## Exponents

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## Laws of Exponents:

Table 1: For  $a \neq 0$ ,  $b \neq 0$ 

Table 1: For $a \neq 0, b \neq 0$	
Product Rule	$a^x \cdot a^y = a^{x+y}$
Quotient Rule	$\frac{a^x}{a^y} = a^{x-y}$
Power Rule	$(a^x)^y = a^{xy}$
Power of a Product Rule	$(ab)^x = a^x b^x$
Power of a Fraction Rule	$\left(\frac{a}{b}\right)^x = \frac{a^x}{b^x}$
Zero Exponent	$a^0 = 1$
Negative Exponent	$a^{-x} = \frac{1}{a^x}$
Fractional Exponent	$a^{x/y} = \sqrt[y]{a^x}$

## Examples:

1. Write in  $\frac{3^3 \cdot 3^2 \cdot 3^{-1}}{3^6}$  in the simplest form.

$$\frac{3^3 \cdot 3^2 \cdot 3^{-1}}{3^6} = 3^{3+2-1-}$$

$$= 3^{-2}$$

$$= \frac{1}{3^2}$$

$$= \frac{1}{0}$$

2. Write in  $\frac{2^3(4\cdot 5)^3}{2^5\cdot 5^4}$  in the simplest form.

Solution:

$$\frac{2^{3}(4\cdot5)^{3}}{2^{5}\cdot5^{4}} = \frac{2^{3}\cdot4^{3}\cdot5^{3}}{2^{5}\cdot5^{4}}$$

$$= \frac{2^{3}\cdot(2^{2})^{3}\cdot5^{3}}{2^{5}\cdot5^{4}}$$

$$= \frac{2^{3}\cdot2^{6}\cdot5^{3}}{2^{5}\cdot5^{4}}$$

$$= 2^{3+6-5}\cdot5^{3-4}$$

$$= 2^{4}\cdot5^{-1}$$

$$= \frac{2^{4}}{5}$$

$$= \frac{16}{5}$$

3. Write in  $\frac{5^{2/3} \cdot 5^{1/4}}{5^{11/12}}$ 

Solution:

$$\begin{aligned} \frac{5^{2/3} \cdot 5^{1/4}}{5^{11/12}} &= 5^{2/3 + 1/4 - 11/12} \\ &= 5^{8/12 + 3/12 - 11/12} \\ &= 5^0 \\ &= 1 \end{aligned}$$