AMG4PSBLAS User's and Reference Guide

A guide for the Algebraic MultiGrid Preconditioners Package based on PSBLAS



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Abstract

AMG4PSBLAS (ALGEBRAIC MULTIGRID PRECONDITIONERS PACKAGE BASED ON PSBLAS) is a package of parallel algebraic multilevel preconditioners included in the PSCToolkit (Parallel Sparse Computation Toolkit) software framework. It is a progress of a software development project started in 2007, named MLD2P4, which originally implemented a multilevel version of some domain decomposition preconditioners of additive-Schwarz type and was based on a parallel decoupled version of the well known smoothed aggregation method to generate the multilevel hierarchy of coarser matrices. In the last years, within the context of the EU-H2020 EoCoE project (Energy Oriented Center of Excellence), the package is being extended for including new algorithms and functionalities to setup and apply new AMG preconditioners with the final aims of improving efficiency and scalability when tens of thousands cores are used and of boosting reliability in dealing with general symmetric positive definite linear systems. Due to the significant number of changes and the increase in scope, we decided to rename the package as AMG4PSBLAS.

AMG4PSBLAS is designed to provide scalable and easy-to-use preconditioners in the context of the PSBLAS (Parallel Sparse Basic Linear Algebra Subprograms) computational framework and can be used in conjuction with the Krylov solvers available in this framework. Our package is based on a completely algebraic approach and users level interfaces assume that the system matrix and preconditioners are represented as PSBLAS distributed sparse matrices. AMG4PSBLAS enables the user to easily specify different features of an algebraic multilevel preconditioner, thus allowing to experiment with different preconditioners for the problem and parallel computers at hand.

The package employs object-oriented design techniques in Fortran 2003, with interfaces to additional third party libraries such as MUMPS, UMFPACK, SuperLU, and SuperLU_Dist, which can be exploited in building multilevel preconditioners. The parallel implementation is based on a Single Program Multiple Data (SPMD) paradigm; the inter-process communication is based on MPI and is managed mainly through PSBLAS.

This guide provides a brief description of the functionalities and the user interface of AMG4PSBLAS.



Contents

Al	ostra	act	i
1	Ger	neral Overview	1
2	Coc	le Distribution	3
3	Cor	nfiguring and Building AMG4PSBLAS	4
	3.1	Prerequisites	4
	3.2	Optional third party libraries	5
	3.3	Configuration options	5
	3.4	Bug reporting	10
	3.5	Example and test programs	10
4	Get	ting Started	11
	4.1	Examples	13
5	Use	er Interface	16
	5.1	Method init	17
	5.2	Method set	18
	5.3	Method hierarchy_build	28
	5.4	Method smoothers_build	29
	5.5	Method build	30
	5.6	Method apply	31
	5.7	Method free	32
	5.8	Method descr	33
	5.9	Auxiliary Methods	33
		5.9.1 Method: dump	33
		5.9.2 Method: clone	33
		5.9.3 Method: sizeof	34
		5.9.4 Method: allocate_wrk	34
		5.9.5 Method: free_wrk	34
6	Add	ding new smoother and solver objects to AMG4PSBLAS	35
7	Err	or Handling	37
A	Lice	ense	38
		nces	40
100	TOLE	11000	TU



1 General Overview 1

1 General Overview

The Algebraic MultiGrid Preconditioners Package based on PSBLAS (AMG4PSBLAS) provides parallel Algebraic MultiGrid (AMG) preconditioners (see, e.g., [3, 27]), to be used in the iterative solution of linear systems,

$$Ax = b, (1)$$

where A is a square, real or complex, sparse symmetric positive definite (s.p.d) matrix. The preconditioners implemented in AMG4PSBLAS are obtained by combining 3 different types of AMG cycles with smoothers and coarsest-level solvers. The V-, W-, and a version of a Krylov-type cycle (K-cycle) [3, 23] are available, which can be combined with Jacobi hybrid forward/backward Gauss-Seidel, block-Jacobi, and additive Schwarz smoothers. Also ℓ_1 versions of Jacobi, block-Jacobi and Gauss-Seidel smoothers are available. An algebraic approach is used to generate a hierarchy of coarse-level matrices and operators, without explicitly using any information on the geometry of the original problem, e.g., the discretization of a PDE. To this end, two different coarsening strategies, based on aggregation, are available:

- a decoupled version of the well known smoothed aggregation procedure proposed in [2, 29], and already included in the previous versions of the package [10, 9];
- the first parallel implementation of a coupled version of Coarsening based on Compatible Weighted Matching introduced in [30, 31] and described in details in [11];

Either exact or approximate solvers can be used on the coarsest-level system. Specifically, different sparse LU factorizations from external packages, native incomplete LU and approximate inverse factorizations, weighted Jacobi, hybrid Gauss-Seidel, block-Jacobi solvers and recursive call to preconditioned Krylov methods are available. All the smoothers can be also exploited as one-level preconditioners.

AMG4PSBLAS is written in Fortran 2003, following an object-oriented design through the exploitation of features such as abstract data type creation, type extension, functional overloading, and dynamic memory management. The parallel implementation is based on a Single Program Multiple Data (SPMD) paradigm. Single and double precision implementations of AMG4PSBLAS are available for both the real and the complex case, which can be used through a single interface.

AMG4PSBLAS has been designed to implement scalable and easy-to-use multilevel preconditioners in the context of the PSBLAS (Parallel Sparse BLAS) computational framework [18, 17]. PSBLAS provides basic linear algebra operators and data management facilities for distributed sparse matrices, kernels for sequential incomplete factorizations needed for the parallel block-Jacobi and additive Schwarz smoothers, and parallel Krylov solvers which can be used with the AMG4PSBLAS preconditioners. The choice of PSBLAS has been mainly motivated by the need of having a portable and efficient software infrastructure implementing "de facto" standard parallel sparse linear algebra kernels, to pursue goals such as performance, portability, modularity ed

extensibility in the development of the preconditioner package. On the other hand, the implementation of AMG4PSBLAS, which was driven by the need to face the exascale challenge, has led to some important revisions and extentions of the PSBLAS infrastructure. The inter-process comunication required by AMG4PSBLAS is encapsulated in the PSBLAS routines; therefore, AMG4PSBLAS can be run on any parallel machine where PSBLAS implementations are available. In the most recent version of PSBLAS (release 3.7), a plug-in for GPU is included; it includes CUDA versions of main vector operations and of sparse matrix-vector multiplication, so that Krylov methods coupled with AMG4PBLAS preconditioners relying on Jacobi and block-Jacobi smoothers with sparse approximate inverses on the blocks can be efficiently executed on cluster of GPUs.

AMG4PSBLAS has a layered and modular software architecture where three main layers can be identified. The lower layer consists of the PSBLAS kernels, the middle one implements the construction and application phases of the preconditioners, and the upper one provides a uniform interface to all the preconditioners. This architecture allows for different levels of use of the package: few black-box routines at the upper layer allow all users to easily build and apply any preconditioner available in AMG4PSBLAS; facilities are also available allowing expert users to extend the set of smoothers and solvers for building new versions of the preconditioners (see Section 6).

This guide is organized as follows. General information on the distribution of the source code is reported in Section 2, while details on the configuration and installation of the package are given in Section 3. The basics for building and applying the preconditioners with the Krylov solvers implemented in PSBLAS are reported in Section 4, where the Fortran codes of a few sample programs are also shown. A reference guide for the user interface routines is provided in Section 5. Information on the extension of the package through the addition of new smoothers and solvers is reported in Section 6. The error handling mechanism used by the package is briefly described in Section 7. The copyright terms concerning the distribution and modification of AMG4PSBLAS are reported in Appendix A.

2 Code Distribution 3

2 Code Distribution

AMG4PSBLAS is available from the web site

https://psctoolkit.github.io/products/amg4psblas/

where contact points for further information can be also found.

The software is available under a modified BSD license, as specified in Appendix A; please note that some of the optional third party libraries may be licensed under a different and more stringent license, most notably the GPL, and this should be taken into account when treating derived works.

The library defines a version string with the constant

amg_version_string_

whose current value is 1.0.

Contributors

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3 Configuring and Building AMG4PSBLAS

In order to build AMG4PSBLAS it is necessary to set up a Makefile with appropriate system-dependent variables; this is done by means of the configure script. The distribution also includes the autoconf and automake sources employed to generate the script, but usually this is not needed to build the software.

AMG4PSBLAS is implemented almost entirely in Fortran 2003, with some interfaces to external libraries in C; the Fortran compiler must support the Fortran 2003 standard plus the extension MOLD= feature, which enhances the usability of ALLOCATE. Many compilers do this; in particular, this is supported by the GNU Fortran compiler, for which we recommend to use at least version 4.8. The software defines data types and interfaces for real and complex data, in both single and double precision.

Building AMG4PSBLAS requires some base libraries (see Section 3.1); interfaces to optional third-party libraries, which extend the functionalities of AMG4PSBLAS (see Section 3.2), are also available. Many Linux distributions (e.g., Ubuntu, Fedora, CentOS) provide precompiled packages for the prerequisite and optional software. In many cases these packages are split between a runtime part and a "developer" part; in order to build AMG4PSBLAS you need both. A description of the base and optional software used by AMG4PSBLAS is given in the next sections.

3.1 Prerequisites

The following base libraries are needed:

BLAS [14, 15, 21] Many vendors provide optimized versions of BLAS; if no vendor version is available for a given platform, the ATLAS software (math-atlas.sourceforge.net) may be employed. The reference BLAS from Netlib (www.netlib.org/blas) are meant to define the standard behaviour of the BLAS interface, so they are not optimized for any particular platform, and should only be used as a last resort. Note that BLAS computations form a relatively small part of the AMG4PSBLAS/PSBLAS computations; they are however critical when using preconditioners based on MUMPS, UMFPACK or SuperLU third party libraries. Note that UMFPACK requires a full LAPACK library; our experience is that configuring ATLAS for building full LAPACK does not work in the correct way. Our advice is first to download the LAPACK tarfile from www.netlib.org/lapack and install it independently of ATLAS. In this case, you need to modify the OPTS and NOOPT definitions for including -fPIC compilation option in the make.inc file of the LAPACK library.

MPI [20, 26] A version of MPI is available on most high-performance computing systems.

PSBLAS [16, 18] Parallel Sparse BLAS (PSBLAS) is available from psctoolkit.github.io/products/psblas/; version 3.7.0 (or later) is required. Indeed, all the prerequisites listed so far are also prerequisites of PSBLAS.

Please note that the four previous libraries must have Fortran interfaces compatible with AMG4PSBLAS; usually this means that they should all be built with the same compiler as AMG4PSBLAS.

3.2 Optional third party libraries

We provide interfaces to the following third-party software libraries; note that these are optional, but if you enable them some defaults for multilevel preconditioners may change to reflect their presence.

- UMFPACK [12] A sparse LU factorization package included in the SuiteSparse library, available from faculty.cse.tamu.edu/davis/suitesparse.html; it provides sequential factorization and triangular system solution for double precision real and complex data. We tested version 4.5.4 of SuiteSparse. Note that for configuring SuiteSparse you should provide the right path to the BLAS and LAPACK libraries in the SuiteSparse_config/SuiteSparse_config.mk file.
- MUMPS [1] A sparse LU factorization package available from mumps.enseeiht.fr; it provides sequential and parallel factorizations and triangular system solution for single and double precision, real and complex data. We tested versions 4.10.0 and 5.0.1.
- SuperLU [13] A sparse LU factorization package available from crd.lbl.gov/~xiaoye/SuperLU/; it provides sequential factorization and triangular system solution for single and double precision, real and complex data. We tested versions 4.3 and 5.0. If you installed BLAS from ATLAS, remember to define the BLASLIB variable in the make inc file.
- SuperLU_Dist [22] A sparse LU factorization package available from the same site as SuperLU; it provides parallel factorization and triangular system solution for double precision real and complex data. We tested versions 3.3 and 4.2. If you installed BLAS from ATLAS, remember to define the BLASLIB variable in the make.inc file and to add the -std=c99 option to the C compiler options. Note that this library requires the ParMETIS library for parallel graph partitioning and fill-reducing matrix ordering, available from glaros.dtc.umn.edu/gkhome/metis/parmetis/overview.

3.3 Configuration options

In order to build AMG4PSBLAS, the first step is to use the **configure** script in the main directory to generate the necessary makefile.

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As a minimal example consider the following:

./configure --with-psblas=PSB-INSTALL-DIR

which assumes that the various MPI compilers and support libraries are available in the standard directories on the system, and specifies only the PSBLAS install directory (note that the latter directory must be specified with an *absolute* path). The full set of options may be looked at by issuing the command ./configure --help, which produces:

'configure' configures MLD2P4 2.1.1 to adapt to many kinds of systems.

Usage: ./configure [OPTION]... [VAR=VALUE]...

To assign environment variables (e.g., CC, CFLAGS...), specify them as VAR=VALUE. See below for descriptions of some of the useful variables.

Defaults for the options are specified in brackets.

Configuration:

-h, --help display this help and exit display options specific to this package --help=short display the short help of all the included packages --help=recursive display version information and exit -V, --version do not print 'checking ...' messages -q, --quiet, --silent --cache-file=FILE cache test results in FILE [disabled] alias for '--cache-file=config.cache' -C, --config-cache -n, --no-create do not create output files --srcdir=DIR find the sources in DIR [configure dir or '..']

Installation directories:

--prefix=PREFIX install architecture-independent files in PREFIX

[/usr/local]

--exec-prefix=EPREFIX install architecture-dependent files in EPREFIX

[PREFIX]

By default, 'make install' will install all the files in '/usr/local/bin', '/usr/local/lib' etc. You can specify an installation prefix other than '/usr/local' using '--prefix', for instance '--prefix=\$HOME'.

For better control, use the options below.

Fine tuning of the installation directories:

--bindir=DIR user executables [EPREFIX/bin]

--sbindir=DIR system admin executables [EPREFIX/sbin]
--libexecdir=DIR program executables [EPREFIX/libexec]
--sysconfdir=DIR read-only single-machine data [PREFIX/etc]

--sharedstatedir=DIR modifiable architecture-independent data [PREFIX/com]

--localstatedir=DIR modifiable single-machine data [PREFIX/var] object code libraries [EPREFIX/lib] --libdir=DIR --includedir=DIR C header files [PREFIX/include] --oldincludedir=DIR C header files for non-gcc [/usr/include] read-only arch.-independent data root [PREFIX/share] --datarootdir=DIR read-only architecture-independent data [DATAROOTDIR] --datadir=DIR info documentation [DATAROOTDIR/info] --infodir=DIR locale-dependent data [DATAROOTDIR/locale] --localedir=DIR man documentation [DATAROOTDIR/man] --mandir=DIR --docdir=DIR documentation root [DATAROOTDIR/doc/mld2p4] --htmldir=DIR html documentation [DOCDIR] --dvidir=DIR dvi documentation [DOCDIR] --pdfdir=DIR pdf documentation [DOCDIR] --psdir=DIR ps documentation [DOCDIR] Program names: --program-prefix=PREFIX prepend PREFIX to installed program names --program-suffix=SUFFIX append SUFFIX to installed program names --program-transform-name=PROGRAM run sed PROGRAM on installed program names Optional Features: --disable-option-checking ignore unrecognized --enable/--with options do not include FEATURE (same as --enable-FEATURE=no) --disable-FEATURE --enable-FEATURE[=ARG] include FEATURE [ARG=yes] less verbose build output (undo: "make V=1") --enable-silent-rules --disable-silent-rules verbose build output (undo: "make V=0") --enable-dependency-tracking do not reject slow dependency extractors --disable-dependency-tracking speeds up one-time build --enable-serial Specify whether to enable a fake mpi library to run in serial mode. --enable-long-integers Specify usage of 64 bits integers. Optional Packages: --with-PACKAGE[=ARG] use PACKAGE [ARG=yes] --without-PACKAGE do not use PACKAGE (same as --with-PACKAGE=no) --with-psblas=DIR The install directory for PSBLAS, for example, --with-psblas=/opt/packages/psblas-3.5 --with-psblas-incdir=DIR Specify the directory for PSBLAS C includes. --with-psblas-moddir=DIR Specify the directory for PSBLAS Fortran modules. --with-psblas-libdir=DIR

	Specify the directory for PSBLAS library.
with-ccopt	additional [CCOPT] flags to be added: will prepend
	to [CCOPT]
with-fcopt	additional [FCOPT] flags to be added: will prepend
	to [FCOPT]
with-libs	List additional link flags here. For example,
	with-libs=-lspecial_system_lib or
	with-libs=-L/path/to/libs
with-clibs	additional [CLIBS] flags to be added: will prepend
WION CILDS	to [CLIBS]
with-flibs	additional [FLIBS] flags to be added: will prepend
WIOH IIIDD	to [FLIBS]
with-library-path	additional [LIBRARYPATH] flags to be added: will
wion library paon	prepend to [LIBRARYPATH]
with-include-path	additional [INCLUDEPATH] flags to be added: will
with include path	prepend to [INCLUDEPATH]
with-module-path	additional [MODULE_PATH] flags to be added: will
wion modulo puon	prepend to [MODULE_PATH]
with-extra-libs	List additional link flags here. For example,
WIOH CAULA IIDD	with-extra-libs=-lspecial_system_lib or
	with-extra-libsL/path/to/libs
with-blas= <lib></lib>	use BLAS library <lib></lib>
with-blasdir= <dir></dir>	search for BLAS library in <dir></dir>
with-lapack= <lib></lib>	use LAPACK library <lib></lib>
with-mumps=LIBNAME	Specify the libname for MUMPS. Default: autodetect
with mamps-biblishin	with minimum "-lmumps_common -lpord"
with-mumpsdir=DIR	Specify the directory for MUMPS library and
with mampsair bit	includes. Note: you will need to add auxiliary
	libraries withextra-libs; this depends on how
	MUMPS was configured and installed, at a minimum you
	will need SCALAPACK and BLAS
with-mumpsincdir=DIR	Specify the directory for MUMPS includes.
with-mumpsmoddir=DIR	Specify the directory for MUMPS Fortran modules.
with-mumpslibdir=DIR	Specify the directory for MUMPS library.
with-umfpack=LIBNAME	Specify the library name for UMFPACK and its support
wrom umrpuom Brzmini	libraries. Default: "-lumfpack -lamd"
with-umfpackdir=DIR	Specify the directory for UMFPACK library and
wion ampackati bit	includes.
with-umfpackincdir=DI	
	Specify the directory for UMFPACK includes.
with-umfpacklibdir=DI	
1	Specify the directory for UMFPACK library.
with-superlu=LIBNAME	Specify the library name for SUPERLU library.
1	Default: "-lsuperlu"
	±

--with-superludir=DIR Specify the directory for SUPERLU library and includes.

--with-superluincdir=DIR

Specify the directory for SUPERLU includes.

--with-superlulibdir=DIR

Specify the directory for SUPERLU library.

--with-superludist=LIBNAME

Specify the libname for SUPERLUDIST library. Requires you also specify SuperLU. Default: "-lsuperlu_dist"

--with-superludistdir=DIR

Specify the directory for SUPERLUDIST library and includes.

--with-superludistincdir=DIR

Specify the directory for SUPERLUDIST includes.

--with-superludistlibdir=DIR

Specify the directory for SUPERLUDIST library.

Some influential environment variables:

FC Fortran compiler command FCFLAGS Fortran compiler flags

LDFLAGS linker flags, e.g. -L<lib dir> if you have libraries in a

nonstandard directory <lib dir>

LIBS libraries to pass to the linker, e.g. -l<library>

CC C compiler command CFLAGS C compiler flags

CPPFLAGS (Objective) C/C++ preprocessor flags, e.g. -I<include dir> if

you have headers in a nonstandard directory <include dir>

MPICC MPI C compiler command

MPIFC MPI Fortran compiler command

CPP C preprocessor

Use these variables to override the choices made by 'configure' or to help it to find libraries and programs with nonstandard names/locations.

Report bugs to https://github.com/sfilippone/mld2p4-2/issues.

For instance, if a user has built and installed PSBLAS 3.7 under the /opt directory and is using the SuiteSparse package (which includes UMFPACK), then MLD2P4 might be configured with:

```
./configure --with-psblas=/opt/psblas-3.5/ \
--with-umfpackincdir=/usr/include/suitesparse/
```

Once the configure script has completed execution, it will have generated the file

Make.inc which will then be used by all Makefiles in the directory tree; this file will be copied in the install directory under the name Make.inc.MLD2P4.

To use the MUMPS solver package, the user has to add the appropriate options to the configure script; by default we are looking for the libraries -ldmumps -lsmumps -

To build the library the user will now enter

make

followed (optionally) by

make install

3.4 Bug reporting

If you find any bugs in our codes, please report them through our issues page on

https://github.com/psctoolkit/amg4psblas/issues

To enable us to track the bug, please provide a log from the failing application, the test conditions, and ideally a self-contained test program reproducing the issue.

3.5 Example and test programs

The package contains the examples and tests directories; both of them are further divided into fileread and pdegen subdirectories. Their purpose is as follows:

examples contains a set of simple example programs with a predefined choice of preconditioners, selectable via integer values. These are intended to get an acquaintance with the multilevel preconditioners available in AMG4PSBLAS.

tests contains a set of more sophisticated examples that will allow the user, via the input files in the runs subdirectories, to experiment with the full range of preconditioners implemented in the package.

The fileread directories contain sample programs that read sparse matrices from files, according to the Matrix Market or the Harwell-Boeing storage format; the pdegen programs generate matrices in full parallel mode from the discretization of a sample partial differential equation.

4 Getting Started 11

4 Getting Started

We describe the basics for building and applying AMG4PSBLAS one-level and multilevel (i.e., AMG) preconditioners with the Krylov solvers included in PSBLAS [16]. The following steps are required:

- 1. Declare the preconditioner data structure. It is a derived data type, amg_xprec_type, where x may be s, d, c or z, according to the basic data type of the sparse matrix (s = real single precision; d = real double precision; c = complex single precision; z = complex double precision). This data structure is accessed by the user only through the AMG4PSBLAS routines, following an object-oriented approach.
- 2. Allocate and initialize the preconditioner data structure, according to a preconditioner type chosen by the user. This is performed by the routine init, which also sets defaults for each preconditioner type selected by the user. The preconditioner types and the defaults associated with them are given in Table 1, where the strings used by init to identify the preconditioner types are also given. Note that these strings are valid also if uppercase letters are substituted by corresponding lowercase ones.
- 3. Modify the selected preconditioner type, by properly setting preconditioner parameters. This is performed by the routine set. This routine must be called only if the user wants to modify the default values of the parameters associated with the selected preconditioner type, to obtain a variant of that preconditioner. Examples of use of set are given in Section 4.1; a complete list of all the preconditioner parameters and their allowed and default values is provided in Section 5, Tables 2-8.
- 4. Build the preconditioner for a given matrix. If the selected preconditioner is multilevel, then two steps must be performed, as specified next.
 - 4.1 Build the AMG hierarchy for a given matrix. This is performed by the routine hierarchy_build.
 - 4.2 Build the preconditioner for a given matrix. This is performed by the routine smoothers_build.

If the selected preconditioner is one-level, it is built in a single step, performed by the routine bld.

- 5. Apply the preconditioner at each iteration of a Krylov solver. This is performed by the method apply. When using the PSBLAS Krylov solvers, this step is completely transparent to the user, since apply is called by the PSBLAS routine implementing the Krylov solver (psb_krylov).
- 6. Free the preconditioner data structure. This is performed by the routine free. This step is complementary to step 1 and should be performed when the preconditioner is no more used.

All the previous routines are available as methods of the preconditioner object. A detailed description of them is given in Section 5. Examples showing the basic use of AMG4PSBLAS are reported in Section 4.1.

TYPE	STRING	DEFAULT PRECONDITIONER
No preconditioner	'NONE'	Considered to use the PSBLAS Krylov
		solvers with no preconditioner.
Diagonal	'DIAG',	Diagonal preconditioner. For any zero
	'JACOBI',	diagonal entry of the matrix to be pre-
	'L1-JACOBI'	conditioned, the corresponding entry of
		the preconditioner is set to 1.
Gauss-Seidel	'GS',	Hybrid Gauss-Seidel (forward), that is,
	'L1-GS'	global block Jacobi with Gauss-Seidel as
		local solver.
Symmetrized Gauss-Seidel	'FBGS',	Symmetrized hybrid Gauss-Seidel, that
	'L1-FBGS'	is, forward Gauss-Seidel followed by back-
		ward Gauss-Seidel.
Block Jacobi	'BJAC',	Block-Jacobi with ILU(0) on the local
	'L1-BJAC'	blocks.
Additive Schwarz	'AS'	Additive Schwarz (AS), with overlap 1
		and $ILU(0)$ on the local blocks.
Multilevel	'ML'	V-cycle with one hybrid forward Gauss-
		Seidel (GS) sweep as pre-smoother and
		one hybrid backward GS sweep as post-
		smoother, decoupled smoothed aggrega-
		tion as coarsening algorithm, and LU
		(plus triangular solve) as coarsest-level
		solver. See the default values in Tables 2-
		8 for further details of the preconditioner.

Table 1: Preconditioner types, corresponding strings and default choices.

Note that the module <code>amg_prec_mod</code>, containing the definition of the preconditioner data type and the interfaces to the routines of AMG4PSBLAS, must be used in any program calling such routines. The modules <code>psb_base_mod</code>, for the sparse matrix and communication descriptor data types, and <code>psb_krylov_mod</code>, for interfacing with the Krylov solvers, must be also used (see Section 4.1).

Remark 1. Coarsest-level solvers based on the LU factorization, such as those implemented in UMFPACK, MUMPS, SuperLU, and SuperLU_Dist, usually lead to smaller numbers of preconditioned Krylov iterations than inexact solvers, when the linear system comes from a standard discretization of basic scalar elliptic PDE problems. However, this does not necessarily correspond to the shortest execution time on parallel

4 Getting Started 13

computers.

4.1 Examples

The code reported in Figure 1 shows how to set and apply the default multilevel preconditioner available in the real double precision version of AMG4PSBLAS (see Table 1). This preconditioner is chosen by simply specifying 'ML' as the second argument of P%init (a call to P%set is not needed) and is applied with the CG solver provided by PSBLAS (the matrix of the system to be solved is assumed to be positive definite). As previously observed, the modules psb_base_mod, amg_prec_mod and psb_krylov_mod must be used by the example program.

The part of the code concerning the reading and assembling of the sparse matrix and the right-hand side vector, performed through the PSBLAS routines for sparse matrix and vector management, is not reported here for brevity; the statements concerning the deallocation of the PSBLAS data structure are neglected too. The complete code can be found in the example program file amg_dexample_ml.f90, in the directory examples/fileread of the AMG4PSBLAS implementation (see Section 3.5). A sample test problem along with the relevant input data is available in examples/fileread/runs. For details on the use of the PSBLAS routines, see the PSBLAS User's Guide [16].

The setup and application of the default multilevel preconditioner for the real single precision and the complex, single and double precision, versions are obtained with straightforward modifications of the previous example (see Section 5 for details). If these versions are installed, the corresponding codes are available in examples/fileread/.

Different versions of the multilevel preconditioner can be obtained by changing the default values of the preconditioner parameters. The code reported in Figure 2 shows how to set a V-cycle preconditioner which applies 1 block-Jacobi sweep as preand post-smoother, and solves the coarsest-level system with 8 block-Jacobi sweeps. Note that the ILU(0) factorization (plus triangular solve) is used as local solver for the block-Jacobi sweeps, since this is the default associated with block-Jacobi and set by P%init. Furthermore, specifying block-Jacobi as coarsest-level solver implies that the coarsest-level matrix is distributed among the processes. Figure 3 shows how to set a W-cycle preconditioner using the Coarsening based on Compatible Weighted Matching. It applies 2 hybrid Gauss-Seidel sweeps as pre- and post-smoother, and solves the coarsest-level system with the multifrontal LU factorization implemented in MUMPS. It is specified that the coarsest-level matrix is distributed, since MUMPS can be used on both replicated and distributed matrices, and by default it is used on replicated ones. The code fragments shown in Figures 2 and 3 are included in the example program file amg_dexample_ml.f90 too. DA CORREGGERE NEL CODICE ESEMPIO 3

Finally, Figure 4 shows the setup of a one-level additive Schwarz preconditioner, i.e., RAS with overlap 2. Note also that a Krylov method different from CG must be used to solve the preconditioned system, since the preconditione in nonsymmetric. The corresponding example program is available in the file amg_dexample_llev.f90.

For all the previous preconditioners, example programs where the sparse matrix and the right-hand side are generated by discretizing a PDE with Dirichlet boundary

```
use psb_base_mod
 use amg_prec_mod
 use psb_krylov_mod
! sparse matrix
 type(psb_dspmat_type) :: A
! sparse matrix descriptor
 type(psb_desc_type) :: desc_A
! preconditioner
 type(amg_dprec_type) :: P
! right-hand side and solution vectors
 type(psb_d_vect_type) :: b, x
! initialize the parallel environment
 call psb_init(ictxt)
 call psb_info(ictxt,iam,np)
! read and assemble the spd matrix A and the right-hand side b
! using PSBLAS routines for sparse matrix / vector management
! initialize the default multilevel preconditioner, i.e. V-cycle
! with basic smoothed aggregation, 1 hybrid forward/backward
! GS sweep as pre/post-smoother and UMFPACK as coarsest-level
! solver
 call P%init('ML',info)
! build the preconditioner
 call P%hierarchy_build(A,desc_A,info)
 call P%smoothers_build(A,desc_A,info)
! set the solver parameters and the initial guess
  . . . . . . .
! solve Ax=b with preconditioned CG
 call psb_krylov('CG',A,P,b,x,tol,desc_A,info)
! deallocate the preconditioner
 call P%free(info)
! deallocate other data structures
! exit the parallel environment
 call psb_exit(ictxt)
  stop
```

Figure 1: setup and application of the default multilevel preconditioner (example 1).

4 Getting Started 15

conditions are also available in the directory examples/pdegen.

```
! build a V-cycle preconditioner with 1 block-Jacobi sweep (with ! ILU(0) on the blocks) as pre- and post-smoother, and 8 block-Jacobi ! sweeps (with ILU(0) on the blocks) as coarsest-level solver call P%init('ML',info) call_P%set('SMOOTHER_TYPE','BJAC',info) call P%set('COARSE_SOLVE','BJAC',info) call P%set('COARSE_SWEEPS',8,info) call P%hierarchy_build(A,desc_A,info) call P%smoothers_build(A,desc_A,info)
```

Figure 2: setup of a multilevel preconditioner based on the default decoupled coarsening

```
! build a W-cycle preconditioner with 2 hybrid Gauss-Seidel sweeps
! as pre- and post-smoother, a distributed coarsest
! matrix, and MUMPS as coarsest-level solver
  call P%init('ML',info)
  call P%set('PAR_AGGR_ALG','COUPLED',info)
  call P%set('ML_CYCLE','WCYCLE',info)
  call P%set('SMOOTHER_TYPE','FBGS',info)
  call P%set('SMOOTHER_SWEEPS',2,info)
  call P%set('COARSE_SOLVE','MUMPS',info)
  call P%set('COARSE_MAT','DIST',info)
  call P%hierarchy_build(A,desc_A,info)
  call P%smoothers_build(A,desc_A,info)
.....
```

Figure 3: setup of a multilevel preconditioner based on the coupled coarsening based on weighted matching

```
! set RAS with overlap 2 and ILU(0) on the local blocks
call P%init('AS',info)
call P%set('SUB_OVR',2,info)
call P%bld(A,desc_A,info)
...
! solve Ax=b with preconditioned BiCGSTAB
call psb_krylov('BICGSTAB',A,P,b,x,tol,desc_A,info)
```

Figure 4: setup of a one-level Schwarz preconditioner.

5 User Interface

The basic user interface of AMG4PBLAS consists of eight methods. The six methods init, set, build, hierarchy_build, smoothers_build and apply encapsulate all the functionalities for the setup and the application of any multilevel and one-level preconditioner implemented in the package. The method free deallocates the preconditioner data structure, while descr prints a description of the preconditioner setup by the user. For backward compatibility, methods are also accessible as stand-alone subroutines.

For each method, the same user interface is overloaded with respect to the real/complex case and the single/double precision; arguments with appropriate data types must be passed to the method, i.e.,

- the sparse matrix data structure, containing the matrix to be preconditioned, must be of type psb_xspmat_type with x = s for real single precision, x = d for real double precision, x = c for complex single precision, x = c for complex double precision;
- the preconditioner data structure must be of type amg_xprec_type, with x = s,
 d, c, z, according to the sparse matrix data structure;
- the arrays containing the vectors v and w involved in the preconditioner application $w = B^{-1}v$ must be of type psb_xvect_type with x = s, d, c, z, in a manner completely analogous to the sparse matrix type;
- real parameters defining the preconditioner must be declared according to the precision of the sparse matrix and preconditioner data structures (see Section 5.2).

A description of each method is given in the remainder of this section.

5 USER INTERFACE 17

5.1 Method init

call p%init(icontx,ptype,info)

This method allocates and initializes the preconditioner p, according to the preconditioner type chosen by the user.

Arguments

icontxt integer, intent(in).

The communication context.

ptype character(len=*), intent(in).

The type of preconditioner. Its values are specified in Table 1.

Note that the strings are case insensitive.

info integer, intent(out).

Error code. If no error, 0 is returned. See Section 7 for details.

5.2 Method set

```
call p%set(what,val,info [,ilev, ilmax, pos, idx])
```

This method sets the parameters defining the preconditioner p. More precisely, the parameter identified by what is assigned the value contained in val.

Arguments

what character(len=*).

The parameter to be set. It can be specified through its name; the string is case-insensitive. See Tables 2-8.

val integer or character(len=*) or real(psb_spk_) or
 real(psb_dpk_), intent(in).

The value of the parameter to be set. The list of allowed values and the corresponding data types is given in Tables 2-8. When the value is of type character(len=*), it is also treated as case insensitive.

info integer, intent(out).

Error code. If no error, 0 is returned. See Section 7 for details.

ilev integer, optional, intent(in).

For the multilevel preconditioner, the level at which the preconditioner parameter has to be set. The levels are numbered in increasing order starting from the finest one, i.e., level 1 is the finest level. If ilev is not present, the parameter identified by what is set at all the appropriate levels (see Tables 2-8).

ilmax integer, optional, intent(in).

For the multilevel preconditioner, when both ilev and ilmax are present, the settings are applied at all levels ilev:ilmax. When ilev is present but ilmax is not, then the default is ilmax=ilev. The levels are numbered in increasing order starting from the finest one, i.e., level 1 is the finest level.

pos charater(len=*), optional, intent(in).

Whether the other arguments apply only to the pre-smoother ('PRE') or to the post-smoother ('POST'). If pos is not present, the other arguments are applied to both smoothers. If the preconditioner is one-level or the parameter identified by what does not concern the smoothers, pos is ignored.

idx integer, optional, intent(in).

An auxiliary input argument that can be passed to the underlying objects. However, in this case the optional arguments ilev, ilmax, pos and idx cannot be used.

A variety of preconditioners can be obtained by a suitable setting of the preconditioner parameters. These parameters can be logically divided into four groups, i.e., parameters defining

1. the type of multilevel cycle and how many cycles must be applied;

5 User Interface 19

- 2. the coarsening algorithm;
- 3. the coarse-space correction at the coarsest level (for multilevel preconditioners only);
- 4. the smoother of the multilevel preconditioners, or the one-level preconditioner.

A list of the parameters that can be set, along with their allowed and default values, is given in Tables 2-8.

Remark 2. A smoother is usually obtained by combining two objects: a smoother (SMOOTHER_TYPE) and a local solver (SUB_SOLVE), as specified in Tables 7-8. For example, the block-Jacobi smoother using ILU(0) on the blocks is obtained by combining the block-Jacobi smoother object with the ILU(0) solver object. Similarly, the hybrid Gauss-Seidel smoother (see Note in Table 7) is obtained by combining the block-Jacobi smoother object with a single sweep of the Gauss-Seidel solver object, while the point-Jacobi smoother is the result of combining the block-Jacobi smoother object with a single sweep of the point-Jacobi solver object. However, for simplicity, shortcuts are provided to set point-Jacobi, hybrid (forward) Gauss-Seidel, and hybrid backward Gauss-Seidel, i.e., the previous smoothers can be defined by setting only SMOOTHER_TYPE to appropriate values (see Tables 7), i.e., without setting SUB_SOLVE too.

The smoother and solver objects are arranged in a hierarchical manner. When specifying a smoother object, its parameters, including the local solver, are set to their default values, and when a solver object is specified, its defaults are also set, overriding in both cases any previous settings even if explicitly specified. Therefore if the user sets a smoother, and wishes to use a solver different from the default one, the call to set the solver must come *after* the call to set the smoother.

Similar considerations apply to the point-Jacobi, Gauss-Seidel and block-Jacobi coarsest-level solvers, and shortcuts are available in this case too (see Table 5).

Remark 3. In general, a coarsest-level solver cannot be used with both the replicated and distributed coarsest-matrix layout; therefore, setting the solver after the layout may change the layout. Similarly, setting the layout after the solver may change the solver.

More precisely, UMFPACK and SuperLU require the coarsest-level matrix to be replicated, while SuperLU_Dist requires it to be distributed. In these cases, setting the coarsest-level solver implies that the layout is redefined according to the solver, ovverriding any previous settings. MUMPS, point-Jacobi, hybrid Gauss-Seidel and block-Jacobi can be applied to replicated and distributed matrices, thus their choice does not modify any previously specified layout. It is worth noting that, when the matrix is replicated, the point-Jacobi, hybrid Gauss-Seidel and block-Jacobi solvers reduce to the corresponding local solver objects (see Remark 2). For the point-Jacobi and Gauss-Seidel solvers, these objects correspond to a *single* point-Jacobi sweep and a *single* Gauss-Seidel sweep, respectively, which are very poor solvers.

On the other hand, the distributed layout can be used with any solver but UMFPACK and SuperLU; therefore, if any of these two solvers has already been selected, the coarsest-

level solver is changed to block-Jacobi, with the previously chosen solver applied to the local blocks. Likewise, the replicated layout can be used with any solver but SuperLu_Dist; therefore, if SuperLu_Dist has been previously set, the coarsest-level solver is changed to the default sequential solver.

Remark 4. The argument idx can be used to allow finer control for those solvers; for instance, by specifying the keyword MUMPS_IPAR_ENTRY and an appropriate value for idx, it is possible to set any entry in the MUMPS integer control array. See also Sec. 6.

what	DATA TYPE	val	DEFAULT	COMMENTS
'ML_CYCLE'	character(len=*) 'VCYCLE'	,VCYCLE,	, VCYCLE,	Multilevel cycle: V-cycle, W-cycle, K-cycle,
		,WCYCLE,		and additive composition.
		'KCYCLE'		
		'ADD'		
'OUTER_SWEEPS'	integer	Any integer	1	Number of multilevel cycles.
		number ≥ 1		

Table 2: Parameters defining the multilevel cycle and the number of cycles to be applied.

	22	AMO	4PSBLAS	USER'S	AND REFEREN	ICE GUIDE	
'AGGR_PROL'	'AGGR_SIZE'	AGGR_TYPE	PAR_AGGR_ALG'	'MAX_LEVS'	MIN_CR_RATIO'	MIN_COARSE_SIZE'	
character(len=*)	integer	character(len=*)	character(len=*)	integer	real	integer	
'SMOOTHED',	Any integer number power of 2 and > 2	SOC1	'DEC', 'SYMDEC', 'COUPLED'	Any integer number > 1	Any number > 1	Any number > 0	
'SMOOTHED'	4	'SOC1', 'SOC2', 'MATCHBOXP'	'DEC'	20	.51 51	-1	
Prolongator used by the aggregation algorithm: smoothed or unsmoothed (i.e.,	Maximum size of aggregates when the coupled aggregation based on matching is applied. For aggressive coarsening with size of aggregate larger than 8 we recommend the use of smoothed prolongators. MOD-IFICARE CODICE	Type of aggregation algorithm: currently, for the decoupled aggregation we implement two measures of strength of connection, the one by Vaněk, Mandel and Brezina [29], and the one by Gratton et al [19]. The coupled aggregation is based on a parallel version of the half-approximate matching implemented in the MatchBox-P software package AGGIUNGERE LINK AL PACKAGE?	Parallel aggregation algorithm. the SYMDEC option applies decoupled aggregation to the sparsity pattern of $A+A^T$.	Maximum number of levels. The aggregation stops if the number of levels reaches this value (see Note).	Minimum coarsening ratio. The aggregation stops if the ratio between the global matrix dimensions at two consecutive levels is lower than or equal to this threshold (see Note).	Coarse size threshold. The aggregation stops if the global number of variables of the computed coarsest matrix is lower than or equal to this threshold (see Note). If negative, it is ignored in favour of the default for 'MIN_COARSE_SIZE_PER_PROCESS'.	variables of the computed coarsest matrix is lower than or equal to this threshold multiplied by the number of processes.

minimum coarsening ratio, or the maximum number of levels is reached. Therefore, the actual number of levels may be Note. The aggregation algorithm stops when at least one of the following criteria is met: the coarse size threshold, the coarse size threshold per property of the same of the following criteria is met: the coarse size threshold, the coarse size threshold per property of the following criteria is met: the coarse size threshold, the coarse size threshold per property of the following criteria is met: the coarse size threshold, the coarse size threshold per property of the following criteria is met: the coarse size threshold per property of the following criteria is met: the coarse size threshold per property of the following criteria is met: the coarse size threshold, the coarse size threshold per property of the following criteria is met: the coarse size threshold per property of the following criteria is met: the coarse size threshold per property of the following criteria is met: the coarse size threshold per property of the following criteria is met: the coarse size threshold per property of the following criteria is met: the coarse size threshold per property of the coarse size threshold per property of the following criteria is met: the coarse size threshold per property of the coars

tentative prolongator).

what	DATA TYPE	val	DEFAULT	COMMENTS
'AGGR_ORD'	character(len=*)	'NATURAL'	'NATURAL'	Initial ordering of indices for the decou-
		'DEGREE'		pled aggregation algorithm: either nat-
				ural ordering or sorted by descending
				degrees of the nodes in the matrix graph.
'AGGR_THRESH'	real(kind_parameter) Any real	Any real	0.01	The threshold θ in the decoupled aggre-
		number $\in [0,1]$		gation algorithm, see (??) in Section ??.
				See also the note at the bottom of this
				table.
'AGGR_FILTER'	character(len=*)	'FILTER'	'NOFILTER'	Matrix used in computing the smoothed
		'NOFILTER'		prolongator: filtered or unfiltered
				(see (??) in Section ??).
Note. Different thresho	olds at different levels, suc	ch as those used i	n [29, Section 5.	Note. Different thresholds at different levels, such as those used in [29, Section 5.1], can be easily set by invoking the rou-
tine set with the parameter ilev.	neter ilev.			

Table 4: Parameters defining the aggregation algorithm (continued).

double precision version – UMF if installed, then MUMPS if installed, then SLU if installed, ILU	single precision version – MUMPS if installed, then SLU if installed, ILU otherwise;	Note. Defaults for COARSE_SOLVE and COARSE_SUBSOLVE are chosen in the following order:						'COARSE_SUBSOLVE'																	'COARSE_SOLVE'		'COARSE_MAT'	what
$_{l}$ – UMF if installed, then	 MUMPS if installed, th 	$RSE_SOLVE $ and $COARSE$						character(len=*)																	<pre>character(len=*)</pre>		<pre>character(len=*)</pre>	DATA TYPE
n MUMPS if in	en SLU if ins	_SUBSOLVE a		UMF,	MUMPS	MILU	'ILUT'	'ILU'										'PCG'	'BJAC'	GS'	JACOBI,	'SLUDIST'	SLU	'UMF'	MUMPS	'REPL'	DIST	val
stalled, then	talled, ILU o	re chosen in						See Note.																	See Note.		REPL'	DEFAULT
SLU if installed, ILU otherwise.	therwise;	the following order:	۱ ≒۰	GPU? Note that UMFPACK and SuperLUDist	MUMPS, SuperLU or UMFPACK (plus triangular	level solver: $ILU(p)$, $ILU(p,t)$, $MILU(p)$, LU from	in case the block Jacobi solver is chosen as coarsest-	Solver for the diagonal blocks of the coarse matrix,	double precision.	UMFPACK and SuperLU_Dist are available only in	of the solver (see Remark 3, p. 24). Note also that	layout is set to a default value which allows the use	any of the previous solvers is specified, the matrix	either a replicated or a distributed matrix. When	require it to be distributed, MUMPS can be used with	be replicated, SLUDIST, JACOBI, GS, BJAC and PCG	Note that UMF and SLU require the coarsest matrix to	with $\mathrm{ILU}(0)$ on the blocks.	coupled with the block-Jacobi preconditioner	versions; preconditioned Conjugate Gradient	hybrid Gauss-Seidel or block-Jacobi and related ℓ_1 -	SuperLU_Dist (plus triangular solve); point-Jacobi,	angular solve); distributed LU from MUMPS or	from MUMPS, UMFPACK, or SuperLU (plus tri-	Solver used at the coarsest level: sequential LU	cesses or replicated on each of them.	Coarsest matrix layout: distributed among the pro-	COMMENTS

Table 5: Parameters defining the coarse-space correction at the coarsest level.

what	DATA TYPE	val	DEFAULT	DEFAULT COMMENTS
'COARSE_SWEEPS'	integer	Any integer 10	10	Number of sweeps when JACOBI, GS or BJAC is
		number > 0		chosen as coarsest-level solver. Aggiungere
				criterio di arresto del PCG?
'COARSE_FILLIN'	integer	\mid Any integer \mid 0	0	Fill-in level p of the ILU factorizations.
		number ≥ 0		
'COARSE_ILUTHRS'	real(kind_parameter) Any real	Any real	0	Drop tolerance t in the $LU(p, t)$ factorization.
		number ≥ 0		

Table 6: Parameters defining the coarse-space correction at the coarsest level (continued).

what	DATA TYPE	val	DEFAULT	COMMENTS
'SMOOTHER_TYPE'	<pre>character(len=*)</pre>	JACOBI,	'FBGS'	Type of smoother used in the multi-
		'GS'		level preconditioner: point-Jacobi, hybrid
		'BGS'		(forward) Gauss-Seidel, hybrid backward
		'BJAC'		Gauss-Seidel, block-Jacobi, ℓ_1 -versions?
		'AS'		and Additive Schwarz.
				It is ignored by one-level preconditioners.
'SUB_SOLVE'	<pre>character(len=*)</pre>	JACOBI,	GS and BGS for pre- and	The local solver to be used with the
		'GS'	post-smoothers of multi-	smoother or one-level preconditioner (see
		'BGS'	level preconditioners, re-	Remark 2, page 24): point-Jacobi, hybrid
		'ILU'	spectively	(forward) Gauss-Seidel, hybrid backward
		'ILUT'	ILU for block-Jacobi	Gauss-Seidel, $ILU(p)$, $ILU(p,t)$, $MILU(p)$
		'MILU'	and Additive Schwarz	LU from MUMPS, SuperLU or UMFPACF
		'MUMPS'	one-level precondition-	(plus triangular solve). See Note for details
		'SLU'	ers ℓ_1 -versions?	on hybrid Gauss-Seidel.
		'UMF'		
'SMOOTHER_SWEEPS'	integer	Any integer	1	Number of sweeps of the smoother or one-
		number ≥ 0		level preconditioner. In the multilevel case,
				no pre-smother or post-smoother is used
				if this parameter is set to 0 together with
				pos='PRE' or pos='POST, respectively.
'SUB_OVR'	integer	Any integer	1	Number of overlap layers, for Additive
		number ≥ 0		Schwarz only.

Table 7: Parameters defining the smoother or the details of the one-level preconditioner.

what	DATA TYPE	val	DEFAULT	COMMENTS
'SUB_RESTR'	character(len=*)	'HALO'	'HALO'	Type of restriction operator, for Additive
		'NONE'		Schwarz only: HALO for taking into account
				the overlap, NONE for neglecting it.
				Note that HALO must be chosen for the classi-
				cal Addditive Schwarz smoother and its RAS
				variant.
'SUB_PROL'	character(len=*)	, SUM,	'NONE'	Type of prolongation operator, for Additive
		'NONE'		Schwarz only: SUM for adding the contributions
				from the overlap, NONE for neglecting them.
				Note that SUM must be chosen for the classical
				Additive Schwarz smoother, and NONE for its
				RAS variant.
'SUB_FILLIN'	integer	Any integer	0	Fill-in level p of the incomplete LU factoriza-
		number ≥ 0		tions.
'SUB_ILUTHRS'	real(kind_parameter) Any real num-	Any real num-	0	Drop tolerance t in the $\mathrm{ILU}(p,t)$ factorization.
		$ber \geq 0$		
'MUMPS_LOC_GLOB'	character(len=*)	LOCAL_SOLVER'	GLOBAL_SOLVER	GLOBAL_SOLVER! Whether MUMPS should be used as a dis-
		GLOBAL_SOLVER'		tributed solver, or as a serial solver acting only
				on the part of the matrix local to each process.
'MUMPS_IPAR_ENTRY'	integer	Any integer	0	Set an entry in the MUMPS integer control
		number		array, as chosen via the idx optional argument.
'MUMPS_RPAR_ENTRY'	real	Any real number	0	Set an entry in the MUMPS real control array,
				as chosen via the idx optional argument.

Table 8: Parameters defining the smoother or the details of the one-level preconditioner (continued).

5.3 Method hierarchy_build

call p%hierarchy_build(a,desc_a,info)

This method builds the hierarchy of matrices and restriction/prolongation operators for the multilevel preconditioner p, according to the requirements made by the user through the methods init and set.

Arguments

a type(psb_xspmat_type), intent(in).

The sparse matrix structure containing the local part of the matrix to be preconditioned. Note that x must be chosen according to the real/complex, single/double precision version of AMG4PSBLAS under use. See the PSBLAS User's Guide for details [16].

desc_a type(psb_desc_type), intent(in).

The communication descriptor of a. See the PSBLAS User's Guide for details [16].

info integer, intent(out).

Error code. If no error, 0 is returned. See Section 7 for details.

5 User Interface 29

5.4 Method smoothers_build

```
call p%smoothers_build(a,desc_a,p,info[,amold,vmold,imold])
```

This method builds the smoothers and the coarsest-level solvers for the multilevel preconditioner p, according to the requirements made by the user through the methods init and set, and based on the aggregation hierarchy produced by a previous call to hierarchy_build (see Section 5.3).

Arguments

- a type(psb_xspmat_type), intent(in).
 - The sparse matrix structure containing the local part of the matrix to be preconditioned. Note that x must be chosen according to the real/complex, single/double precision version of AMG4PSBLAS under use. See the PSBLAS User's Guide for details [16].
- desc_a type(psb_desc_type), intent(in).
 The communication descriptor of a. See the PSBLAS User's Guide for
 details [16].
- info integer, intent(out). Error code. If no error, 0 is returned. See Section 7 for details.
- amold class(psb_x_base_sparse_mat), intent(in), optional. The desired dynamic type for internal matrix components; this allows e.g. running on GPUs; it needs not be the same on all processes. See the PSBLAS User's Guide for details [16].
- vmold class(psb_x_base_vect_type), intent(in), optional. The desired dynamic type for internal vector components; this allows e.g. running on GPUs.
- imold class(psb_i_base_vect_type), intent(in), optional.

 The desired dynamic type for internal integer vector components; this allows e.g. running on GPUs.

5.5 Method build

```
call p%build(a,desc_a,info[,amold,vmold,imold])
```

This method builds the preconditioner p according to the requirements made by the user through the methods init and set (see Sections 5.3 and 5.4 for multilevel preconditioners). It is mostly provided for backward compatibility; indeed, it is internally implemented by invoking the two previous methods hierarchy_build and smoothers_build, whose nomenclature would however be somewhat unnatural when dealing with simple one-level preconditioners.

Arguments

a type(psb_xspmat_type), intent(in).

The sparse matrix structure containing the local part of the matrix to be preconditioned. Note that x must be chosen according to the real/complex, single/double precision version of AMG4PSBLAS under use. See the PSBLAS User's Guide for details [16].

desc_a type(psb_desc_type), intent(in).
 The communication descriptor of a. See the PSBLAS User's Guide for
 details [16].

info integer, intent(out).

Error code. If no error, 0 is returned. See Section 7 for details.

amold class(psb_x_base_sparse_mat), intent(in), optional. The desired dynamic type for internal matrix components; this allows e.g. running on GPUs; it needs not be the same on all processes. See the PSBLAS User's Guide for details [16].

vmold class(psb_x_base_vect_type), intent(in), optional. The desired dynamic type for internal vector components; this allows e.g. running on GPUs.

imold class(psb_i_base_vect_type), intent(in), optional.

The desired dynamic type for internal integer vector components; this allows e.g. running on GPUs.

The method can be used to build multilevel preconditioners too.

5 User Interface 31

5.6 Method apply

```
call p%apply(x,y,desc_a,info [,trans,work])
```

This method computes $y = op(B^{-1})x$, where B is a previously built preconditioner, stored into p, and op denotes the preconditioner itself or its transpose, according to the value of trans. Note that, when AMG4PSBLAS is used with a Krylov solver from PSBLAS, p%apply is called within the PSBLAS method psb_krylov and hence it is completely transparent to the user.

Arguments

x $type(kind_parameter)$, dimension(:), intent(in). The local part of the vector x. Note that type and $kind_parameter$ must

be chosen according to the real/complex, single/double precision version of AMG4PSBLAS under use.

y type(kind_parameter), dimension(:), intent(out).

The local part of the vector y. Note that type and $kind_parameter$ must be chosen according to the real/complex, single/double precision version of AMG4PSBLAS under use.

desc_a type(psb_desc_type), intent(in).

The communication descriptor associated to the matrix to be preconditioned.

info integer, intent(out).

Error code. If no error, 0 is returned. See Section 7 for details.

trans character(len=1), optional, intent(in).

If trans = 'N', 'n' then $op(B^{-1}) = B^{-1}$; if trans = 'T', 't' then $op(B^{-1}) = B^{-T}$ (transpose of B^{-1}); if trans = 'C', 'c' then $op(B^{-1}) = B^{-C}$ (conjugate transpose of B^{-1}).

work $type(kind_parameter)$, dimension(:), optional, target.

Workspace. Its size should be at least 4 * psb_cd_get_local_cols(desc_a) (see the PSBLAS User's Guide). Note that type and kind_parameter must be chosen according to the real/complex, single/double precision version of AMG4PSBLAS under use.

5.7 Method free

call p%free(p,info)

This method deallocates the preconditioner data structure p.

Arguments

info integer, intent(out).

Error code. If no error, 0 is returned. See Section 7 for details.

5 User Interface 33

5.8 Method descr

```
call p%descr(info, [iout])
```

This method prints a description of the preconditioner p to the standard output or to a file. It must be called after hierarchy_build and smoothers_build, or build, have been called.

Arguments

info integer, intent(out).

Error code. If no error, 0 is returned. See Section 7 for details.

iout integer, intent(in), optional.

The id of the file where the preconditioner description will be printed; the default is the standard output.

5.9 Auxiliary Methods

Various functionalities are implemented as additional methods of the preconditioner object.

5.9.1 Method: dump

call p%dump(info[,istart,iend,prefix,head,ac,rp,smoother,solver,global_num])

Dump on file.

Arguments

info integer, intent(out).

Error code. If no error, 0 is returned. See Section 7 for details.

amold $class(psb_x_base_sparse_mat)$, intent(in), optional.

The desired dynamic type for internal matrix components; this allows e.g. running on GPUs; it needs not be the same on all processes. See the PSBLAS User's Guide for details [16].

5.9.2 Method: clone

call p%clone(pout,info)

Create a (deep) copy of the preconditioner object.

Arguments

pout type(amg_xprec_type), intent(out).

The copy of the preconditioner data structure. Note that x must be chosen according to the real/complex, single/double precision version of

AMG4PSBLAS under use.

info integer, intent(out).

Error code. If no error, 0 is returned. See Section 7 for details.

5.9.3 Method: sizeof

Return memory footprint in bytes.

5.9.4 Method: allocate_wrk

Allocate internal work vectors. Each application of the preconditioner uses a number of work vectors which are allocated internally as necessary; therefore allocation and deallocation of memory occurs multiple times during the execution of a Krylov method. In most cases this strategy is perfectly acceptable, but on some platforms, most notably GPUs, memory allocation is a slow operation, and the default behaviour would lead to a slowdown. This method allows to trade space for time by preallocating the internal workspace outside of the invocation of a Krylov method. When using GPUs or other specialized devices, the vmold argument is also necessary to ensure the internal work vectors are of the appropriate dynamic type to exploit the accelerator hardware; when allocation occurs internally this is taken care of based on the dynamic type of the x argument to the apply method.

Arguments

info integer, intent(out).

Error code. If no error, 0 is returned. See Section 7 for details.

vmold class(psb_x_base_vect_type), intent(in), optional.

The desired dynamic type for internal vector components; this allows e.g.

running on GPUs.

5.9.5 Method: free_wrk

Deallocate internal work vectors.

Arguments

info integer, intent(out).

Error code. If no error, 0 is returned. See Section 7 for details.

5 User Interface 35

6 Adding new smoother and solver objects to AMG4PSBLAS

Developers can add completely new smoother and/or solver classes derived from the base objects in the library (see Remark 2 in Section 5.2), without recompiling the library itself.

To do so, it is necessary first to select the base type to be extended. In our experience, it is quite likely that the new application needs only the definition of a "solver" object, which is almost always acting only on the local part of the distributed matrix. The parallel actions required to connect the various solver objects are most often already provided by the block-Jacobi or the additive Schwarz smoothers. To define a new solver, the developer will then have to define its components and methods, perhaps taking one of the predefined solvers as a starting point, if possible.

Once the new smoother/solver class has been developed, to use it in the context of the multilevel preconditioners it is necessary to:

- declare in the application program a variable of the new type;
- pass that variable as the argument to the set routine as in the following:

```
call p%set(smoother,info [,ilev,ilmax,pos])
call p%set(solver,info [,ilev,ilmax,pos])
```

• link the code implementing the various methods into the application executable.

The new solver object is then dynamically included in the preconditioner structure, and acts as a *mold* to which the preconditioner will conform, even though the AMG4PSBLAS library has not been modified to account for this new development.

It is possible to define new values for the keyword WHAT in the set routine; if the library code does not recognize a keyword, it passes it down the composition hierarchy (levels containing smoothers containing in turn solvers), so that it can be eventually caught by the new solver. By the same token, any keyword/value pair that does not pertain to a given smoother should be passed down to the contained solver, and any keyword/value pair that does not pertain to a given solver is by default ignored.

An example is provided in the source code distribution under the folder ${\tt tests/newslv}$. In this example we are implementing a new incomplete factorization variant (which is simply the ${\tt ILU}(0)$ factorization under a new name). Because of the specifics of this case, it is possible to reuse the basic structure of the ${\tt ILU}$ solver, with its ${\tt L/D/U}$ components and the methods needed to apply the solver; only a few methods, such as the description and most importantly the build, need to be ovverridden (rewritten).

The interfaces for the calls shown above are defined using

The other arguments are defined in the way described in Sec. 5.2. As an example, in the tests/newslv code we define a new object of type amg_d_tlu_solver_type, and we pass it as follows:

```
! sparse matrix and preconditioner
type(psb_dspmat_type) :: a
type(amg_dprec_type) :: prec
type(amg_d_tlu_solver_type) :: tlusv

....
!
! prepare the preconditioner: an ML with defaults, but with TLU solver at
! intermediate levels. All other parameters are at default values.
!
call prec%init('ML', info)
call prec%hierarchy_build(a,desc_a,info)
nlv = prec%get_nlevs()
call prec%set(tlusv, info,ilev=1,ilmax=max(1,nlv-1))
call prec%smoothers_build(a,desc_a,info)
```

7 Error handling 37

7 Error Handling

The error handling in AMG4PSBLAS is based on the PSBLAS error handling. Error conditions are signaled via an integer argument info; whenever an error condition is detected, an error trace stack is built by the library up to the top-level, user-callable routine. This routine will then decide, according to the user preferences, whether the error should be handled by terminating the program or by returning the error condition to the user code, which will then take action, and whether an error message should be printed. These options may be set by using the PSBLAS error handling routines; for further details see the PSBLAS User's Guide [16].

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Algebraic MultiGrid Preconditioners Package
based on PSBLAS (Parallel Sparse BLAS version 3.7)

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MultiLevel Domain Decomposition Parallel Preconditioners Package based on PSBLAS (Parallel Sparse BLAS version 3.5)

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