

The diagram shows triangle OAB, in which the position vectors of A and B with respect to O are given by

$$\overrightarrow{OA} = 2\mathbf{i} + \mathbf{j} - 3\mathbf{k}$$
 and $\overrightarrow{OB} = -3\mathbf{i} + 2\mathbf{j} - 4\mathbf{k}$.

C is a point on \overrightarrow{OA} such that $\overrightarrow{OC} = p\overrightarrow{OA}$, where p is a constant.

(i) Find angle
$$AOB$$
. [4]

(ii) Find
$$\overrightarrow{BC}$$
 in terms of p and vectors \mathbf{i} , \mathbf{j} and \mathbf{k} . [1]

(iii) Find the value of p given that BC is perpendicular to OA. [4]