

In the diagram, ABC is a triangle in which AB = 4 cm, BC = 6 cm and angle $ABC = 150^{\circ}$. The line CX is perpendicular to the line ABX.

(i) Find the exact length of BX and show that angle
$$CAB = \tan^{-1} \left(\frac{3}{4 + 3\sqrt{3}} \right)$$
. [4]

(ii) Show that the exact length of
$$AC$$
 is $\sqrt{(52 + 24\sqrt{3})}$ cm. [2]