

The diagram shows a cuboid OABCDEFG with a horizontal base OABC in which OA = 4 cm and AB = 15 cm. The height OD of the cuboid is 2 cm. The point X on AB is such that AX = 5 cm and the point P on DG is such that DP = p cm, where P is a constant. Unit vectors \mathbf{i} , \mathbf{j} and \mathbf{k} are parallel to OA, OC and OD respectively.

- (i) Find the possible values of p such that angle $OPX = 90^{\circ}$. [4]
- (ii) For the case where p = 9, find the unit vector in the direction of \overrightarrow{XP} . [2]
- (iii) A point Q lies on the face CBFG and is such that XQ is parallel to AG. Find \overrightarrow{XQ} . [3]