_data, train_labels, test_labels, train_balance, test_balance

# Train-Dev-Test split function
def train_dev_test_split(x_data, y_labels, split_list, tolerance=0.1, output='Loaders', debug=False):
    """
    Compute a Train, Development (Hold-Out) and a Test set split w. PyTorch Dataset conversion (and eventual Loaders initialization)
    """
    if len(split_list) == 3:
        # Train - Dev+Test separation
        print('Training --- Devel/Test SPLIT')
        train_data, testTMP_data, train_labels, testTMP_labels, _, _ = train_test_split_aux(x_data, y_labels, (split_list[1] * 100) / np.sum(split_list[1:] * 100), tolerance)
        print('-----')

        # Dev - Test separation
        print('Devel --- Test SPLIT')

        split = ((split_list[1] * 100) / np.sum(split_list[1:] * 100)) * 100 # Split in %
        dev_data, test_data, dev_labels, test_labels, _, _ = train_test_split_aux(testTMP_data, testTMP_labels, split, tolerance)
        print('-----')

        # Tensor Conversion
        train_data_tensor = torch.tensor(train_data).float()
        train_labels_tensor = torch.tensor(train_labels, dtype=torch.int64).squeeze()
        dev_data_tensor = torch.tensor(dev_data).float()
        dev_labels_tensor = torch.tensor(dev_labels, dtype=torch.int64).squeeze()
        test_data_tensor = torch.tensor(test_data).float()
        test_labels_tensor = torch.tensor(test_labels, dtype=torch.int64).squeeze()
        if debug is True:
            print(f'Training Data Shape: {train_data.shape}')
            print(f'Development Data Shape: {dev_data.shape}')
            print(f'Testing Data Shape: {test_data.shape}')

        # Balance Evaluation

```



```

        print(f'Training Set      Balance: {np.mean(train_labels)}')
        print(f'Development Set  Balance: {np.mean(dev_labels)}')
        print(f'Testing Set     Balance: {np.mean(test_labels)}')

    if output != 'Loaders':
        return train_data_tensor, train_labels_tensor, dev_data_tensor, dev_labels_tensor, test_data_tensor, test_labels_t
    else:
        # PyTorch Dataset Conversion
        train_dataset = torch.utils.data.TensorDataset(torch.tensor(train_data).float(), torch.tensor(train_labels, dtype=
        dev_dataset = torch.utils.data.TensorDataset(torch.tensor(dev_data).float(), torch.tensor(dev_labels, dtype=torch.
        test_dataset = torch.utils.data.TensorDataset(torch.tensor(test_data).float(), torch.tensor(test_labels, dtype=torch.

        # DataLoader (Batches) --> Drop-Last control to optimize training
        trainLoader = DataLoader(train_dataset, shuffle=False, batch_size = 32, drop_last=True)
        devLoader = DataLoader(dev_dataset, shuffle=False, batch_size = dev_dataset.tensors[0].shape[0])
        testLoader = DataLoader(test_dataset, shuffle=False, batch_size = test_dataset.tensors[0].shape[0])
        if debug is True:
            print(f'Training Set      Batch Size: {trainLoader.batch_size}')
            print(f'Development Set Batch Size: {devLoader.batch_size}')
            print(f'Testing Set     Batch Size: {testLoader.batch_size}')

        return trainLoader, devLoader, testLoader
else:
    # Train - Test separation
    print('Training --- Test      SPLIT')
    train_data, test_data, train_labels, test_labels, _, _ = train_test_split_aux(x_data, y_labels, split_list[1] * 100, t
    print('-----')

    # Tensor Conversion
    train_data_tensor = torch.tensor(train_data).float()
    train_labels_tensor = torch.tensor(train_labels, dtype=torch.int64).squeeze()
    test_data_tensor = torch.tensor(test_data).float()
    test_labels_tensor = torch.tensor(test_labels, dtype=torch.int64).squeeze()
    if debug is True:
        print(f'Training Data      Shape: {train_data.shape}')
        print(f'Testing Data       Shape: {test_data.shape}')

    # Balance Evaluation
    print(f'Training Set      Balance: {np.mean(train_labels)}')
    print(f'Testing Set     Balance: {np.mean(test_labels)}')

    if output != 'Loaders':
        return train_data_tensor, train_labels_tensor, test_data_tensor, test_labels_tensor
    else:
        # PyTorch Dataset Conversion
        train_dataset = torch.utils.data.TensorDataset(torch.tensor(train_data).float(), torch.tensor(train_labels, dtype=
        test_dataset = torch.utils.data.TensorDataset(torch.tensor(test_data).float(), torch.tensor(test_labels, dtype=torch.

        # DataLoader (Batches) --> Drop-Last control to optimize training
        trainLoader = DataLoader(train_dataset, shuffle=False, batch_size = 32, drop_last=True)
        testLoader = DataLoader(test_dataset, shuffle=False, batch_size = test_dataset.tensors[0].shape[0])
        if debug is True:
            print(f'Training Set      Batch Size: {trainLoader.batch_size}')
            print(f'Testing Set     Batch Size: {testLoader.batch_size}')

        return trainLoader, testLoader

```

## ▼ One-Class Architecture (Binary Classifier)

(see "[One-Class\\_Sub-Network\\_Analysis.ipynb](#)")

Multi-Layer Perceptron

- Input Layer: 3 features [formant ratios, min-max normalized]
- Hidden Layer: 100 units
- Output Layer: 1 normalized probability
- Learning Rate: 0.0001 ( $10^{-4}$ )
- Optimizer: Adam (Adaptive Momentum)

- Mini-Batch Training:

- . Re-iterated Sub-Dataset Shuffling
- . Early Stopping (Test Accuracy driven)
- . Batch size = 32

- Regularization:

- . Weight Decay (L2 Penalty): 0.0001 ( $10^{-4}$ )
- . Dropout:
  - \* Input Layer Drop Rate: 0.8

```

    * Hidden Layer Drop Rate: 0.5.
. Batch Normalization

```

- *MLP Classifier Architecture* class definition
- *Mini-Batch Training* function definition

```

# Dynamic Multi-Layer Architecture Class (w. units, activation function, batch normalization and dropOut rate specification)
class binaryClassifier(nn.Module):
    def __init__(self, n_units, act_fun, rate_in, rate_hidden, model_name):
        super().__init__()

        self.layers = nn.ModuleDict()
        self.name = model_name

        # Input Layer
        self.layers['input'] = nn.Linear(4, n_units)

        # Hidden Layer
        self.layers[f'hidden'] = nn.Linear(n_units, n_units)
        self.layers[f'batch_norm'] = nn.BatchNorm1d(n_units)

        # Output Layer
        self.layers['output'] = nn.Linear(n_units, 1)

        # Activation Function
        self.actfun = act_fun

        # Dropout Parameter
        self.dr_in = rate_in
        self.dr_hidden = rate_hidden

        # Weights & Bias initialization
        for layer in self.layers.keys():
            try:
                nn.init.kaiming_normal_(self.layers[layer].weight, mode='fan_in')
            except:
                pass
            self.layers[layer].bias.data.fill_(0.)

# Forward Pass Method
def forward(self, x):

    # Activation function object computation
    actfun = getattr(torch.nn, self.actfun)

    # Input Layer pass
    x = actfun()(self.layers['input'](x))
    x = F.dropout(x, p=self.dr_in, training=self.training)

    # Single Hidden Layer pass
    x = self.layers[f'batch_norm'](x)
    x = actfun()(self.layers[f'hidden'](x))
    x = F.dropout(x, p=self.dr_hidden, training=self.training)

    # Output Layer pass
    x = self.layers['output'](x)
    x = nn.Sigmoid()(x)

    return x

# Batch Training function (w. Adam Optimizer & L2 penalty term) Re-Definition
def mini_batch_train_test(model, weight_decay, epochs: int, learning_rate, train_loader, dev_loader, test_loader, debug=False)
    """
    Train & Test an ANN Architecture via Mini-Batch Training (w. Train/Dev/Test PyTorch Loaders) and Adam Backpropagation Opti
    """
    # Loss Function initialization
    loss_function = nn.BCELoss()

    # Optimizer Algorithm initialization
    optimizer = torch.optim.Adam(model.parameters(), lr=learning_rate, weight_decay=weight_decay)

    # Output list initialization
    train_accuracies = []
    train_losses = []
    dev_accuracies = []

    # TRAINING Phase
    for epoch in range(epochs):
        model.train() # TRAINING Switch ON

```

```

batch_accuracies = []
batch_losses = []

# Training BATCHES Loop
for data_batch, labels_batch in train_loader:
    train_predictions = model(data_batch)
    train_loss = loss_function(train_predictions.squeeze(), labels_batch.type(torch.int64).float())
    batch_losses.append(train_loss.detach())

    # Backpropagation
    optimizer.zero_grad()
    train_loss.backward()
    optimizer.step()

    # Accuracy
    train_accuracy = 100 * torch.mean(((train_predictions.squeeze() > 0.5) == labels_batch.type(torch.int64).squeeze()))

    # Batch Stats appending
    batch_accuracies.append(train_accuracy.detach())
    batch_losses.append(train_loss.detach())

# Training Stats appending
train_accuracies.append(np.mean(batch_accuracies)) # Average of Batch Accuracies = Training step accuracy
train_losses.append(np.mean(batch_losses)) # Average of Batch Losses = Training step Losses

# EVALUATION (Dev) Phase
model.eval()
with torch.no_grad():
    dev_data_batch, dev_labels_batch = next(iter(dev_loader))
    dev_predictions = model(dev_data_batch)

    dev_accuracy = 100 * torch.mean(((dev_predictions.squeeze() > 0.5) == dev_labels_batch.type(torch.int64).squeeze()))

    if debug is True:
        if epoch % 100 == 0:
            print(f'Epoch {epoch} --> DEV ACCURACY: {dev_accuracy.detach():.3f} %')
            print('-----')

    # Evaluation accuracy appending
    dev_accuracies.append(dev_accuracy.detach())

# TEST Phase
model.eval()
with torch.no_grad():
    test_data_batch, test_labels_batch = next(iter(test_loader))
    test_predictions = model(test_data_batch)
    test_accuracy = 100 * torch.mean(((test_predictions.squeeze() > 0.5) == test_labels_batch.type(torch.int64).squeeze()))

    if debug is True:
        print(f'TEST ACCURACY: {test_accuracy.detach():.2f} %')
        print('-----')

return train_accuracies, train_losses, dev_accuracies, test_accuracy.detach()

```

## ▼ OCON (One-Class-One-Net) Model

### Binary classifiers **Parallelization**

- *Classifiers-Bank* function definition
  - *Models Parameters* inspection
- Classifiers **Sequential** Training & Evaluation
- *Models Parameters State Save/Load* function definition

- MaxNet output algorithm
- Argmax output algorithm

```

def OCON_bank(one_class_function, hidden_units, act_fun, dr_in, dr_hidden, classes_list):
    """
    Create a One-Class-One-Network parallelization bank of an input Sub-Network definition
    """
    # Sub-Net names creation
    models_name_list = []
    for i in range(len(classes_list)):
        models_name_list.append("{}_{}".format(classes_list[i], "subnet")) # Class name + _subnet

    # Sub-Networks instances creation
    sub_nets = [] # Sub Network list initialization

```

```

for i in range(len(models_name_list)):

    torch.manual_seed(SEED) # Seed re-initialization

    # Sub-Net instance creation
    locals()[models_name_list[i]] = one_class_function(hidden_units, act_fun, dr_in, dr_hidden, models_name_list[i])
    sub_nets.append(locals()[models_name_list[i]])

return sub_nets

# Load Architecture Parameters State function
def load_model_state(model, state_dict_path):
    """
    Load an existent State Dictionary in a defined model
    """

    model.load_state_dict(torch.load(state_dict_path))
    print(f'Loaded Parameters (from "{state_dict_path}") into: {model.name}')

    return model

# Build The OCON Model
ocon_vowels = OCON_bank(binaryClassifier, 100, 'ReLU', 0.8, 0.5, vowels) # Best MLP (see "One-Class_Binary_Classifier_Analysis")

# Load Pre-Trained Architectures in a fresh Model instance:
#ocon_vowels = OCON_bank(binaryClassifier, 100, 'ReLU', 0.8, 0.5, vowels) # Best MLP (see "One-Class_Binary_Classifier_Analysis")
#states_path = ["Trained_models_state/ae_subnet_Params.pth",
#               "Trained_models_state/ah_subnet_Params.pth",
#               "Trained_models_state/aw_subnet_Params.pth",
#               "Trained_models_state/eh_subnet_Params.pth",
#               "Trained_models_state/er_subnet_Params.pth",
#               "Trained_models_state/ei_subnet_Params.pth",
#               "Trained_models_state/ih_subnet_Params.pth",
#               "Trained_models_state/iy_subnet_Params.pth",
#               "Trained_models_state/oa_subnet_Params.pth",
#               "Trained_models_state/oo_subnet_Params.pth",
#               "Trained_models_state/uh_subnet_Params.pth",
#               "Trained_models_state/uw_subnet_Params.pth"]
#
#for i in range(len(ocon_vowels)):
#    load_model_state(ocon_vowels[i], states_path[i])

# OCON Evaluation function
def OCON_eval(ocon_models_bank, features_dataset: np.ndarray = x_data_minmax, labels: np.ndarray = y_labels_raw_np):
    """
    Evaluate OCON models-bank over an entire dataset
    """

    # Output lists initialization
    predictions = []
    dist_errors = []
    eval_accuracies = []
    g_truths = [] # For plotting purposes

    # Evaluate each Sub-Network...
    for i in range(len(ocon_models_bank)):
        ocon_models_bank[i].eval() # Put j-esimal Sub-Network in Evaluation Mode
        print(f'{ocon_models_bank[i].name.upper()} Evaluation -', end=' ')

        with torch.no_grad():

            # Make predictions
            features_data_tensor = torch.tensor(features_dataset).float()
            raw_eval_predictions = ocon_models_bank[i](features_data_tensor)

            # Create Ground Truths
            ground_truth = np.where(labels == i, 1, 0)
            ground_truth_tensor = torch.tensor(ground_truth, dtype=torch.int64).squeeze()

            # Compute Errors
            dist_error = ground_truth_tensor - raw_eval_predictions.detach().squeeze() # Distances
            eval_accuracy = 100 * torch.mean(((raw_eval_predictions.detach().squeeze() > 0.5) == ground_truth_tensor).float())
            print(f'Accuracy: {eval_accuracy:.2f}%')

    # Outputs append
    predictions.append(raw_eval_predictions.detach())
    dist_errors.append(dist_error.detach())
    eval_accuracies.append(eval_accuracy.detach())

    g_truths.append(ground_truth)

```

```

    return predictions, dist_errors, eval_accuracies, g_truths

# For Pre-Trained Models
#ocon_predictions, ocon_dist_errors, ocon_eval_accuracies, ocon_g_truths = OCON_eval(ocon_vowels)

# Model Parameters State function
def model_desc(model):
    """
    Print a Console report of Neural Network Model parameters
    """
    # Parameters Description
    print('Params Description:')
    trainable_params = 0

    for parameter in model.named_parameters():
        print(f'Parameter Name      : {parameter[0]}')
        print(f'Parameter Weights   : {parameter[1][:]}')
        if parameter[1].requires_grad:
            print(f'...with {parameter[1].numel()} TRAINABLE parameters')
            trainable_params += parameter[1].numel()

    print('.....')

    print('-----')

    # Nodes Count
    nodes = 0
    for param_name, param_tensor in model.named_parameters():
        if 'bias' in param_name:
            nodes += len(param_tensor)

    print(f'Total Nodes          : {nodes}')
    print('-----')

# OCON-Model Description
for i in range(len(ocon_vowels)):
    print(f'OCON "{ocon_vowels[i].name}" Classifier STATE')
    model_desc(ocon_vowels[i])
    print()

# Training/Eval/Testing Parameters
epochs = 1000 # For each "Data Batch-Set"
loss_break = 0.20 # loss (for Early Stopping)
acc_break = 90. # % accuracy (for Early Stopping)
min_tolerance = 0.01 # ...for sub-dataset balancing

# Outputs Initialization
loss_functions = [[] for _ in range(len(ocon_vowels))]
training_accuracies = [[] for _ in range(len(ocon_vowels))]
evaluation_accuracies = [[] for _ in range(len(ocon_vowels))]
test_accuracies = [[] for _ in range(len(ocon_vowels))]
training_times = []

# OCON Sub-Networks Training
from time import perf_counter
debug = False

for i, vowel in enumerate(vowels):
    print(f'Architecture "{ocon_vowels[i].name}" TRAINING PHASE')

    start_timer = perf_counter()
    # Iterated (w. Batch-Sets shuffling) Mini-Batch Training
    iteration = 0 # Batch Training iteration counter
    mean_loss = 1.
    test_accuracy = 0.

    while (mean_loss > loss_break) or (test_accuracy < acc_break):
        # Dataset processing
        sub_data, sub_data_labels_bin, _ = one_hot_encoder(sel_class_number=i, dataset=x_data_minmax, debug=debug)
        print('-----')
        trainLoader, devLoader, testLoader = train_dev_test_split(sub_data, sub_data_labels_bin, [0.5, 0.25, 0.25], tolerance=

        # Train/Test Architecture
        train_accuracies, train_losses, dev_accuracies, test_accuracy = mini_batch_train_test(ocon_vowels[i], weight_decay=0.0
        print(f'Sub-Net "{vowel.upper()}" Epoch {(iteration + 1) * epochs} - TEST ACCURACY: {test_accuracy:.2f}%', end=' ')

        # Outputs append
        loss_functions[i].append(train_losses)
        training_accuracies[i].append(train_accuracies)
        evaluation_accuracies[i].append(dev_accuracies)

```

```

        test_accuracies[i].append(test_accuracy)

    # Repeating condition evaluation
    mean_loss = np.mean(train_losses[-50: ]) # Last 50 losses mean
    print(f'- MEAN LOSS: {mean_loss}')

    iteration += 1 # Go to next Batch training iteration

print(f'Training STOPPED at iteration {iteration}')
print('-----')
stop_timer = perf_counter()

print(f'"{ocon_vowels[i].name}" Training COMPLETED in {float(stop_timer - start_timer)}sec.')
training_times.append(stop_timer - start_timer)
print('-----')

# Graphical smoothing filter
def smooth(data, k=100):
    """
    A Convolution LP filter w. interval definition
    """
    return np.convolve(data, np.ones(k) / k, mode='same')

# Training Phase Plots
plt.figure(figsize=(12, 5 * 12))

# loss_functions, training_accuracies, evaluation_accuracies, test_accuracies, training_times
classes = len(ocon_vowels)

for i in range(classes):
    plt.subplot(classes, 2, (i * 2) + 1)
    flat_loss_function = [item for sublist in loss_functions[i] for item in sublist]

    plt.plot(smooth(flat_loss_function), 'k-')
    plt.axhline(loss_break, color='r', linestyle='--')
    plt.title(f'{ocon_vowels[i].name.upper()} Training Loss')
    plt.xlabel('Epochs')
    plt.xlim([100, len(flat_loss_function) - 100])
    plt.ylabel('GT - Predicted diff. (probability)')
    plt.grid()

    plt.subplot(classes, 2, (i * 2) + 2)
    flat_training_accuracy = [item for sublist in training_accuracies[i] for item in sublist]
    flat_dev_accuracy = [item for sublist in evaluation_accuracies[i] for item in sublist]
    flat_test_accuracy = test_accuracies[i]

    plt.plot(smooth(flat_training_accuracy), 'k-', label='Training')
    plt.plot(smooth(flat_dev_accuracy), color='grey', label='Development')
    if len(flat_test_accuracy) > 1:
        plt.plot([(n + 1) * epochs for n in range(len(flat_test_accuracy))], flat_test_accuracy, 'r-', label=f'Test')
    else:
        plt.axhline(test_accuracy, color='r', linestyle='-', label=f'Test')
    plt.title(f'{ocon_vowels[i].name.upper()} Accuracy (after {training_times[i]:.2f}sec.)')
    plt.xlabel('Epochs')
    plt.xlim([100, len(flat_training_accuracy) - 100])
    plt.ylabel('Accuracy (in %)')
    plt.ylim([40, 101])
    plt.grid()
    plt.legend(loc='best')

plt.tight_layout()
plt.savefig('OCON_training_phase')
plt.show()

# OCON Evaluation
ocon_predictions, ocon_dist_errors, ocon_eval_accuracies, ocon_g_truths = OCON_eval(ocon_vowels)

# Dataset Evaluation Analysis Plot
plt.figure(figsize=(18, 5 * len(ocon_vowels)))
plot_ticks = end_idx[:]
plot_ticks = np.delete(plot_ticks, -1)

for i in range(len(ocon_vowels)):
    plt.subplot(len(ocon_vowels), 3, (i * 3) + 1)
    plt.plot(ocon_predictions[i], 'k.', label='Raw Predictions')
    plt.plot(ocon_g_truths[i], 'rx', label='Ground Truths')
    plt.axhline(0.5, linestyle='--', color='grey')
    plt.title(f'{ocon_vowels[i].name.upper()} Predictions Accuracy: {ocon_eval_accuracies[i]:.2f}%')
    plt.xlabel('Data (Indices)')
    plt.xticks(ticks=plot_ticks, labels=vowels)

```

```

plt.ylabel('Normalized Probability')
plt.grid()
plt.legend(loc='best')

plt.subplot(len(ocon_vowels), 3, (i * 3) + 2)
plt.plot(ocon_dist_errors[i], 'k')
plt.title(f'Predicted to Measured Error')
plt.xlabel('Data (Indices)')
plt.xticks(ticks=plot_ticks, labels=vowels)
plt.ylabel('Normalized Probability Error')
plt.ylim([-1.1, 1.1])
plt.grid()

plt.subplot(len(ocon_vowels), 3, (i * 3) + 3)

# Predictions list processing
predictions_temp = ocon_predictions[i]
class_predictions = [item for sublist in predictions_temp for item in sublist] # Turn a list of lists in a single list (c
for j in range(len(class_predictions)): # Turn a list of tensors of one variable in a list of scalars (item() method)
    class_predictions[j] = class_predictions[j].item()

# Positives & False-Positives extraction
positives = []
for w in range(len(vowels)):
    num = (np.array(class_predictions[end_idx[w]: end_idx[w + 1]]) > 0.5).sum()
    positives.append(num)

plt.bar(np.arange(len(vowels)), positives, color='k')
plt.title(f'"{vowels[i]}" Positive Probabilities Distribution')
plt.xlabel('Normalized Probabilities')
plt.ylabel('Occurences')
plt.xticks([n for n in range(12)], vowels)
plt.grid()

plt.tight_layout()
plt.savefig('OCON_bank_evaluation')
plt.show()

# Model Parameters Save/Load functions
from pathlib import Path

def save_model_state(model, folder_name: str = "Trained_models_state"):
    """
    Save Pre-Trained model parameters in a State Dictionary
    """

    MODEL_PATH = Path(folder_name) # Placed in root
    MODEL_PATH.mkdir(parents=True, exist_ok=True) # Pre-existing folder (w. same name) monitoring
    MODEL_NAME = '{}_{}'.format(model.name, "Params.pth")
    MODEL_SAVE_PATH = MODEL_PATH / MODEL_NAME

    print(f"Saving {model.name} Parameters in: {MODEL_SAVE_PATH}")
    torch.save(obj=model.state_dict(), f=MODEL_SAVE_PATH)

    return MODEL_SAVE_PATH

# Save Pre-Trained Models-bank
states_path = [] # Path for each model parameters state
for i in range(len(ocon_vowels)):
    state_path = save_model_state(ocon_vowels[i])
    states_path.append(state_path)
print()

```

## ▼ Output Maxnet Algorithm

```

# OCON "MaxNet" Architecture (Weightening + Non Linearity apply)
class OCON_MaxNet(nn.Module):
    def __init__(self, n_units, act_fun, eps):
        super().__init__()

        self.layers = nn.ModuleDict()
        self.eps_weight = eps

        # MaxNet Layer
        self.layers['MAXNET'] = nn.Linear(n_units, n_units)

        # Weights & Bias initialization
        self.layers['MAXNET'].weight.data.fill_(self.eps_weight)
        for i in range(n_units):

# nn.Module: base class to inherit from
# self + attributes (architecture hyper-paramet

# Dictionary to store Model layers

# Key 'MaxNet' layer specification

```

```

        self.layers['MAXNET'].weight[i][i].data.fill_(1.) # Self Weight = 1

        self.layers['MAXNET'].bias.data.fill_(0.)

        # Activation Function
        self.actfun = act_fun # Function string-name attribute association

# Forward Pass Method
def forward(self, x):

    # Activation function object computation
    actfun = getattr(torch.nn, self.actfun)

    # Maxnet Layer pass                                     --> Output Weightening (Dot Product) "Linear transfc
    x = actfun()(self.layers['MAXNET'](x.squeeze().float()))

    # Self

    return x

# Build OCON MaxNetwork Architecture
torch.manual_seed(SEED)
ocon_maxnet = OCON_MaxNet(n_units=12, act_fun='ReLU', eps=0.25)

# MaxNet & Sub-Networks Parameters
print('OCON MaxNet STATE')
model_desc(ocon_maxnet)

def maxnet_algo(maxnet_function, n_units, act_fun, eps, input_array):
    """
    MaxNet Re-iteration algorithm for Maximum Value retrieving from an input array
    """
    non_zero_outs = np.count_nonzero(input_array) # Non Zero Values initialization
    maxnet_in = torch.from_numpy(input_array) # MaxNet Input Tensor initialization

    results = [] # Results initialization

    counter = 0
    while non_zero_outs != 1:
        counter += 1

        # Create the MaxNet
        torch.manual_seed(SEED) # Redundant
        maxnet = maxnet_function(n_units = n_units, act_fun = act_fun, eps = eps)

        # Compute Forward Pass
        results = maxnet(maxnet_in)

        # Non_zero outputs & Maxnet Input Update
        non_zero_outs = np.count_nonzero(results.detach().numpy())
        maxnet_in = results.detach() # Save results for next iteration

    print(f'Maximum Value found in {counter} iterations')
    return np.argmax(results.detach().numpy())

# MaxNet on Sub-Networks predictions
ocon_predictions_prob = np.zeros((len(ocon_predictions), x_data_minmax.shape[0])) # NumPy predictions matrix (12 * 1617)

# Convert from List of Tensors to 2D NumPy Array
for i in range(len(ocon_predictions)):
    ocon_predictions_prob[i, :] = ocon_predictions[i].detach().squeeze().numpy()

maxnet_class_predictions = [] # Classes Outputs list initialization
# MaxNet application
for i in range(x_data_minmax.shape[0]):
    print(f'Dataset Sample({i + 1}) Class Evaluation')

    samp_predictions = ocon_predictions_prob[:, i] # Array of 12 predictions for each Dataset sample (OCON outputs)
    class_prediction = maxnet_algo(OCON_MaxNet, n_units=12, act_fun='ReLU', eps=-0.1, input_array=samp_predictions) # MaxNet
    maxnet_class_predictions.append(class_prediction) # Result appending
    print('-----')

maxnet_accuracy = 100 * np.mean((np.array(maxnet_class_predictions).reshape(1617, 1) == y_labels_raw_np)) # Accuracy computat
print(f'Maxnet Output --> Phoneme ACCURACY: {maxnet_accuracy}%')

# Argmax on Sub-Networks predictions (...for multiple 1s probabilities MaxNet infinite loops)
#ocon_predictions_prob = np.zeros((len(new_ocon_predictions), x_data_minmax.shape[0])) # NumPy predictions matrix (12 * 1617)
#
# Convert from List of Tensors to 2D NumPy Array
#for i in range(len(new_ocon_predictions)):

```



```

# ocon_predictions_prob[i, :] = new_ocon_predictions[i].detach().squeeze().numpy()
#
#maxnet_class_predictions = np.argmax(ocon_predictions_prob, axis=0)
#maxnet_accuracy = 100 * np.mean((np.array(maxnet_class_predictions).reshape(1617, 1) == y_labels_raw_np)) # Accuracy computa
#print(f'Maxnet Output ACCURACY: {maxnet_accuracy}%')

# Evaluation Analysis Plot
plt.figure(figsize=(30, 5))
plt.suptitle(f'OCON Bank + MaxNet Evaluation: {maxnet_accuracy:.0f}%')

plot_x_ticks = end_idx[: ]
plot_x_ticks = np.delete(plot_x_ticks, len(end_idx) - 1)
plot_y_ticks = [n for n in range(len(vowels))]

plt.plot(y_labels_raw_np, 'rs', label='Ground Truths')
plt.plot(maxnet_class_predictions, 'k.', label='MAXNET Outputs')
plt.xlabel('Dataset samples')
plt.xticks(ticks=plot_x_ticks, labels=vowels)
plt.xlim([-10, len(y_labels_raw_np) + 10])
plt.ylabel('Labels')
plt.yticks(ticks=plot_y_ticks, labels=vowels)
plt.legend(loc='best')
plt.grid()

plt.tight_layout()
plt.savefig('OCON_model_evaluation')
plt.show()

```



## ▼ *OCON Model Analysis*

3-features NO-Children Dataset

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**Year:** 2023

**Affiliation:** A.Casella Conservatory (student)

**Master Degree Thesis:** "Vowels phonemes Analysis & Classification by means of OCON rectifiers Deep Learning Architectures"

**Description:** Python scripts for One-Class-One-Network (OCON) Model analysis and optimization

```
# Numerical computations packages/modules
import numpy as np
import torch
import torch.nn as nn
import torch.nn.functional as F

# Dataset processing modules
from torch.utils.data import DataLoader
from sklearn.model_selection import train_test_split

# Graphic visualization modules
import matplotlib.pyplot as plt
import matplotlib_inline
matplotlib_inline.backend_inline.set_matplotlib_formats('svg')

# Common Seed initialization
SEED = 42 # ... the answer to the ultimate question of Life, the Universe, and Everything... (cit.)

# PyTorch Processing Units evaluation
device = 'cuda' if torch.cuda.is_available() else 'cpu'
print(f'AVAILABLE Processing Unit: {device.upper()}')
!nvidia-smi
```

## ▼ *HGCW Dataset*

- *Dataset\_utils.npz* file read
- *One-Hot encoding* definition
- *Train/Dev/Test split* definition

```
# Load HGCW 4_features_men Dataset
HGCW_dataset_utils_m = np.load(file='./HGCW_dataset_utils_men.npz')
print('MEN Sub-Dataset')
print('Raw features', HGCW_dataset_utils_m['HGCW_raw'].shape)
print('Fundamental Normalized features', HGCW_dataset_utils_m['HGCW_fund_norm'].shape)
print('MinMax features', HGCW_dataset_utils_m['HGCW_minmax'].shape)
print('Labels', HGCW_dataset_utils_m['HGCW_labels'].shape)
print('Classes size', HGCW_dataset_utils_m['classes_size'].shape)
print('Classes indices', HGCW_dataset_utils_m['classes_idx'].shape)

x_data_raw_np_m = HGCW_dataset_utils_m['HGCW_raw']
x_data_fund_norm_m = HGCW_dataset_utils_m['HGCW_fund_norm']
x_data_minmax_m = HGCW_dataset_utils_m['HGCW_minmax']
y_labels_raw_np_m = HGCW_dataset_utils_m['HGCW_labels']
vow_size_m = HGCW_dataset_utils_m['classes_size']
end_idx_m = HGCW_dataset_utils_m['classes_idx']
print()

# Load HGCW 4_features_women Dataset
HGCW_dataset_utils_w = np.load(file='./HGCW_dataset_utils_women.npz')
print('WOMEN Sub-Dataset')
print('Raw features', HGCW_dataset_utils_w['HGCW_raw'].shape)
print('Fundamental Normalized features', HGCW_dataset_utils_w['HGCW_fund_norm'].shape)
print('MinMax features', HGCW_dataset_utils_w['HGCW_minmax'].shape)
print('Labels', HGCW_dataset_utils_w['HGCW_labels'].shape)
print('Classes size', HGCW_dataset_utils_w['classes_size'].shape)
print('Classes indices', HGCW_dataset_utils_w['classes_idx'].shape)

x_data_raw_np_w = HGCW_dataset_utils_w['HGCW_raw']
x_data_fund_norm_w = HGCW_dataset_utils_w['HGCW_fund_norm']
x_data_minmax_w = HGCW_dataset_utils_w['HGCW_minmax']
y_labels_raw_np_w = HGCW_dataset_utils_w['HGCW_labels']
vow_size_w = HGCW_dataset_utils_w['classes_size']
end_idx_w = HGCW_dataset_utils_w['classes_idx']
```

```

# Auxiliary lists
vowels = ['ae', 'ah', 'aw', 'eh', 'er', 'ei', 'ih', 'iy', 'oa', 'oo', 'uh', 'uw'] # Vowels list
colors = ['red', 'saddlebrown', 'darkorange', 'darkgoldenrod', 'gold', 'darkkhaki', 'olive', 'darkgreen', 'steelblue', 'fuchsia']

# MEN Sub-Dataset Plot
dataset = x_data_minmax_m # x_data_fund_norm

plt.figure(figsize=(12, 15))
plt.suptitle('MEN Normalized Dataset "2-Features" separation')

for index, vowel in enumerate(vowels):

    first_coords = dataset[end_idx_m[index]: end_idx_m[index + 1], 1]
    second_coords = dataset[end_idx_m[index]: end_idx_m[index + 1], 2]
    third_coords = dataset[end_idx_m[index]: end_idx_m[index + 1], 3]

    plt.subplot(3, 1, 1)
    plt.title('$1_{st}$ VS $2_{nd}$')
    plt.scatter(first_coords, second_coords, marker='o', color=colors[index], label=f'Vowel "{vowel}"')
    plt.xlabel('$1_{st}$ Formant Frequency ratio')
    plt.ylabel('$2_{nd}$ Formant Frequency ratio')
    plt.legend(loc='best')
    plt.grid(True)

    plt.subplot(3, 1, 2)
    plt.title('$1_{st}$ VS $3_{rd}$')
    plt.scatter(first_coords, third_coords, marker='o', color=colors[index], label=f'Vowel "{vowel}"')
    plt.xlabel('$1_{st}$ Formant Frequency ratio')
    plt.ylabel('$3_{rd}$ Formant Frequency ratio')
    plt.legend(loc='best')
    plt.grid(True)

    plt.subplot(3, 1, 3)
    plt.title('$2_{nd}$ VS $3_{rd}$')
    plt.scatter(second_coords, third_coords, marker='o', color=colors[index], label=f'Vowel "{vowel}"')
    plt.xlabel('$2_{nd}$ Formant Frequency ratio')
    plt.ylabel('$3_{rd}$ Formant Frequency ratio')
    plt.legend(loc='best')
    plt.grid(True)

plt.tight_layout()
plt.savefig("men_normalized_dataset_plot")
plt.show()

# WOMEN Sub-Dataset Plot
dataset = x_data_minmax_w # x_data_fund_norm

plt.figure(figsize=(12, 15))
plt.suptitle('WOMEN Normalized Dataset "2-Features" separation')

for index, vowel in enumerate(vowels):

    first_coords = dataset[end_idx_w[index]: end_idx_w[index + 1], 1]
    second_coords = dataset[end_idx_w[index]: end_idx_w[index + 1], 2]
    third_coords = dataset[end_idx_w[index]: end_idx_w[index + 1], 3]

    plt.subplot(3, 1, 1)
    plt.title('$1_{st}$ VS $2_{nd}$')
    plt.scatter(first_coords, second_coords, marker='o', color=colors[index], label=f'Vowel "{vowel}"')
    plt.xlabel('$1_{st}$ Formant Frequency ratio')
    plt.ylabel('$2_{nd}$ Formant Frequency ratio')
    plt.legend(loc='best')
    plt.grid(True)

    plt.subplot(3, 1, 2)
    plt.title('$1_{st}$ VS $3_{rd}$')
    plt.scatter(first_coords, third_coords, marker='o', color=colors[index], label=f'Vowel "{vowel}"')
    plt.xlabel('$1_{st}$ Formant Frequency ratio')
    plt.ylabel('$3_{rd}$ Formant Frequency ratio')
    plt.legend(loc='best')
    plt.grid(True)

    plt.subplot(3, 1, 3)
    plt.title('$2_{nd}$ VS $3_{rd}$')
    plt.scatter(second_coords, third_coords, marker='o', color=colors[index], label=f'Vowel "{vowel}"')
    plt.xlabel('$2_{nd}$ Formant Frequency ratio')
    plt.ylabel('$3_{rd}$ Formant Frequency ratio')
    plt.legend(loc='best')
    plt.grid(True)

```

```

plt.tight_layout()
plt.savefig("women_normalized_dataset_plot")
plt.show()

# Stacked Dataset Creation (Labels ordered, same as original files)
x_data_raw_np = np.zeros((x_data_raw_np_m.shape[0] + x_data_raw_np_w.shape[0], x_data_raw_np_w.shape[1]))
x_data_fund_norm = np.zeros((x_data_fund_norm_m.shape[0] + x_data_fund_norm_w.shape[0], x_data_fund_norm_w.shape[1]))
x_data_minmax = np.zeros((x_data_minmax_m.shape[0] + x_data_minmax_w.shape[0], x_data_minmax_w.shape[1]))
y_labels_raw_np = np.zeros((y_labels_raw_np_m.shape[0] + y_labels_raw_np_w.shape[0], y_labels_raw_np_w.shape[1]))

vow_size = []
end_idx = [0]

for i in range(len(vowels)):
    # Extract and Vertical Stack Class-specific Data from both Sub-Datasets
    class_data_raw_np = np.vstack((x_data_raw_np_m[end_idx_m[i]: end_idx_m[i + 1], :], x_data_raw_np_w[end_idx_w[i]: end_idx_w[i + 1], :]))
    class_data_fund_norm = np.vstack((x_data_fund_norm_m[end_idx_m[i]: end_idx_m[i + 1], :], x_data_fund_norm_w[end_idx_w[i]: end_idx_w[i + 1], :]))
    class_data_minmax = np.vstack((x_data_minmax_m[end_idx_m[i]: end_idx_m[i + 1], :], x_data_minmax_w[end_idx_w[i]: end_idx_w[i + 1], :]))
    class_labels_raw_np = np.vstack((y_labels_raw_np_m[end_idx_m[i]: end_idx_m[i + 1], :], y_labels_raw_np_w[end_idx_w[i]: end_idx_w[i + 1], :]))

    vow_size.append(class_data_minmax.shape[0])
    end_idx.append(end_idx[i] + class_data_minmax.shape[0])

# Append to Output Matrices
x_data_raw_np[end_idx[i]: end_idx[i + 1], :] = class_data_raw_np
x_data_fund_norm[end_idx[i]: end_idx[i + 1], :] = class_data_fund_norm
x_data_minmax[end_idx[i]: end_idx[i + 1], :] = class_data_minmax
y_labels_raw_np[end_idx[i]: end_idx[i + 1], :] = class_labels_raw_np

print('HGCW (NO-Children) Sub-Dataset')
print('Raw features Data shape:', x_data_raw_np.shape)
print('Fundamental Normalized features Data shape:', x_data_fund_norm.shape)
print('MinMax features Data shape:', x_data_minmax.shape)
print('Labels Data shape:', y_labels_raw_np.shape)
print('Classes size Data shape:', len(vow_size))
print('Classes indices Data shape:', len(end_idx))

# Dataset Plot
dataset = x_data_minmax # x_data_fund_norm

plt.figure(figsize=(12, 15))
plt.suptitle('NO-CHILDREN Normalized Dataset "2-Features" separation')

for index, vowel in enumerate(vowels):

    first_coords = dataset[end_idx[index]: end_idx[index + 1], 1]
    second_coords = dataset[end_idx[index]: end_idx[index + 1], 2]
    third_coords = dataset[end_idx[index]: end_idx[index + 1], 3]

    plt.subplot(3, 1, 1)
    plt.title('$1_{st}$ VS $2_{nd}$')
    plt.scatter(first_coords, second_coords, marker='o', color=colors[index], label=f'Vowel "{vowel}"')
    plt.xlabel('$1_{st}$ Formant Frequency ratio')
    plt.ylabel('$2_{nd}$ Formant Frequency ratio')
    plt.legend(loc='best')
    plt.grid(True)

    plt.subplot(3, 1, 2)
    plt.title('$1_{st}$ VS $3_{rd}$')
    plt.scatter(first_coords, third_coords, marker='o', color=colors[index], label=f'Vowel "{vowel}"')
    plt.xlabel('$1_{st}$ Formant Frequency ratio')
    plt.ylabel('$3_{rd}$ Formant Frequency ratio')
    plt.legend(loc='best')
    plt.grid(True)

    plt.subplot(3, 1, 3)
    plt.title('$2_{nd}$ VS $3_{rd}$')
    plt.scatter(second_coords, third_coords, marker='o', color=colors[index], label=f'Vowel "{vowel}"')
    plt.xlabel('$2_{nd}$ Formant Frequency ratio')
    plt.ylabel('$3_{rd}$ Formant Frequency ratio')
    plt.legend(loc='best')
    plt.grid(True)

plt.tight_layout()
plt.savefig("no-children_normalized_dataset_plot")
plt.show()

# Class-specific One-hot encoding (Binarization)
def one_hot_encoder(sel_class_number: int = 3, dataset: np.ndarray = x_data_minmax, orig_labels: int = len(vowels), classes_si

```

```

classes = [n for n in range(orig_labels)] # Class Labels list initialization

# Auxiliary Parameters Initialization
if sel_class_number < len(classes):
    classes.remove(sel_class_number) # REST Classes list
    if debug is True:
        print(f'Selected Class "{vowels[sel_class_number]}" : {classes_size[sel_class_number]} samples')
    sub_classes_size = classes_size[sel_class_number] // len(classes)
    if debug is True:
        print(f'Rest Classes size (...each): {sub_classes_size} samples')

# 1-Subset processing
sub_data = dataset[classes_idx[sel_class_number]: classes_idx[sel_class_number + 1], :] # Selected Class feature slice
sub_data_labels_bin = np.ones((classes_size[sel_class_number], 1), dtype='int') # Selected Class labels (1) creation
sub_data_labels = np.ones((classes_size[sel_class_number], 1), dtype='int') * sel_class_number

# 0-Subset processing
for i in classes:
    class_i_indices = np.random.choice(np.arange(classes_idx[i], classes_idx[i + 1], 1), size=sub_classes_size, replace=True)
    sub_class_i_array = dataset[class_i_indices, :]
    sub_class_labels_bin_array = np.zeros((sub_class_i_array.shape[0], 1), dtype='int') # Rest I-esimal Class labels
    sub_class_labels_array = np.ones((sub_class_i_array.shape[0], 1), dtype='int') * i

    # Outputs append
    sub_data = np.vstack((sub_data, sub_class_i_array))
    sub_data_labels_bin = np.vstack((sub_data_labels_bin, sub_class_labels_bin_array))
    sub_data_labels = np.vstack((sub_data_labels, sub_class_labels_array))
else:
    raise ValueError(f'Invalid Class ID: "{sel_class_number}" --> It must be less than {len(classes)}!')

return sub_data, sub_data_labels_bin, sub_data_labels

# Train/Test split (auxiliary function)
def train_test_split_aux(features_dataset, labels_dataset, test_perc, tolerance):
    """
    An auxiliary Train_Test_split function (based on Scikit Learn implementation) w. balance tolerance specification
    """
    test_size = int(test_perc / 100 * len(features_dataset))
    train_balance = 0 # Output Training set balance value initialization
    test_balance = 0 # Output Testing set balance value initialization

    min_tol = np.mean(labels_dataset) - tolerance
    max_tol = np.mean(labels_dataset) + tolerance
    print(f'Data Balancing (TARGET = {np.mean(labels_dataset)} +/- {tolerance}): ', end='')

    while (min_tol >= train_balance or train_balance >= max_tol) or (min_tol >= test_balance or test_balance >= max_tol):
        train_data, test_data, train_labels, test_labels = train_test_split(features_dataset, labels_dataset, test_size=test_size, random_state=None)
        train_balance = np.mean(train_labels)
        test_balance = np.mean(test_labels)
        print('.', end='')
    else:
        print('OK')

    return train_data, test_data, train_labels, test_labels, train_balance, test_balance

# Train-Dev-Test split function
def train_dev_test_split(x_data, y_labels, split_list, tolerance=0.1, output='Loaders', debug=False):
    """
    Compute a Train, Development (Hold-Out) and a Test set split w. PyTorch Dataset conversion (and eventual Loaders initialization)
    """
    if len(split_list) == 3:
        # Train - Dev+Test separation
        print('Training --- Devel/Test SPLIT')
        train_data, testTMP_data, train_labels, testTMP_labels, _, _ = train_test_split_aux(x_data, y_labels, (split_list[1] * 100) / np.sum(split_list[1:]), tolerance)
        print('-----')

        # Dev - Test separation
        print('Devel --- Test SPLIT')

        split = ((split_list[1] * 100) / np.sum(split_list[1:])) * 100 # Split in %
        dev_data, test_data, dev_labels, test_labels, _, _ = train_test_split_aux(testTMP_data, testTMP_labels, split, tolerance)
        print('-----')

    # Tensor Conversion
    train_data_tensor = torch.tensor(train_data).float()
    train_labels_tensor = torch.tensor(train_labels, dtype=torch.int64).squeeze()
    dev_data_tensor = torch.tensor(dev_data).float()
    dev_labels_tensor = torch.tensor(dev_labels, dtype=torch.int64).squeeze()
    test_data_tensor = torch.tensor(test_data).float()
    test_labels_tensor = torch.tensor(test_labels, dtype=torch.int64).squeeze()
    if debug is True:
        print(f'Training Data Shape: {train_data.shape}')

```

```

        print(f'Development Data      Shape: {dev_data.shape}')
        print(f'Testing Data         Shape: {test_data.shape}')

        # Balance Evaluation
        print(f'Training Set          Balance: {np.mean(train_labels)}')
        print(f'Development Set       Balance: {np.mean(dev_labels)}')
        print(f'Testing Set           Balance: {np.mean(test_labels)}')

    if output != 'Loaders':
        return train_data_tensor, train_labels_tensor, dev_data_tensor, dev_labels_tensor, test_data_tensor, test_labels_t
    else:
        # PyTorch Dataset Conversion
        train_dataset = torch.utils.data.TensorDataset(torch.tensor(train_data).float(), torch.tensor(train_labels, dtype=
        dev_dataset = torch.utils.data.TensorDataset(torch.tensor(dev_data).float(), torch.tensor(dev_labels, dtype=torch.
        test_dataset = torch.utils.data.TensorDataset(torch.tensor(test_data).float(), torch.tensor(test_labels, dtype=torch.

        # DataLoader (Batches) --> Drop-Last control to optimize training
        trainLoader = DataLoader(train_dataset, shuffle=False, batch_size = 32, drop_last=True)
        devLoader = DataLoader(dev_dataset, shuffle=False, batch_size = dev_dataset.tensors[0].shape[0])
        testLoader = DataLoader(test_dataset, shuffle=False, batch_size = test_dataset.tensors[0].shape[0])
        if debug is True:
            print(f'Training Set      Batch Size: {trainLoader.batch_size}')
            print(f'Development Set Batch Size: {devLoader.batch_size}')
            print(f'Testing Set       Batch Size: {testLoader.batch_size}')

        return trainLoader, devLoader, testLoader
else:
    # Train - Test separation
    print('Training --- Test      SPLIT')
    train_data, test_data, train_labels, test_labels, _, _ = train_test_split_aux(x_data, y_labels, split_list[1] * 100, t
    print('-----')

    # Tensor Conversion
    train_data_tensor = torch.tensor(train_data).float()
    train_labels_tensor = torch.tensor(train_labels, dtype=torch.int64).squeeze()
    test_data_tensor = torch.tensor(test_data).float()
    test_labels_tensor = torch.tensor(test_labels, dtype=torch.int64).squeeze()
    if debug is True:
        print(f'Training Data      Shape: {train_data.shape}')
        print(f'Testing Data         Shape: {test_data.shape}')

        # Balance Evaluation
        print(f'Training Set          Balance: {np.mean(train_labels)}')
        print(f'Testing Set           Balance: {np.mean(test_labels)}')

    if output != 'Loaders':
        return train_data_tensor, train_labels_tensor, test_data_tensor, test_labels_tensor
    else:
        # PyTorch Dataset Conversion
        train_dataset = torch.utils.data.TensorDataset(torch.tensor(train_data).float(), torch.tensor(train_labels, dtype=
        test_dataset = torch.utils.data.TensorDataset(torch.tensor(test_data).float(), torch.tensor(test_labels, dtype=torch.

        # DataLoader (Batches) --> Drop-Last control to optimize training
        trainLoader = DataLoader(train_dataset, shuffle=False, batch_size = 32, drop_last=True)
        testLoader = DataLoader(test_dataset, shuffle=False, batch_size = test_dataset.tensors[0].shape[0])
        if debug is True:
            print(f'Training Set      Batch Size: {trainLoader.batch_size}')
            print(f'Testing Set       Batch Size: {testLoader.batch_size}')

        return trainLoader, testLoader

```

## ▼ One-Class Architecture (Binary Classifier)

(see "One-Class\_Sub-Network\_Analysis.ipynb")

Multi-Layer Perceptron

- Input Layer: 3 features [formant ratios, min-max normalized]
- Hidden Layer: 100 units
- Output Layer: 1 normalized probability
- Learning Rate: 0.0001 ( $10^{-4}$ )
- Optimizer: Adam (Adaptive Momentum)

- Mini-Batch Training:

- . Re-iterated Sub-Dataset Shuffling
- . Early Stopping (Test Accuracy driven)
- . Batch size = 32

- Regularization:

```

. Weight Decay (L2 Penalty): 0.0001 (10^-4)
. Dropout:
    * Input Layer Drop Rate: 0.8
    * Hidden Layer Drop Rate: 0.5.
. Batch Normalization

```

- *MLP Classifier Architecture* class definition
- *Mini-Batch Training* function definition

```

# Dynamic Multi-Layer Architecture Class (w. units, activation function, batch normalization and dropOut rate specification)
class binaryClassifier(nn.Module):
    def __init__(self, n_units, act_fun, rate_in, rate_hidden, model_name):
        super().__init__()

        self.layers = nn.ModuleDict()
        self.name = model_name

        # Input Layer
        self.layers['input'] = nn.Linear(3, n_units)

        # Hidden Layer
        self.layers[f'hidden'] = nn.Linear(n_units, n_units)
        self.layers[f'batch_norm'] = nn.BatchNorm1d(n_units)

        # Output Layer
        self.layers['output'] = nn.Linear(n_units, 1)

        # Activation Function
        self.actfun = act_fun

        # Dropout Parameter
        self.dr_in = rate_in
        self.dr_hidden = rate_hidden

        # Weights & Bias initialization
        for layer in self.layers.keys():
            try:
                nn.init.kaiming_normal_(self.layers[layer].weight, mode='fan_in')
            except:
                pass
            self.layers[layer].bias.data.fill_(0.)

# Forward Pass Method
def forward(self, x):

    # Activation function object computation
    actfun = getattr(torch.nn, self.actfun)

    # Input Layer pass
    x = actfun()(self.layers['input'](x))
    x = F.dropout(x, p=self.dr_in, training=self.training)

    # Single Hidden Layer pass
    x = self.layers[f'batch_norm'](x)
    x = actfun()(self.layers[f'hidden'](x))
    x = F.dropout(x, p=self.dr_hidden, training=self.training)

    # Output Layer pass
    x = self.layers['output'](x)
    x = nn.Sigmoid()(x)

    return x

# Batch Training function (w. Adam Optimizer & L2 penalty term) Re-Definition
def mini_batch_train_test(model, weight_decay, epochs: int, learning_rate, train_loader, dev_loader, test_loader, debug=False)
    """
    Train & Test an ANN Architecture via Mini-Batch Training (w. Train/Dev/Test PyTorch Loaders) and Adam Backpropagation Opti
    """
    # Loss Function initialization
    loss_function = nn.BCELoss()

    # Optimizer Algorithm initialization
    optimizer = torch.optim.Adam(model.parameters(), lr=learning_rate, weight_decay=weight_decay)

    # Output list initialization
    train_accuracies = []
    train_losses = []
    dev_accuracies = []

```



```

# TRAINING Phase
for epoch in range(epochs):
    model.train() # TRAINING Switch ON

    batch_accuracies = []
    batch_losses = []

    # Training BATCHES Loop
    for data_batch, labels_batch in train_loader:
        train_predictions = model(data_batch)
        train_loss = loss_function(train_predictions.squeeze(), labels_batch.type(torch.int64).float())
        batch_losses.append(train_loss.detach())

        # Backpropagation
        optimizer.zero_grad()
        train_loss.backward()
        optimizer.step()

        # Accuracy
        train_accuracy = 100 * torch.mean(((train_predictions.squeeze() > 0.5) == labels_batch.type(torch.int64).squeeze()))

        # Batch Stats appending
        batch_accuracies.append(train_accuracy.detach())
        batch_losses.append(train_loss.detach())

    # Training Stats appending
    train_accuracies.append(np.mean(batch_accuracies)) # Average of Batch Accuracies = Training step accuracy
    train_losses.append(np.mean(batch_losses)) # Average of Batch Losses = Training step Losses

# EVALUATION (Dev) Phase
model.eval()
with torch.no_grad():
    dev_data_batch, dev_labels_batch = next(iter(dev_loader))
    dev_predictions = model(dev_data_batch)

    dev_accuracy = 100 * torch.mean(((dev_predictions.squeeze() > 0.5) == dev_labels_batch.type(torch.int64).squeeze()))

    if debug is True:
        if epoch % 100 == 0:
            print(f'Epoch {epoch} --> DEV ACCURACY: {dev_accuracy.detach():.3f} %')
            print('-----')

        # Evaluation accuracy appending
        dev_accuracies.append(dev_accuracy.detach())

# TEST Phase
model.eval()
with torch.no_grad():
    test_data_batch, test_labels_batch = next(iter(test_loader))
    test_predictions = model(test_data_batch)
    test_accuracy = 100 * torch.mean(((test_predictions.squeeze() > 0.5) == test_labels_batch.type(torch.int64).squeeze()))

    if debug is True:
        print(f'TEST ACCURACY: {test_accuracy.detach():.2f} %')
        print('-----')

return train_accuracies, train_losses, dev_accuracies, test_accuracy.detach()

```

## ▼ OCON (One-Class-One-Net) Model

### Binary classifiers **Parallelization**

- *Classifiers-Bank* function definition
  - *Models Parameters* inspection
- Classifiers **Sequential** Training & Evaluation
- *Models Parameters State Save/Load* function definition

- 
- MaxNet output algorithm
  - Argmax output algorithm

```

def OCON_bank(one_class_function, hidden_units, act_fun, dr_in, dr_hidden, classes_list):
    """
    Create a One-Class-One-Network parallelization bank of an input Sub-Network definition
    """
    # Sub-Net names creation
    models_name_list = []
    for i in range(len(classes_list)):
        models_name_list.append("{}_{}".format(classes_list[i], "subnet")) # Class name + _subnet

```

```

# Sub-Networks instances creation
sub_nets = [] # Sub Network list initialization

for i in range(len(models_name_list)):

    torch.manual_seed(SEED) # Seed re-initialization

    # Sub-Net instance creation
    locals()[models_name_list[i]] = one_class_function(hidden_units, act_fun, dr_in, dr_hidden, models_name_list[i])
    sub_nets.append(locals()[models_name_list[i]])

return sub_nets

# Load Architecture Parameters State function
def load_model_state(model, state_dict_path):
    """
    Load an existent State Dictionary in a defined model
    """

    model.load_state_dict(torch.load(state_dict_path))
    print(f'Loaded Parameters (from "{state_dict_path}") into: {model.name}')

    return model

# Build The OCON Model
ocon_vowels = OCON_bank(binaryClassifier, 100, 'ReLU', 0.8, 0.5, vowels) # Best MLP (see "One-Class_Binary_Classifier_Analysi

# Load Pre-Trained Architectures in a fresh Model instance:
#ocon_vowels = OCON_bank(binaryClassifier, 100, 'ReLU', 0.8, 0.5, vowels) # Best MLP (see "One-Class_Binary_Classifier_Analys
#states_path = ["Trained_models_state/ae_subnet_Params.pth",
#               "Trained_models_state/ah_subnet_Params.pth",
#               "Trained_models_state/aw_subnet_Params.pth",
#               "Trained_models_state/eh_subnet_Params.pth",
#               "Trained_models_state/er_subnet_Params.pth",
#               "Trained_models_state/ei_subnet_Params.pth",
#               "Trained_models_state/ih_subnet_Params.pth",
#               "Trained_models_state/iy_subnet_Params.pth",
#               "Trained_models_state/oa_subnet_Params.pth",
#               "Trained_models_state/oo_subnet_Params.pth",
#               "Trained_models_state/uH_subnet_Params.pth",
#               "Trained_models_state/uw_subnet_Params.pth"]
#
#for i in range(len(ocon_vowels)):
#    load_model_state(ocon_vowels[i], states_path[i])

# OCON Evaluation function
def OCON_eval(ocon_models_bank, features_dataset: np.ndarray = x_data_minmax[:, 1:], labels: np.ndarray = y_labels_raw_np):
    """
    Evaluate OCON models-bank over an entire dataset
    """
    # Output lists initialization
    predictions = []
    dist_errors = []
    eval_accuracies = []
    g_truths = [] # For plotting purposes

    # Evaluate each Sub-Network...
    for i in range(len(ocon_models_bank)):
        ocon_models_bank[i].eval() # Put j-esimal Sub-Network in Evaluation Mode
        print(f'{ocon_models_bank[i].name.upper()} Evaluation -', end=' ')

        with torch.no_grad():

            # Make predictions
            features_data_tensor = torch.tensor(features_dataset).float()
            raw_eval_predictions = ocon_models_bank[i](features_data_tensor)

            # Create Ground Truths
            ground_truth = np.where(labels == i, 1, 0)
            ground_truth_tensor = torch.tensor(ground_truth, dtype=torch.int64).squeeze()

            # Compute Errors
            dist_error = ground_truth_tensor - raw_eval_predictions.detach().squeeze() # Distances
            eval_accuracy = 100 * torch.mean(((raw_eval_predictions.detach().squeeze() > 0.5) == ground_truth_tensor).float())
            print(f'Accuracy: {eval_accuracy:.2f}%')

    # Outputs append
    predictions.append(raw_eval_predictions.detach())
    dist_errors.append(dist_error.detach())

```

```

eval_accuracies.append(eval_accuracy.detach())

g_truths.append(ground_truth)

return predictions, dist_errors, eval_accuracies, g_truths

# For Pre-Trained Models
#ocon_predictions, ocon_dist_errors, ocon_eval_accuracies, ocon_g_truths = OCON_eval(ocon_vowels)

# Model Parameters State function
def model_desc(model):
    """
    Print a Console report of Neural Network Model parameters
    """
    # Parameters Description
    print('Params Description:')
    trainable_params = 0

    for parameter in model.named_parameters():
        print(f'Parameter Name      : {parameter[0]}')
        print(f'Parameter Weights   : {parameter[1][:]}')
        if parameter[1].requires_grad:
            print(f'...with {parameter[1].numel()} TRAINABLE parameters')
            trainable_params += parameter[1].numel()

    print('.....')

    print('-----')

    # Nodes Count
    nodes = 0
    for param_name, param_tensor in model.named_parameters():
        if 'bias' in param_name:
            nodes += len(param_tensor)

    print(f'Total Nodes          : {nodes}')
    print('-----')

# OCON-Model Description
for i in range(len(ocon_vowels)):
    print(f'OCON "{ocon_vowels[i].name}" Classifier STATE')
    model_desc(ocon_vowels[i])
    print()

# Training/Eval/Testing Parameters
epochs = 1000 # For each "Data Batch-Set"
loss_break = 0.15 # loss (for Early Stopping)
acc_break = 90. # % accuracy (for Early Stopping)
min_tolerance = 0.01 # ...for sub-dataset balancing

# Outputs Initialization
loss_functions = [[] for _ in range(len(ocon_vowels))]
training_accuracies = [[] for _ in range(len(ocon_vowels))]
evaluation_accuracies = [[] for _ in range(len(ocon_vowels))]
test_accuracies = [[] for _ in range(len(ocon_vowels))]
training_times = []

# OCON Sub-Networks Training
from time import perf_counter
debug = False

for i, vowel in enumerate(vowels):
    print(f'Architecture "{ocon_vowels[i].name}" TRAINING PHASE')

    start_timer = perf_counter()
    # Iterated (w. Batch-Sets shuffling) Mini-Batch Training
    iteration = 0 # Batch Training iteration counter
    mean_loss = 1.
    test_accuracy = 0.

    while (mean_loss > loss_break) or (test_accuracy < acc_break):
        # Dataset processing
        sub_data, sub_data_labels_bin, _ = one_hot_encoder(sel_class_number=i, dataset=x_data_minmax, debug=debug)
        print('-----')
        trainLoader, devLoader, testLoader = train_dev_test_split(sub_data[:, 1:], sub_data_labels_bin, [0.4, 0.3, 0.3], toler

        # Train/Test Architecture
        train_accuracies, train_losses, dev_accuracies, test_accuracy = mini_batch_train_test(ocon_vowels[i], weight_decay=0.0
        print(f'Sub-Net "{vowel.upper()}" Epoch {(iteration + 1) * epochs} - TEST ACCURACY: {test_accuracy:.2f}%', end=' ')

```

```

# Outputs append
loss_functions[i].append(train_losses)
training_accuracies[i].append(train_accuracies)
evaluation_accuracies[i].append(dev_accuracies)
test_accuracies[i].append(test_accuracy)

# Repeating condition evaluation
mean_loss = np.mean(train_losses[-50: ]) # Last 100 losses mean
print(f'- MEAN LOSS: {mean_loss}')

iteration += 1 # Go to next Batch training iteration

print(f'Training STOPPED at iteration {iteration}')
print('-----')
stop_timer = perf_counter()

print(f'"{ocon_vowels[i].name}" Training COMPLETED in {float(stop_timer - start_timer)}sec.')
training_times.append(stop_timer - start_timer)
print('-----')

# Graphical smoothing filter
def smooth(data, k=100):
    """
    A Convolution LP filter w. interval definition
    """
    return np.convolve(data, np.ones(k) / k, mode='same')

# Training Phase Plots
plt.figure(figsize=(12, 5 * 12))

# loss_functions, training_accuracies, evaluation_accuracies, test_accuracies, training_times
classes = len(ocon_vowels)

for i in range(classes):
    plt.subplot(classes, 2, (i * 2) + 1)
    flat_loss_function = [item for sublist in loss_functions[i] for item in sublist]

    plt.plot(smooth(flat_loss_function), 'k-')
    plt.axhline(loss_break, color='r', linestyle='--')
    plt.title(f'{ocon_vowels[i].name.upper()} Training Loss')
    plt.xlabel('Epochs')
    plt.xlim([100, len(flat_loss_function) - 100])
    plt.ylabel('GT - Predicted diff. (probability)')
    plt.grid()

    plt.subplot(classes, 2, (i * 2) + 2)
    flat_training_accuracy = [item for sublist in training_accuracies[i] for item in sublist]
    flat_dev_accuracy = [item for sublist in evaluation_accuracies[i] for item in sublist]
    flat_test_accuracy = test_accuracies[i]

    plt.plot(smooth(flat_training_accuracy), 'k-', label='Training')
    plt.plot(smooth(flat_dev_accuracy), color='grey', label='Development')
    if len(flat_test_accuracy) > 1:
        plt.plot([(n + 1) * epochs for n in range(len(flat_test_accuracy))], flat_test_accuracy, 'r-', label=f'Test')
    else:
        plt.axhline(test_accuracy, color='r', linestyle='-', label=f'Test')
    plt.title(f'{ocon_vowels[i].name.upper()} Accuracy (after {training_times[i]:.2f}sec.)')
    plt.xlabel('Epochs')
    plt.xlim([100, len(flat_training_accuracy) - 100])
    plt.ylabel('Accuracy (in %)')
    plt.ylim([40, 101])
    plt.grid()
    plt.legend(loc='best')

plt.tight_layout()
plt.savefig('OCON_training_phase')
plt.show()

# OCON Evaluation
ocon_predictions, ocon_dist_errors, ocon_eval_accuracies, ocon_g_truths = OCON_eval(ocon_vowels)

# Dataset Evaluation Analysis Plot
plt.figure(figsize=(18, 5 * len(ocon_vowels)))
plot_ticks = end_idx[:]
plot_ticks = np.delete(plot_ticks, -1)

for i in range(len(ocon_vowels)):
    plt.subplot(len(ocon_vowels), 3, (i * 3) + 1)
    plt.plot(ocon_predictions[i], 'k.', label='Raw Predictions')
    plt.plot(ocon_g_truths[i], 'rx', label='Ground Truths')

```

```

plt.axhline(0.5, linestyle='--', color='grey')
plt.title(f'{ocon_vowels[i].name.upper()} Predictions Accuracy: {ocon_eval_accuracies[i]:.2f}%')
plt.xlabel('Data (Indices)')
plt.xticks(ticks=plot_ticks, labels=vowels)
plt.ylabel('Normalized Probability')
plt.grid()
plt.legend(loc='best')

plt.subplot(len(ocon_vowels), 3, (i * 3) + 2)
plt.plot(ocon_dist_errors[i], 'k')
plt.title(f'Predicted to Measured Error')
plt.xlabel('Data (Indices)')
plt.xticks(ticks=plot_ticks, labels=vowels)
plt.ylabel('Normalized Probability Error')
plt.ylim([-1.1, 1.1])
plt.grid()

plt.subplot(len(ocon_vowels), 3, (i * 3) + 3)

# Predictions list processing
predictions_temp = ocon_predictions[i]
class_predictions = [item for sublist in predictions_temp for item in sublist] # Turn a list of lists in a single list (c
for j in range(len(class_predictions)): # Turn a list of tensors of one variable in a list of scalars (item() method)
    class_predictions[j] = class_predictions[j].item()

# Positives & False-Positives extraction
positives = []
for w in range(len(vowels)):
    num = (np.array(class_predictions[end_idx[w]: end_idx[w + 1]]) > 0.5).sum()
    positives.append(num)

plt.bar(np.arange(len(vowels)), positives, color='k')
plt.title(f'"{vowels[i]}" Positive Probabilities Distribution')
plt.xlabel('Normalized Probabilities')
plt.ylabel('Occurences')
plt.xticks([n for n in range(12)], vowels)
plt.grid()

plt.tight_layout()
plt.savefig('OCON_bank_evaluation')
plt.show()

# Model Parameters Save/Load functions
from pathlib import Path

def save_model_state(model, folder_name: str = "Trained_models_state"):
    """
    Save Pre-Trained model parameters in a State Dictionary
    """

    MODEL_PATH = Path(folder_name) # Placed in root
    MODEL_PATH.mkdir(parents=True, exist_ok=True) # Pre-existing folder (w. same name) monitoring
    MODEL_NAME = '{}_{}'.format(model.name, "Params.pth")
    MODEL_SAVE_PATH = MODEL_PATH / MODEL_NAME

    print(f"Saving {model.name} Parameters in: {MODEL_SAVE_PATH}")
    torch.save(obj=model.state_dict(), f=MODEL_SAVE_PATH)

    return MODEL_SAVE_PATH

# Save Pre-Trained Models-bank
states_path = [] # Path for each model parameters state
for i in range(len(ocon_vowels)):
    state_path = save_model_state(ocon_vowels[i])
    states_path.append(state_path)
print()

```

## ➤ Output Maxnet Algorithm

```

# OCON "MaxNet" Architecture (Weightening + Non Linearity apply)
class OCON_MaxNet(nn.Module):
    def __init__(self, n_units, act_fun, eps):
        super().__init__()

        self.layers = nn.ModuleDict()
        self.eps_weight = eps

        # MaxNet Layer
        self.layers['MAXNET'] = nn.Linear(n_units, n_units)

```

# nn.Module: base class to inherit from  
# self + attributes (architecture hyper-paramet

# Dictionary to store Model layers

# Key 'MaxNet' layer specification

```

# Weights & Bias initialization
self.layers['MAXNET'].weight.data.fill_(self.eps_weight)
for i in range(n_units):
    self.layers['MAXNET'].weight[i][i].data.fill_(1.) # Self Weight = 1

self.layers['MAXNET'].bias.data.fill_(0.)

# Activation Function
self.actfun = act_fun # Function string-name attribute association

# Forward Pass Method
def forward(self, x):

    # Activation function object computation
    actfun = getattr(torch.nn, self.actfun)

    # Maxnet Layer pass --> Output Weightening (Dot Product) "Linear transfo
    x = actfun()(self.layers['MAXNET'](x.squeeze().float()))

    # Self

    return x

# Build OCON MaxNetwork Architecture
torch.manual_seed(SEED)
ocon_maxnet = OCON_MaxNet(n_units=12, act_fun='ReLU', eps=0.25)

# MaxNet & Sub-Networks Parameters
print('OCON MaxNet STATE')
model_desc(ocon_maxnet)

def maxnet_algo(maxnet_function, n_units, act_fun, eps, input_array):
    """
    MaxNet Re-iteration algorithm for Maximum Value retrieving from an input array
    """
    non_zero_outs = np.count_nonzero(input_array) # Non Zero Values initialization
    maxnet_in = torch.from_numpy(input_array) # MaxNet Input Tensor initialization

    results = [] # Results initialization

    counter = 0
    while non_zero_outs != 1:
        counter += 1

        # Create the MaxNet
        torch.manual_seed(SEED) # Redundant
        maxnet = maxnet_function(n_units = n_units, act_fun = act_fun, eps = eps)

        # Compute Forward Pass
        results = maxnet(maxnet_in)

        # Non_zero outputs & Maxnet Input Update
        non_zero_outs = np.count_nonzero(results.detach().numpy())
        maxnet_in = results.detach() # Save results for next iteration

    print(f'Maximum Value found in {counter} iterations')
    return np.argmax(results.detach().numpy())

# MaxNet on Sub-Networks predictions
ocon_predictions_prob = np.zeros((len(ocon_predictions), x_data_minmax.shape[0])) # NumPy predictions matrix (12 * 1617)

# Convert from List of Tensors to 2D NumPy Array
for i in range(len(ocon_predictions)):
    ocon_predictions_prob[i, :] = ocon_predictions[i].detach().squeeze().numpy()

maxnet_class_predictions = [] # Classes Outputs list initialization
# MaxNet application
for i in range(x_data_minmax.shape[0]):
    print(f'Dataset Sample({i + 1}) Class Evaluation')

    samp_predictions = ocon_predictions_prob[:, i] # Array of 12 predictions for each Dataset sample (OCON outputs)
    class_prediction = maxnet_algo(OCON_MaxNet, n_units=12, act_fun='ReLU', eps=-0.1, input_array=samp_predictions) # MaxNet
    maxnet_class_predictions.append(class_prediction) # Result appending
    print('-----')

maxnet_accuracy = 100 * np.mean((np.array(maxnet_class_predictions).reshape(1090, 1) == y_labels_raw_np)) # Accuracy computat
print(f'Maxnet Output --> Phoneme ACCURACY: {maxnet_accuracy}%')

```

```

# Argmax on Sub-Networks predictions (...for multiple 1s probabilities MaxNet infinite loops)
#ocon_predictions_prob = np.zeros((len(new_ocon_predictions), x_data_minmax.shape[0])) # NumPy predictions matrix (12 * 1617)
#
# Convert from List of Tensors to 2D NumPy Array
#for i in range(len(new_ocon_predictions)):
#    ocon_predictions_prob[i, :] = new_ocon_predictions[i].detach().squeeze().numpy()
#
#maxnet_class_predictions = np.argmax(ocon_predictions_prob, axis=0)
#maxnet_accuracy = 100 * np.mean((np.array(maxnet_class_predictions).reshape(1617, 1) == y_labels_raw_np)) # Accuracy computa
#print(f'Maxnet Output ACCURACY: {maxnet_accuracy}%')

# Evaluation Analysis Plot
plt.figure(figsize=(30, 5))
plt.suptitle(f'OCON Bank + MaxNet Evaluation: {maxnet_accuracy:.0f}%')

plot_x_ticks = end_idx[: ]
plot_x_ticks = np.delete(plot_x_ticks, len(end_idx) - 1)
plot_y_ticks = [n for n in range(len(vowels))]

plt.plot(y_labels_raw_np, 'rs', label='Ground Truths')
plt.plot(maxnet_class_predictions, 'k.', label='MAXNET Outputs')
plt.xlabel('Dataset samples')
plt.xticks(ticks=plot_x_ticks, labels=vowels)
plt.xlim([-10, len(y_labels_raw_np) + 10])
plt.ylabel('Labels')
plt.yticks(ticks=plot_y_ticks, labels=vowels)
plt.legend(loc='best')
plt.grid()

plt.tight_layout()
plt.savefig('OCON_model_evaluation')
plt.show()

```





## ▼ OCON Model Analysis

(12-features Complete Dataset)

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**Year:** 2023

**Affiliation:** A.Casella Conservatory (student)

**Master Degree Thesis:** "Vowel phonemes Analysis & Classification by means of OCON rectifiers Deep Learning Architectures"

**Description:** Python scripts for One-Class-One-Network (OCON) Model analysis and optimization

```
# Numerical computations packages/modules
import numpy as np
import torch
import torch.nn as nn
import torch.nn.functional as F

# Dataset processing modules
from torch.utils.data import DataLoader
from sklearn.model_selection import train_test_split

# Graphic visualization modules
import matplotlib.pyplot as plt
import matplotlib_inline
matplotlib_inline.backend_inline.set_matplotlib_formats('svg')

# Common Seed initialization
SEED = 42 # ... the answer to the ultimate question of Life, the Universe, and Everything... (cit.)

# PyTorch Processing Units evaluation
device = 'cuda' if torch.cuda.is_available() else 'cpu'
print(f'AVAILABLE Processing Unit: {device.upper()}')
!nvidia-smi
```

## ▼ HGCW Dataset

- *Dataset\_utils.npz* file read
- *One-Hot encoding* definition
- *Train/Dev/Test split* definition

```
# Load HGCW 12_features_all Dataset
HGCW_dataset_utils = np.load(file='./HGCW_dataset_utils.npz')
print('Raw features Data shape:', HGCW_dataset_utils['HGCW_raw'].shape)
print('Fundamental Normalized features Data shape:', HGCW_dataset_utils['HGCW_fund_norm'].shape)
print('MinMax features Data shape:', HGCW_dataset_utils['HGCW_minmax'].shape)
print('Labels Data shape:', HGCW_dataset_utils['HGCW_labels'].shape)
print('Classes size Data shape:', HGCW_dataset_utils['classes_size'].shape)
print('Classes indices Data shape:', HGCW_dataset_utils['classes_idx'].shape)

x_data_raw_np = HGCW_dataset_utils['HGCW_raw']
x_data_fund_norm = HGCW_dataset_utils['HGCW_fund_norm']
x_data_minmax = HGCW_dataset_utils['HGCW_minmax']
y_labels_raw_np = HGCW_dataset_utils['HGCW_labels']
vow_size = HGCW_dataset_utils['classes_size']
end_idx = HGCW_dataset_utils['classes_idx']

# Auxiliary lists
vowels = ['ae', 'ah', 'aw', 'eh', 'er', 'ei', 'ih', 'iy', 'oa', 'oo', 'uh', 'uw'] # Vowels list
colors = ['red', 'saddlebrown', 'darkorange', 'darkgoldenrod', 'gold', 'darkkhaki', 'olive', 'darkgreen', 'steelblue', 'fuchsia']

# Class-specific One-hot encoding (Binarization)
def one_hot_encoder(sel_class_number: int = 3, dataset: np.ndarray = x_data_minmax, orig_labels: int = len(vowels), classes_size: int = len(classes_size)):
    classes = [n for n in range(orig_labels)] # Class Labels list initialization

    # Auxiliary Parameters Initialization
    if sel_class_number < len(classes):
        classes.remove(sel_class_number) # REST Classes list
        if debug is True:
            print(f'Selected Class "{vowels[sel_class_number]}" : {classes_size[sel_class_number]} samples')
        sub_classes_size = classes_size[sel_class_number] // len(classes)
        if debug is True:
            print(f'Rest Classes size (...each): {sub_classes_size} samples')
```

```

# 1-Subset processing
sub_data = dataset[classes_idx[sel_class_number]: classes_idx[sel_class_number + 1], :] # Selected Class feature slice
sub_data_labels_bin = np.ones((classes_size[sel_class_number], 1), dtype='int') # Selected Class labels (1) creation
sub_data_labels = np.ones((classes_size[sel_class_number], 1), dtype='int') * sel_class_number

# 0-Subset processing
for i in classes:
    class_i_indices = np.random.choice(np.arange(classes_idx[i], classes_idx[i + 1], 1), size=sub_classes_size, replace=True)
    sub_class_i_array = dataset[class_i_indices, :]
    sub_class_labels_bin_array = np.zeros((sub_class_i_array.shape[0], 1), dtype='int') # Rest I-esimal Class labels
    sub_class_labels_array = np.ones((sub_class_i_array.shape[0], 1), dtype='int') * i

    # Outputs append
    sub_data = np.vstack((sub_data, sub_class_i_array))
    sub_data_labels_bin = np.vstack((sub_data_labels_bin, sub_class_labels_bin_array))
    sub_data_labels = np.vstack((sub_data_labels, sub_class_labels_array))
else:
    raise ValueError(f'Invalid Class ID: "{sel_class_number}" --> It must be less than {len(classes)}!')

return sub_data, sub_data_labels_bin, sub_data_labels

# Train/Test split (auxiliary function)
def train_test_split_aux(features_dataset, labels_dataset, test_perc, tolerance):
    """
    An auxiliary Train_Test_split function (based on Scikit Learn implementation) w. balance tolerance specification
    """
    test_size = int(test_perc / 100 * len(features_dataset))
    train_balance = 0 # Output Training set balance value initialization
    test_balance = 0 # Output Testing set balance value initialization

    min_tol = np.mean(labels_dataset) - tolerance
    max_tol = np.mean(labels_dataset) + tolerance
    print(f'Data Balancing (TARGET = {np.mean(labels_dataset)} +- {tolerance}): ', end='')

    while (min_tol >= train_balance or train_balance >= max_tol) or (min_tol >= test_balance or test_balance >= max_tol):
        train_data, test_data, train_labels, test_labels = train_test_split(features_dataset, labels_dataset, test_size=test_size, random_state=None)
        train_balance = np.mean(train_labels)
        test_balance = np.mean(test_labels)
        print('.', end='')
    else:
        print('OK')

    return train_data, test_data, train_labels, test_labels, train_balance, test_balance

# Train-Dev-Test split function
def train_dev_test_split(x_data, y_labels, split_list, tolerance=0.1, output='Loaders', debug=False):
    """
    Compute a Train, Development (Hold-Out) and a Test set split w. PyTorch Dataset conversion (and eventual Loaders initialization)
    """
    if len(split_list) == 3:
        # Train - Dev+Test separation
        print('Training --- Devel/Test SPLIT')
        train_data, testTMP_data, train_labels, testTMP_labels, _, _ = train_test_split_aux(x_data, y_labels, (split_list[1] * 100) / 100, tolerance)
        print('-----')

        # Dev - Test separation
        print('Devel --- Test SPLIT')

        split = ((split_list[1] * 100) / np.sum(split_list[1:] * 100)) * 100 # Split in %
        dev_data, test_data, dev_labels, test_labels, _, _ = train_test_split_aux(testTMP_data, testTMP_labels, split, tolerance)
        print('-----')

        # Tensor Conversion
        train_data_tensor = torch.tensor(train_data).float()
        train_labels_tensor = torch.tensor(train_labels, dtype=torch.int64).squeeze()
        dev_data_tensor = torch.tensor(dev_data).float()
        dev_labels_tensor = torch.tensor(dev_labels, dtype=torch.int64).squeeze()
        test_data_tensor = torch.tensor(test_data).float()
        test_labels_tensor = torch.tensor(test_labels, dtype=torch.int64).squeeze()
        if debug is True:
            print(f'Training Data Shape: {train_data.shape}')
            print(f'Development Data Shape: {dev_data.shape}')
            print(f'Testing Data Shape: {test_data.shape}')

        # Balance Evaluation
        print(f'Training Set Balance: {np.mean(train_labels)}')
        print(f'Development Set Balance: {np.mean(dev_labels)}')
        print(f'Testing Set Balance: {np.mean(test_labels)}')

    if output != 'Loaders':
        return train_data_tensor, train_labels_tensor, dev_data_tensor, dev_labels_tensor, test_data_tensor, test_labels_tensor

```

```

else:
    # PyTorch Dataset Conversion
    train_dataset = torch.utils.data.TensorDataset(torch.tensor(train_data).float(), torch.tensor(train_labels, dtype=
dev_dataset = torch.utils.data.TensorDataset(torch.tensor(dev_data).float(), torch.tensor(dev_labels, dtype=torch.
test_dataset = torch.utils.data.TensorDataset(torch.tensor(test_data).float(), torch.tensor(test_labels, dtype=torch.

    # DataLoader (Batches) --> Drop-Last control to optimize training
    trainLoader = DataLoader(train_dataset, shuffle=False, batch_size = 32, drop_last=True)
    devLoader = DataLoader(dev_dataset, shuffle=False, batch_size = dev_dataset.tensors[0].shape[0])
    testLoader = DataLoader(test_dataset, shuffle=False, batch_size = test_dataset.tensors[0].shape[0])
    if debug is True:
        print(f'Training Set      Batch Size: {trainLoader.batch_size}')
        print(f'Development Set Batch Size: {devLoader.batch_size}')
        print(f'Testing Set      Batch Size: {testLoader.batch_size}')

    return trainLoader, devLoader, testLoader
else:
    # Train - Test separation
    print('Training --- Test      SPLIT')
    train_data, test_data, train_labels, test_labels, _, _ = train_test_split_aux(x_data, y_labels, split_list[1] * 100, t
    print('-----')

    # Tensor Conversion
    train_data_tensor = torch.tensor(train_data).float()
    train_labels_tensor = torch.tensor(train_labels, dtype=torch.int64).squeeze()
    test_data_tensor = torch.tensor(test_data).float()
    test_labels_tensor = torch.tensor(test_labels, dtype=torch.int64).squeeze()
    if debug is True:
        print(f'Training Data      Shape: {train_data.shape}')
        print(f'Testing Data      Shape: {test_data.shape}')

    # Balance Evaluation
    print(f'Training Set      Balance: {np.mean(train_labels)}')
    print(f'Testing Set      Balance: {np.mean(test_labels)}')

    if output != 'Loaders':
        return train_data_tensor, train_labels_tensor, test_data_tensor, test_labels_tensor
    else:
        # PyTorch Dataset Conversion
        train_dataset = torch.utils.data.TensorDataset(torch.tensor(train_data).float(), torch.tensor(train_labels, dtype=
        test_dataset = torch.utils.data.TensorDataset(torch.tensor(test_data).float(), torch.tensor(test_labels, dtype=torch.

        # DataLoader (Batches) --> Drop-Last control to optimize training
        trainLoader = DataLoader(train_dataset, shuffle=False, batch_size = 32, drop_last=True)
        testLoader = DataLoader(test_dataset, shuffle=False, batch_size = test_dataset.tensors[0].shape[0])
        if debug is True:
            print(f'Training Set      Batch Size: {trainLoader.batch_size}')
            print(f'Testing Set      Batch Size: {testLoader.batch_size}')

        return trainLoader, testLoader

```

## ▼ One-Class Architecture (Binary Classifier)

(see "One-Class\_Sub-Network\_Analysis.ipynb")

Multi-Layer Perceptron

- Input Layer: 3 features [formant ratios, min-max normalized]
- Hidden Layer: 100 units
- Output Layer: 1 normalized probability
- Learning Rate: 0.0001 ( $10^{-4}$ )
- Optimizer: Adam (Adaptive Momentum)

- Mini-Batch Training:

- . Re-iterated Sub-Dataset Shuffling
- . Early Stopping (Test Accuracy driven)
- . Batch size = 32

- Regularization:

- . Weight Decay (L2 Penalty): 0.0001 ( $10^{-4}$ )
- . Dropout:
  - \* Input Layer Drop Rate: 0.8
  - \* Hidden Layer Drop Rate: 0.5.
- . Batch Normalization

- *MLP Classifier Architecture* class definition
- *Mini-Batch Training* function definition

```

# Dynamic Multi-Layer Architecture Class (w. units, activation function, batch normalization and dropOut rate specification)
class binaryClassifier(nn.Module):
    def __init__(self, n_units, act_fun, rate_in, rate_hidden, model_name):
        super().__init__()

        self.layers = nn.ModuleDict()
        self.name = model_name

        # Input Layer
        self.layers['input'] = nn.Linear(12, n_units)

        # Hidden Layer
        self.layers[f'hidden'] = nn.Linear(n_units, n_units)
        self.layers[f'batch_norm'] = nn.BatchNorm1d(n_units)

        # Output Layer
        self.layers['output'] = nn.Linear(n_units, 1)

        # Activation Function
        self.actfun = act_fun

        # Dropout Parameter
        self.dr_in = rate_in
        self.dr_hidden = rate_hidden

        # Weights & Bias initialization
        for layer in self.layers.keys():
            try:
                nn.init.kaiming_normal_(self.layers[layer].weight, mode='fan_in')
            except:
                pass
            self.layers[layer].bias.data.fill_(0.)

# Forward Pass Method
def forward(self, x):

    # Activation function object computation
    actfun = getattr(torch.nn, self.actfun)

    # Input Layer pass
    x = actfun()(self.layers['input'](x))
    x = F.dropout(x, p=self.dr_in, training=self.training)

    # Single Hidden Layer pass
    x = self.layers[f'batch_norm'](x)
    x = actfun()(self.layers[f'hidden'](x))
    x = F.dropout(x, p=self.dr_hidden, training=self.training)

    # Output Layer pass
    x = self.layers['output'](x)
    x = nn.Sigmoid()(x)

    return x

# Batch Training function (w. Adam Optimizer & L2 penalty term) Re-Definition
def mini_batch_train_test(model, weight_decay, epochs: int, learning_rate, train_loader, dev_loader, test_loader, debug=False)
    """
    Train & Test an ANN Architecture via Mini-Batch Training (w. Train/Dev/Test PyTorch Loaders) and Adam Backpropagation Opti
    """
    # Loss Function initialization
    loss_function = nn.BCELoss()

    # Optimizer Algorithm initialization
    optimizer = torch.optim.Adam(model.parameters(), lr=learning_rate, weight_decay=weight_decay)

    # Output list initialization
    train_accuracies = []
    train_losses = []
    dev_accuracies = []

    # TRAINING Phase
    for epoch in range(epochs):
        model.train() # TRAINING Switch ON

        batch_accuracies = []
        batch_losses = []

        # Training BATCHES Loop
        for data_batch, labels_batch in train_loader:
            train_predictions = model(data_batch)
            train_loss = loss_function(train_predictions.squeeze(), labels_batch.type(torch.int64).float())

```

```

        batch_losses.append(train_loss.detach())

        # Backpropagation
        optimizer.zero_grad()
        train_loss.backward()
        optimizer.step()

        # Accuracy
        train_accuracy = 100 * torch.mean(((train_predictions.squeeze() > 0.5) == labels_batch.type(torch.int64).squeeze()))

        # Batch Stats appending
        batch_accuracies.append(train_accuracy.detach())
        batch_losses.append(train_loss.detach())

    # Training Stats appending
    train_accuracies.append(np.mean(batch_accuracies)) # Average of Batch Accuracies = Training step accuracy
    train_losses.append(np.mean(batch_losses)) # Average of Batch Losses = Training step Losses

# EVALUATION (Dev) Phase
model.eval()
with torch.no_grad():
    dev_data_batch, dev_labels_batch = next(iter(dev_loader))
    dev_predictions = model(dev_data_batch)

    dev_accuracy = 100 * torch.mean(((dev_predictions.squeeze() > 0.5) == dev_labels_batch.type(torch.int64).squeeze()))

    if debug is True:
        if epoch % 100 == 0:
            print(f'Epoch {epoch} --> DEV ACCURACY: {dev_accuracy.detach():.3f} %')
            print('-----')

        # Evaluation accuracy appending
        dev_accuracies.append(dev_accuracy.detach())

# TEST Phase
model.eval()
with torch.no_grad():
    test_data_batch, test_labels_batch = next(iter(test_loader))
    test_predictions = model(test_data_batch)
    test_accuracy = 100 * torch.mean(((test_predictions.squeeze() > 0.5) == test_labels_batch.type(torch.int64).squeeze()))

    if debug is True:
        print(f'TEST ACCURACY: {test_accuracy.detach():.2f} %')
        print('-----')

return train_accuracies, train_losses, dev_accuracies, test_accuracy.detach()

```

## ▼ OCON (One-Class-One-Net) Model

### Binary classifiers **Parallelization**

- *Classifiers-Bank* function definition
  - *Models Parameters* inspection
- Classifiers **Sequential** Training & Evaluation
- *Models Parameters State Save/Load* function definition

- 
- MaxNet output algorithm
  - Argmax output algorithm

```

def OCON_bank(one_class_function, hidden_units, act_fun, dr_in, dr_hidden, classes_list):
    """
    Create a One-Class-One-Network parallelization bank of an input Sub-Network definition
    """
    # Sub-Net names creation
    models_name_list = []
    for i in range(len(classes_list)):
        models_name_list.append("{}_{}".format(classes_list[i], "subnet")) # Class name + _subnet

    # Sub-Networks instances creation
    sub_nets = [] # Sub Network list initialization

    for i in range(len(models_name_list)):

        torch.manual_seed(SEED) # Seed re-initialization

        # Sub-Net instance creation
        locals()[models_name_list[i]] = one_class_function(hidden_units, act_fun, dr_in, dr_hidden, models_name_list[i])
        sub_nets.append(locals()[models_name_list[i]])

```

```

    return sub_nets

# Load Architecture Parameters State function
def load_model_state(model, state_dict_path):
    """
    Load an existent State Dictionary in a defined model
    """

    model.load_state_dict(torch.load(state_dict_path))
    print(f'Loaded Parameters (from "{state_dict_path}") into: {model.name}')

    return model

# Build The OCON Model
ocon_vowels = OCON_bank(binaryClassifier, 100, 'ReLU', 0.8, 0.5, vowels) # Best MLP (see "One-Class_Binary_Classifier_Analysi

# Load Pre-Trained Architectures in a fresh Model instance:
#ocon_vowels = OCON_bank(binaryClassifier, 100, 'ReLU', 0.8, 0.5, vowels) # Best MLP (see "One-Class_Binary_Classifier_Analysi
#states_path = [ "Trained_models_state/ae_subnet_Params.pth",
#               "Trained_models_state/ah_subnet_Params.pth",
#               "Trained_models_state/aw_subnet_Params.pth",
#               "Trained_models_state/eh_subnet_Params.pth",
#               "Trained_models_state/er_subnet_Params.pth",
#               "Trained_models_state/ei_subnet_Params.pth",
#               "Trained_models_state/ih_subnet_Params.pth",
#               "Trained_models_state/iy_subnet_Params.pth",
#               "Trained_models_state/oa_subnet_Params.pth",
#               "Trained_models_state/oo_subnet_Params.pth",
#               "Trained_models_state/uh_subnet_Params.pth",
#               "Trained_models_state/uw_subnet_Params.pth"]
#
#for i in range(len(ocon_vowels)):
#    load_model_state(ocon_vowels[i], states_path[i])

# OCON Evaluation function
def OCON_eval(ocon_models_bank, features_dataset: np.ndarray = x_data_minmax[:, 1:], labels: np.ndarray = y_labels_raw_np):
    """
    Evaluate OCON models-bank over an entire dataset
    """
    # Output lists initialization
    predictions = []
    dist_errors = []
    eval_accuracies = []
    g_truths = [] # For plotting purposes

    # Evaluate each Sub-Network...
    for i in range(len(ocon_models_bank)):
        ocon_models_bank[i].eval() # Put j-esimal Sub-Network in Evaluation Mode
        print(f'{ocon_models_bank[i].name.upper()} Evaluation -', end=' ')

        with torch.no_grad():

            # Make predictions
            features_data_tensor = torch.tensor(features_dataset).float()
            raw_eval_predictions = ocon_models_bank[i](features_data_tensor)

            # Create Ground Truths
            ground_truth = np.where(labels == i, 1, 0)
            ground_truth_tensor = torch.tensor(ground_truth, dtype=torch.int64).squeeze()

            # Compute Errors
            dist_error = ground_truth_tensor - raw_eval_predictions.detach().squeeze() # Distances
            eval_accuracy = 100 * torch.mean(((raw_eval_predictions.detach().squeeze() > 0.5) == ground_truth_tensor).float())
            print(f'Accuracy: {eval_accuracy:.2f}%')

            # Outputs append
            predictions.append(raw_eval_predictions.detach())
            dist_errors.append(dist_error.detach())
            eval_accuracies.append(eval_accuracy.detach())

        g_truths.append(ground_truth)

    return predictions, dist_errors, eval_accuracies, g_truths

# For Pre-Trained Models
#ocon_predictions, ocon_dist_errors, ocon_eval_accuracies, ocon_g_truths = OCON_eval(ocon_vowels)

# Model Parameters State function
def model_desc(model):

```

```

"""
Print a Console report of Neural Network Model parameters
"""
# Parameters Description
print('Params Description:')
trainable_params = 0

for parameter in model.named_parameters():
    print(f'Parameter Name      : {parameter[0]}')
    print(f'Parameter Weights   : {parameter[1][:]}')
    if parameter[1].requires_grad:
        print(f'...with {parameter[1].numel()} TRAINABLE parameters')
        trainable_params += parameter[1].numel()

    print('.....')

print('-----')

# Nodes Count
nodes = 0
for param_name, param_tensor in model.named_parameters():
    if 'bias' in param_name:
        nodes += len(param_tensor)

print(f'Total Nodes          : {nodes}')
print('-----')

# OCON-Model Description
for i in range(len(ocon_vowels)):
    print(f'OCON "{ocon_vowels[i].name}" Classifier STATE')
    model_desc(ocon_vowels[i])
    print()

# Training/Eval/Testing Parameters
epochs = 1000 # For each "Data Batch-Set"
loss_break = 0.15 # loss (for Early Stopping)
acc_break = 95. # % accuracy (for Early Stopping)
min_tolerance = 0.01 # ...for sub-dataset balancing

# Outputs Initialization
loss_functions = [[] for _ in range(len(ocon_vowels))]
training_accuracies = [[] for _ in range(len(ocon_vowels))]
evaluation_accuracies = [[] for _ in range(len(ocon_vowels))]
test_accuracies = [[] for _ in range(len(ocon_vowels))]
training_times = []

# OCON Sub-Networks Training
from time import perf_counter
debug = False

for i, vowel in enumerate(vowels):
    print(f'Architecture "{ocon_vowels[i].name}" TRAINING PHASE')

    start_timer = perf_counter()
    # Iterated (w. Batch-Sets shuffling) Mini-Batch Training
    iteration = 0 # Batch Training iteration counter
    mean_loss = 1.
    test_accuracy = 0.

    while (mean_loss > loss_break) or (test_accuracy < acc_break):
        # Dataset processing
        sub_data, sub_data_labels_bin, _ = one_hot_encoder(sel_class_number=i, dataset=x_data_minmax, debug=debug)
        print('-----')
        trainLoader, devLoader, testLoader = train_dev_test_split(sub_data[:, 1:], sub_data_labels_bin, [0.5, 0.25, 0.25], tol

        # Train/Test Architecture
        train_accuracies, train_losses, dev_accuracies, test_accuracy = mini_batch_train_test(ocon_vowels[i], weight_decay=0.0
        print(f'Sub-Net "{vowel.upper()}" Epoch {(iteration + 1) * epochs} - TEST ACCURACY: {test_accuracy:.2f}%', end=' ')

        # Outputs append
        loss_functions[i].append(train_losses)
        training_accuracies[i].append(train_accuracies)
        evaluation_accuracies[i].append(dev_accuracies)
        test_accuracies[i].append(test_accuracy)

        # Repeating condition evaluation
        mean_loss = np.mean(train_losses[-50: ]) # Last 100 losses mean
        print(f'- MEAN LOSS: {mean_loss}')

    iteration += 1 # Go to next Batch training iteration

```

```

print(f'Training STOPPED at iteration {iteration}')
print('-----')
stop_timer = perf_counter()

print(f'"{ocon_vowels[i].name}" Training COMPLETED in {float(stop_timer - start_timer)}sec.')
training_times.append(stop_timer - start_timer)
print('-----')

# Graphical smoothing filter
def smooth(data, k=100):
    """
    A Convolution LP filter w. interval definition
    """
    return np.convolve(data, np.ones(k) / k, mode='same')

# Training Phase Plots
plt.figure(figsize=(12, 5 * 12))

# loss_functions, training_accuracies, evaluation_accuracies, test_accuracies, training_times
classes = len(ocon_vowels)

for i in range(classes):
    plt.subplot(classes, 2, (i * 2) + 1)
    flat_loss_function = [item for sublist in loss_functions[i] for item in sublist]

    plt.plot(smooth(flat_loss_function), 'k-')
    plt.axhline(loss_break, color='r', linestyle='--')
    plt.title(f'{ocon_vowels[i].name.upper()} Training Loss')
    plt.xlabel('Epochs')
    plt.xlim([100, len(flat_loss_function) - 100])
    plt.ylabel('GT - Predicted diff. (probability)')
    plt.grid()

    plt.subplot(classes, 2, (i * 2) + 2)
    flat_training_accuracy = [item for sublist in training_accuracies[i] for item in sublist]
    flat_dev_accuracy = [item for sublist in evaluation_accuracies[i] for item in sublist]
    flat_test_accuracy = test_accuracies[i]

    plt.plot(smooth(flat_training_accuracy), 'k-', label='Training')
    plt.plot(smooth(flat_dev_accuracy), color='grey', label='Development')
    if len(flat_test_accuracy) > 1:
        plt.plot([(n + 1) * epochs for n in range(len(flat_test_accuracy))], flat_test_accuracy, 'r-', label=f'Test')
    else:
        plt.axhline(test_accuracy, color='r', linestyle='-', label=f'Test')
    plt.title(f'{ocon_vowels[i].name.upper()} Accuracy (after {training_times[i]:.2f}sec.)')
    plt.xlabel('Epochs')
    plt.xlim([100, len(flat_training_accuracy) - 100])
    plt.ylabel('Accuracy (in %)')
    plt.ylim([40, 101])
    plt.grid()
    plt.legend(loc='best')

plt.tight_layout()
plt.savefig('OCON_training_phase')
plt.show()

# OCON Evaluation
ocon_predictions, ocon_dist_errors, ocon_eval_accuracies, ocon_g_truths = OCON_eval(ocon_vowels)

# Dataset Evaluation Analysis Plot
plt.figure(figsize=(18, 5 * len(ocon_vowels)))
plot_ticks = end_idx[:]
plot_ticks = np.delete(plot_ticks, -1)

for i in range(len(ocon_vowels)):
    plt.subplot(len(ocon_vowels), 3, (i * 3) + 1)
    plt.plot(ocon_predictions[i], 'k.', label='Raw Predictions')
    plt.plot(ocon_g_truths[i], 'rx', label='Ground Truths')
    plt.axhline(0.5, linestyle='--', color='grey')
    plt.title(f'{ocon_vowels[i].name.upper()} Predictions Accuracy: {ocon_eval_accuracies[i]:.2f}%')
    plt.xlabel('Data (Indices)')
    plt.xticks(ticks=plot_ticks, labels=vowels)
    plt.ylabel('Normalized Probability')
    plt.grid()
    plt.legend(loc='best')

    plt.subplot(len(ocon_vowels), 3, (i * 3) + 2)
    plt.plot(ocon_dist_errors[i], 'k')
    plt.title(f'Predicted to Measured Error')
    plt.xlabel('Data (Indices)')

```



```

plt.xticks(ticks=plot_ticks, labels=vowels)
plt.ylabel('Normalized Probability Error')
plt.ylim([-1.1, 1.1])
plt.grid()

plt.subplot(len(ocon_vowels), 3, (i * 3) + 3)

# Predictions list processing
predictions_temp = ocon_predictions[i]
class_predictions = [item for sublist in predictions_temp for item in sublist] # Turn a list of lists in a single list (c
for j in range(len(class_predictions)): # Turn a list of tensors of one variable in a list of scalars (item() method)
    class_predictions[j] = class_predictions[j].item()

# Positives & False-Positives extraction
positives = []
for w in range(len(vowels)):
    num = (np.array(class_predictions[end_idx[w]: end_idx[w + 1]]) > 0.5).sum()
    positives.append(num)

plt.bar(np.arange(len(vowels)), positives, color='k')
plt.title(f'"{vowels[i]}" Positive Probabilities Distribution')
plt.xlabel('Normalized Probabilities')
plt.ylabel('Occurences')
plt.xticks([n for n in range(12)], vowels)
plt.grid()

plt.tight_layout()
plt.savefig('OCON_bank_evaluation')
plt.show()

# Model Parameters Save/Load functions
from pathlib import Path

def save_model_state(model, folder_name: str = "Trained_models_state"):
    """
    Save Pre-Trained model parameters in a State Dictionary
    """

    MODEL_PATH = Path(folder_name) # Placed in root
    MODEL_PATH.mkdir(parents=True, exist_ok=True) # Pre-existing folder (w. same name) monitoring
    MODEL_NAME = '{}_{}'.format(model.name, "Params.pth")
    MODEL_SAVE_PATH = MODEL_PATH / MODEL_NAME

    print(f"Saving {model.name} Parameters in: {MODEL_SAVE_PATH}")
    torch.save(obj=model.state_dict(), f=MODEL_SAVE_PATH)

    return MODEL_SAVE_PATH

# Save Pre-Trained Models-bank
states_path = [] # Path for each model parameters state
for i in range(len(ocon_vowels)):
    state_path = save_model_state(ocon_vowels[i])
    states_path.append(state_path)
print()

```

## ▼ Output Maxnet Algorithm

```

# OCON "MaxNet" Architecture (Weightening + Non Linearity apply)
class OCON_MaxNet(nn.Module):
    def __init__(self, n_units, act_fun, eps):
        super().__init__()

        self.layers = nn.ModuleDict() # Dictionary to store Model layers
        self.eps_weight = eps

        # MaxNet Layer
        self.layers['MAXNET'] = nn.Linear(n_units, n_units) # Key 'MaxNet' layer specification

        # Weights & Bias initialization
        self.layers['MAXNET'].weight.data.fill_(self.eps_weight)
        for i in range(n_units):
            self.layers['MAXNET'].weight[i][i].data.fill_(1.) # Self Weight = 1

        self.layers['MAXNET'].bias.data.fill_(0.)

        # Activation Function
        self.actfun = act_fun # Function string-name attribute association

# Forward Pass Method

```

```

def forward(self, x):

    # Activation function object computation
    actfun = getattr(torch.nn, self.actfun)

    # Maxnet Layer pass                                     --> Output Weightening (Dot Product) "Linear transfo
    x = actfun()(self.layers['MAXNET'](x.squeeze().float()))

    # Self

    return x

# Build OCON MaxNetwork Architecture
torch.manual_seed(SEED)
ocon_maxnet = OCON_MaxNet(n_units=12, act_fun='ReLU', eps=0.25)

# MaxNet & Sub-Networks Parameters
print('OCON MaxNet STATE')
model_desc(ocon_maxnet)

def maxnet_algo(maxnet_function, n_units, act_fun, eps, input_array):
    """
    MaxNet Re-iteration algorithm for Maximum Value retrieving from an input array
    """
    non_zero_outs = np.count_nonzero(input_array) # Non Zero Values initialization
    maxnet_in = torch.from_numpy(input_array) # MaxNet Input Tensor initialization

    results = [] # Results initialization

    counter = 0
    while non_zero_outs != 1:
        counter += 1

        # Create the MaxNet
        torch.manual_seed(SEED) # Redundant
        maxnet = maxnet_function(n_units = n_units, act_fun = act_fun, eps = eps)

        # Compute Forward Pass
        results = maxnet(maxnet_in)

        # Non_zero outputs & Maxnet Input Update
        non_zero_outs = np.count_nonzero(results.detach().numpy())
        maxnet_in = results.detach() # Save results for next iteration

    print(f'Maximum Value found in {counter} iterations')
    return np.argmax(results.detach().numpy())

# MaxNet on Sub-Networks predictions
ocon_predictions_prob = np.zeros((len(ocon_predictions), x_data_minmax.shape[0])) # NumPy predictions matrix (12 * 1617)

# Convert from List of Tensors to 2D NumPy Array
for i in range(len(ocon_predictions)):
    ocon_predictions_prob[i, :] = ocon_predictions[i].detach().squeeze().numpy()

maxnet_class_predictions = [] # Classes Outputs list initialization
# MaxNet application
for i in range(x_data_minmax.shape[0]):
    print(f'Dataset Sample({i + 1}) Class Evaluation')

    samp_predictions = ocon_predictions_prob[:, i] # Array of 12 predictions for each Dataset sample (OCON outputs)
    class_prediction = maxnet_algo(OCON_MaxNet, n_units=12, act_fun='ReLU', eps=-0.1, input_array=samp_predictions) # MaxNet
    maxnet_class_predictions.append(class_prediction) # Result appending
    print('-----')

maxnet_accuracy = 100 * np.mean((np.array(maxnet_class_predictions).reshape(1597, 1) == y_labels_raw_np)) # Accuracy computat
print(f'Maxnet Output --> Phoneme ACCURACY: {maxnet_accuracy}%')

# Argmax on Sub-Networks predictions (...for multiple 1s probabilities MaxNet infinite loops)
#ocon_predictions_prob = np.zeros((len(new_ocon_predictions), x_data_minmax.shape[0])) # NumPy predictions matrix (12 * 1617)
#
# Convert from List of Tensors to 2D NumPy Array
#for i in range(len(new_ocon_predictions)):
#    ocon_predictions_prob[i, :] = new_ocon_predictions[i].detach().squeeze().numpy()
#
#maxnet_class_predictions = np.argmax(ocon_predictions_prob, axis=0)
#maxnet_accuracy = 100 * np.mean((np.array(maxnet_class_predictions).reshape(1617, 1) == y_labels_raw_np)) # Accuracy computa
#print(f'Maxnet Output ACCURACY: {maxnet_accuracy}%')

```

```

# Evaluation Analysis Plot
plt.figure(figsize=(30, 5))
plt.suptitle(f'OCN Bank + MaxNet Evaluation: {maxnet_accuracy:.0f}%')

plot_x_ticks = end_idx[:]
plot_x_ticks = np.delete(plot_x_ticks, len(end_idx) - 1)
plot_y_ticks = [n for n in range(len(vowels))]

plt.plot(y_labels_raw_np, 'rs', label='Ground Truths')
plt.plot(maxnet_class_predictions, 'k.', label='MAXNET Outputs')
plt.xlabel('Dataset samples')
plt.xticks(ticks=plot_x_ticks, labels=vowels)
plt.xlim([-10, len(y_labels_raw_np) + 10])
plt.ylabel('Labels')
plt.yticks(ticks=plot_y_ticks, labels=vowels)
plt.legend(loc='best')
plt.grid()

plt.tight_layout()
plt.savefig('OCN_model_evaluation')
plt.show()

```



## ▼ OCON Model Analysis

(13-features Complete Dataset - Speaker Recognition)

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**Year:** 2023

**Affiliation:** A.Casella Conservatory (student)

**Master Degree Thesis:** "Vowel phonemes Analysis & Classification by means of OCON rectifiers Deep Learning Architectures"

**Description:** Python scripts for One-Class-One-Network (OCON) Model analysis and optimization

```
# Numerical computations packages/modules
import numpy as np
import torch
import torch.nn as nn
import torch.nn.functional as F

# Dataset processing modules
from torch.utils.data import DataLoader
from sklearn.model_selection import train_test_split

# Graphic visualization modules
import matplotlib.pyplot as plt
import matplotlib_inline
matplotlib_inline.backend_inline.set_matplotlib_formats('svg')

# Common Seed initialization
SEED = 42 # ... the answer to the ultimate question of Life, the Universe, and Everything... (cit.)

# PyTorch Processing Units evaluation
device = 'cuda' if torch.cuda.is_available() else 'cpu'
print(f'AVAILABLE Processing Unit: {device.upper()}')
!nvidia-smi
```

## ▼ HGCW Dataset

- *Dataset\_utils.npz* file read
- *One-Hot encoding* definition
- *Train/Dev/Test split* definition

```
# Load HGCW 13_features_complete_(w_speaker) Dataset
HGCW_dataset_utils = np.load(file='./HGCW_dataset_utils.npz')
print('Raw features Data shape:', HGCW_dataset_utils['HGCW_raw'].shape)
print('Fundamental Normalized features Data shape:', HGCW_dataset_utils['HGCW_fund_norm'].shape)
print('MinMax features Data shape:', HGCW_dataset_utils['HGCW_minmax'].shape)
print('Phoneme Labels Data shape:', HGCW_dataset_utils['HGCW_phon_labels'].shape)
print('Speaker Labels Data shape:', HGCW_dataset_utils['HGCW_spk_labels'].shape)
print('Phoneme Classes size Data shape:', HGCW_dataset_utils['phon_size'].shape)
print('Phoneme Classes indices Data shape:', HGCW_dataset_utils['phon_idx'].shape)
print('Phoneme-Speaker coordinates Data shape:', HGCW_dataset_utils['phon_spk_coords'].shape) # (Start_Idx, Vow-Spk group)

x_data_raw_np = HGCW_dataset_utils['HGCW_raw']
x_data_fund_norm = HGCW_dataset_utils['HGCW_fund_norm']
x_data_minmax = HGCW_dataset_utils['HGCW_minmax']
y_labels_raw_np = HGCW_dataset_utils['HGCW_phon_labels']
z_labels_raw_np = HGCW_dataset_utils['HGCW_spk_labels']
vow_size = HGCW_dataset_utils['phon_size']
end_idx = HGCW_dataset_utils['phon_idx']
phon_spk_coords = HGCW_dataset_utils['phon_spk_coords']

# Auxiliary lists
vowels = ['ae', 'ah', 'aw', 'eh', 'er', 'ei', 'ih', 'iy', 'oa', 'oo', 'uh', 'uw'] # Vowels list (0 - 11)
speakers = ['b', 'g', 'm', 'w'] # Speakers list (0 - 3)
colors = ['green', 'blue', 'red'] # ['red', 'saddlebrown', 'darkorange', 'darkgoldenrod', 'gold', 'darkkhaki', 'olive', 'dark

# Fundamental Frequency - Min-Max Scaling
print(f'Previous Fundamental Frequency Min: {x_data_minmax[:, 0].min()}, Max: {x_data_minmax[:, 0].max()}')
x_data_minmax[:, 0] = (x_data_minmax[:, 0] - x_data_minmax[:, 0].min()) / (x_data_minmax[:, 0].max() - x_data_minmax[:, 0].min())
print(f'Actual Fundamental Frequency Min: {x_data_minmax[:, 0].min()}, Max: {x_data_minmax[:, 0].max()}')
```

```

# Children Labels encoding
z_labels_raw_np_alt = np.where(z_labels_raw_np <= 1, 0, z_labels_raw_np - 1)
speakers_alt = ['c', 'm', 'w']

def one_hot_encoder(sel_speaker_num=0, dataset=x_data_minmax, spk_labels=z_labels_raw_np_alt, speakers=speakers_alt, debug=False):

    if sel_speaker_num < len(speakers):
        classes = [n for n in range(len(speakers))] # Speaker indices
        sub_groups_size = [] # Same as vow_size list

        sub_data_one = dataset[np.where(spk_labels == sel_speaker_num)[0], :] # Extract selected speaker sub-dataset
        sub_labels_one = np.ones((sub_data_one.shape[0], 1), dtype='int') # Binarized 1-Label creation
        sub_labels_one_orig = np.ones((sub_data_one.shape[0], 1), dtype='int') * sel_speaker_num # Create a copy of original
        sub_groups_size.append(sub_data_one.shape[0])
        if debug is True:
            print(f'Selected Class "{speakers[sel_speaker_num]}"-speaker : {sub_data_one.shape[0]} samples')

        sub_speakers_size = sub_data_one.shape[0] // 2 # Size for each other speaker sub-group (balancing)
        if debug is True:
            print(f'Rest Classes size (...each): {sub_speakers_size} samples')

        sub_data_zero = np.zeros((sub_speakers_size * 2, sub_data_one.shape[1])) # Zero-label features dataset initialization
        sub_labels_zero_orig = np.zeros((sub_speakers_size * 2, 1), dtype='int') # Original labels subset array initialization

        classes.remove(sel_speaker_num) # Remove selected speaker index
        counter = 0
        for i in classes: # For other speakers...
            sub_data_zero_class = dataset[np.where(spk_labels == i)[0], :] # Extract speaker subgroup
            subset_indices = np.random.choice(np.arange(0, sub_data_zero_class.shape[0], 1), size=sub_speakers_size, replace=False)

            sub_data_zero[counter * sub_speakers_size : (counter * sub_speakers_size) + sub_speakers_size, :] = sub_data_zero_class
            sub_labels_zero_orig[counter * sub_speakers_size : (counter * sub_speakers_size) + sub_speakers_size, :] = np.ones
            sub_groups_size.append(sub_data_zero_class[subset_indices].shape[0])

            counter += 1

        sub_labels_zero = np.zeros((sub_data_zero.shape[0], 1), dtype='int') # Binarized 0 Label creation

        # Output Matrices
        sub_data = np.vstack((sub_data_one, sub_data_zero)) # Vertical stacking 1s and 0s features array
        sub_data_labels_bin = np.vstack((sub_labels_one, sub_labels_zero)) # Vertical Stacking 1s and 0s labels array
        sub_data_labels_orig = np.vstack((sub_labels_one_orig, sub_labels_zero_orig)) # Vertical stacking original (1-class)
    else:
        raise ValueError(f'Invalid Class ID: "{sel_speaker_num}" --> It must be less than {len(speakers)}!')

    return sub_data, sub_data_labels_bin, sub_data_labels_orig, sub_groups_size

# Test Call
sel_speaker_num = 0
sub_data, sub_data_labels_bin, sub_data_labels_orig, sub_groups_size = one_hot_encoder(sel_speaker_num, dataset=x_data_minmax,
print(f'Output Array shapes: {sub_data.shape}, {sub_data_labels_bin.shape}, {sub_data_labels_orig.shape}, {len(sub_groups_size)}')

# Sub-Dataset Plot (previous example)
classes = [n for n in range(len(speakers_alt))]

plt.figure(figsize=(12, 15))
plt.suptitle(f'Sub-Dataset ("{speakers_alt[sel_speaker_num].upper()}"-speaker - example) One-Hot Encoding')

counter = 0
for index in range(len(speakers_alt)):
    if index == sel_speaker_num:
        first_coords = sub_data[:sub_groups_size[0], 1]
        second_coords = sub_data[:sub_groups_size[0], 2]
        third_coords = sub_data[:sub_groups_size[0], 3]
    else:
        start_index = sub_groups_size[0] + counter * sub_groups_size[1]
        end_index = start_index + sub_groups_size[1]

        first_coords = sub_data[start_index: end_index, 1]
        second_coords = sub_data[start_index: end_index, 2]
        third_coords = sub_data[start_index: end_index, 3]

        counter += 1

plt.subplot(3, 2, 1)
plt.title('$1_{st}$ VS $2_{nd}$')
plt.scatter(first_coords, second_coords, marker='o', color=colors[index], label=f'{speakers_alt[index]}-speaker')
plt.xlabel('$1_{st}$ Formant Ratio')
plt.ylabel('$2_{nd}$ Formant Ratio')
plt.legend(loc='best')
plt.grid(True)

```

```

plt.subplot(3, 2, 3)
plt.title('$1_{st}$ VS $3_{rd}$')
plt.scatter(first_coords, third_coords, marker='o', color=colors[index], label=f'"{speakers_alt[index]}"-speaker')
plt.xlabel('$1_{st}$ Formant Ratio')
plt.ylabel('$3_{rd}$ Formant Ratio')
plt.legend(loc='best')
plt.grid(True)

plt.subplot(3, 2, 5)
plt.title('$2_{nd}$ VS $3_{rd}$')
plt.scatter(second_coords, third_coords, marker='o', color=colors[index], label=f'"{speakers_alt[index]}"-speaker')
plt.xlabel('$2_{nd}$ Formant Ratio')
plt.ylabel('$3_{rd}$ Formant Ratio')
plt.legend(loc='best')
plt.grid(True)

plt.subplot(3, 2, 2)
plt.title('$1_{st}$ VS $2_{nd}$ Binarized')
plt.scatter(sub_data[0: sub_groups_size[0], 1], sub_data[0: sub_groups_size[0], 2], color=colors[sel_speaker_num], label=f'"{s
plt.scatter(sub_data[sub_groups_size[0]: , 1], sub_data[sub_groups_size[0]: , 2], color='grey', label=f'Rest')
plt.xlabel('$1_{st}$ Formant Ratio')
plt.ylabel('$2_{nd}$ Formant Ratio')
plt.legend(loc='best')
plt.grid(True)

plt.subplot(3, 2, 4)
plt.title('$1_{st}$ VS $3_{rd}$ Binarized')
plt.scatter(sub_data[0: sub_groups_size[0], 1], sub_data[0: sub_groups_size[0], 3], color=colors[sel_speaker_num], label=f'"{s
plt.scatter(sub_data[sub_groups_size[0]: , 1], sub_data[sub_groups_size[0]: , 3], color='grey', label=f'Rest')
plt.xlabel('$1_{st}$ Formant Ratio')
plt.ylabel('$3_{rd}$ Formant Ratio')
plt.legend(loc='best')
plt.grid(True)

plt.subplot(3, 2, 6)
plt.title('$2_{nd}$ VS $3_{rd}$ Binarized')
plt.scatter(sub_data[0: sub_groups_size[0], 2], sub_data[0: sub_groups_size[0], 3], color=colors[sel_speaker_num], label=f'"{s
plt.scatter(sub_data[sub_groups_size[0]: , 2], sub_data[sub_groups_size[0]: , 3], color='grey', label=f'Rest')
plt.xlabel('$2_{nd}$ Formant Ratio')
plt.ylabel('$3_{rd}$ Formant Ratio')
plt.legend(loc='best')
plt.grid(True)

plt.tight_layout()
plt.savefig(f'{speakers_alt[sel_speaker_num]}_speaker_one_hot_encoding')
plt.show()

# Train/Test split (auxiliary function)
def train_test_split_aux(features_dataset, labels_dataset, test_perc, tolerance):
    """
    An auxiliary Train_Test_split function (based on Scikit Learn implementation) w. balance tolerance specification
    """
    test_size = int(test_perc / 100 * len(features_dataset))
    train_balance = 0 # Output Training set balance value initialization
    test_balance = 0 # Output Testing set balance value initialization

    min_tol = np.mean(labels_dataset) - tolerance
    max_tol = np.mean(labels_dataset) + tolerance
    print(f'Data Balancing (TARGET = {np.mean(labels_dataset)} +/- {tolerance}): ', end='')

    while (min_tol >= train_balance or train_balance >= max_tol) or (min_tol >= test_balance or test_balance >= max_tol):
        train_data, test_data, train_labels, test_labels = train_test_split(features_dataset, labels_dataset, test_size=test_s
        train_balance = np.mean(train_labels)
        test_balance = np.mean(test_labels)
        print('.', end='')
    else:
        print('OK')

    return train_data, test_data, train_labels, test_labels, train_balance, test_balance

# Train-Dev-Test split function
def train_dev_test_split(x_data, y_labels, split_list, tolerance=0.1, output='Loaders', debug=False):
    """
    Compute a Train, Development (Hold-Out) and a Test set split w. PyTorch Dataset conversion (and eventual Loaders initializ
    """
    if len(split_list) == 3:
        # Train - Dev+Test separation
        print('Training --- Devel/Test SPLIT')
        train_data, testTMP_data, train_labels, testTMP_labels, _, _ = train_test_split_aux(x_data, y_labels, (split_list[1] *
        print('-----')

```

```

# Dev - Test separation
print('Devel    ---    Test SPLIT')

split = ((split_list[1] * 100) / np.sum(split_list[1:] * 100)) * 100 # Split in %
dev_data, test_data, dev_labels, test_labels, _, _ = train_test_split_aux(testTMP_data, testTMP_labels, split, toleran
print('-----')

# Tensor Conversion
train_data_tensor = torch.tensor(train_data).float()
train_labels_tensor = torch.tensor(train_labels, dtype=torch.int64).squeeze()
dev_data_tensor = torch.tensor(dev_data).float()
dev_labels_tensor = torch.tensor(dev_labels, dtype=torch.int64).squeeze()
test_data_tensor = torch.tensor(test_data).float()
test_labels_tensor = torch.tensor(test_labels, dtype=torch.int64).squeeze()
if debug is True:
    print(f'Training Data      Shape: {train_data.shape}')
    print(f'Development Data   Shape: {dev_data.shape}')
    print(f'Testing Data        Shape: {test_data.shape}')

# Balance Evaluation
print(f'Training Set          Balance: {np.mean(train_labels)}')
print(f'Development Set       Balance: {np.mean(dev_labels)}')
print(f'Testing Set           Balance: {np.mean(test_labels)}')

if output != 'Loaders':
    return train_data_tensor, train_labels_tensor, dev_data_tensor, dev_labels_tensor, test_data_tensor, test_labels_t
else:
    # PyTorch Dataset Conversion
    train_dataset = torch.utils.data.TensorDataset(torch.tensor(train_data).float(), torch.tensor(train_labels, dtype=
dev_dataset = torch.utils.data.TensorDataset(torch.tensor(dev_data).float(), torch.tensor(dev_labels, dtype=torch.
test_dataset = torch.utils.data.TensorDataset(torch.tensor(test_data).float(), torch.tensor(test_labels, dtype=tor

# DataLoader (Batches) --> Drop-Last control to optimize training
trainLoader = DataLoader(train_dataset, shuffle=False, batch_size = 32, drop_last=True)
devLoader = DataLoader(dev_dataset, shuffle=False, batch_size = dev_dataset.tensors[0].shape[0])
testLoader = DataLoader(test_dataset, shuffle=False, batch_size = test_dataset.tensors[0].shape[0])
if debug is True:
    print(f'Training Set      Batch Size: {trainLoader.batch_size}')
    print(f'Development Set    Batch Size: {devLoader.batch_size}')
    print(f'Testing Set        Batch Size: {testLoader.batch_size}')

    return trainLoader, devLoader, testLoader
else:
    # Train - Test separation
    print('Training --- Test    SPLIT')
    train_data, test_data, train_labels, test_labels, _, _ = train_test_split_aux(x_data, y_labels, split_list[1] * 100, t
    print('-----')

# Tensor Conversion
train_data_tensor = torch.tensor(train_data).float()
train_labels_tensor = torch.tensor(train_labels, dtype=torch.int64).squeeze()
test_data_tensor = torch.tensor(test_data).float()
test_labels_tensor = torch.tensor(test_labels, dtype=torch.int64).squeeze()
if debug is True:
    print(f'Training Data      Shape: {train_data.shape}')
    print(f'Testing Data        Shape: {test_data.shape}')

# Balance Evaluation
print(f'Training Set          Balance: {np.mean(train_labels)}')
print(f'Testing Set           Balance: {np.mean(test_labels)}')

if output != 'Loaders':
    return train_data_tensor, train_labels_tensor, test_data_tensor, test_labels_tensor
else:
    # PyTorch Dataset Conversion
    train_dataset = torch.utils.data.TensorDataset(torch.tensor(train_data).float(), torch.tensor(train_labels, dtype=
test_dataset = torch.utils.data.TensorDataset(torch.tensor(test_data).float(), torch.tensor(test_labels, dtype=tor

# DataLoader (Batches) --> Drop-Last control to optimize training
trainLoader = DataLoader(train_dataset, shuffle=False, batch_size = 32, drop_last=True)
testLoader = DataLoader(test_dataset, shuffle=False, batch_size = test_dataset.tensors[0].shape[0])
if debug is True:
    print(f'Training Set      Batch Size: {trainLoader.batch_size}')
    print(f'Testing Set        Batch Size: {testLoader.batch_size}')

    return trainLoader, testLoader

```

## ▼ One-Class Architecture (Binary Classifier)

(see "One-Class\_Sub-Network\_Analysis.ipynb")



## Multi-Layer Perceptron

- Input Layer: 3 features [formant ratios, min-max normalized]
- Hidden Layer: 100 units
- Output Layer: 1 normalized probability
- Learning Rate: 0.0001 ( $10^{-4}$ )
- Optimizer: Adam (Adaptive Momentum)

### - Mini-Batch Training:

- . Re-iterated Sub-Dataset Shuffling
- . Early Stopping (Test Accuracy driven)
- . Batch size = 32

### - Regularization:

- . Weight Decay (L2 Penalty): 0.0001 ( $10^{-4}$ )
- . DropOut:
  - \* Input Layer Drop Rate: 0.8
  - \* Hidden Layer Drop Rate: 0.5.
- . Batch Normalization

- *MLP Classifier Architecture* class definition
- *Mini-Batch Training* function definition

```
# Dynamic Multi-Layer Architecture Class (w. units, activation function, batch normalization and dropOut rate specification)
class binaryClassifier(nn.Module):
    def __init__(self, n_units, act_fun, rate_in, rate_hidden, model_name):
        super().__init__()

        self.layers = nn.ModuleDict()
        self.name = model_name

        # Input Layer
        self.layers['input'] = nn.Linear(13, n_units)

        # Hidden Layer
        self.layers[f'hidden'] = nn.Linear(n_units, n_units)
        self.layers[f'batch_norm'] = nn.BatchNorm1d(n_units)

        # Output Layer
        self.layers['output'] = nn.Linear(n_units, 1)

        # Activation Function
        self.actfun = act_fun

        # Dropout Parameter
        self.dr_in = rate_in
        self.dr_hidden = rate_hidden

        # Weights & Bias initialization
        for layer in self.layers.keys():
            try:
                nn.init.kaiming_normal_(self.layers[layer].weight, mode='fan_in')
            except:
                pass
            self.layers[layer].bias.data.fill_(0.)

# Forward Pass Method
def forward(self, x):

    # Activation function object computation
    actfun = getattr(torch.nn, self.actfun)

    # Input Layer pass
    x = actfun()(self.layers['input'](x))
    x = F.dropout(x, p=self.dr_in, training=self.training)

    # Single Hidden Layer pass
    x = self.layers[f'batch_norm'](x)
    x = actfun()(self.layers[f'hidden'](x))
    x = F.dropout(x, p=self.dr_hidden, training=self.training)

    # Output Layer pass
    x = self.layers['output'](x)
    x = nn.Sigmoid()(x)

    return x
```

```

# Batch Training function (w. Adam Optimizer & L2 penalty term) Re-Definition
def mini_batch_train_test(model, weight_decay, epochs: int, learning_rate, train_loader, dev_loader, test_loader, debug=False)
    """
    Train & Test an ANN Architecture via Mini-Batch Training (w. Train/Dev/Test PyTorch Loaders) and Adam Backpropagation Opti
    """
    # Loss Function initialization
    loss_function = nn.BCELoss()

    # Optimizer Algorithm initialization
    optimizer = torch.optim.Adam(model.parameters(), lr=learning_rate, weight_decay=weight_decay)

    # Output list initialization
    train_accuracies = []
    train_losses = []
    dev_accuracies = []

    # TRAINING Phase
    for epoch in range(epochs):
        model.train() # TRAINING Switch ON

        batch_accuracies = []
        batch_losses = []

        # Training BATCHES Loop
        for data_batch, labels_batch in train_loader:
            train_predictions = model(data_batch)
            train_loss = loss_function(train_predictions.squeeze(), labels_batch.type(torch.int64).float())
            batch_losses.append(train_loss.detach())

            # Backpropagation
            optimizer.zero_grad()
            train_loss.backward()
            optimizer.step()

            # Accuracy
            train_accuracy = 100 * torch.mean(((train_predictions.squeeze() > 0.5) == labels_batch.type(torch.int64).squeeze()))

            # Batch Stats appending
            batch_accuracies.append(train_accuracy.detach())
            batch_losses.append(train_loss.detach())

        # Training Stats appending
        train_accuracies.append(np.mean(batch_accuracies)) # Average of Batch Accuracies = Training step accuracy
        train_losses.append(np.mean(batch_losses)) # Average of Batch Losses = Training step Losses

    # EVALUATION (Dev) Phase
    model.eval()
    with torch.no_grad():
        dev_data_batch, dev_labels_batch = next(iter(dev_loader))
        dev_predictions = model(dev_data_batch)

        dev_accuracy = 100 * torch.mean(((dev_predictions.squeeze() > 0.5) == dev_labels_batch.type(torch.int64).squeeze()))

        if debug is True:
            if epoch % 100 == 0:
                print(f'Epoch {epoch} --> DEV ACCURACY: {dev_accuracy.detach():.3f} %')
                print('-----')

        # Evaluation accuracy appending
        dev_accuracies.append(dev_accuracy.detach())

    # TEST Phase
    model.eval()
    with torch.no_grad():
        test_data_batch, test_labels_batch = next(iter(test_loader))
        test_predictions = model(test_data_batch)
        test_accuracy = 100 * torch.mean(((test_predictions.squeeze() > 0.5) == test_labels_batch.type(torch.int64).squeeze()))

        if debug is True:
            print(f'TEST ACCURACY: {test_accuracy.detach():.2f} %')
            print('-----')

    return train_accuracies, train_losses, dev_accuracies, test_accuracy.detach()

```

## ▼ OCON (One-Class-One-Net) Model

Binary classifiers **Parallelization**

- *Classifiers-Bank* function definition
  - *Models Parameters* inspection

- Classifiers **Sequential** Training & Evaluation
  - *Models Parameters State Save/Load* function definition
- 

- MaxNet output algorithm
- Argmax output algorithm

```
def OCON_bank(one_class_function, hidden_units, act_fun, dr_in, dr_hidden, classes_list):
    """
    Create a One-Class-One-Network parallelization bank of an input Sub-Network definition
    """
    # Sub-Net names creation
    models_name_list = []
    for i in range(len(classes_list)):
        models_name_list.append("{}_{}".format(classes_list[i], "subnet")) # Class name + _subnet

    # Sub-Networks instances creation
    sub_nets = [] # Sub Network list initialization

    for i in range(len(models_name_list)):

        torch.manual_seed(SEED) # Seed re-initialization

        # Sub-Net instance creation
        locals()[models_name_list[i]] = one_class_function(hidden_units, act_fun, dr_in, dr_hidden, models_name_list[i])
        sub_nets.append(locals()[models_name_list[i]])

    return sub_nets

# Load Architecture Parameters State function
def load_model_state(model, state_dict_path):
    """
    Load an existent State Dictionary in a defined model
    """

    model.load_state_dict(torch.load(state_dict_path))
    print(f'Loaded Parameters (from "{state_dict_path}") into: {model.name}')

    return model

# Build The OCON Model
ocon_speakers = OCON_bank(binaryClassifier, 100, 'ReLU', 0.8, 0.5, speakers_alt) # Best MLP (see "One-Class_Binary_Classifier

# Load Pre-Trained Architectures in a fresh Model instance:
#ocon_vowels = OCON_bank(binaryClassifier, 100, 'ReLU', 0.8, 0.5, speaker) # Best MLP (see "One-Class_Binary_Classifier_Analy
#states_path = ["Trained_models_state/b_subnet_Params.pth",
#               "Trained_models_state/g_subnet_Params.pth",
#               "Trained_models_state/m_subnet_Params.pth",
#               "Trained_models_state/w_subnet_Params.pth"]
#
#for i in range(len(ocon_speakers)):
#    load_model_state(ocon_speakers[i], states_path[i])

# OCON Evaluation function
def OCON_eval(ocon_models_bank, features_dataset: np.ndarray = x_data_minmax, labels: np.ndarray = z_labels_raw_np_alt):
    """
    Evaluate OCON models-bank over an entire dataset
    """
    # Output lists initialization
    predictions = []
    dist_errors = []
    eval_accuracies = []
    g_truths = [] # For plotting purposes

    # Evaluate each Sub-Network...
    for i in range(len(ocon_models_bank)):
        ocon_models_bank[i].eval() # Put j-esimal Sub-Network in Evaluation Mode
        print(f'{ocon_models_bank[i].name.upper()} Evaluation -', end=' ')

        with torch.no_grad():

            # Make predictions
            features_data_tensor = torch.tensor(features_dataset).float()
            raw_eval_predictions = ocon_models_bank[i](features_data_tensor)

            # Create Ground Truths
            ground_truth = np.where(labels == i, 1, 0)
            ground_truth_tensor = torch.tensor(ground_truth, dtype=torch.int64).squeeze()

            # Compute Errors
```

```

        dist_error = ground_truth_tensor - raw_eval_predictions.detach().squeeze() # Distances
        eval_accuracy = 100 * torch.mean(((raw_eval_predictions.detach().squeeze() > 0.5) == ground_truth_tensor).float())
        print(f'Accuracy: {eval_accuracy:.2f}%')

    # Outputs append
    predictions.append(raw_eval_predictions.detach())
    dist_errors.append(dist_error.detach())
    eval_accuracies.append(eval_accuracy.detach())

    g_truths.append(ground_truth)

    return predictions, dist_errors, eval_accuracies, g_truths

# For Pre-Trained Models
#ocon_predictions, ocon_dist_errors, ocon_eval_accuracies, ocon_g_truths = OCON_eval(ocon_speakers)

# Model Parameters State function
def model_desc(model):
    """
    Print a Console report of Neural Network Model parameters
    """
    # Parameters Description
    print('Params Description:')
    trainable_params = 0

    for parameter in model.named_parameters():
        print(f'Parameter Name      : {parameter[0]}')
        print(f'Parameter Weights    : {parameter[1][:]}')
        if parameter[1].requires_grad:
            print(f'...with {parameter[1].numel()} TRAINABLE parameters')
            trainable_params += parameter[1].numel()

    print('.....')

    print('-----')

    # Nodes Count
    nodes = 0
    for param_name, param_tensor in model.named_parameters():
        if 'bias' in param_name:
            nodes += len(param_tensor)

    print(f'Total Nodes          : {nodes}')
    print('-----')

# OCON-Model Description
for i in range(len(ocon_speakers)):
    print(f'OCON "{ocon_speakers[i].name}" Classifier STATE')
    model_desc(ocon_speakers[i])
    print()

# Training/Eval/Testing Parameters
epochs = 1000 # For each "Data Batch-Set"
loss_breaks = [0.36, 0.08, 0.45] # loss (for Early Stopping) --> class-specific (empyirical)
acc_breaks = [80., 97., 80.] # % accuracy (for Early Stopping) --> class-specific (empyirical)
min_tolerance = 0.01 # ...for sub-dataset balancing

# Outputs Initialization
loss_functions = [[] for _ in range(len(ocon_speakers))]
training_accuracies = [[] for _ in range(len(ocon_speakers))]
evaluation_accuracies = [[] for _ in range(len(ocon_speakers))]
test_accuracies = [[] for _ in range(len(ocon_speakers))]
training_times = []

# OCON Sub-Networks Training
from time import perf_counter
debug = False

for i, speaker in enumerate(speakers_alt):

    # Class-specific Early Stopping parameters
    loss_break = loss_breaks[i]
    acc_break = acc_breaks[i]

    print(f'Architecture "{ocon_speakers[i].name}" TRAINING PHASE')
    print(f'EARLY STOP THRESHOLD: Loss={loss_break}, Accuracy={acc_break}%')

    start_timer = perf_counter()
    # Iterated (w. Batch-Sets shuffling) Mini-Batch Training
    iteration = 0 # Batch Training iteration counter

```

```

mean_loss = 1.
test_accuracy = 0.

while (mean_loss > loss_break) or (test_accuracy < acc_break):
    # Dataset processing
    sub_data, sub_data_labels_bin, _, _ = one_hot_encoder(sel_speaker_num=i, dataset=x_data_minmax, debug=debug)
    print('-----')
    trainLoader, devLoader, testLoader = train_dev_test_split(sub_data, sub_data_labels_bin, [0.5, 0.25, 0.25], tolerance=

    # Train/Test Architecture
    train_accuracies, train_losses, dev_accuracies, test_accuracy = mini_batch_train_test(ocon_speakers[i], weight_decay=0
    print(f'Sub-Net "{speaker.upper()}" Epoch {(iteration + 1) * epochs} - TEST ACCURACY: {test_accuracy:.2f}%', end=' ')

    # Outputs append
    loss_functions[i].append(train_losses)
    training_accuracies[i].append(train_accuracies)
    evaluation_accuracies[i].append(dev_accuracies)
    test_accuracies[i].append(test_accuracy)

    # Repeating condition evaluation
    mean_loss = np.mean(train_losses[-50: ]) # Last 50 losses mean
    print(f'- MEAN LOSS: {mean_loss}')

    iteration += 1 # Go to next Batch training iteration

print(f'Training STOPPED at iteration {iteration}')
print('-----')
stop_timer = perf_counter()

print(f'"{ocon_speakers[i].name}" Training COMPLETED in {float(stop_timer - start_timer)}sec.')
training_times.append(stop_timer - start_timer)
print('-----')

# Graphical smoothing filter
def smooth(data, k=100):
    """
    A Convolution LP filter w. interval definition
    """
    return np.convolve(data, np.ones(k) / k, mode='same')

# Training Phase Plots
plt.figure(figsize=(12, 5 * 3))

# loss_functions, training_accuracies, evaluation_accuracies, test_accuracies, training_times
classes = len(ocon_speakers)

for i in range(classes):
    plt.subplot(classes, 2, (i * 2) + 1)
    flat_loss_function = [item for sublist in loss_functions[i] for item in sublist]

    plt.plot(smooth(flat_loss_function), 'k-')
    plt.axhline(loss_breaks[i], color='r', linestyle='--')
    plt.title(f'{ocon_speakers[i].name.upper()} Training Loss')
    plt.xlabel('Epochs')
    plt.xlim([100, len(flat_loss_function) - 100])
    plt.ylabel('GT - Predicted diff. (probability)')
    plt.grid()

    plt.subplot(classes, 2, (i * 2) + 2)
    flat_training_accuracy = [item for sublist in training_accuracies[i] for item in sublist]
    flat_dev_accuracy = [item for sublist in evaluation_accuracies[i] for item in sublist]
    flat_test_accuracy = test_accuracies[i]

    plt.plot(smooth(flat_training_accuracy), 'k-', label='Training')
    plt.plot(smooth(flat_dev_accuracy), color='grey', label='Development')
    if len(flat_test_accuracy) > 1:
        plt.plot([(n + 1) * epochs for n in range(len(flat_test_accuracy))], flat_test_accuracy, 'r-', label=f'Test')
    else:
        plt.axhline(test_accuracy, color='r', linestyle='-', label=f'Test')
    plt.title(f'{ocon_speakers[i].name.upper()} Accuracy (after {training_times[i]:.2f}sec.)')
    plt.xlabel('Epochs')
    plt.xlim([100, len(flat_training_accuracy) - 100])
    plt.ylabel('Accuracy (in %)')
    plt.ylim([40, 101])
    plt.grid()
    plt.legend(loc='best')

plt.tight_layout()
plt.savefig('OCON_training_phase')
plt.show()

```

```

sub_groups_size

# OCON Evaluation

# Dataset & Labels Ordering (Plot conveniences)
x_data_minmax_ordered = np.zeros((1, x_data_minmax.shape[1]))
z_labels_raw_np_alt_ordered = np.zeros((1, 1), dtype='int')
data_size = []

# Groups Ordering iteration
for i in range(len(ocon_speakers)):
    indices = np.where(z_labels_raw_np_alt == i)[0]
    data_size.append(len(indices))

    x_data_minmax_ordered = np.vstack((x_data_minmax_ordered, x_data_minmax[indices]))
    z_labels_raw_np_alt_ordered = np.vstack((z_labels_raw_np_alt_ordered, z_labels_raw_np_alt[indices]))

x_data_minmax_ordered = np.delete(x_data_minmax_ordered, 0, axis=0) # Remove 1st initialization null row
z_labels_raw_np_alt_ordered = np.delete(z_labels_raw_np_alt_ordered, 0, axis=0) # Remove 1st initialization null label
print(f'Features Dataset Shapes : original {x_data_minmax.shape} VS ordered {x_data_minmax_ordered.shape}')
print(f'Labels Dataset Shapes : original {z_labels_raw_np_alt.shape} VS ordered {z_labels_raw_np_alt_ordered.shape}')

ocon_predictions, ocon_dist_errors, ocon_eval_accuracies, ocon_g_truths = OCON_eval(ocon_speakers, features_dataset=x_data_min

# Dataset Evaluation Analysis Plot
plt.figure(figsize=(18, 5 * len(ocon_speakers)))
plot_ticks = []
for n in range(len(data_size)):
    plot_ticks.append(np.sum(data_size[: n], dtype='int'))

iter_idx = plot_ticks + [len(x_data_minmax_ordered)]

for i in range(len(ocon_speakers)):
    plt.subplot(len(ocon_speakers), 3, (i * 3) + 1)
    plt.plot(ocon_predictions[i], 'k.', label='Raw Predictions')
    plt.plot(ocon_g_truths[i], 'rx', label='Ground Truths')
    plt.axhline(0.5, linestyle='--', color='grey')
    plt.title(f'{ocon_speakers[i].name.upper()} Predictions Accuracy: {ocon_eval_accuracies[i]:.2f}%')
    plt.xlabel('Data (Indices)')
    plt.xticks(plot_ticks, speakers_alt)
    plt.ylabel('Normalized Probability')
    plt.grid()
    plt.legend(loc='best')

    plt.subplot(len(ocon_speakers), 3, (i * 3) + 2)
    plt.plot(ocon_dist_errors[i], 'k')
    plt.title(f'Predicted to Measured Error')
    plt.xlabel('Data (Indices)')
    plt.xticks(plot_ticks, speakers_alt)
    plt.ylabel('Normalized Probability Error')
    plt.ylim([-1.1, 1.1])
    plt.grid()

    plt.subplot(len(ocon_speakers), 3, (i * 3) + 3)

    # Predictions list processing
    predictions_temp = ocon_predictions[i]
    class_predictions = [item for sublist in predictions_temp for item in sublist] # Turn a list of lists in a single list (c
    for j in range(len(class_predictions)): # Turn a list of tensors of one variable in a list of scalars (item() method)
        class_predictions[j] = class_predictions[j].item()

    # Positives & False-Positives extraction
    positives = []
    for w in range(len(speakers_alt)):
        num = (np.array(class_predictions[iter_idx[w]: iter_idx[w + 1]]) > 0.5).sum()
        positives.append(num)

    plt.bar(np.arange(len(speakers_alt)), positives, color='k')
    plt.title(f'{speakers_alt[i]} Positive Probabilities Distribution')
    plt.xlabel('Normalized Probabilities')
    plt.ylabel('Occurences')
    plt.xticks([n for n in range(3)], speakers_alt)
    plt.grid()

plt.tight_layout()
plt.savefig('OCON_bank_evaluation')
plt.show()

# Model Parameters Save/Load functions
from pathlib import Path

```

```

def save_model_state(model, folder_name: str = "Trained_models_state"):
    """
    Save Pre-Trained model parameters in a State Dictionary
    """

    MODEL_PATH = Path(folder_name) # Placed in root
    MODEL_PATH.mkdir(parents=True, exist_ok=True) # Pre-existing folder (w. same name) monitoring
    MODEL_NAME = '{}_{}'.format(model.name, "Params.pth")
    MODEL_SAVE_PATH = MODEL_PATH / MODEL_NAME

    print(f"Saving {model.name} Parameters in: {MODEL_SAVE_PATH}")
    torch.save(obj=model.state_dict(), f=MODEL_SAVE_PATH)

    return MODEL_SAVE_PATH

# Save Pre-Trained Models-bank
states_path = [] # Path for each model parameters state
for i in range(len(ocon_speakers)):
    state_path = save_model_state(ocon_speakers[i])
    states_path.append(state_path)
print()

```

## ▼ Output Maxnet Algorithm

```

# OCON "MaxNet" Architecture (Weightening + Non Linearity apply)
class OCON_MaxNet(nn.Module):
    def __init__(self, n_units, act_fun, eps):
        super().__init__()

        self.layers = nn.ModuleDict() # Dictionary to store Model layers
        self.eps_weight = eps

        # MaxNet Layer
        self.layers['MAXNET'] = nn.Linear(n_units, n_units) # Key 'MaxNet' layer specification

        # Weights & Bias initialization
        self.layers['MAXNET'].weight.data.fill_(self.eps_weight)
        for i in range(n_units):
            self.layers['MAXNET'].weight[i][i].data.fill_(1.) # Self Weight = 1

        self.layers['MAXNET'].bias.data.fill_(0.)

        # Activation Function
        self.actfun = act_fun # Function string-name attribute association

# Forward Pass Method
def forward(self, x):

    # Activation function object computation
    actfun = getattr(torch.nn, self.actfun)

    # Maxnet Layer pass
    x = actfun()(self.layers['MAXNET'](x.squeeze().float())) --> Output Weightening (Dot Product) "Linear transfo

    # Self

    return x

# Build OCON MaxNetwork Architecture
torch.manual_seed(SEED)
ocon_maxnet = OCON_MaxNet(n_units=3, act_fun='ReLU', eps=0.25)

# MaxNet & Sub-Networks Parameters
print('OCON MaxNet STATE')
model_desc(ocon_maxnet)

def maxnet_algo(maxnet_function, n_units, act_fun, eps, input_array):
    """
    MaxNet Re-iteration algorithm for Maximum Value retrieving from an input array
    """
    non_zero_outs = np.count_nonzero(input_array) # Non Zero Values initialization
    maxnet_in = torch.from_numpy(input_array) # MaxNet Input Tensor initialization

    results = [] # Results initialization

    counter = 0
    while non_zero_outs != 1:
        counter += 1

```

```

# Create the MaxNet
torch.manual_seed(SEED) # Redundant
maxnet = maxnet_function(n_units = n_units, act_fun = act_fun, eps = eps)

# Compute Forward Pass
results = maxnet(maxnet_in)

# Non_zero outputs & Maxnet Input Update
non_zero_outs = np.count_nonzero(results.detach().numpy())
maxnet_in = results.detach() # Save results for next iteration

print(f'Maximum Value found in {counter} iterations')
return np.argmax(results.detach().numpy())

# MaxNet on Sub-Networks predictions
ocon_predictions_prob = np.zeros((len(ocon_predictions), x_data_minmax_ordered.shape[0])) # NumPy predictions matrix (12 * 16)

# Convert from List of Tensors to 2D NumPy Array
for i in range(len(ocon_predictions)):
    ocon_predictions_prob[i, :] = ocon_predictions[i].detach().squeeze().numpy()

maxnet_class_predictions = [] # Classes Outputs list initialization
# MaxNet application
for i in range(x_data_minmax.shape[0]):
    print(f'Dataset Sample({i + 1}) Class Evaluation')

    samp_predictions = ocon_predictions_prob[:, i] # Array of 12 predictions for each Dataset sample (OCON outputs)
    class_prediction = maxnet_algo(OCON_MaxNet, n_units=3, act_fun='ReLU', eps=-0.1, input_array=samp_predictions) # MaxNet C
    maxnet_class_predictions.append(class_prediction) # Result appending
    print('-----')

maxnet_accuracy = 100 * np.mean((np.array(maxnet_class_predictions).reshape(1597, 1) == z_labels_raw_np_alt_ordered)) # Accur
print(f'Maxnet Output --> Speaker ACCURACY: {maxnet_accuracy}%')

# Argmax on Sub-Networks predictions (...for multiple ls probabilities MaxNet infinite loops)
#ocon_predictions_prob = np.zeros((len(new_ocon_predictions), x_data_minmax.shape[0])) # NumPy predictions matrix (12 * 1617)
#
# Convert from List of Tensors to 2D NumPy Array
#for i in range(len(new_ocon_predictions)):
#    ocon_predictions_prob[i, :] = new_ocon_predictions[i].detach().squeeze().numpy()
#
#maxnet_class_predictions = np.argmax(ocon_predictions_prob, axis=0)
#maxnet_accuracy = 100 * np.mean((np.array(maxnet_class_predictions).reshape(1617, 1) == y_labels_raw_np)) # Accuracy computa
#print(f'Maxnet Output ACCURACY: {maxnet_accuracy}%')

# Evaluation Analysis Plot
plt.figure(figsize=(30, 5))
plt.suptitle(f'OCON Bank + MaxNet Evaluation: {maxnet_accuracy:.0f}%')

plot_y_ticks = [n for n in range(len(speakers_alt))]

plt.plot(z_labels_raw_np_alt_ordered, 'rs', label='Ground Truths')
plt.plot(maxnet_class_predictions, 'k.', label='MAXNET Outputs')
plt.xlabel('Dataset samples')
plt.xticks(ticks=plot_ticks, labels=speakers_alt)
plt.xlim([-10, len(y_labels_raw_np) + 10])
plt.ylabel('Labels')
plt.yticks(ticks=plot_y_ticks, labels=speakers_alt)
plt.legend(loc='best')
plt.grid()

plt.tight_layout()
plt.savefig('OCON_model_evaluation')
plt.show()

```