LOT: Porticle Filter and Manke-Carlo Localization.

* Summing of LOG localization.

the localization problem becomes a state estimation problem.

beller)=p(xt | U.Z.m) L4> EKF, UKF.

Assume (for now)
$$C_t^i = j$$
 ($z^i \rightarrow m_j$) Known cosumpndan

Partiale litter (PF)

$$\int bel(x_t) = \int \rho(x_t|x_{t-1},u_t) bel(x_{t-1}) dx_{t-1}$$

$$bel(x_t) = y \rho(z(x_t) bel(x_t)$$

* Gaussian litters { KF linear functions }

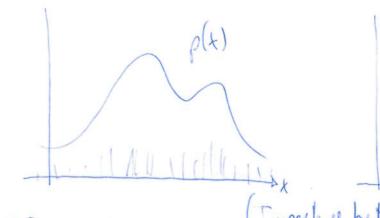
EXF 4 non-linear }

Unimodal distribution.

A Non-paramétric - Posticle filter (PF)

Unimo dal gove.

Exi



 $x^{[m]} \sim \rho(x)$ $w^{[m]} = \rho(x^{[m]})$

(Importance factors)
Weighted samples. Particles become a
good representation of distribution
(if M is large enought)

a: neights on PS1? Sample mean, sample vovenna?

1. Porticle filler (Xt-1, Mt, Ze):

2: for m = 1: M

3: $x_t^{[m]} \sim \rho(x_t | M_t, x_{t-1}^{[m]})$

4: wfm7 = p(zt | xfm])

 $\bar{\chi}_t = \bar{\chi}_t \cup \langle x_t^{(m)}, w_t^{(m)} \rangle$

6: $\chi_t = \text{resample}^* (\overline{\chi}_t)$

(better correction)
To are "Janua" from beller) and not bel

correction

propagation bel(kx)

[Gordon] reading introduces resampling and required for the

PF to work properly

* Bayer peller for full stakes bel (Xo:t) = p(xo:t| Mit; Zit) particles $x_{0:t}^{[m]} = x_{0}^{[m]}, x_{1}^{[m]}, \dots, x_{t}^{[m]}$ Sequence of states. bel(xo:t) = 1 p(2t | xo:t, Z1:t-1, U1:t) p(xo:t | Z1:t-1, U1:t) Marlor+ Bays = y p(Zt | Xt) p(Xt | Xo:t-1, Z1:t-1, U1:t) p(Xo:t-1 | Z1:t-1, U1.t) = 2 p(20 | xt) p(xt | xt-1, Ut) p(xot-1 | Z1:t-1, U1:t-1) From this full state Bayer (no marjiralization)
given a particle $x_{t-1}^{fm]}$ n bel $(x_0:t-1)$ ($a: w_{t-1}^{fm]}$ on simple $\frac{1}{1000} = 1 \cdot w_{t-1}^{(m)} = 1 \cdot w_{t-1}$ Note - [0] tos each particle in the Mut we sample plxolximilae) p(xolx[m] m)

Motion model (R)

X Importance sampling Ep (I(xeA) (= | I(xeA) p(x) dx $= \int \mathbb{I}(x \in A) \frac{\rho(x)}{q(x)} \cdot q(x) dx$ = Eg 4 I (x + A) · w(x) 4 $W(t) = \frac{p(t)}{q(t)}$ Impartance lactor. p(x) tweet distribution (usually we con't use) g(t) proposal distribution. Tx: Probability of sample and 1. v X in [15, 17] if p(x) = N(0,1)? A= x 1 15 < x < 17 4 $\mathcal{I} P(x \in A) = Z I(x^m \in A) \cdot p(x^m) / p(x^m) / p(x^m)$ hard to sample this event. 2) I.S.: $P(x \in A) = Z I(x^m \in A) \frac{P(x^m)}{q(x^m)} \cdot q(x^m)$, $x^m \cdot q(x)$ (proposal destibution)

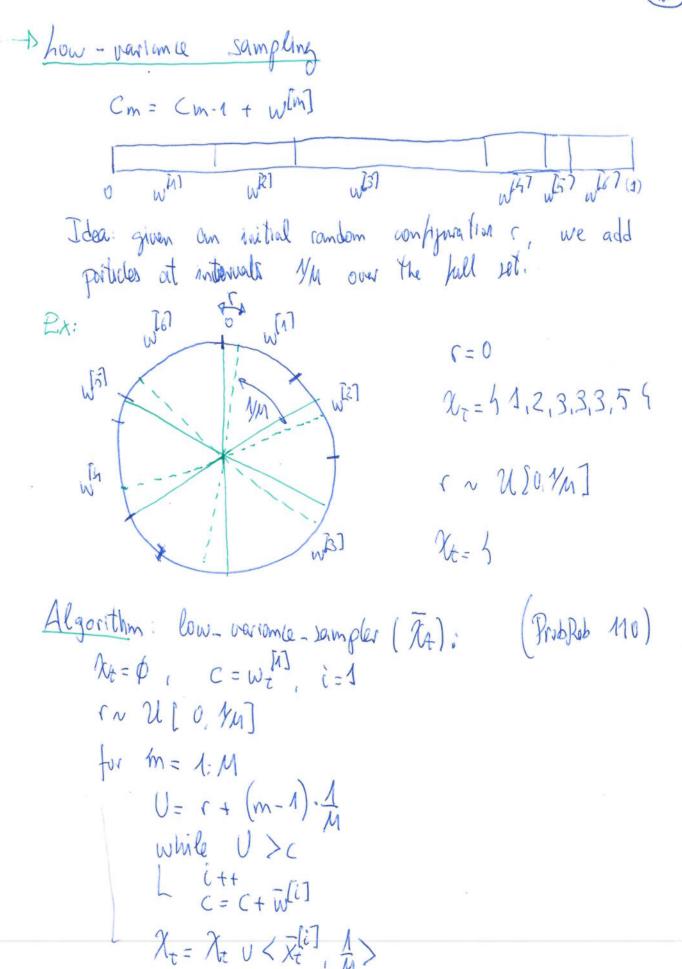
with this proposal distribution we don't need trillions of samples but only handreds. $w^m = \frac{N(x^m; 0, 1)}{N(x^m; 16, 1)}$

-> Correction step (line 4) bel (xo.t) = 1 p(Zt(xt) bel(xo.t)

Proposal distribution tayet distribution Rt particle at represents this belief. In order to correctly characterize the portarior del (x: +) we are going to neight the particles drawn (already) To with proper weight or importance factors. Xtm7 = Xt [m] (previously drawn) from proposed dot w to = & towjet distribution = & platent = 2 p(2+ (x+(m)). bel(x0:t) = n. p(2+ |x+(m)) the size of the point congrands to wint new weight wfm? Problem: creater an almost empty set of purlicles with weights non-zero > Degenerally over time. and many particles with low weights.

* Resemply (the solution)
Idea: surroual of the fittent. Only The most likely particles (win] 1) 'might' source.
Ex: Y No samples ove roundender Selected ox wins No selected ox wins
from M samples on Rt we get M samples on Xt (closer to true be
- Independent Resampling. First solution
We create a cumulative distribution prinction:
Cm = Cm-1 + w[m] (+ normalization)
(Co=0) WEIT WEIT WEIT WEIT WEIT WEIT WEIT WEIT
for m = 1: M u ~ ULO, 1) (am form distribution)
$j = jind (c_m, u)$
$\chi_{t} = \chi_{t} \cup \langle \chi_{t}^{[i]}, w_{t}^{[i]} \rangle$

A Problem: over time, independent sexampling underces a loss of diversity in the particle population &t



return 20.

* Monte-Carlo localization (Mal) Q readings: Dellawit'99
We want to solve the Markor localization (208) using PF. bel $(x_t) = p(x_t \mid \mathcal{U}, Z, m)$ _____ & χ_t Porlide set tepremily belief. map of and marks Algorithm: MCL (Rom, Mt. Zt, m): 1: X= Xt = d 2: for m = 1: M 3: X_t^{lm} = Sample_motion_model (uc, X_{t-1}^{lm}) (205) Wtm] = measurement_model (Z, xtm], m) (106,5 $\bar{\chi}_t = \bar{\chi}_t \cup \langle x_t^{[m]}, w_t^{[m]} \rangle$

6: Xt = low-varionce-sampling (Rt)

Next beclive SLAM: Probled Chito + readings a concern