

Final
Algebraic Coding Theory
Math 525
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Problem 5: Let β be a primitive element of $\text{GF}(2^8)$, the finite field with 256 elements. Determine the minimum distance of the cyclic code of length 255 over $\text{GF}(2^8)$ generated by $g(x) = (x + \beta)(x + \beta^{18})$.

From here, we can see that the generator polynomial has 2 roots, β and β^{18} . We also know that because it is a BCH code it will correct up to 2 errors in a $n = 255$ digit block. Thus, we get that the minimum distance is 5