

DD2520, Applied Cryptography

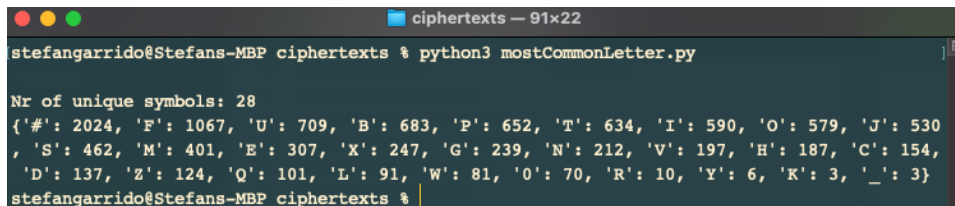
Cryptanalysis of Ciphertexts

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Ciphertext 1

The analysis began with an initial overview of the cipher to see if any patterns were observable. The first thing to remark was the large amount of occurrences of the character `#`. Additionally, "words" in between `#` seemed to occur more than once. A quick comparison to ciphertext 2 showed the frequency of the character `#` was minimal in the second ciphertext. A python program was created to measure the frequency of each symbol in ciphertext 1, the results are seen on figure 1. Based on this, an assumption was made that the character `#` could potentially be used to substitute the underscore character, which corresponds to an empty/space/blank character.



```
stefangarrido@Stefans-MBP ciphertexts % python3 mostCommonLetter.py

Nr of unique symbols: 28
{'#': 2024, 'F': 1067, 'U': 709, 'B': 683, 'P': 652, 'T': 634, 'I': 590, 'O': 579, 'J': 530, 'S': 462, 'M': 401, 'E': 307, 'X': 247, 'G': 239, 'N': 212, 'V': 197, 'H': 187, 'C': 154, 'D': 137, 'Z': 124, 'Q': 101, 'L': 91, 'W': 81, '0': 70, 'R': 10, 'Y': 6, 'K': 3, '_': 3}
```

Figure 1: Output of the program *mostCommonLetter.py*

A python program was created to analyse the frequency of each encrypted word found in between `#`, see figure 2 for a partial result of the output. Based on the analysis of the Oxford English Corpus and the Corpus of Contemporary American English (COCA) list [1], the most common word in English is the word **"the"**. The encrypted word with most occurrences, according to the python program, was **"UIF"**. An assumption was made that **UIF** corresponds to the word **the**, and as such: $U=T$, $I=H$, and $F=E$. The mapping from F to E seems to match the frequency of the letter E seen on figure 1. Based on common English words, the same type of assumptions were made for the words **"B"** and **"UP"**, resulting in: $B=A$, $U=T$, and $P=O$.

```

stefangarrido@Stefans-MBP ciphertxts % python3 mostCommonWord.py
File to open: cipher1.txt

Nr of unique words: 773
{'UIF': 96, 'B': 95, 'JT': 54, 'UP': 52, 'IF': 45, 'PG': 37, 'NBO': 36, 'LJT': 35, 'BOE': 34, 'XIP': 28,
'GPS': 27, 'JO': 23, 'BU': 22, 'CF': 20, 'XJUI': 19, 'OPU': 19, 'BSF': 18, 'CZ': 16, 'UIBU': 14, 'XIFO':
14, 'CVU': 14, 'POF': 13, 'NFO': 12, 'GSJFOET': 12, 'OP': 11, 'NBZ': 11, 'TIPVME': 11, 'JU': 10, 'PO': 10
, 'BMM': 10, 'XIBU': 10, 'UIBO': 9, 'GSPN': 8, 'LOPXT': 8, 'CFTU': 8, 'LOPX': 8, 'IBT': 8, 'PS': 8, 'ZPV'
: 8, 'CFUURS': 7, 'IBWF': 7, 'PWFS': 7, 'XJMM': 7, 'BO': 7, 'NBOZ': 7, 'J': 6, 'TIBMM': 6, 'OFWFS': 6, 'I
JN': 6, 'BOPUIFS': 6, 'TP': 6, 'HJGU': 6, 'MJGF': 6, 'GBMTF': 6, 'HPPE': 5, 'UPP': 5, 'NVDI': 5, 'XJTF':
5, 'UIPVHI': 5, 'GPPM': 5, 'UFMM': 5, 'FBSMZ': 5, 'BT': 5, 'UIFZ': 5, 'TQFBL': 5, 'UIJOH': 5, 'TFOTF': 4,
'PKO': 4, 'TPOT': 4, 'OJHIU': 4, 'HVFTU': 4, 'TPO': 4, 'TJMFUO': 4, 'DBO': 4, 'PGUFO': 4, 'UIPTF': 4, 'M
BVHI': 4, 'IPNF': 4, 'BNPOH': 4, 'BTL': 4, 'XPSET': 4, 'UIFSF': 4, 'FOPVHI': 4, 'GSJFOETIJQ': 4, 'USVTU':
4, 'TFMEPN': 4, 'OPS': 4, 'TPNF': 4, 'EJF': 4, 'MPWF': 4, 'TXPSE': 4, 'JDF': 4, 'USBWFMFS': 3, 'DBOOPU'
: 3, 'DBSSZ': 3, 'NPSF': 3, 'NFBE': 3, 'HJWF': 3, 'XBT': 3, 'EBZ': 3, 'MJWF': 3, 'UBML': 3, 'HFFT': 3, 'I
PX': 3, 'JNM': 3, 'NBLEF': 3, 'PUIFST': 3, 'DPNFT': 3, 'GJOET': 3, 'XJTEPN': 3, 'XFMM': 3, 'IBQQFOT': 3,
'UIFJS': 3, 'NFBM': 3, 'UBLF': 3, 'PVU': 3, 'UISPVHI': 3, 'MPOH': 3, 'T': 3, 'XFBMUI': 3, 'GSJFOE': 3, 'G
BJS': 3, 'EP': 3, 'IJHIXBZ': 3, 'GJSF': 3, 'CPME': 3, 'NJEEMFXJTF': 3, 'DVOOJOH': 3, 'DMFWFS': 3, 'GMBNE'
: 3, 'XJU': 3, 'HFBS': 2, 'SJDIFT': 2, 'XSFUDIFE': 2, 'ESJOL': 2, 'XPVME': 2, 'MFTT': 2, 'CFDPNFT': 2, 'O

```

Figure 2: Partial output of the program *mostCommonWord.py*

As a results of these assumptions and the given hint in the assignment it was concluded that a Caesar cipher was used, where each letter was encrypted by shifting one step to the right. A third python program was created to reverse the encryption. The results seen on figure 3 shows that ciphertext 1 was successfully decoded.

```

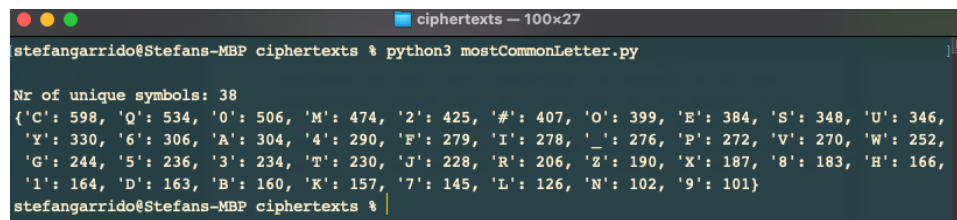
stefangarrido@Stefans-MBP ciphertxts % python3 decryptCipher1.py
BETTER GEAR THAN GOOD SENSE A TRAVELLER CANNOT CARRY BETTER THAN RICHES FOR A WRETCHED MAN FAR FROM
HIS OWN HOME
BETTER GEAR THAN GOOD SENSE A TRAVELLER CANNOT CARRY A MORE TEDIOUS BURDEN THAN TOO MUCH DRINK A TRA
VELLER CANNOT CARRY
LESS GOOD THAN BELIEF WOULD HAVE IT IS MEAD FOR THE SONS OF MEN A MAN KNOWS LESS THE MORE HE DRINKS
BECOMES A BEFUDDLED FOOL
IFORGET IS THE NAME MEN GIVE THE HERON WHO HOVERS OVER THE FAST FETTERED I WAS IN HIS FEATHERS THAT
NIGHT WHEN A GUEST IN GUNNLODS COURT
DRUNK I GOT DEAD DRUNK WHEN FJALAR THE WISE WAS WITH ME BEST IS THE BANQUET ONE LOOKS BACK ON AFTER
AND REMEMBERS ALL THAT HAPPENED
SILENCE BECOMES THE SON OF A PRINCE TO BE SILENT BUT BRAVE IN BATTLE IT BEFITS A MAN TO BE MERRY AND
GLAD UNTIL THE DAY OF HIS DEATH
THE COWARD BELIEVES HE WILL LIVE FOREVER IF HE HOLDS BACK IN THE BATTLE BUT IN OLD AGE HE SHALL HAVE
NO PEACE THOUGH SPEARS HAVE SPARED HIS LIMBS
WHEN HE MEETS FRIENDS THE FOOL GAPE IS SHY AND SHEEPISH AT FIRST THEN HE SIPS HIS MEAD AND IMMEDIAT
ELY ALL KNOW WHAT AN OAF HE IS HE WHO HAS SEEN AND SUFFERED MUCH AND KNOWS THE WAYS OF THE WORLD WHO
HAS TRAVELLED CAN TELL WHAT SPIRIT GOVERNS THE MEN HE MEETS DRINK YOUR MEAD BUT IN MODERATION TALK
SENSE OR BE SILENT NO MAN IS CALLED DISCOURTEOUS WHO GOES TO BED AT AN EARLY HOUR
A GLUTTONOUS MAN WHO GUZZLES AWAY BRINGS SORROW ON HIMSELF AT THE TABLE OF THE WISE HE IS TAUNTED OF
TEN MOCKED FOR HIS BLOATED BELLY
THE HERD KNOWS ITS HOMING TIME AND LEAVES THE GRAZING GROUND BUT THE GLUTTON NEVER KNOWS HOW MUCH HI
S BELLY IS ABLE TO HOLD
AN ILL TEMPERED UNHAPPY MAN RIDICULES ALL HE HEARS MAKES FUN OF OTHERS REFUSING ALWAYS TO SEE THE FA
ULTS IN HIMSELF
FOOLISH IS HE WHO FRETS AT NIGHT AND LIES AWAKE TO WORRY A WEARY MAN WHEN MORNING COMES HE FINDS ALL
AS BAD AS BEFORE

```

Figure 3: Partial output of the program *decryptCipher1.py*

Ciphertext 2

The analysis began with an initial overview of the cipher to see if any patterns were observable. Unlike ciphertext 1, no obvious patterns could be observed. A frequency analysis was done on ciphertext 2 using the same program used in ciphertext 1. The results seen on figure 4 shows that the frequency of the letters seems to be more uniformly distributed compared to ciphertext 1.



```
stefangarrido@Stefans-MBP ciphertexts % python3 mostCommonLetter.py

Nr of unique symbols: 38
{'C': 598, 'Q': 534, 'O': 506, 'M': 474, '2': 425, '#': 407, 'O': 399, 'E': 384, 'S': 348, 'U': 346,
 'Y': 330, '6': 306, 'A': 304, '4': 290, 'F': 279, 'I': 278, '_': 276, 'P': 272, 'V': 270, 'W': 252,
 'G': 244, '5': 236, '3': 234, 'T': 230, 'J': 228, 'R': 206, 'Z': 190, 'X': 187, '8': 183, 'H': 166,
 '1': 164, 'D': 163, 'B': 160, 'K': 157, '7': 145, 'L': 126, 'N': 102, '9': 101}
```

Figure 4: Partial output of the program *mostCommonLetter.py*

This result seemed to hint to the use of a Vigenère cipher, which is an extended Caesar cipher that uses multiple keys. The Vigenère key was assumed to have the format: $k = (k_0, \dots, k_{l-1})$, where $k_i \in Z_{38}$. Given this assumption, a python program was created in order to brute force the combination of keys. The program alternates k_i for every position based on the given key length and tries every combination of the given alphabet. The idea was to start with a key length of two, analyse the results, and increase the key length if needed. Only the first line of the ciphertext 2 was used in order to keep the brute forcing to a reasonable time and allow for reasonable amount of output. Additionally, in order to minimize the amount of brute forcing, an assumption was made that the first symbol in the ciphertext 2 was a letter and not a number. The reasoning was that a sentence would most likely begin with a word not containing numbers.

In total, output for key length = 2,...,9 was generated and analyzed. Trying combinations for a key larger than 4 took too much time. The solution to this was to replace each corresponding k_i , where $i = 4, 5, 6, 7, 8$, with a simple dot ".". The idea was to generate a larger key containing some unknown parts in hope that an English sentence would be readable. Figure 5 shows partial outputs for key length 4 and 8. Common words found in [1] were manually searched for, but no indication of an English sentence could be found.

After a long search with no results, the previous assumption of a sentence not beginning with a number was dismissed. New outputs were generated for key length = 2,...,9 and analyzed manually. A new search for common words was performed but no results. A search of combinations of numbers

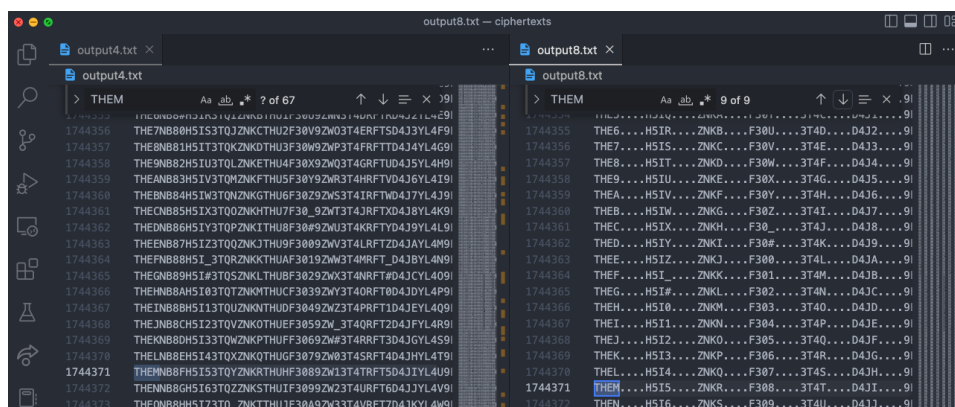


Figure 5: Partial outputs of the program *bruteForceCipher2.py*

was done, starting with 0123 and 1234. An interest pattern appeared on outputs for key length 3 and 6, seen on figure 6. The first two halves of the lines showed patterns which seemed to align with a sequence of numbers, starting with 01234, and potentially continuing with the English alphabet. Moreover, output from key length 6 showed signs of English words, and the number of symbols up to where the English words began was counted to be 38, the same length of the given alphabet in the assignment. An assumption was therefore made that ciphertext 2 began with an encrypted version of the given alphabet.

In order to verify this assumption, the beginning of ciphertext 2 was mapped to the given alphabet in order to show that a key of a certain key length would rotate and begin the cycle again. The result shown on figure 7 show that a key of length 12 was used, confirming that a Vigenère cipher was used. The key $k = [2, 14, 26, 37, 12, 24, 36, 10, 22, 34, 30, 24]$ was then used in a python program in order to decrypt the ciphertext. The results seen on figure 8 shows that ciphertext 2 was successfully decoded.

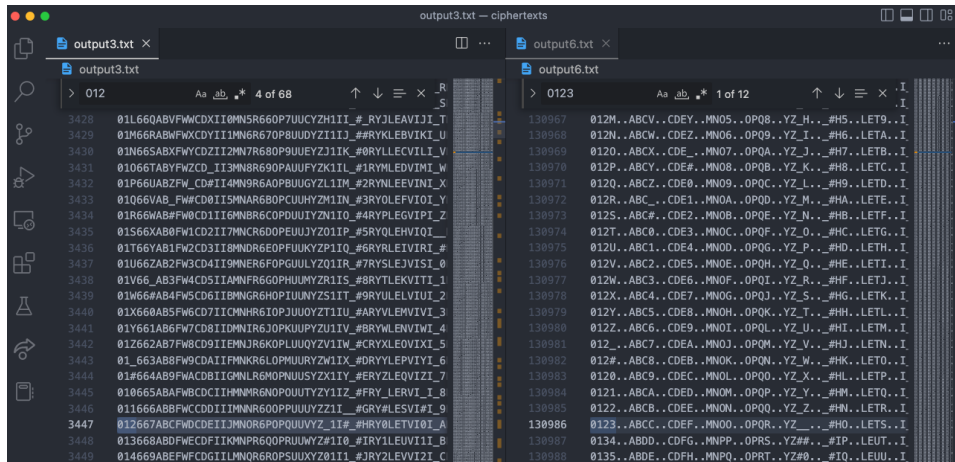


Figure 6: Partial outputs of the program *bruteforceCipher2.py*

Ciphertext	_	P	E	4	U	J	8	Z	O	D	I	P	A	#	Q	G	4	V	...
Numbers of shift forward	2	14	26	37	12	24	36	10	22	34	30	24	2	14	26	37	12	24	...
Plaintext	0	1	2	3	4	5	6	7	8	9	A	B	C	D	E	F	G	H	...

Figure 7: Manual test showing the key used in ciphertext 2

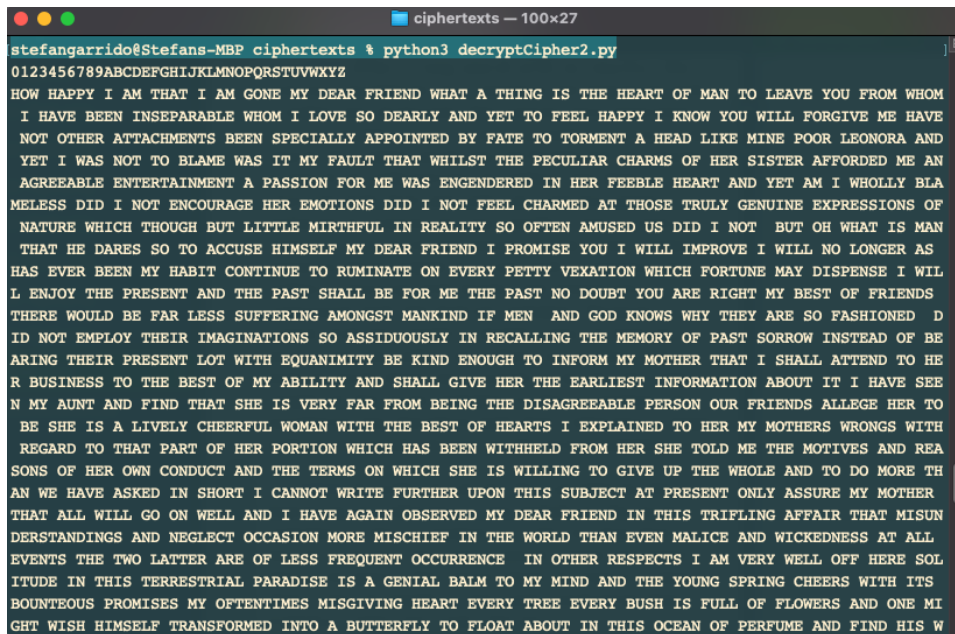


Figure 8: Partial output of the program *decryptCipher2.py*

Appendices

The following code corresponds to the program: mostCommonLetter.py

```

1 import operator
2
3 try:
4     ciphertext = open("cipher1.txt", "r")
5 except:
6     print("Error reading file, check input!")
7     exit()
8
9 #Remove newlines from file
10 ciphertext = ciphertext.read().replace('\n', '')
11 lst = {}
12
13 # Go through every char and count occurrences.
14 for char in ciphertext:
15     if char in lst:
16         lst[char] = lst[char] + 1
17         continue
18     lst[char] = 1
19
20 print()
21 print("Nr of unique symbols:", len(lst))
22 print(dict(sorted(lst.items(), key=operator.itemgetter(1),
23                 reverse=True)))

```

The following code corresponds to the program: mostCommonWord.py

```

1 import operator
2
3 try:
4     ciphertext = open("cipher1.txt", "r")
5 except:
6     print("Error reading file, check input!")
7     exit()
8
9 #Remove newlines from file
10 ciphertext = ciphertext.read().replace('\n', '')
11 #Split at character = #
12 cipherSplitted = ciphertext.split("#")
13 lst = {}
14
15 # Go through every word after splitting at # and count
    occurrences.
16 for word in cipherSplitted:
17     if word == "":
18         continue
19     if word in lst:
20         lst[word] = lst[word] + 1
21         continue
22     lst[word] = 1
23
24 print()

```

```

25 print("Nr of unique words:", len(lst))
26 print(dict(sorted(lst.items(), key=operator.itemgetter(1),
    reverse=True)))

```

The following code corresponds to the program: decryptCipher1.py

```

1 def get_corresp_char(char):
2     ascii_val = ord(char)
3
4     #Special case for 0, # and _
5     if ascii_val == 48:
6         return "\n"
7     if ascii_val == 35:
8         return " "
9     if ascii_val == 95:
10        return "Z"
11
12    # For all other chars move 1 step to the left
13    ascii_val = ascii_val - 1
14    return chr(ascii_val)
15
16 try:
17     ciphertext = open("cipher1.txt", "r")
18 except:
19     print("Error reading file, check input!")
20     exit()
21
22 #Remove newlines from file
23 ciphertext = ciphertext.read().replace('\n', '')
24
25 #Go through every character: decrypt and print
26 for c in ciphertext:
27     print(get_corresp_char(c), end = '')
28
29 print()
30 print("*** Decryption finished ***")

```

The following code corresponds to the program: bruteforceCipher2.py. Note: the code was modified for different key lengths.

```

1 # define first line of ciphertext2 and corresponding used
  alphabet
2 orig_string = "_PE4UJ8ZODIPA#QG4VK9_PU#MBOSG5WLA#4
  BYNTPKCJO3T4CGMMN05JO72QC88AHC#GQ00"
3 symbols = "0123456789ABCDEFGHIJKLMNOPQRSTUVWXYZ_"
4
5 # give every symbol in alphabet a corresponding value: 0,1,...,
  n
6 # and store results in char_to_val_list, val_to_char_list is
  the
7 # reversed key-val pair
8 char_to_val_list = {}
9 val_to_char_list = {}
10 counter = 0
11 for char in symbols:

```



```

12     char_to_val_list[char] = counter
13     val_to_char_list[counter] = char
14     counter += 1
15
16 counter = 0
17 start = 0
18 current = 0
19 # The nested for loops go through each combination for key
    length = 4
20 # Assuming the actual key length is longer, each key lenght > 4
    is
21 # handled by printing a ".", the output is then manually
    analysed
22 for k1 in range(start,38):
23     for k2 in range(0,38):
24         for k3 in range(0,38):
25             for k4 in range(0,38):
26
27                 # The different keys alternate based on key
    length
28                 for char in orig_string:
29                     # reset counter
30                     if counter == 9:
31                         counter = 0
32
33                     # Go trough different printing options
34                     if counter == 0:
35                         current = k1
36                     if counter == 1:
37                         current = k2
38                     if counter == 2:
39                         current = k3
40                     if counter == 3:
41                         current = k4
42                     if counter == 4 or counter == 5 or counter
== 6 or counter == 7 or counter == 8:
43                         print(".", end='')
44                         counter +=1
45                         continue
46
47                     pos = (char_to_val_list[char]+current)%38
48                     print(val_to_char_list[pos], end='')
49                     counter += 1
50                 counter = 0
51                 print()

```

The following code corresponds to the program: decryptCipher2.py.

```

1 symbols = "0123456789ABCDEFGHIJKLMNOPQRSTUVWXYZ_#"
2
3 try:
4     ciphertext = open("cipher2.txt", "r")
5 except:
6     print("Error reading file, check input!")
7     exit()

```



```

8
9 # give every symbol in alphabet a corresponding value: 0,1,...,
  n
10 # and store results in char_to_val_list, val_to_char_list is
    the
11 # reversed key-val pair
12 char_to_val_list = {}
13 val_to_char_list = {}
14 counter = 0
15 for char in symbols:
16     char_to_val_list[char] = counter
17     val_to_char_list[counter] = char
18     counter += 1
19
20 #Remove newlines from file
21 ciphertext = ciphertext.read().replace('\n', '')
22
23 #key for decryption
24 key = [2,14,26,37,12,24,36,10,22,34,30,24]
25 current = 0
26
27 #Go through every character: decrypt and print
28 for char in ciphertext:
29
30     if current == 12:
31         current = 0
32
33     pos = (char_to_val_list[char]+ key[current])%38
34
35     if val_to_char_list[pos] == '_':
36         print(' ', end='')
37         current += 1
38         continue
39
40     if val_to_char_list[pos] == '#':
41         print('\n', end='')
42         current += 1
43         continue
44
45     print(val_to_char_list[pos], end='')
46     current += 1
47 print()
48 print("*** Decryption finished ***")

```

References

- [1] Wikipedia. Most common words in english.
https://en.wikipedia.org/wiki/Most_common_words_in_English.