# Exercise 3.1.3

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# 1 Question

Exercise 3.1.3 Alter the data to k = 50 and n = 100, and compare the posterior for the rate  $\theta$  to the original with k = 5 and n = 10.

# 2 Comments/Solution

Comparing at the posterior distributions (from the plots section below) of the two different datasets reveals that with a lager number of data samples produces posterior estimates that have a narrower and taller (less uncertainity) distribution. Even though the underlying probabilities remain the same a larger data sample size has a better posterior estimate.

The model used to calculate the required values and the plots is scripted below. Copy/pasting the given code will generate the same result on your own machine.

#### 3 Code

#### 3.1 libraries

The libraries required for the script and the plots.

```
# clears workspace
rm(list=ls())
#load libraries
library(rstan)
library(ggplot2)
library(patchwork)
```

#### 3.2 Data

The data required for this particular stan model.

```
# data initialization
k <- 5
n <- 10
k_1 <- 50
n_1 <- 100
# to be passed on to Stan
stan_data <- list(k = k, n = n)
stan_data_1 <- list(k = k_1, n = n_1)</pre>
```

#### 3.3 Stan code

Stan code, that can be written in R as such or in a seperate new file with stan extension.

```
write("// Stan code here in this section

// Inferring theta
data {
  int<lower=1> n;
  int<lower=0> k;
}
parameters {
  real<lower=0,upper=1> theta;
}
model {
  // Prior Distribution for theta
  theta ~ beta(1, 1);

  // Observed Counts
  k ~ binomial(n, theta);
} // ",

"3_1_3.stan")
```

#### 3.4 code in R to run stan

Running stan through R (with the required input parameters).

## 4 Outputs

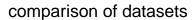
#### 4.1 Model summary

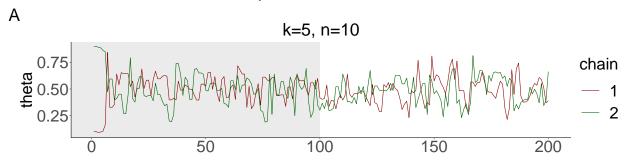
```
For dataset k=5 and n=10. (stan data)
## Inference for Stan model: 3_1_3.
## 2 chains, each with iter=2000; warmup=100; thin=1;
## post-warmup draws per chain=1900, total post-warmup draws=3800.
##
                                     25%
                                            50%
##
          mean se_mean
                         sd
                              2.5%
                                                  75% 97.5% n_eff Rhat
## theta 0.49
                  0.00 0.14
                              0.23 0.40 0.49 0.59 0.76 1464
                  0.02 0.73 -10.88 -8.98 -8.55 -8.37 -8.32 1475
## lp__ -8.83
                                                                     1
##
## Samples were drawn using NUTS(diag_e) at Tue Oct 20 11:44:18 2020.
## For each parameter, n_eff is a crude measure of effective sample size,
## and Rhat is the potential scale reduction factor on split chains (at
## convergence, Rhat=1).
For dataset k=50 and n=100. (stan_data_1)
## Inference for Stan model: 3 1 3.
## 2 chains, each with iter=2000; warmup=100; thin=1;
## post-warmup draws per chain=1900, total post-warmup draws=3800.
##
                               2.5%
                                       25%
                                               50%
                                                          97.5% n_eff Rhat
##
           mean se_mean
                          sd
                                                      75%
## theta
           0.50
                   0.00 0.05
                               0.40
                                      0.46
                                              0.50
                                                     0.53
                                                            0.59 1413
## lp__ -71.22
                   0.02 0.74 -73.22 -71.38 -70.94 -70.75 -70.70 1762
                                                                          1
##
## Samples were drawn using NUTS(diag_e) at Tue Oct 20 11:44:18 2020.
## For each parameter, n_eff is a crude measure of effective sample size,
## and Rhat is the potential scale reduction factor on split chains (at
## convergence, Rhat=1).
```

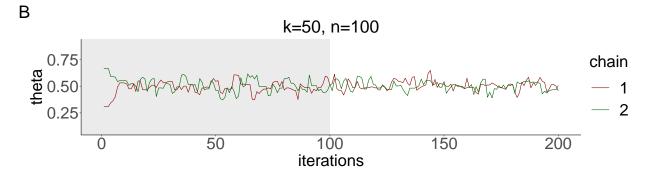
#### 4.2 Plots

#### 4.2.1 Plot (chains)

The initial movement of the chains are shown here (including the warmup phase). The two chains begin from the initial starting points of as defined in the input parameters of the stan model.







### 4.2.2 Plot (posterior)

The plot of the  $\theta$  values per chain superimposed on each other.

# comparison of datasets

