

Exercise 3.3.1

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1 Question

Exercise 3.3.1 Try the data $k1 = 14$, $n1 = 20$, $k2 = 16$, $n2 = 20$. How could you report the inference about the common rate θ ?

2 Comments/Solution

In this example of the dataset we see that the individually the $k1$ and $k2$ both present cases around the probability of 0.75 and the common rate θ is estimated also to be around 0.75. Check out the plots section.

One reasonable reporting strategy here might be to use a measure for central tendency, such as a mean, median, or mode, together with a credible interval, for instance a 95% credible interval.

The model used to calculate the required values and the plots is scripted below. Copy/pasting the given code will generate the same result on your own machine.

3 Code

3.1 libraries

The libraries required for the script and the plots.

```
# clears workspace
rm(list=ls())
#load libraries
library(rstan)
```

```
library(bayestestR)
library(ggplot2)
library(patchwork)
```

3.2 Data

The data required for this particular stan model.

```
# data initialization
k1 <- 14;n1 <- 20;k2 <- 16;n2 <- 20
# to be passed on to Stan
stan_data <- list(k1 = k1, n1 = n1, k2 = k2, n2 = n2)
```

3.3 Stan code

Stan code, that can be written in R as such or in a separate new file with stan extension.

```
write("// Stan code here in this section

// Inferring theta
data {
  int<lower=1> n1;
  int<lower=1> n2;
  int<lower=0> k1;
  int<lower=0> k2;
}
parameters {
  real<lower=0,upper=1> theta;
}
model {
  // Prior on Single Rate Theta
  theta ~ beta(1, 1);
  // Observed Counts
  k1 ~ binomial(n1, theta);
  k2 ~ binomial(n2, theta);
} // ",

"3_3_1.stan")
```

3.4 code in R to run stan

Running stan through R (with the required input parameters).

```
myinits <- list(
  list(theta=.1), # chain 1 starting value
  list(theta=.9)) # chain 2 starting value

# parameters to be monitored:
parameters <- c("theta")

# The following command calls Stan with specific options.
# For a detailed description type "?stan".
mod_fit <- stan(file="3_3_1.stan",
  data=stan_data,
  init=myinits, # If not specified, gives random inits)
```

```

pars=parameters,
iter=2000,
chains=2,
thin=1,
warmup=100, # Stands for burn-in; Default = iter/2
seed=123 # Setting seed; Default is random seed
)

```

4 Outputs

4.1 Model summary

In order of definition.

```

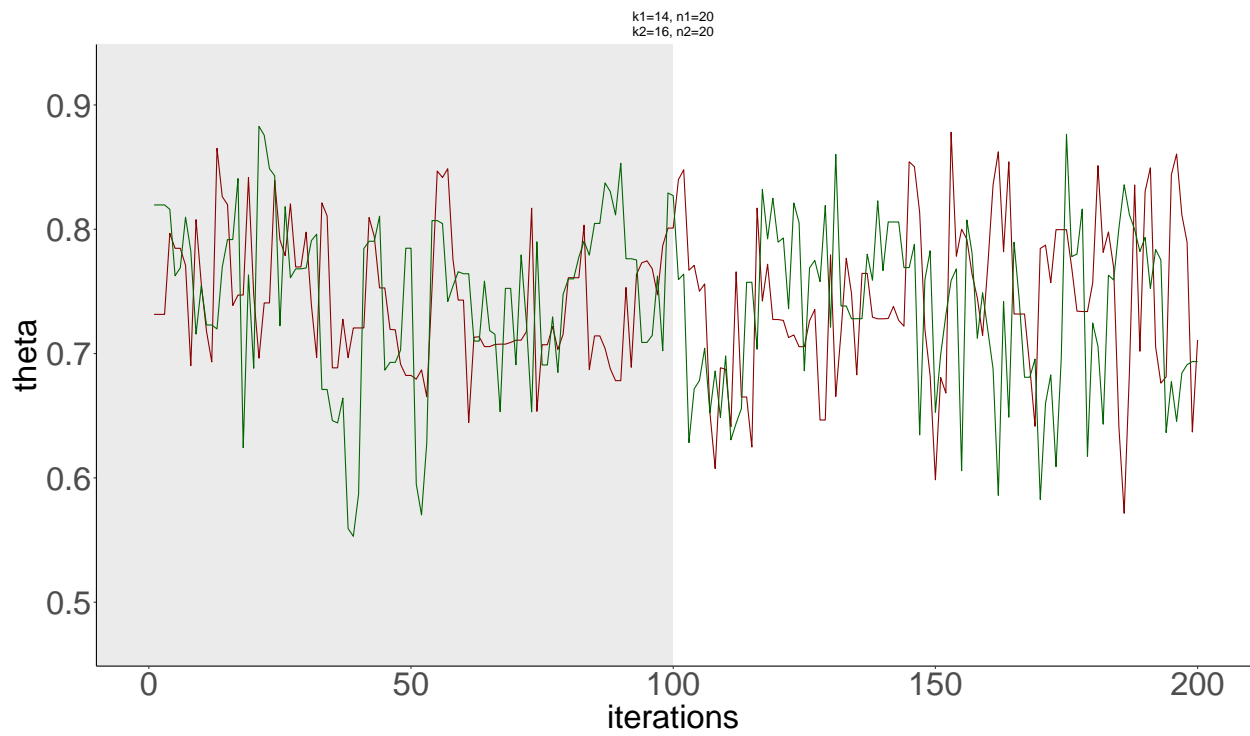
## Inference for Stan model: 3_3_1.
## 2 chains, each with iter=2000; warmup=100; thin=1;
## post-warmup draws per chain=1900, total post-warmup draws=3800.
##
##           mean se_mean   sd  2.5%   25%   50%   75%  97.5% n_eff Rhat
## theta    0.74     0.00 0.07   0.59   0.69   0.74   0.78   0.85  1633    1
## lp__   -24.66     0.02 0.70 -26.64 -24.83 -24.38 -24.20 -24.15  2083    1
##
## Samples were drawn using NUTS(diag_e) at Thu Nov 05 21:18:43 2020.
## For each parameter, n_eff is a crude measure of effective sample size,
## and Rhat is the potential scale reduction factor on split chains (at
## convergence, Rhat=1).

```

4.2 Plots

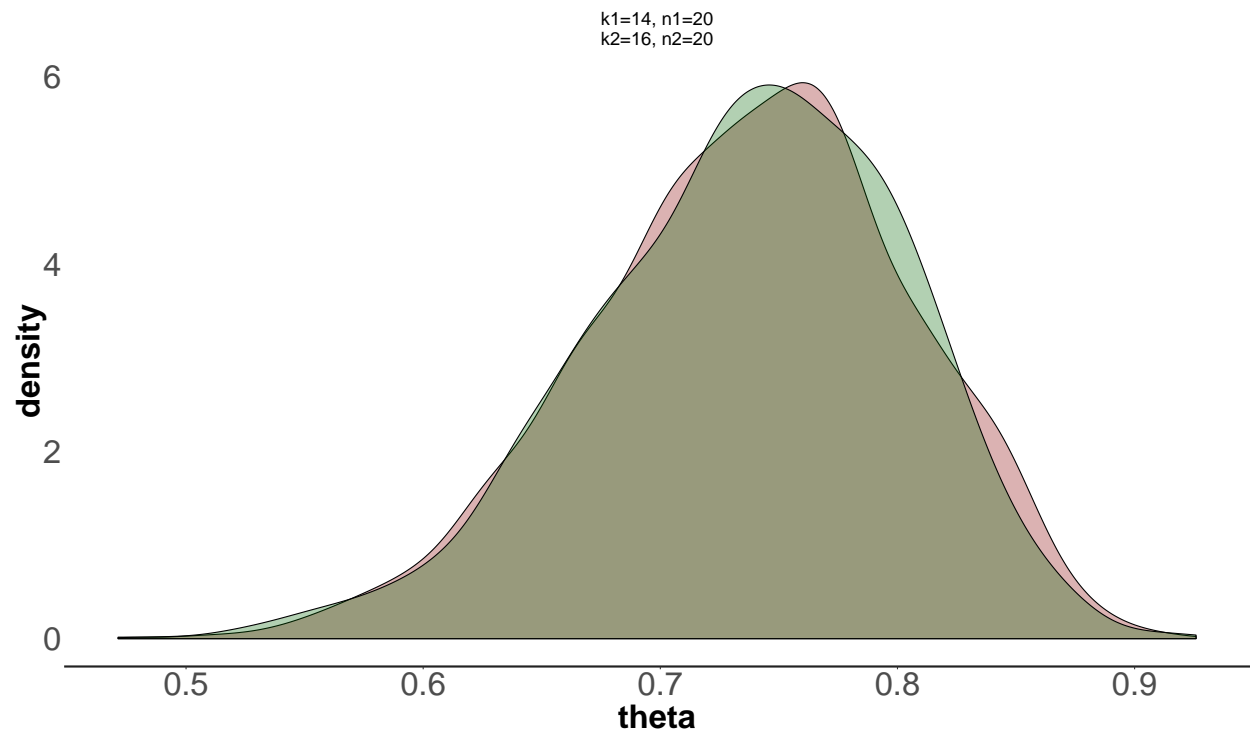
4.2.1 Plot (chains)

The initial movement of the chains are shown here (including the warmup phase). The two chains begin from the initial starting points of as defined in the input parameters of the stan model.



4.2.2 Plot (posterior)

The plot of the θ values per chain superimposed on each other.



4.3 Confidence interval value and the measures of central tendency

The confidence interval values.

```
## # Highest Density Interval
```

```
##
```

```
##      95% HDI
```

```
## [0.61, 0.86]
```

```
## # Equal-Tailed Interval
```

```
##
```

```
##      95% ETI
```

```
## [0.59, 0.85]
```

The mean, median and mode values respectively

```
## [1] 0.7366359 0.7412578 0.7801850
```