Exam 1 Algebraic Coding Theory Math 525 Stephen Giang RedID: 823184070

Problem 3:

(a) An error pattern of weight d that C does not detect.

Given that C is defined as below:

$$C = \{001100, 110111, 011001, 100010\}$$

I was able to see the distance from u = 001100 to v = 011001 was d(u, v) = 3. There is an error pattern e of weight d that can be defined as below:

$$e = u + w = 010101$$

Thus we have an error pattern of weight d=3, that is not detectable by C

(b) An error pattern of weight $\lfloor \frac{d-1}{2} \rfloor + 1$ that C does not correct.

I was able to see the distance from u=001100 to v=011001 was d(u,v)=3. Notice that with d=3, $\lfloor \frac{d-1}{2} \rfloor +1=2$. So I need to find an error pattern of weight 2, that C does not correct. Because d(u,v)=3, if I make an error pattern of weight 2 and add it to u, the result u+e will be closer to v. So let e=010100 such that

$$w = u + e = 011000$$

Now notice that d(w, u) = 2 but the d(w, v) = 1. So C will not correct e = 010100.