

$$\text{tol} = 0.000001$$

$$x_0 = 1$$

$$V = \frac{\pi h^2 (3r - h)}{3}$$

$$r = 1\text{m}, \quad V = 0.75\text{m}^3$$

$$f(h) = \frac{\pi h^2 (3r - h)}{3} - V$$

$$f'(h) = \frac{1}{3} [2\pi h (3r - h) + \pi h^2 (-1)] - 0$$

$$f'(h) = \frac{2\pi h (3r - h) - \pi h^2}{3} = \frac{6\pi h - 2\pi h^2}{3} = \frac{\pi}{3} (6h - 2h^2)$$

Newton:

iteración 1:

$$x_1 = x_0 - (f(x_0)/f'(x_0))$$

$$x_1 = 1 - (1.344395/\pi)$$

$$x_1 = 0.5720657$$

$$E = |x_0 - x_1| = 0.4279343$$

iteración 2:

$$x_2 = x_1 - (f(x_1)/f'(x_1))$$

$$x_2 = 0.5720657 - (0.08206521/2.566279)$$

$$x_2 = 0.5400874 \quad E = 0.0319783$$

iteración 3:

$$x_3 = 0.5400874 - (0.001408988/2.477084)$$

$$x_3 = 0.5395185$$

$$E = (0.5400874 - 0.5395185) = 0.0005689$$

iteración 4:

$$x_4 = 0.5395185 - (0.0000002433/2.780257)$$

$$x_4 = 0.5395184$$

$$E = |0.5395185 - 0.5395184| = 0.0000001 \quad \checkmark$$