

UNIVERSITY OF BERGEN  
DEPARTMENT OF INFORMATICS

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# Title of your master thesis

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## **Abstract**

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### **Acknowledgements**

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Your name

Wednesday 8<sup>th</sup> May, 2024

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# Chapter 1

## Introduction

Natum mucius vim id. Tota detracto ei sed, id sumo sapientem sed. Vim in nostro latine gloriatur, cetero vocent vim id. Erat sanctus eam te, nec assueverit necessitatibus ex, id delectus fabellas has.

Lorem ipsum dolor sit amet, iisque feugait quo eu, sed vocent commodo aliquid an. Minim suavitate dissentiet te eos. Dicunt eirmod adolescens no sed. Esse nonumy melius an mel, mei ut maiorum luptatum. Eu eum iudico scripta, movet option assueverit mel ex, mea at odio noluisse efficiendi. Ad vidisse atomorum conceptam quo, saepe volumus philosophia eos eu, delenit conceptam no usu.

Vituperata sadipscing deterruisset ei mel, at qui nonumy blandit. Delectus dissentiet et sea, ut rebum regione numquam nam, cum ex augue constituto. Te per nihil semper. Posse voluptatum qui an, aliquando democritum disputando id quo, everti perpetua cu vim. Laudem fabellas mei an, eu reprimique quaerendum usu. Quidam prompta fabellas ne est.

### 1.1 Background

Lorem ipsum dolor sit amet, cu graecis propriae sea. Eam feugiat docendi an, ei scripta blandit pri. Nonumes delicata reprimique nam ut. Eu suas alterum concludaturque est, ferri mucius sensibus id sed [1].

We can do glossary for acronymes and abriviations also: Software as a Service (SaaS). As you see the first time it is used, the full version is used, but the second time we use SaaS the short form is used. It is also a link to the lookup.

### 1.1.1 Listings

You can do listings, like in Listing 1.1

Listing 1.1: Look at this cool listing. Find the rest in Appendix A.1

```
1 $ java -jar myAwesomeCode.jar
```

You can also do language highlighting for instance with Golang: And in line 6 of Listing 1.2 you can see that we can ref to lines in listings.

Listing 1.2: Hello world in Golang

```
1 package main
2
3 import "fmt"
4
5 func main() {
6     fmt.Println("hello world")
7 }
```

### 1.1.2 Figures

Example of a centred figure

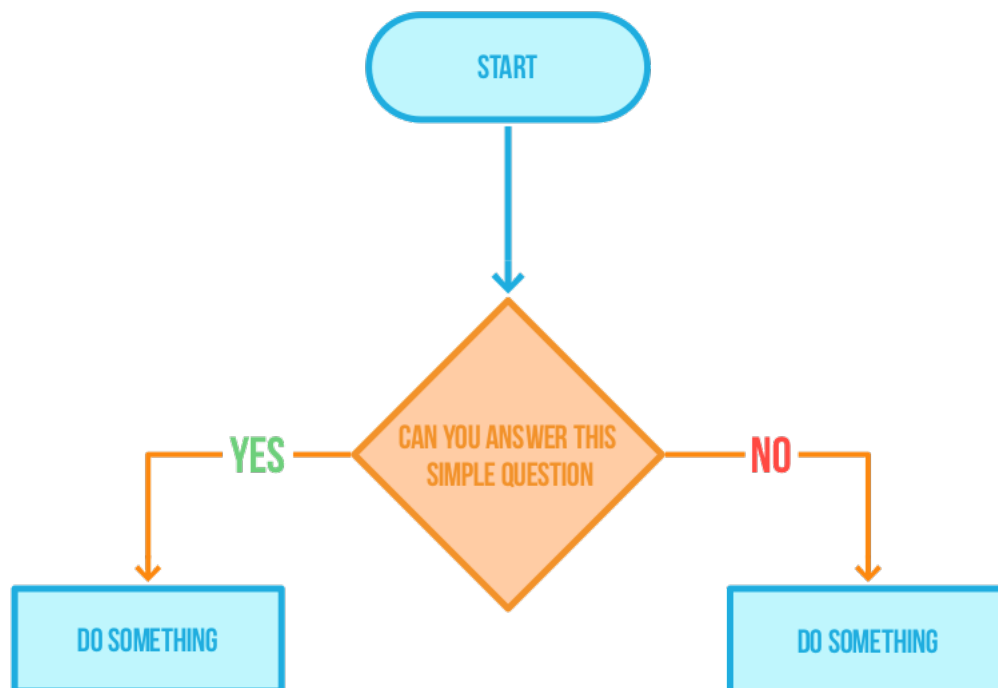


Figure 1.1: Caption for flowchart

Credit: Acme company makes everything <https://acme.com/>

### 1.1.3 Tables

We can also do tables. Protip: use <https://www.tablesgenerator.com/> for generating tables.

Table 1.1: Caption of table

Title1	Title2	Title3
data1	data2	data3

### 1.1.4 Git

Git is fun, use it!

# Chapter 2

## Preliminaries

### 2.1 Graphs

A *graph*  $G = (V, E, from^G, to^G)$  is given by

- $V$ , a collection of *vertices*
- $E$ , a collection of *edges*
- $from^G : E \rightarrow V$ , a mapping from each edge to its source vertex
- $to^G : E \rightarrow V$ , a mapping from each edge to its target vertex

In algorithms, we often use graphs as an abstract structure to represent the fundamental problem behind an algorithms problem without distractions.

TODO: Omskriv, dette er elendig TODO: Hva er det som egentlig er nødvendig å ha med her? Er det noen som noensinne kommer til å lese dette uten å vite hva en graf er? TODO: rettede grafer vs urettede grafer TODO: vektete grafer

### 2.2 Planarity

# Chapter 3

## Algorithm for Shortest Odd Path

### 3.1 Intuition

### 3.2 Psuedocode

Listing 3.1: Main

```
1 fn main(Graph input_graph, int s, int t) -> Option<(int, List<Edge>> {
2   init(input_graph, s, t);
3
4   while ! control() {}
5
6   if d_minus[t] == ∞ {
7     // The graph is a no-instance, no odd s-t-paths exist
8     return None;
9   }
10
11   Edge current_edge = pred[t];
12   List<Edge> path = [current_edge];
13   while from(current_edge) != s {
14     current_edge = pred[mirror(from(current_edge))];
15     if from(current_edge) < input_graph.n() {
16       path.push(current_edge);
17     }
18     else {
19       path.push(shift_edge_by(current_edge, -input_graph.n()));
20     }
21   }
22   return Some(d_minus[t], path);
23 }
```

Listing 3.2: Initialization

```
1 fn init(Graph input_graph, int s, int t) {
2   graph = create_mirror_graph(input_graph);
3
4   for u in 0..n {
```

```

5      d_plus[u] = ∞;
6      d_minus[u] = ∞;
7      pred[u] = null;
8      completed[u] = false;
9  }
10  d_plus[s] = 0;
11  completed[s] = true;
12
13  for edge in graph[s] {
14      pq.push(Vertex(weight(edge), to(edge)));
15      d_minus[to(edge)] = weight(edge);
16      pred[to(edge)] = e;
17  }
18 }

```

Listing 3.3: Control, the main loop

```

1  fn control() -> bool {
2      while ! pq.is_empty() {
3          match pq.top() {
4              Vertex(_, u) => {
5                  if completed[u] {
6                      pq.pop();
7                  }
8                  else {
9                      break;
10                 }
11             },
12             Blossom(_, edge) => {
13                 if base_of(from(edge)) == base_of(to(edge)) {
14                     pq.pop();
15                 }
16                 else {
17                     break;
18                 }
19             }
20         }
21     }
22
23     if pq.is_empty() {
24         // No odd s-t-paths in G exist :(
25         return true;
26     }
27     match pq.pop() {
28         Vertex(delta, l) => {
29             if l == t {
30                 // We have found a shortest odd s-t-path has been
31                 //      ↪ found :)
32                 return true;
33             }
34             grow(l, delta)
35         }
36         Blossom(delta, edge) => {
37             blossom(e);
38         }
39     }
40     return false;
41 }

```

Listing 3.4: Grow

```

1  fn grow(int l, int delta) {
2      int k = mirror(l);
3      d_plus[k] = delta;
4      scan(k);
5  }

```

Listing 3.5: Scan

```

1 fn scan(int u) {
2   completed[u] = true;
3   int dist_u = d_plus[u];
4   for edge in graph[u] {
5     int v = to(edge);
6     int new_dist_v = dist_u + weight(edge);
7
8     if ! completed[v] {
9       if new_dist_v < d_minus[v] {
10        d_minus[v] = new_dist_v;
11        pred[v] = edge;
12        pq.push(Vertex(new_dist_v, v));
13      }
14    }
15    else if d_plus[v] < ∞ and base_of(u) != base_of(v) {
16      pq.push(Blossom(d_plus[u] + d_plus[v] + weight(edge)));
17      if new_dist_v < d_minus[v] {
18        d_minus[v] = new_dist_v;
19        pred[v] = e;
20      }
21    }
22  }
23 }

```

Listing 3.6: Blossom

```

1 fn blossom(Edge edge) {
2   (int, List<Edge>, List<Edge>) (b, p1, p2) =
3     ↪ backtrack_blossom(edge);
4
5   List<int> to_scan1 = set_blossom_values(p1);
6   List<int> to_scan2 = set_blossom_values(p2);
7
8   set_edge_bases(b, p1);
9   set_edge_bases(b, p2);
10
11   for u in to_scan1 {
12     scan(u);
13   }
14   for v in to_scan2 {
15     scan(v);
16   }
17 }

```

Listing 3.7: Backtrack blossom

```

1 fn backtrack_blossom(Edge edge) -> (int, List<Edge>, List<Edge>){
2   // TODO
3 }

```

Listing 3.8: Set blossom values

```

1 fn set_blossom_values(List<Edge> path) -> List<int> {
2   List<int> to_scan = [];
3
4   for edge in path {
5     int u = from(edge);
6     int v = to(edge);
7     int w = weight(edge);
8     in_current_cycle[u] = false;
9     in_current_cycle[v] = false;
10
11     // We can set a d_minus

```

```

12     if d_plus[v] + w < d_minus[u] {
13         d_minus[u] = d_plus[v] + w;
14         pred[u] = reverse(edge);
15     }
16
17     int m = mirror(u);
18     // We can set a d_plus, and scan it
19     if d_minus[u] < d_plus[m] {
20         d_plus[m] = d_minus[u];
21         to_scan.push(m);
22     }
23 }
24
25 return to_scan;
26 }

```

Listing 3.9: Set edge bases

```

1 fn set_edge_bases(int b, List<Edge> path) {
2     for edge in path {
3         let u = from(edge);
4         let m = mirror(edge);
5         set_base(u, b);
6         set_base(m, b);
7     }
8 }

```

Listing 3.10: Basis

```

1 fn init(Graph input_graph, int s, int t) {
2     // omitted
3     Graph graph = create_mirror_graph(input_graph, s, t);
4     for u in 0..graph.n() {
5         basis[u] = u;
6     }
7     // omitted
8 }
9 fn set_base(int b, int u) {
10     basis[u] = b;
11 }
12 fn get_base(int u) -> int {
13     if u != basis[u] {
14         basis[u] = get_base(basis[u]);
15     }
16     return basis[u];
17 }

```

### 3.3 Notes on implementing the psuedocode



# Chapter 4

## Analysis of Shortest Odd Path

### 4.1 Complexity

### 4.2 Benchmarking methodology

### 4.3 Results

### 4.4 Discussion

# Chapter 5

## Algorithm for Network Diversion

### 5.1 Psuedocode

# Chapter 6

## Analysis of Network Diversion

### 6.1 Complexity

### 6.2 Benchmarking methodology

### 6.3 Results

### 6.4 Discussion

## Chapter 7

## Conclusion

# Bibliography

- [1] Diego Ongaro and John Ousterhout. In search of an understandable consensus algorithm. In *Proceedings of the 2014 USENIX Conference on USENIX Annual Technical Conference*, USENIX ATC'14, pages 305–320, Berkeley, CA, USA, 2014. USENIX Association. ISBN 978-1-931971-10-2.

## Appendix A

### Generated code from Protocol buffers

Listing A.1: Source code of something

```
1 System.out.println("Hello Mars");
```