

**Assignment 5**  
**Computer Vision**  
**CS 559**  
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**Problem 1:** Suppose that the boundary of a closed region is represented by a 4-directional chain code. Write a function `Area(ChainCode)` in pseudo-code to compute the area of the region from its chain code representation.

Notice, we can find the area enclosed by a chain code using the area of a polyline:

$$A = \frac{1}{2} \sum_{i=0}^{n-1} (x[i+1]y[i] - x[i]y[i+1])$$

Now we can let the following:

- (i) Let the starting point be notated as  $(x_0, y_0) = (0, 0)$
- (ii) Let 1 be up, 2 be left, 3 be down, and 0 be right
- (iii) Let `ChainCode` be an array consisting of the following numbers:  $\{0, 1, 2, 3\}$

Notice the code below:

```
1 function A = Area(ChainCode)
2
3     xarr = zeros(length(ChainCode) + 1);
4     yarr = zeros(length(ChainCode) + 1);
5
6     % convert ChainCode into polyline
7     x = 0; y = 0;
8     pointIndex = 2;
9     for i = 1 : length(ChainCode)
10         if (ChainCode(i) == 1), y = y + 1;
11         elseif (ChainCode(i) == 2), x = x - 1;
12         elseif (ChainCode(i) == 3), y = y - 1;
13         elseif (ChainCode(i) == 0), x = x + 1;
14         end
15         xarr(pointIndex) = x;
16         yarr(pointIndex) = y;
17         pointIndex = pointIndex + 1;
18     end
19
20     % Shoelace Formula
21     sum = 0;
22     for i = 1 : length(ChainCode)
23         sum = sum + ((xarr(i + 1) * yarr(i)) - (xarr(i) * yarr(i + 1)));
24     end
25     A = abs(sum) / 2;
26
27 end
```

**Problem 2:** Show that the area enclosed by the polyline  $(x_0, y_0), (x_1, y_1), \dots, (x_{n-1}, y_{n-1}), (x_0, y_0)$  is given by

$$A = \frac{1}{2} \sum_{i=0}^{n-1} (x[i+1]y[i] - x[i]y[i+1])$$

*Proof.* Notice, we can take the area of any simple closed loop from the following equation:

$$A = \iint_D dA = \iint_D \left( \frac{dQ}{dx} - \frac{dP}{dy} \right) dA, \quad \text{with } \left( \frac{dQ}{dx} - \frac{dP}{dy} \right) = 1$$

Let the following be true:

$$\frac{dQ}{dx} = \frac{1}{2}, \quad Q = \frac{1}{2}x, \quad \frac{dP}{dy} = \frac{-1}{2}, \quad P = \frac{-1}{2}y$$

Now we can use Green's theorem to say the following:

$$A = \iint_D \left( \frac{dQ}{dx} - \frac{dP}{dy} \right) dA = \oint_C Q dy + P dx = \oint_C \frac{1}{2}x dy - \frac{1}{2}y dx = \frac{1}{2} \oint_C x dy - y dx$$

We now take two points  $(x_0, y_0), (x_1, y_1)$ . We can parameterize the line segment between the two points into:

$$\vec{r}(t) = \langle (1-t)x_0 + tx_1, (1-t)y_0 + ty_1 \rangle$$

Notice the line integral between two points from the following equation:

$$\begin{aligned} \oint_C x dy - y dx &= \int_{t=0}^{t=1} ((1-t)x_0 + tx_1)(-y_0 + y_1) - ((1-t)y_0 + ty_1)(-x_0 + x_1) \\ &= \int_{t=0}^{t=1} -(1-t)x_0y_0 + (1-t)x_0y_1 - tx_1y_0 + tx_1y_1 \\ &\quad + (1-t)x_0y_0 - (1-t)x_1y_0 + tx_0y_1 - tx_1y_1 \\ &= \int_{t=0}^{t=1} (1-t)x_0y_1 - tx_1y_0 - (1-t)x_1y_0 + tx_0y_1 \\ &= tx_0y_1 - \frac{t^2}{2}x_0y_1 - \frac{t^2}{2}x_1y_0 - tx_1y_0 + \frac{t^2}{2}x_1y_0 + \frac{t^2}{2}x_0y_1 \Bigg|_{t=0}^{t=1} \\ &= tx_0y_1 - tx_1y_0 \Bigg|_{t=0}^{t=1} \\ &= -(x_1y_0 - x_0y_1) \end{aligned}$$

Because when parametrizing with  $\vec{r}(t)$ , we have that integral is taken in the counter clockwise order, however, the vertices are read in clockwise order in the shoelace formula, so we get:

$$\oint_C x dy - y dx = - \oint_C x dy - y dx = x_1y_0 - x_0y_1$$

Now we get the following:

$$A = \frac{1}{2} \oint_C x dy - y dx = \frac{1}{2} \sum_{i=0}^{n-1} \oint_{C_i} x dy - y dx = \frac{1}{2} \sum_{i=0}^{n-1} (x_{i+1}y_i - x_iy_{i+1}) = \frac{1}{2} \sum_{i=0}^{n-1} (x[i+1]y[i] - x[i]y[i+1])$$

where  $C_i$  for  $i \in \{0, 1, 2, \dots, n-2, n-1\}$  are the line segments between each vertex  $(x_0, y_0), (x_1, y_1), \dots, (x_{n-1}, y_{n-1}), (x_n = x_0, y_n = y_0)$

□

**Problem 3:** Compare Hough transform and Canny edge detection for region detection in terms of (i) robustness (insensitivity) to noise, (ii) detection of regions with irregular shape, (iii) any common technique that is used both methods.

- (i) robustness (insensitivity) to noise

When it comes to noise, the Canny edge detector uses a Gaussian filter to remove as much noise as possible. The noise reduction however can create disconnections of the edges so the edge detector uses a low and high threshold to refill the disconnections created. If a certain pixel is in between the thresholds, it checks if the neighbor pixels have a high magnitude and if so, it makes it white, or makes it an edge pixel, otherwise it makes it black.

When it comes to noise, the Hough Transform uses an accumulator array. For noise reduction, neighbor elements in the accumulator array are increased.

- (ii) detection of regions with irregular shape

When it comes to detection of regions with irregular shape, the Canny edge detector will have some trouble. Because the detector is dependent on the neighboring pixels, an irregular shape will show irregular neighborhoods, which will make edge detection a lot harder.

When it comes to detection of regions with irregular shape, the shape shouldn't matter with the Hough transform, because it simply takes in all the pixels and transforms it to a polar plane. Here the detection is not dependent on the shape, just simply the pixel coordinates or locations.

- (iii) any common technique that is used both methods

A common technique both share is that they both find the edges so that they can create a region to search and group. This will make separating regions much easier.

**Problem 4:**

- (a) Compare three losses compressions techniques in terms of their suitability for natural images.

Notice the following three losses compressions techniques and their compression ratios for natural images:

- (a) Delta / Differential Coding - 1.8 : 1 ratio
  - (b) Run Length Encoding - 1.1 : 1 ratio
  - (c) Huffman Coding - 1.6 : 1 ratio
- (b) Explain which lossless compression technique use variable code length. Which technique results in the optimal code length?

The Huffman Coding lossless compression technique uses variable code length. This is because in this technique, the codewords are chosen such that  $L_{ave}$  is as close as possible to  $E$ , the measure for average number of bits per pixels. Allowing us to choose our codewords giving us a variable code length. Also because of this variable code length, we can make the code have a minimal code length this resulting in the optimal code length.

**Problem 5:** Consider the 8 by 8 subimage

$$f(x, y) = \begin{bmatrix} 56 & 45 & 51 & 66 & 70 & 61 & 64 & 73 \\ 63 & 59 & 56 & 90 & 109 & 85 & 69 & 72 \\ 62 & 59 & 68 & 103 & 144 & 104 & 66 & 73 \\ 63 & 58 & 71 & 132 & 134 & 106 & 70 & 69 \\ 65 & 61 & 68 & 114 & 116 & 82 & 68 & 70 \\ 79 & 65 & 60 & 67 & 77 & 68 & 58 & 75 \\ 85 & 71 & 54 & 59 & 55 & 61 & 65 & 73 \\ 87 & 79 & 69 & 58 & 65 & 66 & 78 & 94 \end{bmatrix}$$

Apply the JPEG compression algorithm and find and report the 1-D coefficient sequence.

Notice the intermediate steps:

$$\bar{f} = f - 128 = \begin{bmatrix} -72 & -83 & -77 & -62 & -58 & -67 & -64 & -55 \\ -65 & -69 & -72 & -38 & -19 & -43 & -59 & -56 \\ -66 & -69 & -60 & -25 & 16 & -24 & -62 & -55 \\ -65 & -70 & -57 & 4 & 6 & -22 & -58 & -59 \\ -63 & -67 & -60 & -14 & -12 & -46 & -60 & -58 \\ -49 & -63 & -68 & -61 & -51 & -60 & -70 & -53 \\ -43 & -57 & -74 & -69 & -73 & -67 & -63 & -55 \\ -41 & -49 & -59 & -70 & -63 & -62 & -50 & -34 \end{bmatrix}$$

$$\bar{C}(u, v) = \begin{bmatrix} -426.125 & -28.938 & -55.423 & 27.216 & 56.625 & -13.318 & -4.779 & -3.264 \\ 7.489 & -26.110 & -60.683 & 11.661 & 15.989 & -4.170 & -3.059 & 1.695 \\ -50.180 & 4.038 & 77.060 & -12.952 & -23.200 & 2.573 & 3.456 & 6.595 \\ -47.261 & 9.686 & 29.100 & -11.038 & -4.090 & 10.161 & 0.527 & -2.266 \\ 9.375 & -6.109 & -9.619 & -12.588 & 2.125 & 11.001 & -2.645 & -3.143 \\ -11.518 & 1.983 & 1.988 & 2.034 & -2.147 & 5.493 & 4.075 & -5.367 \\ -1.268 & -3.184 & 5.206 & -0.291 & -0.808 & -10.021 & 7.940 & 9.357 \\ -2.772 & -0.432 & -3.038 & -0.277 & 1.154 & -2.056 & -3.032 & 4.655 \end{bmatrix}$$

$$C_q(u, v) = \begin{bmatrix} -27 & -3 & -6 & 2 & 2 & 0 & 0 & 0 \\ 1 & -2 & -4 & 1 & 1 & 0 & 0 & 0 \\ -4 & 0 & 5 & -1 & -1 & 0 & 0 & 0 \\ -3 & 1 & 1 & 0 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{bmatrix}$$

$$C_{q\{1D\}} = \begin{bmatrix} -27 & -3 & 1 & -4 & -2 & -6 & 2 & -4 & 0 & \dots \\ -3 & 1 & 1 & 5 & 1 & 2 & 0 & 1 & -1 & \dots \\ 1 & 0 & 0 & 0 & 0 & 0 & 0 & -1 & \text{EOB} \end{bmatrix}$$

```

1 % Quantization Table
2 q = [16 11 10 16 24 40 51 61;
3 12 12 14 19 26 58 60 55;
4 14 13 16 24 40 57 69 56;
5 14 17 22 29 51 87 80 62;
6 18 22 37 56 68 109 103 77;
7 24 35 55 64 81 104 113 92;
8 49 64 78 87 103 121 120 101;
9 72 92 95 98 112 100 103 99;];
10
11 % Given Matrix
12 f = [56 45 51 66 70 61 64 73 ;
13 63 59 56 90 109 85 69 72 ;
14 62 59 68 103 144 104 66 73 ;
15 63 58 71 132 134 106 70 69 ;
16 65 61 68 114 116 82 68 70 ;
17 79 65 60 67 77 68 58 75 ;
18 85 71 54 59 55 61 65 73 ;
19 87 79 69 58 65 66 78 94];
20
21 % Step 1: bar{f} = f - 128
22 fb = f - 128;
23
24 % Step 2: Use DCT to get bar{C}
25 n = 8; Cb = zeros(8,8);
26 for u = 0 : (n - 1)
27     for v = 0 : (n - 1)
28         if (u == 0), a = sqrt(1 / n);
29         else, a = sqrt(2 / n); end
30
31         if (v == 0), b = sqrt(1 / n);
32         else, b = sqrt(2 / n); end
33
34         sum = 0;
35         for x = 0 : (n - 1)
36             for y = 0 : (n - 1)
37                 sum = sum + fb((x + 1), (y + 1))*cos((pi * (2*x + 1)* u) / (2*n)) * ...
38                 cos((pi * (2*y + 1)* v) / (2*n));
39             end
40         end
41
42         Cb((u + 1), (v + 1)) = a*b*sum;
43     end
44 end
45
46 % Step 3: Quantize bar{C}
47 Cq = round( Cb ./ q);

```

```

1 % Step 4: Arrange into 1D sequence in zig zag order
2 Cq1 = zeros(1,64);
3
4 i = 1; x = 1; y = 1; % Start
5 Cq1(i) = Cq(x, y);
6 i = i + 1; y = y + 1; % Right
7 while (i <= 64 )
8     while (x >= 1 && y >= 1 && x <= 8 && y <= 8)
9         Cq1(i) = Cq(x,y);
10        i = i + 1;
11        x = x + 1; % Down
12        y = y - 1; % Left
13    end
14    if (x > 8)
15        x = x - 1; % Up
16        y = y + 1; % Right
17    end
18    y = y + 1; % Right
19    while (x >= 1 && y >= 1 && x <= 8 && y <= 8)
20        Cq1(i) = Cq(x,y);
21        i = i + 1;
22        x = x - 1; % Up
23        y = y + 1; % Right
24    end
25    if (y > 8)
26        x = x + 1; % Down
27        y = y - 1; % Left
28    end
29    x = x + 1; % Down
30 end
31
32 % Remove trailing zeros
33 len = 64;
34 while (Cq1(len) == 0)
35     len = len - 1;
36 end
37
38 Cq1 = Cq1(1 : len);

```

**Problem 6 (All Code on Last Pages):** Use the region growing function (next page) to detect:

- (a) The red, blue, green regions in the ThreeRegions image by planting one seed in each region simultaneously. You must run the program only once to detect all three regions. This requires just a little modification to the attached function.

For this, I simply modified the code such that it takes in a colored image, 3 seeds, and 3 maximum region distances.



- (b) Determine the centroid, area, and circularity of the regions detected in (a)

For the area, I simply added the red, green, and blue components to get a single black and white matrix. Because this matrix consisted of all 1's and 0's, I added the values of each pixel to count the number of pixels in the region as pixels in the region will be valued at 1 and 0 otherwise.

Area:  $A = 15246$

For the centroid, I got the following:

$$x_c = \frac{1}{A} \sum_{x=0}^{w-1} \sum_{y=0}^{h-1} x f(x, y) = 183.35 \quad y_c = \frac{1}{A} \sum_{x=0}^{w-1} \sum_{y=0}^{h-1} y f(x, y) = 149.63$$

For the circularity, I got all the boundary points by using the canny edge detection. Then I stored the location of all the pixels with values of 1 as they are the edge points. Then I found the distance from each point to the centroid to get  $d_i$ . Then I took the mean to get  $d_{ave}$ . From there, I took the standard deviation to get  $\sigma$ .

$$d_{ave} = \frac{1}{m} \sum_{i=0}^{m-1} d_i = 61.35, \quad \sigma = \sqrt{\sum_{i=0}^{m-1} (d_i - d_{ave})^2} = 605569.1$$



- (c) Detect the boundary of the region containing the red beans that are located in the center of the Beans image. Note that function does not know the location of beans, and only know the features of a single bean, say color and shape of it. This will need some modification to the function.

For this, I simply inputted a RGB color matrix, *ie* [.64 .27 .29], and looped through the program to find that color. Once found, that pixel would be the seed and it would run like part (a).



- (d) Find the minimum distance between regions containing the red beans and the yellow ( in the upper right corner) of the image. Again the function does not know the locations of these two regions.

After finding the circle boundaries over each bean pile found using the function from part (c), I now have the center and radius of each circle.

Notice the following:

$$C_1 = (201.4, 115.6), \quad C_2 = (356.1, 36.6), \quad r_1 = 32.1, \quad r_2 = 33.4$$

To get the minimum distance, all we need to do is take the distance between the centers and subtract the two radii. Notice the following:

$$\begin{aligned} d_{\min} &= \sqrt{(x_{C_2} - x_{C_1})^2 + (y_{C_2} - y_{C_1})^2} - (r_1 + r_2) \\ &= \sqrt{(356.1 - 201.4)^2 + (36.6 - 115.6)^2} - (32.1 + 33.4) \\ &= 108.1923 \text{ pixels} \end{aligned}$$



```

1 function J = regiongrowing(I,x,y,reg_maxdist)
2 %
3 % This function performs "region growing" in an image from a specified
4 % seedpoint (x,y)
5 %
6 % J = regiongrowing(I,x,y,t)
7 %
8 % I : input image
9 % J : logical output image of region
10 % x,y : the position of the seedpoint (if not given uses function getpts)
11 % t : maximum intensity distance (defaults to 0.2)
12 %
13 % The region is iteratively grown by comparing
14 % all unallocated neighbouring pixels to the region.
15 % The difference between a pixel's intensity value and the region's mean,
16 % is used as a measure of similarity. The pixel with the smallest difference
17 % measured this way is allocated to the respective region.
18 % This process stops when the intensity difference between region mean and
19 % new pixel become larger than a certain threshold (t)
20 %
21 % Example:
22 %
23 % I = im2double(imread('medtest.png'));
24 % x = 198; y = 359;
25 % J = regiongrowing(I,x,y,0.2);
26 % figure, imshow(I+J);
27 %
28 % Author: D. Kroon, University of Twente
29 %
30
31 if(exist('reg_maxdist','var') == 0)
32     reg_maxdist = 0.2;
33 end
34
35 if(exist('y','var') == 0)
36     figure, imshow(I,[]);
37     [y,x] = getpts;
38     y = round(y(1)); x = round(x(1));
39 end
40
41 J = zeros(size(I));      % Output
42 Isizes = size(I);        % Dimensions of input image
43 reg_mean = I(x,y);       % The mean of the segmented region
44 reg_size = 1;            % Number of pixels in region
45
46 % Free memory to store neighbours of the (segmented) region
47 neg_free = 10000; neg_pos=0;
48 neg_list = zeros(neg_free,3);
49 pixdist = 0; % Distance of the region newest pixel to the regio mean
50
51 % Neighbor locations (footprint)
52 neighb = [-1 0; 1 0; 0 -1;0 1];

```

```

1 % Start regiogrowing until distance between regio and possible new pixels
2 % become higher than a certain threshold
3 while(pixdist < reg_maxdist && reg_size < numel(I))
4
5     % Add new neighbors pixels
6     for j = 1 : 4
7         % Calculate the neighbour coordinate
8         xn = x + neighb(j,1); yn = y +neighb(j,2);
9
10        % Check if neighbour is inside or outside the image
11        ins = (xn >= 1) && (yn >= 1) && (xn <= Isizes(1)) && (yn <= Isizes(2));
12
13        % Add neighbor if inside and not already part of the segmented area
14        if(ins && (J(xn,yn) == 0))
15            neg_pos = neg_pos+1;
16            neg_list(neg_pos,:) = [xn yn I(xn,yn)]; J(xn,yn)=1;
17        end
18    end
19
20    % Add a new block of free memory
21    if(neg_pos + 10 > neg_free)
22        neg_free = neg_free + 10000;
23        neg_list((neg_pos + 1):neg_free , :) = 0;
24    end
25
26    % Add pixel with intensity nearest to the mean of the region, to the
    region
27    dist = abs(neg_list(1:neg_pos,3) - reg_mean);
28    [pixdist, index] = min(dist);
29    J(x,y) = 2; reg_size = reg_size + 1;
30
31    % Calculate the new mean of the region
32    reg_mean = ( reg_mean*reg_size + neg_list(index,3) ) /(reg_size+1);
33
34    % Save the x and y coordinates of the pixel (for the neighbour add
    proccess)
35    x = neg_list(index,1); y = neg_list(index,2);
36
37    % Remove the pixel from the neighbour (check) list
38    neg_list(index,:) = neg_list(neg_pos,:);
39    neg_pos = neg_pos-1;
40 end
41
42 % Return the segmented area as logical matrix
43 J = J > 1;
44 end

```

```
1   close all;
2   clear all;
3
4   % Problem 6a
5   I1 = im2double(imread('../Figures/ThreeRegions.jpg'));
6   xarr = [180 180 180];
7   yarr = [125 175 215];
8   reg_maxdist = [0.0485 0.2 0.15];
9
10  J1 = Prob6a(I1,xarr,yarr,reg_maxdist);
11  figure(), imshow(J1)
12  bw = J1(:, :, 1) + J1(:, :, 2) + J1(:, :, 3);
13  figure(), imshow(bw)
14
15
16
17  % Problem 6b
18  Area = sum(bw(:, :), 'all');
19
20  sumsx = 0; sumsy = 0;
21  for x = 0 : size(J1,1) - 1
22      for y = 0 : size(J1,2) - 1
23          sumsx = sumsx + x*bw(x+1,y+1);
24          sumsy = sumsy + y*bw(x+1,y+1);
25      end
26  end
27  xc = (1 / Area) * sumsx;
28  yc = (1 / Area) * sumsy;
29  centroid = [xc, yc];
30
31  bound = edge(bw, 'canny');
32  figure(), imshow(bound)
33  points = zeros(Area,3); i = 1;
34  for x = 1 : size(bound,1)
35      for y = 1 : size(bound,2)
36          if (bound(x,y) == 1)
37              points(i,1) = x;
38              points(i,2) = y;
39              points(i,3) = sqrt( ((x - xc)^2) + ((y - yc)^2) );
40              i = i + 1;
41          end
42      end
43  end
44  points = points(1:i,:);
45  dave = sum(points(:,3)) / size(points,1);
46
47  circ = 0;
48  for i = 1 : size(points,1)
49      circ = circ + ((points(i,3) - dave)^2);
50  end
51
```

```
52
53 % Problem 6c
54 I2 = imresize(im2double(imread('../Figures/Beans.jpg')), 1 / 3);
55 color = [.64 .27 .29];
56 reg_maxdist = [0.14 0.12 0.13];
57 J2 = Prob6c(I2,color,reg_maxdist);
58
59 A = edge(rgb2gray(J2), 'canny');
60 [center1, radius1] = imfindcircles(A, [15 50]);
61
62 figure(), imshow(I2)
63 viscircles(center1, radius1,'EdgeColor','r');
64
65
66
67 % Problem 6d
68 color = [.97 .81 .31];
69 reg_maxdist = [0.005 0.3 0.3];
70 J = Prob6c(I2,color,reg_maxdist);
71
72 A = edge(rgb2gray(J), 'canny');
73 [center2, radius2] = imfindcircles(A, [20 100]);
74
75 figure(), imshow(I2)
76 viscircles(center1, radius1,'EdgeColor','r');
77 viscircles(center2, radius2,'EdgeColor','r');
78 line([center1(1) center2(1)], [center1(2), center2(2)],...
79     'linewidth', 2 , 'color', 'red');
80
81 d = sqrt( ((center2(1) - center1(1))^2) + ((center2(2) - center1(2))^2) ) ...
82     - (radius1 + radius2);
83
84
```

```
1 function J = Prob6a(I,xarr,yarr,reg_maxdist)
2
3     J = zeros(size(I)); % output
4     Isizes = size(I); % sizes of image
5     for i = 1 : size(I,3)
6         x = xarr(i);
7         y = yarr(i);
8         neg_free = 10000; % for neighbor list
9         neg_pos = 0; % position of neighbor, and also number of neighbors
10        neg_list = zeros(neg_free,3); % holds all the neighbor information
11        neigb = [-1 0; 1 0; 0 -1; 0 1]; % used for finding 4 direction neighbor
12        pixdist = 0;
13        reg_mean = I(x,y,i);
14        reg_size = 1;
15
16        % checks whether pixdist isn't bigger than the max region distance
17        % checks whether the region isn't bigger than the image
18
19        % if pixdist > reg_maxdist then no neihgbors are similar to region
20        while (pixdist < reg_maxdist(i) && reg_size < numel(I(:,:,i)))
21
22            % finds the 4 neighbors of pixel and adds to neighbor list
23            for j = 1 : 4
24                % j = 1, it goes to the left neighbor
25                % j = 2, it goes to the right neighbor
26                % j = 3, it goes to the up neighbor
27                % j = 4, it goes to the down neighbor
28                % (xn , yn) - neighbor pixel that we working with
29                xn = x + neigb(j,1);
30                yn = y + neigb(j,2);
31
32                % is (xn,yn) within the image boundarys 1 < xn, yn < dim(image)
33                ins = (xn >= 1) && (yn >= 1) && (xn <= Isizes(1)) && ...
34                    (yn <= Isizes(2));
35
36                % checks if inside image, then checks if neighbor pixel wasn't
37                % already counted as a neighbor
38                if (ins && (J(xn,yn,i) == 0))
39                    neg_pos = neg_pos + 1; % increment neighbor
40                    % saves neighbor location and data
41                    neg_list(neg_pos, :) = [xn yn I(xn, yn,i)];
42                    J(xn, yn,i) = 1; % notes as neighbor
43                end
44            end
45
46            % Make neighbor list bigger if needed;
47            if (neg_pos + 10 > neg_free)
48                neg_free = neg_free + 10000;
49                neg_list( (neg_pos + 1) : neg_free, :) = 0;
50            end
51        end
52    end
```

```
52         % dist finds distance between the neighbor and the mean
53         dist = abs( neg_list(1: neg_pos,3) - reg_mean ) ;
54
55         % pixdist is the smallest distance from one neighbor to the mean
56         % index is the index of the neighbor that has the smallest distance
57         % from the mean
58         [pixdist, index] = min(dist);
59
60         % Path which the algorithm goes is the path of 2s
61         J(x,y,i) = 2;
62         % increments region size
63         reg_size = reg_size + 1;
64
65         % mean = (mean * reg_size + closest neighbor value) / (reg_size + 1)
66         reg_mean = (reg_mean * reg_size + neg_list(index,3))/(reg_size+1);
67
68         % restarts except starts with closest neighbor
69         x = neg_list(index,1);
70         y = neg_list(index,2);
71
72         % replaces the closest neighbor with the last neighbor
73         neg_list(index,:) = neg_list(neg_pos,:);
74
75         % decrements neg_pos so the last neighbor gets overwritten
76         neg_pos = neg_pos-1;
77     end
78
79     % converts path of 2's into path of 1's and everything else is 0
80     J(:, :, i) = J(:, :, i) > 1;
81 end
82 end
```

```

1 function [J, center1, radius1] = Prob6c(I,color,reg_maxdist)
2
3     xarr = [0 0 0];
4     yarr = [0 0 0];
5
6     for i = 1 : size(I,1)
7         for j = 1 : size(I,2)
8             if ( abs(color(1) - I(i,j,1)) <= .02 && ...
9                 abs(color(2) - I(i,j,2)) <= .02 && ...
10                 abs(color(3) - I(i,j,3)) <= .02 )
11                 xarr = [i i i];
12                 yarr = [j j j];
13                 break;
14             end
15         end
16         if (xarr(1) ~= 0)
17             break;
18         end
19     end
20
21     J = zeros(size(I)); % output
22     Isizes = size(I); % sizes of image
23     for i = 1 : size(I,3)
24         x = xarr(i);
25         y = yarr(i);
26         neg_free = 10000; % for neighbor list
27         neg_pos = 0; % position of neighbor, and also number of neighbors
28         neg_list = zeros(neg_free,3); % holds all the neighbor information
29         neighb = [-1 0; 1 0; 0 -1; 0 1]; % used for finding 4 direction neighbor
30         pixdist = 0;
31         reg_mean = I(x,y,i);
32         reg_size = 1;
33
34         % checks whether pixdist isn't bigger than the max region distance
35         % checks whether the region isn't bigger than the image
36
37         % if pixdist > reg_maxdist then no neighbors are similar to region
38         while (pixdist < reg_maxdist(i) && reg_size < numel(I(:, :, i)))
39
40             % finds the 4 neighbors of pixel and adds to neighbor list
41             for j = 1 : 4
42                 % j = 1, it goes to the left neighbor
43                 % j = 2, it goes to the right neighbor
44                 % j = 3, it goes to the up neighbor
45                 % j = 4, it goes to the down neighbor
46                 % (xn , yn) - neighbor pixel that we working with
47                 xn = x + neighb(j,1);
48                 yn = y + neighb(j,2);
49
50                 % is (xn,yn) within the image boundarys 1 < xn, yn < dim(image)

```



```
52         ins = (xn >= 1) && (yn >= 1) && (xn <= Isizes(1)) && ...
53             (yn <= Isizes(2));
54
55         % checks if inside image, then checks if neighbor pixel wasn't
56         % already counted as a neighbor
57         if (ins && (J(xn,yn,i) == 0))
58             neg_pos = neg_pos + 1; % increment neighbor
59             % saves neighbor location and data
60             neg_list(neg_pos, :) = [xn yn I(xn, yn,i)];
61             J(xn, yn,i) = 1; % notes as neighbor
62         end
63     end
64
65     % Make neighbor list bigger if needed;
66     if (neg_pos + 10 > neg_free)
67         neg_free = neg_free + 10000;
68         neg_list( (neg_pos + 1) : neg_free, :) = 0;
69     end
70
71     % dist finds distance between the neighbor and the mean
72     dist = abs( neg_list(1: neg_pos,3) - reg_mean ) ;
73
74     % pixdist is the smallest distance from one neighbor to the mean
75     % index is the index of the neighbor that has the smallest distance
76     % from the mean
77     [pixdist, index] = min(dist);
78
79     % Path which the algorithm goes is the path of 2s
80     J(x,y,i) = 2;
81     % increments region size
82     reg_size = reg_size + 1;
83
84     % mean = (mean * reg_size + closest neighbor value) / (reg_size + 1)
85     reg_mean = (reg_mean * reg_size + neg_list(index,3))/(reg_size+1);
86
87     % restarts except starts with closest neighbor
88     x = neg_list(index,1);
89     y = neg_list(index,2);
90
91     % replaces the closest neighbor with the last neighbor
92     neg_list(index,:) = neg_list(neg_pos,:);
93
94     % decrements neg_pos so the last neighbor gets overwritten
95     neg_pos = neg_pos-1;
96 end
97
98 % converts path of 2's into path of 1's and everything else is 0
99 J(:, :, i) = J(:, :, i) > 1;
100 end
101 end
```