

4 Relative to an origin O , the position vectors of points A and B are given by

$$\overrightarrow{OA} = \mathbf{i} + 2\mathbf{j} \quad \text{and} \quad \overrightarrow{OB} = 4\mathbf{i} + p\mathbf{k}.$$

(i) In the case where $p = 6$, find the unit vector in the direction of \overrightarrow{AB} . [3]

(ii) Find the values of p for which angle $AOB = \cos^{-1} \left(\frac{1}{5} \right)$. [4]