

## Lab 3

### Analysis of $d$ -ary heaps

A  $d$ -ary heap is like a binary heap, but (with one possible exception) non-leaf nodes have  $d$  children instead of 2 children.

1. How would you represent a  $d$ -ary heap in an array? (10%)
2. What is the height of a  $d$ -ary heap of  $n$  elements in terms of  $n$  and  $d$ ? (10%);
3. Given an efficient implementation of EXTRACT-MAX in a  $d$ -ary max-heap. Analyze its running time in terms of  $d$  and  $n$ . (20%);
4. Given an efficient implementation of INSERT in a  $d$ -ary max-heap. Analyze its running time in terms of  $d$  and  $n$ . (20%);
5. Give an efficient implementation of INCREASE-KEY( $A, i, k$ ), which first sets  $A[i]$  to  $\max(A[i], k)$  and then updates the  $d$ -ary max-heap structure appropriately. Analyze its running time in terms of  $d$  and  $n$ . (20%);
6. Document. (20%)