

The diagram shows a triangular prism with a horizontal rectangular base ADFC, where CF = 12 units and DF = 6 units. The vertical ends ABC and DEF are isosceles triangles with AB = BC = 5 units. The mid-points of BE and DF are M and N respectively. The origin O is at the mid-point of AC.

Unit vectors i, j and k are parallel to OC, ON and OB respectively.

(i) Find the length of 
$$OB$$
. [1]

(ii) Express each of the vectors 
$$\overrightarrow{MC}$$
 and  $\overrightarrow{MN}$  in terms of i, j and k. [3]

(iii) Evaluate  $\overrightarrow{MC} \cdot \overrightarrow{MN}$  and hence find angle CMN, giving your answer correct to the nearest degree. [4]