

In the diagram, AB is an arc of a circle, centre O and radius 6 cm, and angle  $AOB = \frac{1}{3}\pi$  radians. The line AX is a tangent to the circle at A, and OBX is a straight line.

(i) Show that the exact length of AX is  $6\sqrt{3}$  cm. [1]

Find, in terms of  $\pi$  and  $\sqrt{3}$ ,

- (ii) the area of the shaded region, [3]
- (iii) the perimeter of the shaded region. [4]