

Programming Assignment 11

Due at your recitation session on November 18-22

Reading

Read Chapter 6 in the textbook.

Programming

In this assignment, you will design classes to model *filters*, a basic concept in signal processing. A filter repeatedly takes an input value and produces an output value. In the simplest case (*scalar filters*), the inputs and outputs are doubles, but filters can operate on different types (double vectors are popular), and in fact the type of the input and of the output may differ. The simplest filter always produces as output the same value it has read as input:

Input	Output
3.	3.
0.	0.
-1.	-1.
2.	2.

More useful filters output the maximum, minimum, or the arithmetic mean of the input signal seen so far. The maximum and the minimum are defined according to some total order on the input values. These filters are useful to find extreme points in the signal (for example, the maximum round-trip time of a packet exchange over the Internet). The arithmetic mean filter is a scalar filter, and can be used to average a sequence of data readings.

Filters can support an optional reset operation. The reset uses a parameter of the same type as the input. The meaning of reset depends on the type of filter. For example, a max filter will return the maximum value seen since the last reset. In fact, max, min, and average filters come in two types:

- Filters that return the max, min, average input value since the beginning or since the last reset, whichever occurred last, and
- Filters that return the max, min, or average of the last N values (or less if less than N values are available since the beginning or the last reset).

For example,

Input	Reset	Max ∞	Max 3
-1		-1	-1
1		1	1
2		2	2
	0		
-1		0	0
3		3	3
1		3	3
2		3	3
1		3	2

A *filter cascade* is a filter that consists of a sequence of filters: a filter in the sequence takes its input from the output of the preceding filter. For example, the cascade of a max2 filter followed by a min3 filter are:

Input	Max2 Output	Cascade Output
-1	-1	-1
3	3	-1
1	3	-1
2	2	2
1	2	2

A cascade cannot be reset as a whole, but each individual filter can if the individual filter supports the reset operation.

A *scalar linear filter* is a scalar filter governed by:

$$y_i + a_1 y_{i-1} + a_2 y_{i-2} + \dots + a_M y_{i-M} = b_0 x_i + b_1 x_{i-1} + b_2 x_{i-2} + \dots + b_N x_{i-N}$$

where x_i is the i th value of the input, y_i is the i th value of the output, and the a_1, \dots, a_M and b_0, \dots, b_N are the filter parameters. A scalar filter can be reset to a value r , in which case the record of all of previous input values is set to r and the record of all previous output values is set to $r \left(\sum_{i=0}^N b_i \right) / \left(1 + \sum_{i=1}^M a_i \right)$ (can you see why?). If there are not enough inputs, the missing values of x and y are taken to be equal to their value as calculated during the last reset. If no reset ever occurred, the missing values are taken to be equal to 0. For example, if $M=N=1$, $a_1=.1$, $b_0=b_1=.5$, then

$$y_i = (x_i + x_{i-1}) / 2 - y_{i-1} / 10,$$

and so:

Input	Reset	Output
-1		-.5
1		.05
2		1.495
	0	
-1		-.5
3		1.05
1		1.895
2		1.3105
1		1.36895

Scalar filters have a wide range of applications: for example, they can be used to smooth out the input signal, or to remove a periodic carrier signal from the input, or to determine the signal trend.

An important type of linear filters is when $a_1=a_2=\dots=a_M=0$, which is called a *FIR filter*. A simple but useful case of a FIR filter always outputs the input multiplied by a constant factor: in this case, $b_1=b_2=\dots=b_N=0$ and b_0 is called the filter *gain*. Another useful FIR filter is the *binomial filter*, in which $b_i = \binom{N}{i}$ (binomial filters are often used to smooth out a window of data, for example in speech or image processing).

Your job is to create an object-oriented design for filters, which have been described above. Types of filters should be represented by classes, and commonality among filter types can be expressed through inheritance or containment. Submit a design documents that describes your architectural decisions. Implement classes, methods, pseudo-code, error-handling, and test cases to validate and improve your design. Create a filter.git repository where to submit your submission.

Discussion Guidelines

The class discussion will focus on class design.

Evaluation Guidelines

At this stage of the course, a more strict view will be taken of the following basic issues:

- Routines with McCabe's complexity exceeding 4
- Improperly named routines
- Repeated code