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# Assignment 1

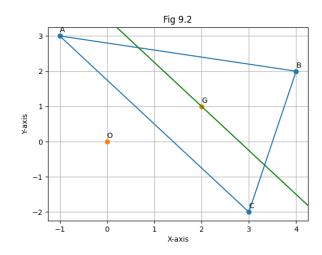
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## **Question:**

A(-1, 3), B(4,2) and C(3,-2) are the vertices of a triangle.

- a) Find the coordinates of the centroid G of the triangle
- b) Find the equation of the line through G and parallel to AC.

### **Solution:**



1) Let A, B, C be the points vectors.

$$\mathbf{A} = \begin{pmatrix} -1\\3 \end{pmatrix}, \mathbf{B} = \begin{pmatrix} 4\\2 \end{pmatrix}, \mathbf{C} = \begin{pmatrix} 3\\-2 \end{pmatrix}$$
 (1)

Using centroid formula, the desired point vector **G** is given by:

$$\mathbf{G} = \frac{1}{3}(\mathbf{A} + \mathbf{B} + \mathbf{C}) \tag{2}$$

$$=\frac{1}{3}\left(\begin{pmatrix}-1\\3\end{pmatrix}+\begin{pmatrix}4\\2\end{pmatrix}+\begin{pmatrix}3\\-2\end{pmatrix}\right) \qquad (3)$$

$$=\frac{1}{3} \begin{pmatrix} 6\\3 \end{pmatrix} \tag{4}$$

$$= \begin{pmatrix} 2 \\ 1 \end{pmatrix} \tag{5}$$

 ${\bf G}$  is the point vector  $\begin{pmatrix} 2\\1 \end{pmatrix}$ 

2) Let L be the line that passes through G such that  $L \parallel AC$  The direction vector of AC is,

$$\mathbf{m} = \mathbf{A} - \mathbf{C} \tag{6}$$

$$\mathbf{m} = \begin{pmatrix} -1\\3 \end{pmatrix} - \begin{pmatrix} 3\\-2 \end{pmatrix} \tag{7}$$

$$\mathbf{m} = \begin{pmatrix} -4\\5 \end{pmatrix} \tag{8}$$

Normal vector of the line is n, such that

$$\mathbf{m}^{\mathsf{T}}\mathbf{n} = 0 \tag{9}$$

$$\begin{pmatrix} -4 & 5 \end{pmatrix} \mathbf{n} = 0 \tag{10}$$

$$\mathbf{n} = \begin{pmatrix} 5\\4 \end{pmatrix} \tag{11}$$

$$\mathbf{n}^{\top} = \begin{pmatrix} 5 & 4 \end{pmatrix} \tag{12}$$

The normal equation of the line L is given by,

$$\mathbf{n}^{\top}(\mathbf{x} - \mathbf{G}) = 0 \tag{13}$$

$$\begin{pmatrix} 5 & 4 \end{pmatrix} \begin{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix} - \begin{pmatrix} 2 \\ 1 \end{pmatrix} \end{pmatrix} = 0 \tag{14}$$

$$\begin{pmatrix} 5 & 4 \end{pmatrix} \begin{pmatrix} x - 2 \\ y - 1 \end{pmatrix} = 0 \tag{15}$$

Thus, line L 
$$\equiv$$
  $\begin{pmatrix} 5 & 4 \end{pmatrix} \begin{pmatrix} x-2 \\ y-1 \end{pmatrix} = 0$