



The diagram shows an open container constructed out of  $200 \text{ cm}^2$  of cardboard. The two vertical end pieces are isosceles triangles with sides  $5x \text{ cm}$ ,  $5x \text{ cm}$  and  $8x \text{ cm}$ , and the two side pieces are rectangles of length  $y \text{ cm}$  and width  $5x \text{ cm}$ , as shown. The open top is a horizontal rectangle.

(i) Show that  $y = \frac{200 - 24x^2}{10x}$ . [3]

(ii) Show that the volume,  $V \text{ cm}^3$ , of the container is given by  $V = 240x - 28.8x^3$ . [2]

Given that  $x$  can vary,

(iii) find the value of  $x$  for which  $V$  has a stationary value, [3]

(iv) determine whether it is a maximum or a minimum stationary value. [2]