

The diagram shows a sector OAB of a circle with centre O and radius r. Angle AOB is  $\theta$  radians. The point C on OA is such that BC is perpendicular to OA. The point D is on BC and the circular arc AD has centre C.

(i) Find 
$$AC$$
 in terms of  $r$  and  $\theta$ . [1]

(ii) Find the perimeter of the shaded region *ABD* when  $\theta = \frac{1}{3}\pi$  and r = 4, giving your answer as an exact value. [6]