

**10** Functions  $f$  and  $g$  are defined by

$$\begin{aligned} f : x &\mapsto 2x + 1, & x \in \mathbb{R}, \ x > 0, \\ g : x &\mapsto \frac{2x - 1}{x + 3}, & x \in \mathbb{R}, \ x \neq -3. \end{aligned}$$

- (i) Solve the equation  $gf(x) = x$ . [3]
- (ii) Express  $f^{-1}(x)$  and  $g^{-1}(x)$  in terms of  $x$ . [4]
- (iii) Show that the equation  $g^{-1}(x) = x$  has no solutions. [3]
- (iv) Sketch in a single diagram the graphs of  $y = f(x)$  and  $y = f^{-1}(x)$ , making clear the relationship between the graphs. [3]