

- 10**    **(i)** Express  $x^2 - 2x - 15$  in the form  $(x + a)^2 + b$ . [2]

The function  $f$  is defined for  $p \leq x \leq q$ , where  $p$  and  $q$  are positive constants, by

$$f : x \mapsto x^2 - 2x - 15.$$

The range of  $f$  is given by  $c \leq f(x) \leq d$ , where  $c$  and  $d$  are constants.

- (ii)** State the smallest possible value of  $c$ . [1]

For the case where  $c = 9$  and  $d = 65$ ,

- (iii)** find  $p$  and  $q$ , [4]

- (iv)** find an expression for  $f^{-1}(x)$ . [3]