

9 The functions f and g are defined for all real values of x by

$$f(x) = (3x-2)^2 + k \quad \text{and} \quad g(x) = 5x-1,$$

where k is a constant.

(a) Given that the range of the function gf is $gf(x) \geq 39$, find the value of k . [4]

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(b) For this value of k , determine the range of the function f_g . [2]

[illegible]

[illegible]

- (c) The function h is defined for all real values of x and is such that $gh(x) = 35x + 19$.

Find an expression for $g^{-1}(x)$ and hence, or otherwise, find an expression for $h(x)$. [3]

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