

Exercise 3.2.1

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1 Question

Exercise 3.2.1 Compare the data sets $k_1 = 8$, $n_1 = 10$, $k_2 = 7$, $n_2 = 10$ and $k_1 = 80$, $n_1 = 100$, $k_2 = 70$, $n_2 = 100$. Before you run the code, try to predict the effect that adding more trials has on the posterior distribution for δ .

2 Comments/Solution

Looking at the posterior distribution from the previous exercises we know that adding more data will make the posterior estimate narrower and less uncertain. Now we can also run the model script of the two datasets and observe these effects. Have a look at the plots section below.

The model used to calculate the required values and the plots is scripted below. Copy/pasting the given code will generate the same result on your own machine.

3 Code

3.1 libraries

The libraries required for the script and the plots.

```
# clears workspace
rm(list=ls())
#load libraries
library(rstan)
library(ggplot2)
library(patchwork)
```

3.2 Data

The data required for this particular stan model.

```
# data initialization
k1 <- 8;n1 <- 10;k2 <- 7;n2 <- 10
# to be passed on to Stan
stan_data <- list(k1 = k1, n1 = n1, k2 = k2, n2 = n2)
#
k1 <- 80;n1 <- 100;k2 <- 70;n2 <- 100
# to be passed on to Stan
stan_data_1 <- list(k1 = k1, n1 = n1, k2 = k2, n2 = n2)
```

3.3 Stan code

Stan code, that can be written in R as such or in a separate new file with stan extension.

```
write("// Stan code here in this section

// Inferring delta through theta1 and theta2
data {
  int<lower=1> n1;
  int<lower=1> n2;
  int<lower=0> k1;
  int<lower=0> k2;
}
parameters {
  real<lower=0,upper=1> theta1;
  real<lower=0,upper=1> theta2;
}
transformed parameters {
  real<lower=-1,upper=1> delta;
  delta <- theta1 - theta2;
}
model {
  // Prior Distribution for Rate Theta
  theta1 ~ beta(1, 1);
  theta2 ~ beta(1, 1);
  // Observed Counts
  k1 ~ binomial(n1, theta1);
  k2 ~ binomial(n2, theta2);
} // ",

"3_2_1.stan")
```

3.4 code in R to run stan

Running stan through R (with the required input parameters).

```
myinits <- list(
  list(theta1=.1), # chain 1 starting value
  list(theta2=.9)) # chain 2 starting value

# parameters to be monitored:
parameters <- c("delta", "theta1", "theta2")
```

```

# The following command calls Stan with specific options.
# For a detailed description type "?stan".
mod_fit <- stan(file="3_2_1.stan",
               data=stan_data,
               init=myinits, # If not specified, gives random inits
               pars=parameters,
               iter=2000,
               chains=2,
               thin=1,
               warmup=100, # Stands for burn-in; Default = iter/2
               seed=123 # Setting seed; Default is random seed
)
mod_fit_1 <- stan(file="3_2_1.stan",
                 data=stan_data_1,
                 init=myinits, # If not specified, gives random inits
                 pars=parameters,
                 iter=2000,
                 chains=2,
                 thin=1,
                 warmup=100, # Stands for burn-in; Default = iter/2
                 seed=123 # Setting seed; Default is random seed
)

```

4 Outputs

4.1 Model summary

In order of definition.

```

## Inference for Stan model: 3_2_1.
## 2 chains, each with iter=2000; warmup=100; thin=1;
## post-warmup draws per chain=1900, total post-warmup draws=3800.
##
##          mean se_mean   sd  2.5%    25%    50%    75%   97.5% n_eff Rhat
## delta      0.08    0.00 0.17  -0.27  -0.03   0.09   0.20   0.42  4004   1
## theta1     0.75    0.00 0.12   0.47   0.68   0.76   0.84   0.94  3651   1
## theta2     0.67    0.00 0.13   0.39   0.58   0.68   0.76   0.89  4070   1
## lp__    -15.44     0.03 1.08 -18.34 -15.84 -15.10 -14.69 -14.42  1660   1
##
## Samples were drawn using NUTS(diag_e) at Wed Oct 21 15:01:26 2020.
## For each parameter, n_eff is a crude measure of effective sample size,
## and Rhat is the potential scale reduction factor on split chains (at
## convergence, Rhat=1).

## Inference for Stan model: 3_2_1.
## 2 chains, each with iter=2000; warmup=100; thin=1;
## post-warmup draws per chain=1900, total post-warmup draws=3800.
##
##          mean se_mean   sd  2.5%    25%    50%    75%   97.5% n_eff
## delta      0.10    0.00 0.06  -0.01   0.06   0.10   0.14   0.21  3951
## theta1     0.79    0.00 0.04   0.71   0.77   0.80   0.82   0.86  3569
## theta2     0.70    0.00 0.05   0.60   0.67   0.70   0.73   0.78  4005
## lp__    -115.50     0.02 0.98 -117.96 -115.89 -115.18 -114.79 -114.53  1978
##          Rhat

```

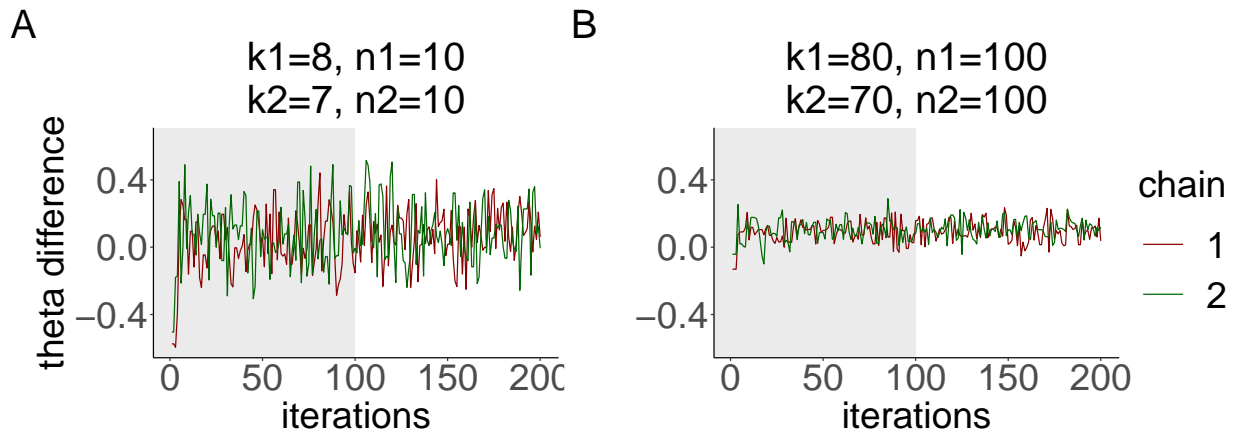
```
## delta      1
## theta1     1
## theta2     1
## lp__       1
##
## Samples were drawn using NUTS(diag_e) at Wed Oct 21 15:01:26 2020.
## For each parameter, n_eff is a crude measure of effective sample size,
## and Rhat is the potential scale reduction factor on split chains (at
## convergence, Rhat=1).
```

4.2 Plots

4.2.1 Plot (chains)

The initial movement of the chains are shown here (including the warmup phase). The two chains begin from the initial starting points of as defined in the input parameters of the stan model.

comparison of datasets



4.2.2 Plot (posterior)

The plot of the δ values per chain superimposed on each other.

comparison of datasets

