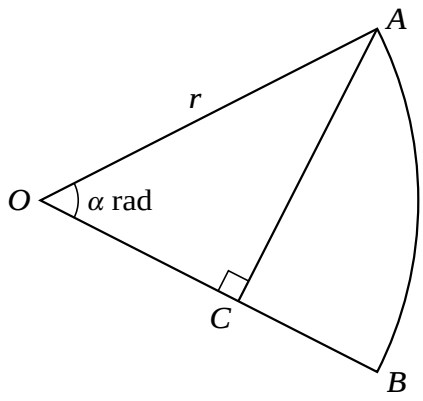
11



In the diagram, OAB is a sector of a circle with centre O and radius r. The point C on OB is such that angle ACO is a right angle. Angle AOB is α radians and is such that AC divides the sector into two regions of equal area.

(i) Show that $\sin\alpha\cos\alpha = \frac{1}{2}\alpha$. [4]

It is given that the solution of the equation in part **(i)** is $\alpha = 0.9477$, correct to 4 decimal places.

(ii) Find the ratio

perimeter of region OAC : perimeter of region ACB,

giving your answer in the form k : 1, where k is given correct to 1 decimal place. [5]

(iii) Find angle AOB in degrees. [1]