

In the diagram, OAB is an isosceles triangle with OA = OB and angle $AOB = 2\theta$ radians. Arc PST has centre O and radius r, and the line ASB is a tangent to the arc PST at S.

- (i) Find the total area of the shaded regions in terms of r and θ . [4]
- (ii) In the case where $\theta = \frac{1}{3}\pi$ and r = 6, find the total perimeter of the shaded regions, leaving your answer in terms of $\sqrt{3}$ and π .