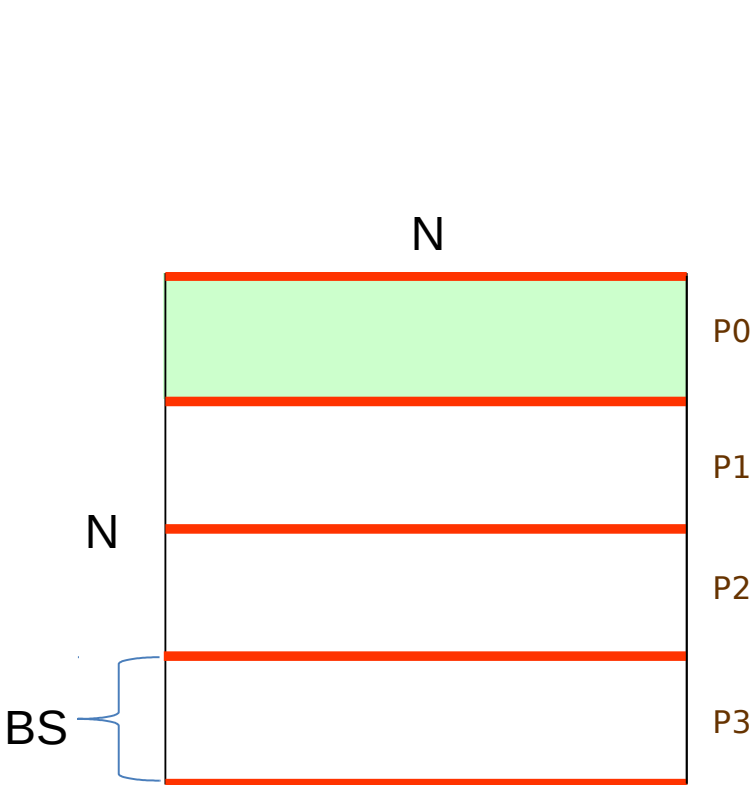


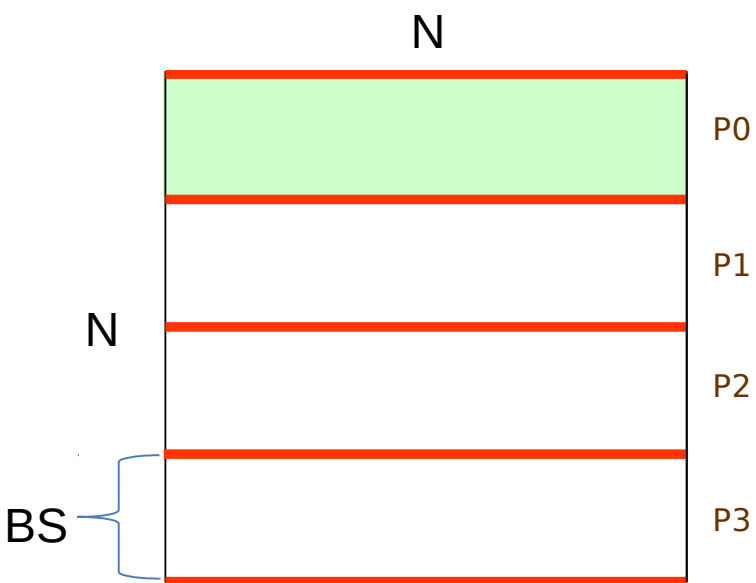
Block geometric data decomposition by rows of input data Matrix_in. Variable sum replicated



```
// Sequential
Sum = 0;
for(i=0; i<N; i++)
    for (j=0; j<N; j++)
        sum+= f(Matrix_in[i][j])
```

nt = number of threads
BS = number of rows in a block equal to N/nt

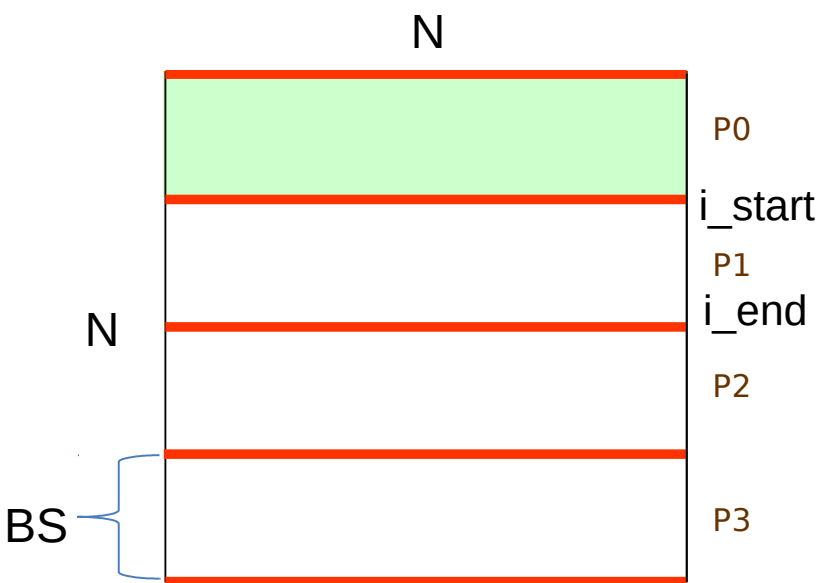
Block geometric data decomposition by rows



```
// Parallel version using omp for
sum = 0;
#pragma omp parallel
#pragma omp for private(j) schedule(static) reduction(+:sum)
for(i=0; i<N; i++)
    for (j=0; j<N; j++)
        sum+= f(Matrix_in[i][j])
```

nt = number of threads
BS = number of rows in a block equal to N/nt

Block geometric data decomposition by rows



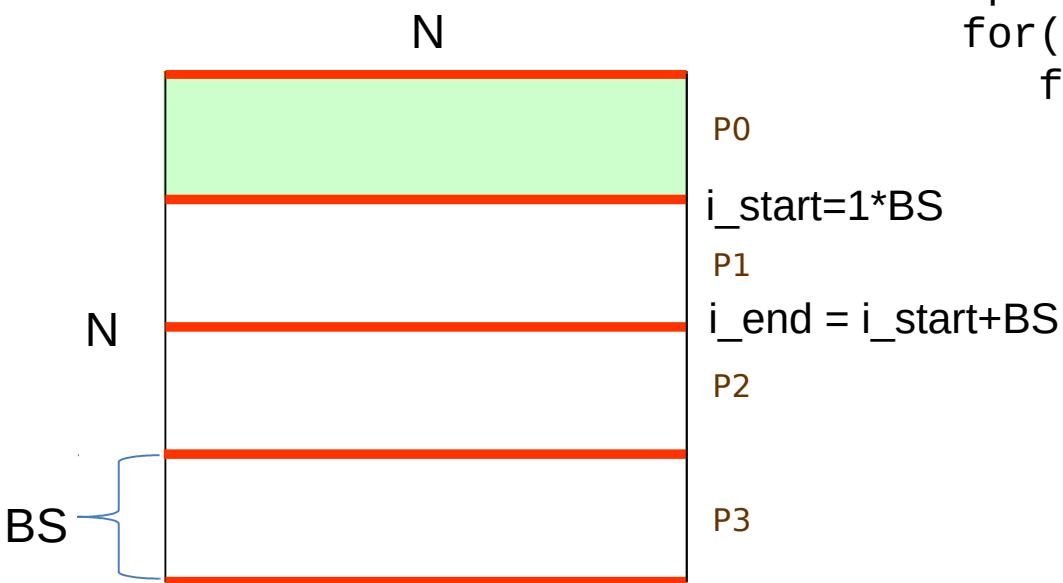
nt = number of threads
BS = number of rows in a block equal to N/nt

```
// Parallel version using omp for
sum = 0;
#pragma omp parallel
#pragma omp for private(j) schedule(static) reduction(+:sum)
for(i=0; i<N; i++)
    for (j=0; j<N; j++)
        sum+= f(Matrix_in[i][j])

// Parallel version without omp for
sum = 0;
#pragma omp parallel private(i,j) reduction(+:sum)
{
    int i_start = ?
    int i_end = ?

    for(i=i_start; i<i_end; i++)
        for (j=0; j<N; j++)
            sum+= f(Matrix_in[i][j])
}
```

Block geometric data decomposition by rows



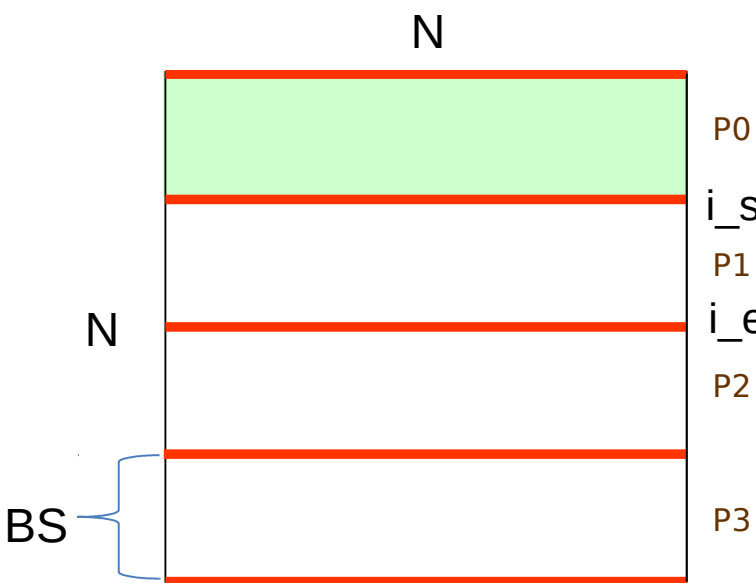
nt = number of threads
BS = number of rows in a block equal to N/nt

```
// Parallel version using omp for
sum = 0;
#pragma omp parallel
#pragma omp for private(j) schedule(static) reduction(+:sum)
for(i=0; i<N; i++)
    for (j=0; j<N; j++)
        sum+= f(Matrix_in[i][j])
```

```
// Parallel version without omp for
sum = 0;
#pragma omp parallel private(i,j) reduction(+:sum)
{
    int my_id    = omp_get_thread_num();
    int BS       = N/omp_get_num_threads();
    int i_start  = my_id * BS;
    int i_end    = i_start + BS;

    for(i=i_start; i<i_end; i++)
        for (j=0; j<N; j++)
            sum+= f(Matrix_in[i][j])
}
```

Block geometric data decomposition by rows



nt = number of threads
BS = number of rows in a block equal to N/nt

```
// Parallel version using omp for
sum = 0;
#pragma omp parallel
#pragma omp for private(j) schedule(static) reduction(+:sum)
for(i=0; i<N; i++)
    for (j=0; j<N; j++)
        sum+= f(Matrix_in[i][j])
```

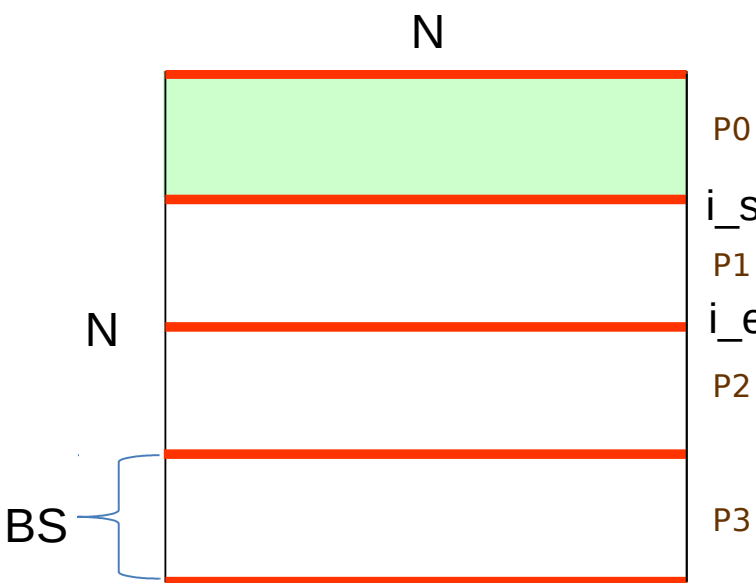
```
// Parallel version without omp for
sum = 0;
#pragma omp parallel private(i,j) reduction(+:sum)
```

Is N multiple of nt?

```
for(i=i_start; i<i_end; i++)
    for (j=0; j<N; j++)
        sum+= f(Matrix_in[i][j])
}
```

n();
eads();

Block geometric data decomposition by rows



nt = number of threads
BS = number of rows in a block equal to N/nt

```
// Parallel version using omp for
sum = 0;
#pragma omp parallel
#pragma omp for private(j) schedule(static) reduction(+:sum)
for(i=0; i<N; i++)
    for (j=0; j<N; j++)
        sum+= f(Matrix_in[i][j])
```

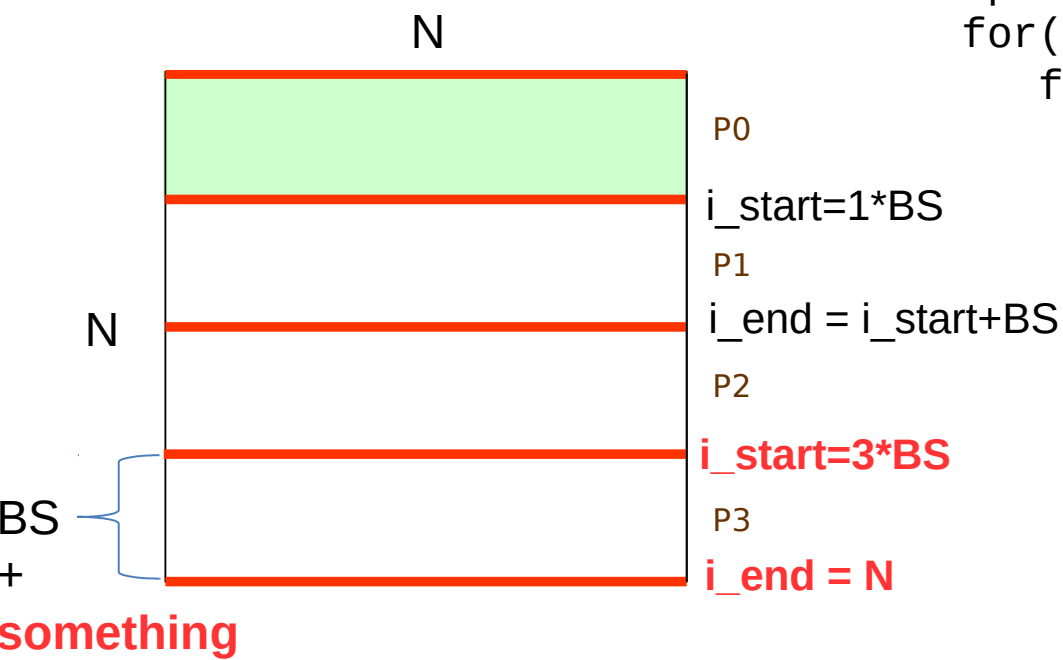
```
// Parallel version without omp for
sum = 0;
#pragma omp parallel private(i,j) reduction(+:sum)
```

Is N multiple of nt? No?
Let's give more rows to the last thread!

```
for(i=i_start; i<i_end; i++)
    for (j=0; j<N; j++)
        sum+= f(Matrix_in[i][j])
}
```

n();
eads();

Block geometric data decomposition by rows



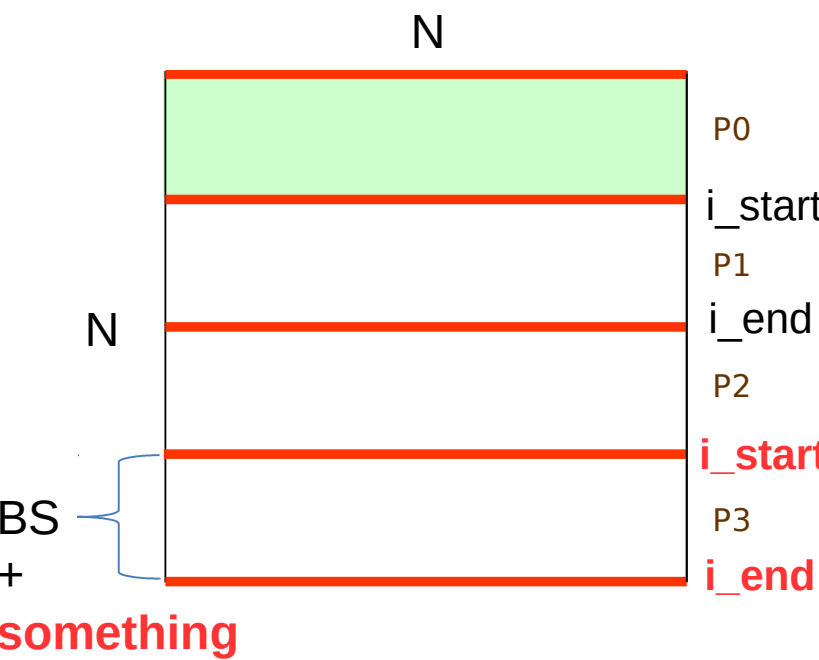
nt = number of threads
BS = number of rows in a block equal to N/nt

```
// Parallel version using omp for
sum = 0;
#pragma omp parallel
#pragma omp for private(j) schedule(static) reduction(+:sum)
for(i=0; i<N; i++)
    for (j=0; j<N; j++)
        sum+= f(Matrix_in[i][j])
```

```
// Parallel version without omp for
sum = 0;
#pragma omp parallel private(i,j) reduction(+:sum)
{
    int my_id    = omp_get_thread_num();
    int BS       = N/omp_get_num_threads();
    int i_start  = my_id * BS;
    int i_end    = i_start + BS;
    if (my_id == omp_get_num_threads()-1)
        i_end = N;

    for(i=i_start; i<i_end; i++)
        for (j=0; j<N; j++)
            sum+= f(Matrix_in[i][j])
}
```

Block geometric data decomposition by rows



nt = number of threads
BS = number of rows in a block equal to N/nt

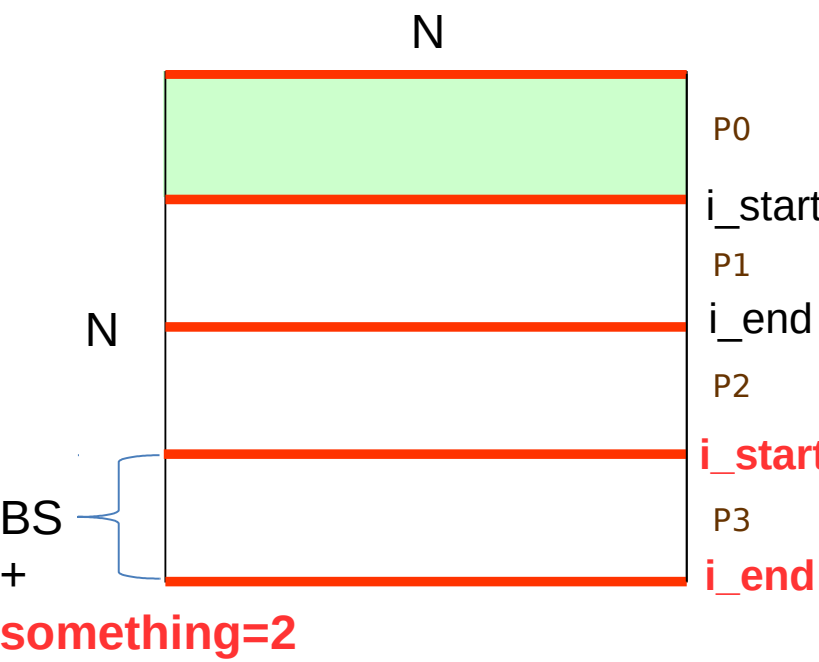
```
// Parallel version using omp for
sum = 0;
#pragma omp parallel
#pragma omp for private(j) schedule(static) reduction(+:sum)
for(i=0; i<N; i++)
    for (j=0; j<N; j++)
        sum+= f(Matrix_in[i][j])
```

```
// Parallel version without omp for
sum = 0;
#pragma omp parallel private(i,j) reduction(+:sum)
{
    int my_id = omp_get_thread_num();
    int n_threads = omp_get_num_threads();
    int i_start = my_id * (N/n_threads);
    int i_end = (my_id+1) * (N/n_threads);
    for(i=i_start; i<i_end; i++)
        for (j=0; j<N; j++)
            sum+= f(Matrix_in[i][j])
}
```

Can we maximize load balance?
Maximum one row more per thread?

```
for(i=i_start; i<i_end; i++)
    for (j=0; j<N; j++)
        sum+= f(Matrix_in[i][j])
}
```


Block geometric data decomposition by rows



nt = number of threads
BS = number of rows in a block equal to N/nt

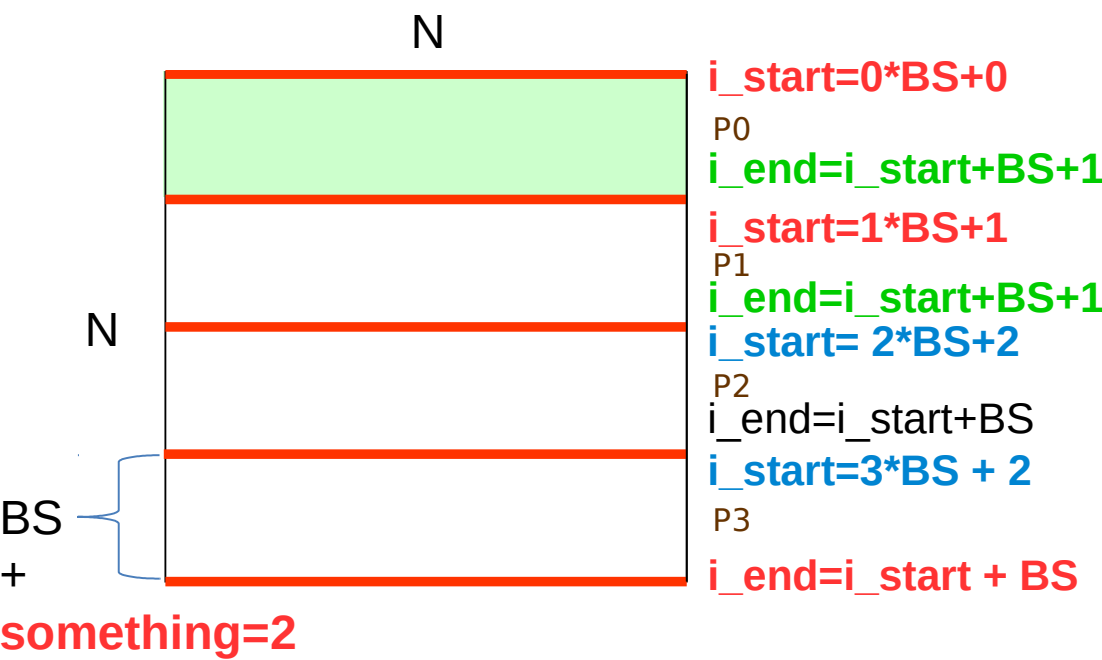
```
// Parallel version using omp for
sum = 0;
#pragma omp parallel
#pragma omp for private(j) schedule(static) reduction(+:sum)
for(i=0; i<N; i++)
    for (j=0; j<N; j++)
        sum+= f(Matrix_in[i][j])
```

```
// Parallel version without omp for
sum = 0;
#pragma omp parallel private(i,j) reduction(+:sum)
{
    int my_id = omp_get_thread_num();
    int n_threads = omp_get_num_threads();
```

Assume ... something is equal to 2

```
    i_start = my_id * BS;
    i_end = (my_id + 1) * BS;
    if (i_end > N) i_end = N;
    for(i=i_start; i<i_end; i++)
        for (j=0; j<N; j++)
            sum+= f(Matrix_in[i][j])
}
```

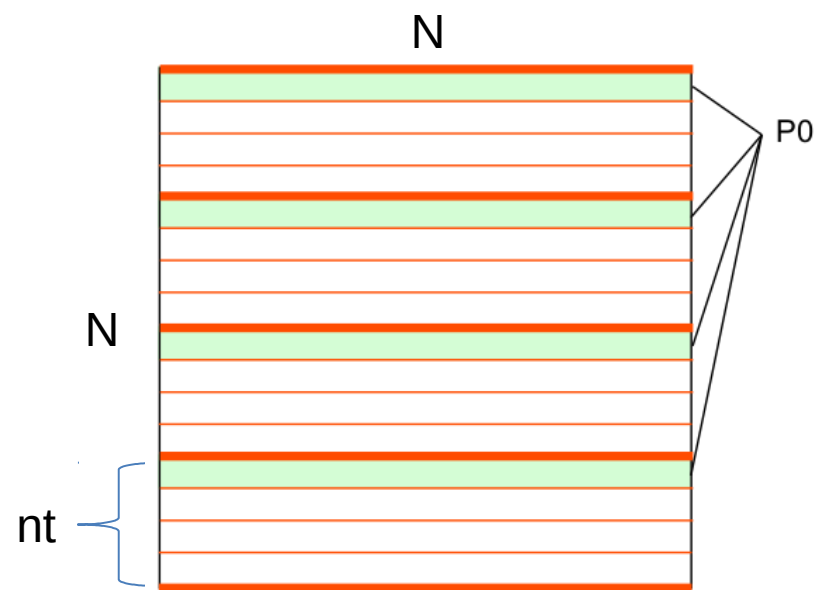
Block geometric data decomposition by rows



nt = number of threads
BS = number of rows in a block equal to N/nt

```
// Parallel version without omp for
sum = 0;
#pragma omp parallel private(i,j) reduction(+:sum)
{
    int my_id      = omp_get_thread_num();
    int nt         = omp_get_num_threads();
    int BS         = N/nt;
    int something  = N%nt;
    int i_start    = my_id * BS;
    if (my_id < something)
        i_start = i_start + my_id;
    else
        i_start = i_start + something;
    int i_end      = i_start + BS;
    if (my_id < something)
        i_end = i_end+1;
    for(i=i_start; i<i_end; i++)
        for (j=0; j<N; j++)
            sum+= f(Matrix_in[i][j])
}
```

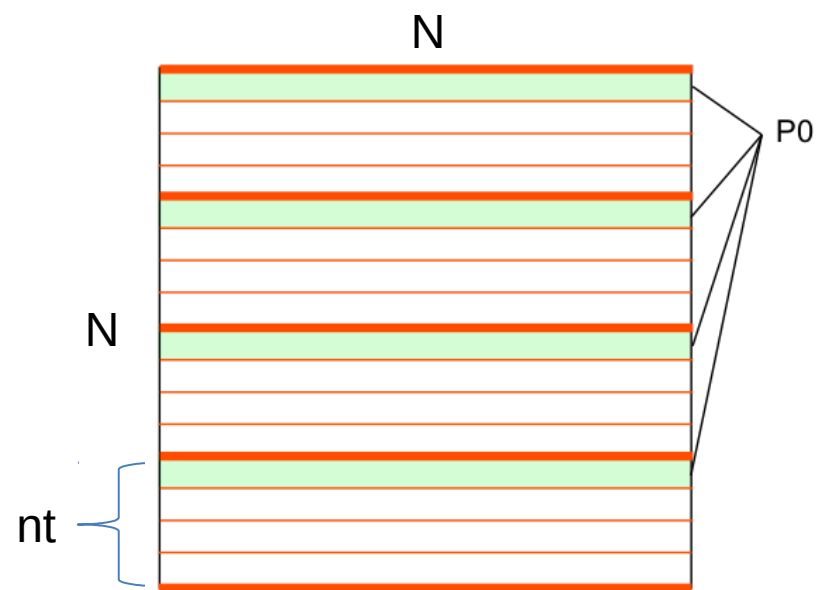
Cyclic geometric data decomposition by rows of input data Matrix_in. Variable sum replicated



nt = number of threads

```
// Sequential
Sum = 0;
for(i=0; i<N; i++)
    for (j=0; j<N; j++)
        sum+= f(Matrix_in[i][j])
```

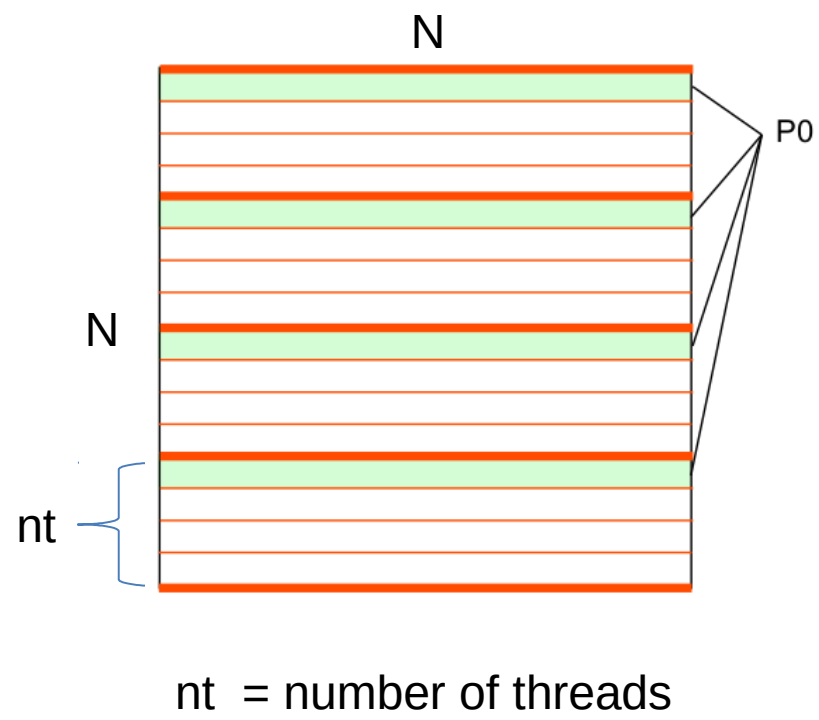
Cyclic geometric data decomposition by rows



nt = number of threads

```
// Parallel version using omp for
sum = 0;
#pragma omp parallel
#pragma omp for private(j) schedule(static,1) reduction(+:sum)
for(i=0; i<N; i++)
    for (j=0; j<N; j++)
        sum+= f(Matrix_in[i][j])
```

Cyclic geometric data decomposition by rows

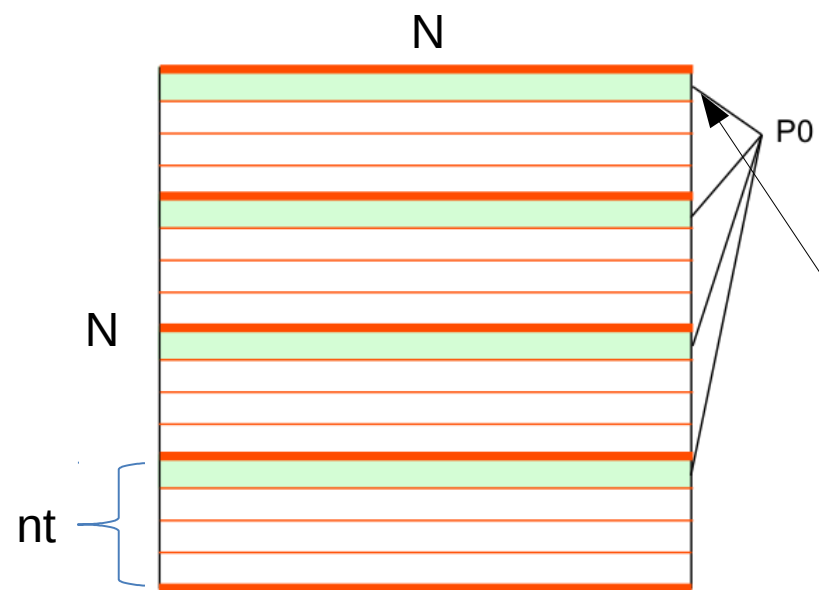


```
// Parallel version using omp for
sum = 0;
#pragma omp parallel
#pragma omp for private(j) schedule(static,1) reduction(+:sum)
for(i=0; i<N; i++)
    for (j=0; j<N; j++)
        sum+= f(Matrix_in[i][j])
```

```
// Parallel version without omp for
sum = 0;
#pragma omp parallel private(i,j) reduction(+:sum)
{
    int i_start = ?
    int i_end = ?

    for(i=i_start; i<i_end; i+= ?)
        for (j=0; j<N; j++)
            sum+= f(Matrix_in[i][j])
}
```

Cyclic geometric data decomposition by rows



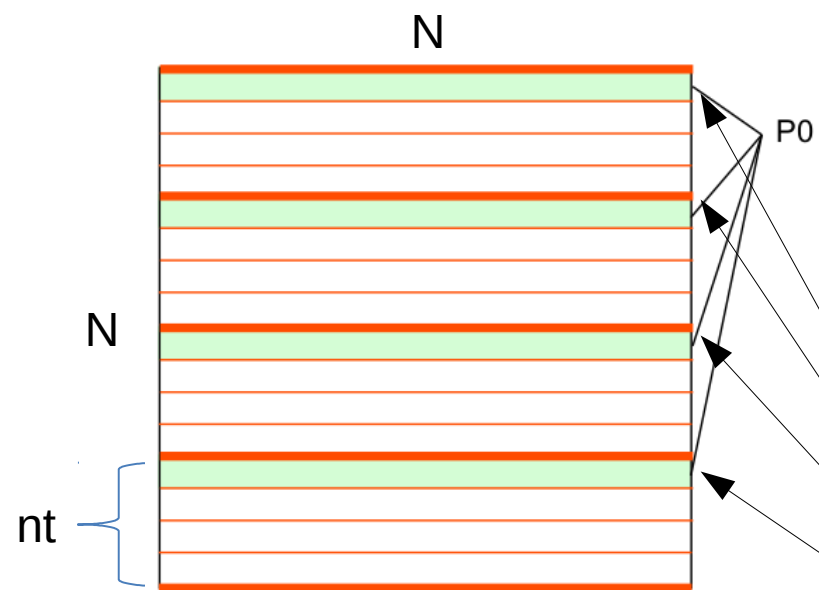
nt = number of threads

```
// Parallel version using omp for
sum = 0;
#pragma omp parallel
#pragma omp for private(j) schedule(static,1) reduction(+:sum)
for(i=0; i<N; i++)
    for (j=0; j<N; j++)
        sum+= f(Matrix_in[i][j])

// Parallel version without omp for
sum = 0;
#pragma omp parallel private(i,j) reduction(+:sum)
{
    int my_id    = omp_get_thread_num();
    int nt       = omp_get_num_threads();
    int i_start  = my_id
    int i_end    = N

    for(i=i_start; i<i_end; i+=nt)
        for (j=0; j<N; j++)
            sum+= f(Matrix_in[i][j])
}
```

Cyclic geometric data decomposition by rows



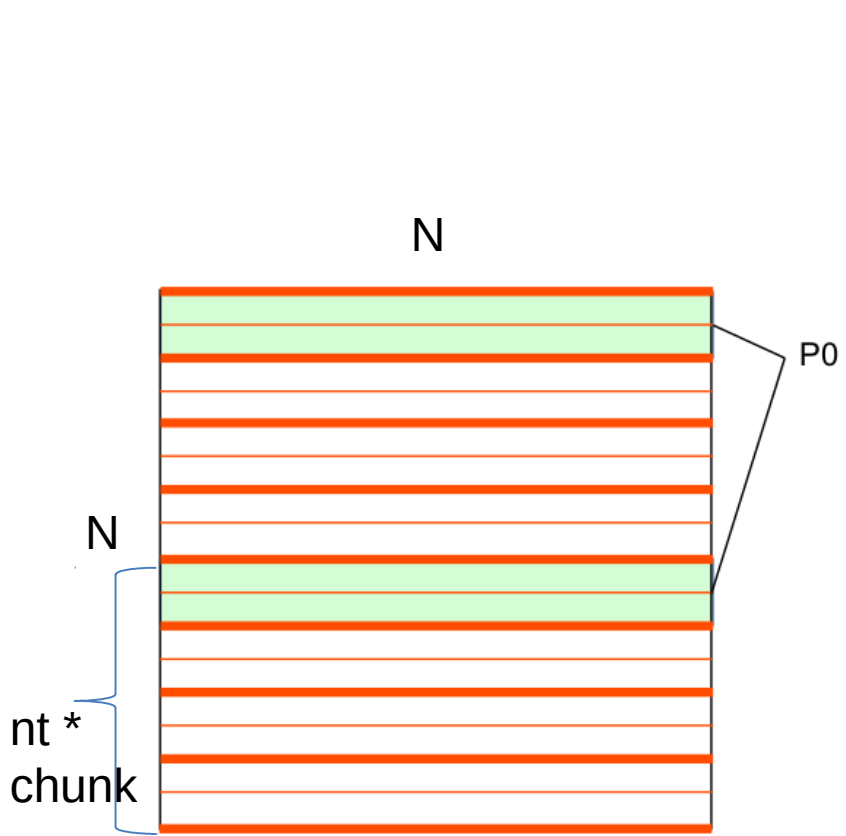
nt = number of threads

```
// Parallel version using omp for
sum = 0;
#pragma omp parallel
#pragma omp for private(j) schedule(static,1) reduction(+:sum)
for(i=0; i<N; i++)
    for (j=0; j<N; j++)
        sum+= f(Matrix_in[i][j])

// Parallel version without omp for
sum = 0;
#pragma omp parallel private(i,j) reduction(+:sum)
{
    int my_id    = omp_get_thread_num();
    int nt       = omp_get_num_threads();
    int i_start  = my_id
    int i_end    = N

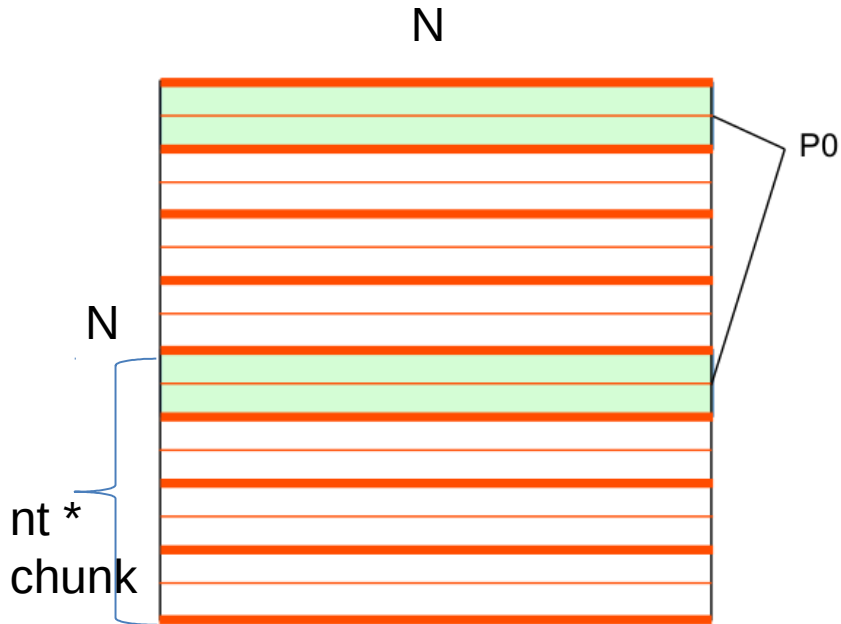
    for(i=i_start; i<i_end; i+=nt)
        for (j=0; j<N; j++)
            sum+= f(Matrix_in[i][j])
}
```

Block-Cyclic geometric data decomposition by rows of input data Matrix_in. Variable sum replicated



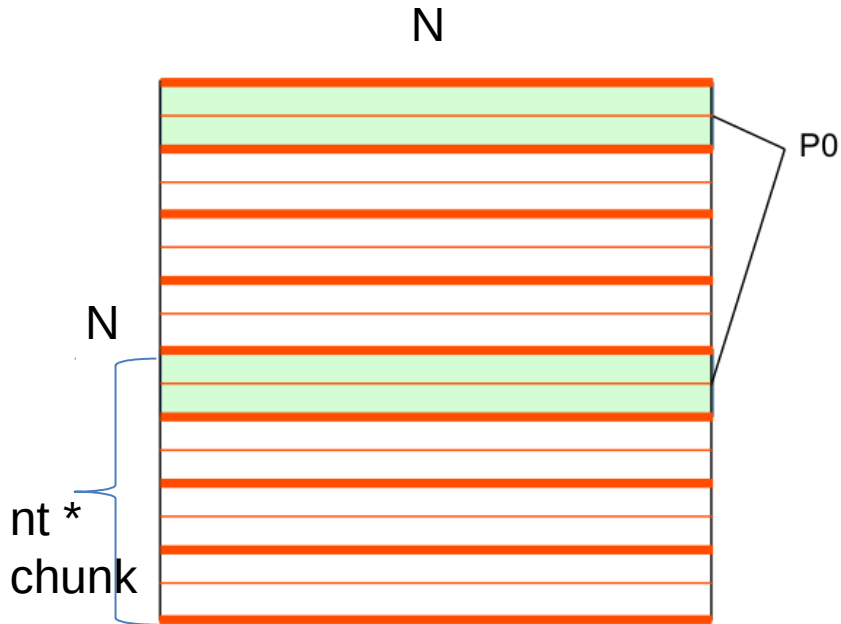
```
// Sequential
Sum = 0;
for(i=0; i<N; i++)
    for (j=0; j<N; j++)
        sum+= f(Matrix_in[i][j])
```


Block-Cyclic geometric data decomposition by rows



```
// Parallel version using omp for
sum = 0;
#pragma omp parallel
#pragma omp for private(j) schedule(static,2) reduction(+:sum)
for(i=0; i<N; i++)
    for (j=0; j<N; j++)
        sum+= f(Matrix_in[i][j])
```

Block-Cyclic geometric data decomposition by rows



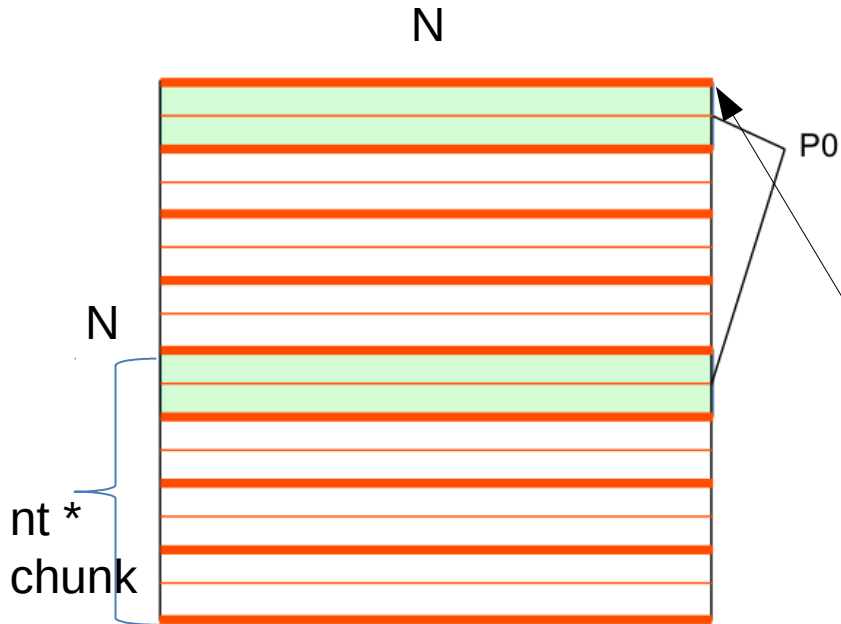
```
// Parallel version using omp for
sum = 0;
#pragma omp parallel
#pragma omp for private(j) schedule(static,2) reduction(+:sum)
for(i=0; i<N; i++)
    for (j=0; j<N; j++)
        sum+= f(Matrix_in[i][j])
```

```
// Parallel version without omp for
sum = 0;
#pragma omp parallel private(ii,i,j) reduction(+:sum)
{

    int i_start = ?;
    int i_end   = ?;

    for(ii=i_start; ii<i_end; ii+=?)
    for (?)
        for (j=0; j<N; j++)
            sum+= f(Matrix_in[i][j])
}
```

Block-Cyclic geometric data decomposition by rows

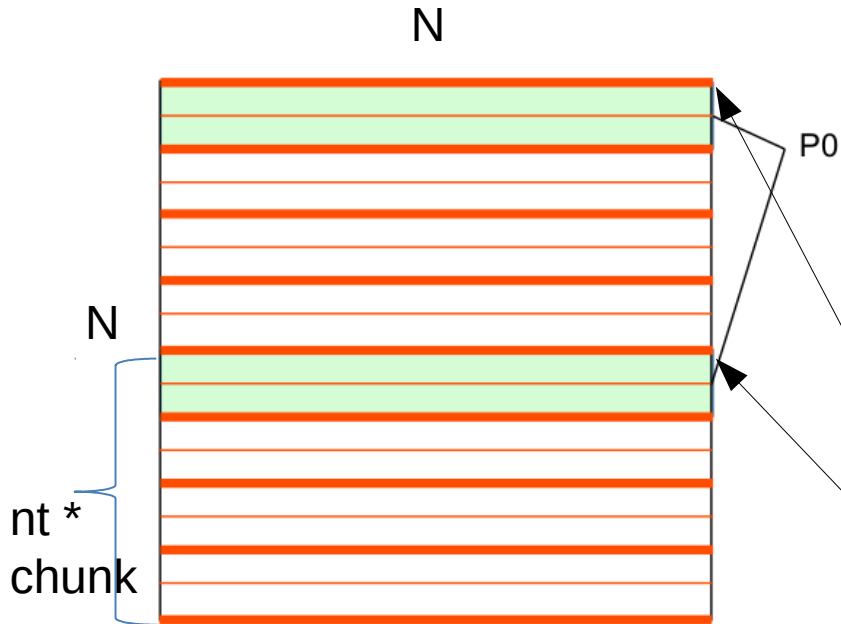


```
// Parallel version using omp for
sum = 0;
#pragma omp parallel
#pragma omp for private(j) schedule(static,2) reduction(+:sum)
for(i=0; i<N; i++)
    for (j=0; j<N; j++)
        sum+= f(Matrix_in[i][j])
```

```
// Parallel version without omp for
sum = 0;
#pragma omp parallel private(ii,i,j) reduction(+:sum)
{
    int nt      = omp_get_num_threads();
    int my_id    = omp_get_thread_num();
    int i_start = my_id*2;
    int i_end    = N;

    for(ii=i_start; ii<i_end; ii+=nt*2)
        for (i=ii; i<ii+2; i++)
            for (j=0; j<N; j++)
                sum+= f(Matrix_in[i][j])
}
```

Block-Cyclic geometric data decomposition by rows

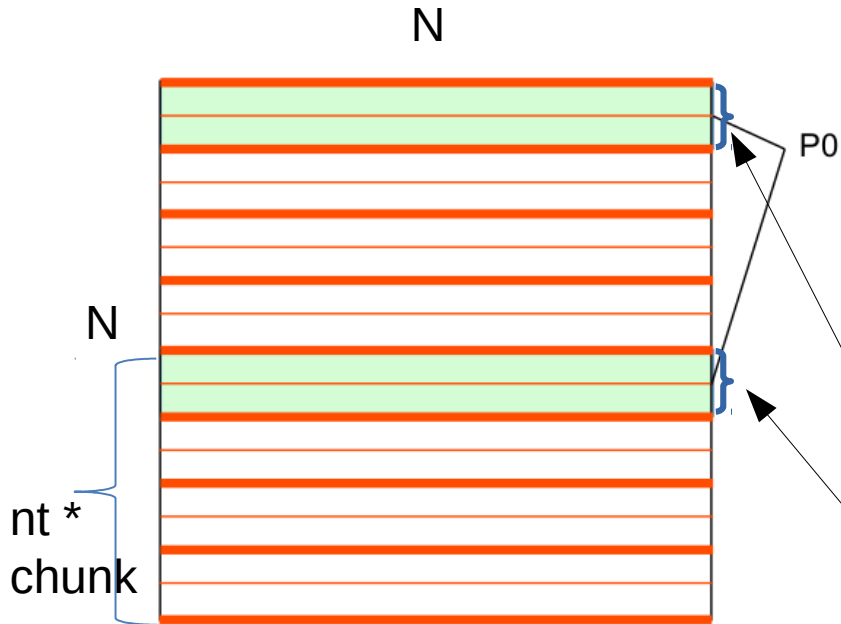


```
// Parallel version using omp for
sum = 0;
#pragma omp parallel
#pragma omp for private(j) schedule(static,2) reduction(+:sum)
for(i=0; i<N; i++)
    for (j=0; j<N; j++)
        sum+= f(Matrix_in[i][j])
```

```
// Parallel version without omp for
sum = 0;
#pragma omp parallel private(ii,i,j) reduction(+:sum)
{
    int nt      = omp_get_num_threads();
    int my_id    = omp_get_thread_num();
    int i_start = my_id*2;
    int i_end    = N;

    for(ii=i_start; ii<i_end; ii+=nt*2)
        for (i=ii; i<ii+2; i++)
            for (j=0; j<N; j++)
                sum+= f(Matrix_in[i][j])
}
```

Block-Cyclic geometric data decomposition by rows



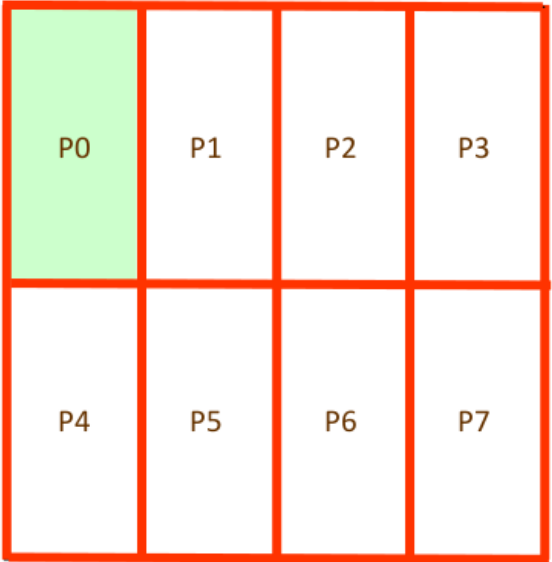
```
// Parallel version using omp for
sum = 0;
#pragma omp parallel
#pragma omp for private(j) schedule(static,2) reduction(+:sum)
for(i=0; i<N; i++)
    for (j=0; j<N; j++)
        sum+= f(Matrix_in[i][j])
```

```
// Parallel version without omp for
sum = 0;
#pragma omp parallel private(ii,i,j) reduction(+:sum)
{
    int nt      = omp_get_num_threads();
    int my_id    = omp_get_thread_num();
    int i_start = my_id*2;
    int i_end   = N;

    for(ii=i_start; ii<i_end; ii+=nt*2)
        for (i=ii; i<ii+2; i++)
            for (j=0; j<N; j++)
                sum+= f(Matrix_in[i][j])
}
```

Geometric data decomposition by BLOCKS of N/2 rows and N/4 columns (BSi x BSj)

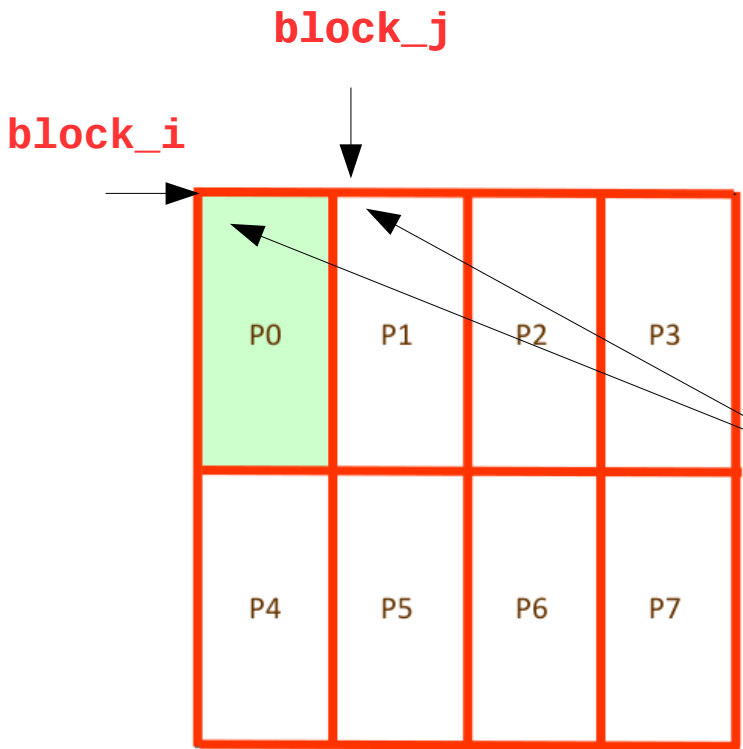
```
// Parallel version using omp for
sum = 0;
#pragma omp parallel
#pragma omp for private(j) schedule(static,2) reduction(+:sum)
for(i=0; i<N; i++)
    for (j=0; j<N; j++)
        sum+= f(Matrix_in[i][j])
```



```
// Parallel version without omp for
sum = 0;
#pragma omp parallel private(ii,i,j) reduction(+:sum) num_threads(8)
{
    int my_id
    int block_i = my_id/4; // 0 or 1 indicates which row of blocks
    int block_j = my_id%4; // 0,1,2,3 indicates which column of blocks
    int BSi = N/2;         // Assume N is multiple of 2
    int BSj = N/4;         // Assume N is multiple of 4
    int i_start = block_i * Bsi; // where should thread start?
    int i_end = i_start + BSi;
    int j_start = block_j * BSj;
    for(i=i_start; i<i_end; i++)
        for (j=j_start; j<j_end; j++)
            sum+= f(Matrix_in[i][j])
}
```

Geometric data decomposition by BLOCKS of N/2 rows and N/4 columns (BSi x BSj)

For the case of
my_id=1
block_i=my_id/4=0
block_j=my_id%4=1

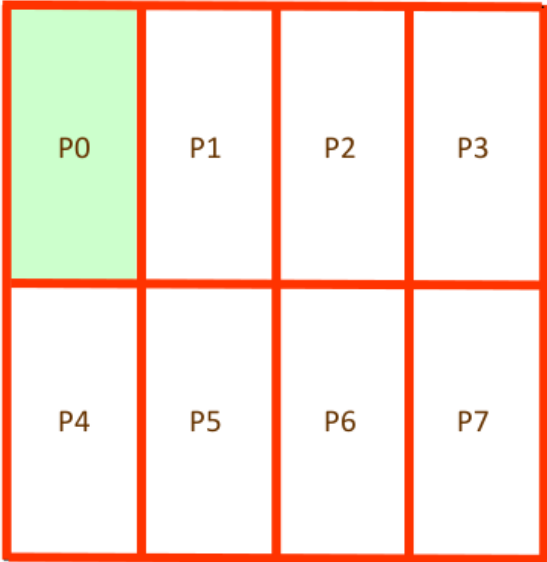


```
// Parallel version using omp for
sum = 0;
#pragma omp parallel
#pragma omp for private(j) schedule(static,2) reduction(+:sum)
for(i=0; i<N; i++)
    for (j=0; j<N; j++)
        sum+= f(Matrix_in[i][j])
```

```
// Parallel version without omp for
sum = 0;
#pragma omp parallel private(ii,i,j) reduction(+:sum) num_threads(8)
{
    int my_id
    int block_i = my_id/4; // 0 or 1 indicates which row of blocks
    int block_j = my_id%4; // 0,1,2,3 indicates which column of blocks
    int BSi = N/2; // Assume N is multiple of 2
    int BSj = N/4; // Assume N is multiple of 4
    int i_start = block_i * Bsi; // where should thread start?
    int i_end = i_start + BSi;
    int j_start = block_j * BSj;
    for(i=i_start; i<i_end; i++)
        for (j=j_start; j<j_end; j++)
            sum+= f(Matrix_in[i][j])
}
```

Geometric data decomposition by BLOCKS of N/2 rows and N/4 columns (BSi x BSj)

For the case of
my_id=1
block_i=my_id/4=0
block_j=my_id%4=1



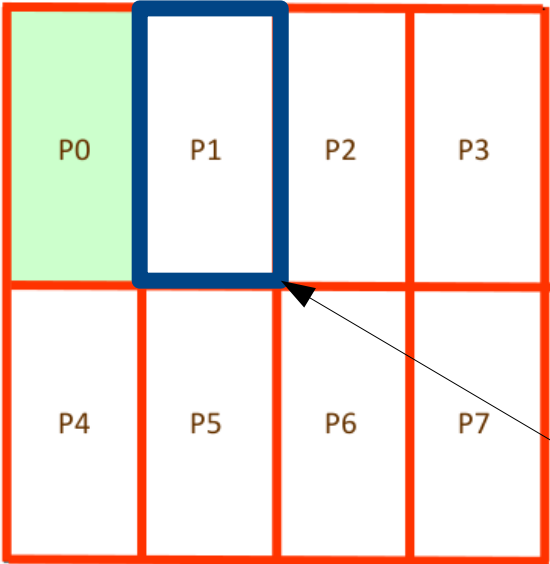
```
// Parallel version using omp for
sum = 0;
#pragma omp parallel
#pragma omp for private(j) schedule(static,2) reduction(+:sum)
for(i=0; i<N; i++)
    for (j=0; j<N; j++)
        sum+= f(Matrix_in[i][j])
```

```
// Parallel version without omp for
sum = 0;
#pragma omp parallel private(ii,i,j) reduction(+:sum) num_threads(2x4)
{
    int my_id
    int block_i = my_id/4; // 0 or 1 indicates which row of blocks
    int block_j = my_id%4; // 0,1,2,3 indicates which column of blocks
    int BSi = N/2; // Assume N is multiple of 2
    int BSj = N/4; // Assume N is multiple of 4
    int i_start = block_i * BSi; // where should thread start?
    int i_end = i_start + BSi;
    int j_start = block_j * BSj;
    for(i=i_start; i<i_end; i++)
        for (j=j_start; j<j_end; j++)
            sum+= f(Matrix_in[i][j])
}
```


Geometric data decomposition by BLOCKS of N/2 rows and N/4 columns (BSi x BSj)

For the case of
my_id=1
block_i=my_id/4=0
block_j=my_id%4=1

```
// Parallel version using omp for
sum = 0;
#pragma omp parallel
#pragma omp for private(j) schedule(static,2) reduction(+:sum)
for(i=0; i<N; i++)
    for (j=0; j<N; j++)
        sum+= f(Matrix_in[i][j])
```



```
// Parallel version without omp for
sum = 0;
#pragma omp parallel private(ii,i,j) reduction(+:sum) num_threads(8)
{
    int my_id
    int block_i = my_id/4; // 0 or 1 indicates which row of blocks
    int block_j = my_id%4; // 0,1,2,3 indicates which column of blocks
    int BSi = N/2;         // Assume N is multiple of 2
    int BSj = N/4;         // Assume N is multiple of 4
    int i_start = block_i * Bsi; // where should thread start?
    int i_end = i_start + BSi;
    int j_start = block_j * BSj;
    for(i=i_start; i<i_end; i++)
        for (j=j_start; j<j_end; j++)
            sum+= f(Matrix_in[i][j])
}
```