

- 9** Relative to an origin  $O$ , the position vectors of the points  $A$ ,  $B$ ,  $C$  and  $D$  are given by

$$\overrightarrow{OA} = \begin{pmatrix} 1 \\ 3 \\ -1 \end{pmatrix}, \quad \overrightarrow{OB} = \begin{pmatrix} 3 \\ -1 \\ 3 \end{pmatrix}, \quad \overrightarrow{OC} = \begin{pmatrix} 4 \\ 2 \\ p \end{pmatrix} \quad \text{and} \quad \overrightarrow{OD} = \begin{pmatrix} -1 \\ 0 \\ q \end{pmatrix},$$

where  $p$  and  $q$  are constants. Find

- (i) the unit vector in the direction of  $\overrightarrow{AB}$ , [3]
- (ii) the value of  $p$  for which angle  $AOC = 90^\circ$ , [3]
- (iii) the values of  $q$  for which the length of  $\overrightarrow{AD}$  is 7 units. [4]