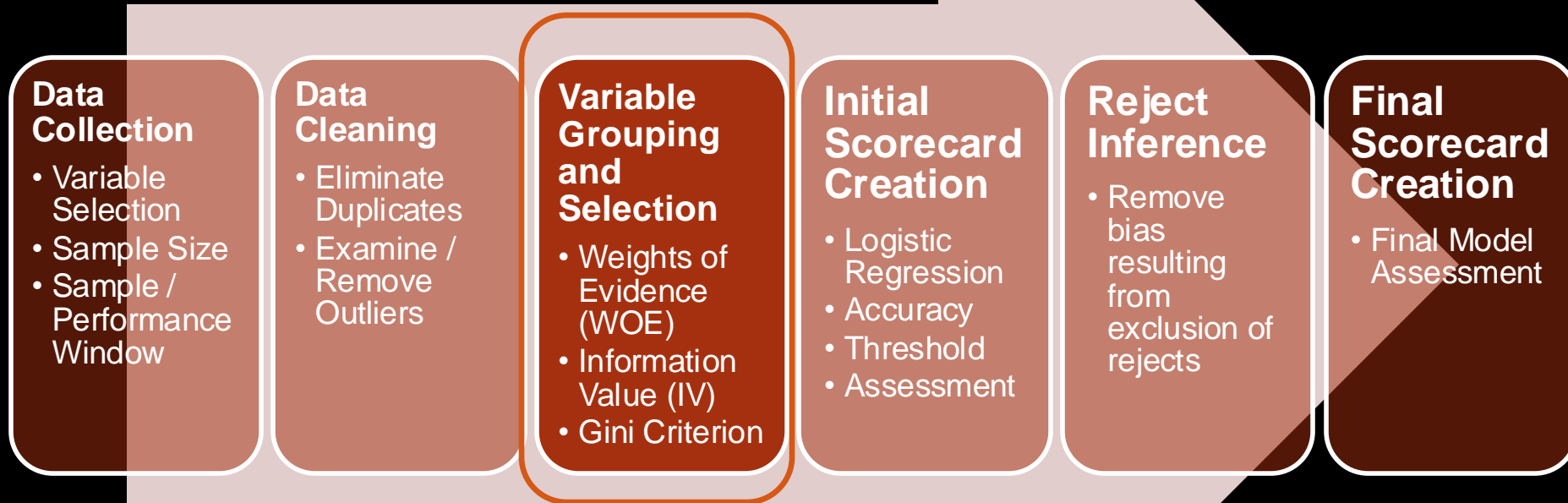


SCORECARD VARIABLE GROUPING AND SELECTION

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Institute for Advanced Analytics

Process Flow



VARIABLE GROUPING

Variable Grouping and Selection

- Scorecards end up with only just groups within a variable.
- Objectives:
 1. Eliminate weak characteristics (variables) or those that do not conform to good business logic.
 2. Group the strongest characteristics' attribute levels in order to produce a model in scorecard format.
- Function/package “scorecard” or “smbinning” in R.
- Package “scorecard” or “OptBinning” in Python.

Variable	Level
MISS	$x < 24$
MISS	$24 \leq x < 36$
MISS	$36 \leq x < 48$
MISS	$x \geq 48$
HOME	OWN
HOME	RENT

Why Grouping (Binning)?

- Goal is to help simplify analysis through grouping:
 - Useful for understanding relationships – no worries about explaining coefficients.
 - Modeling nonlinearities – similar to decision trees.
(NO MORE LOGISTIC REGRESSION LINEARITY ASSUMPTION!)
 - Dealing with outliers – contained in the smallest / largest group.
 - Missing values typically in own group.

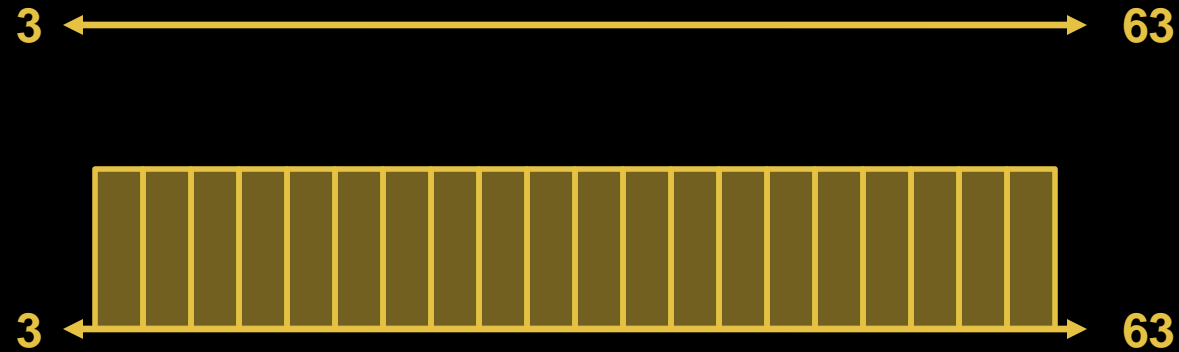
Initial Characteristic Analysis – Pre-binning

- Need a starting point for the grouping / binning.
 - Quantiles are most popular technique.
- Pre-bin the interval variables into a number of user-specified quantiles / buckets for fine detailed groupings.
- Aggregate the fine detailed groupings into a smaller number to produce coarse groupings.
 - Chi-squared tests to combine groups.

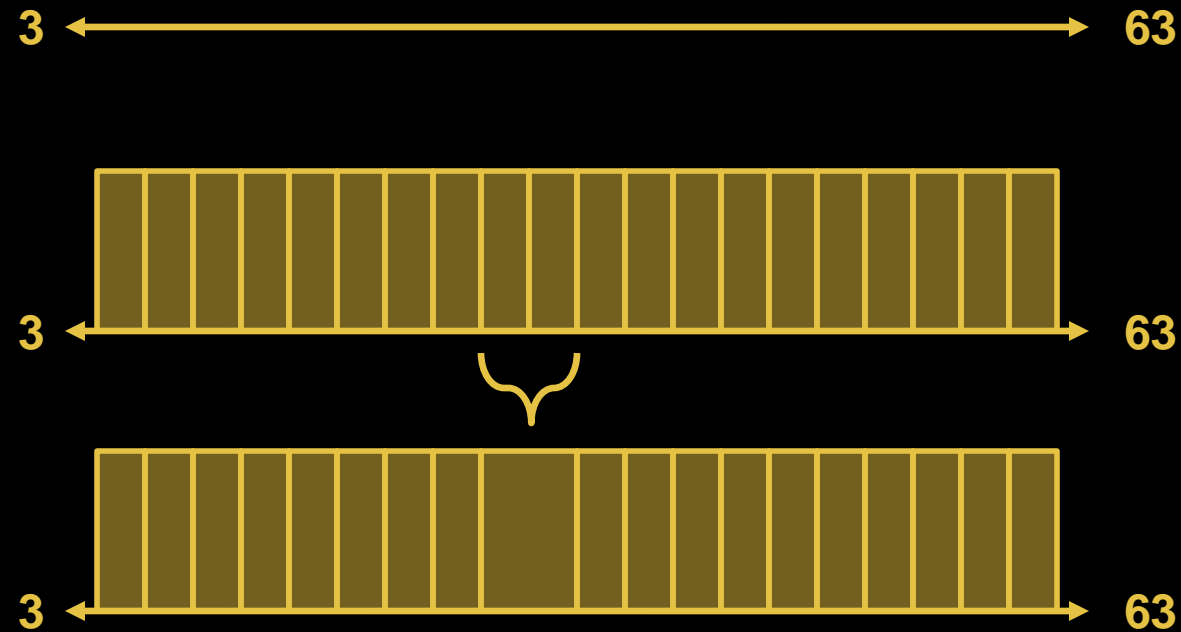
Initial Characteristic Analysis – Pre-binning

3 ←————→ 63

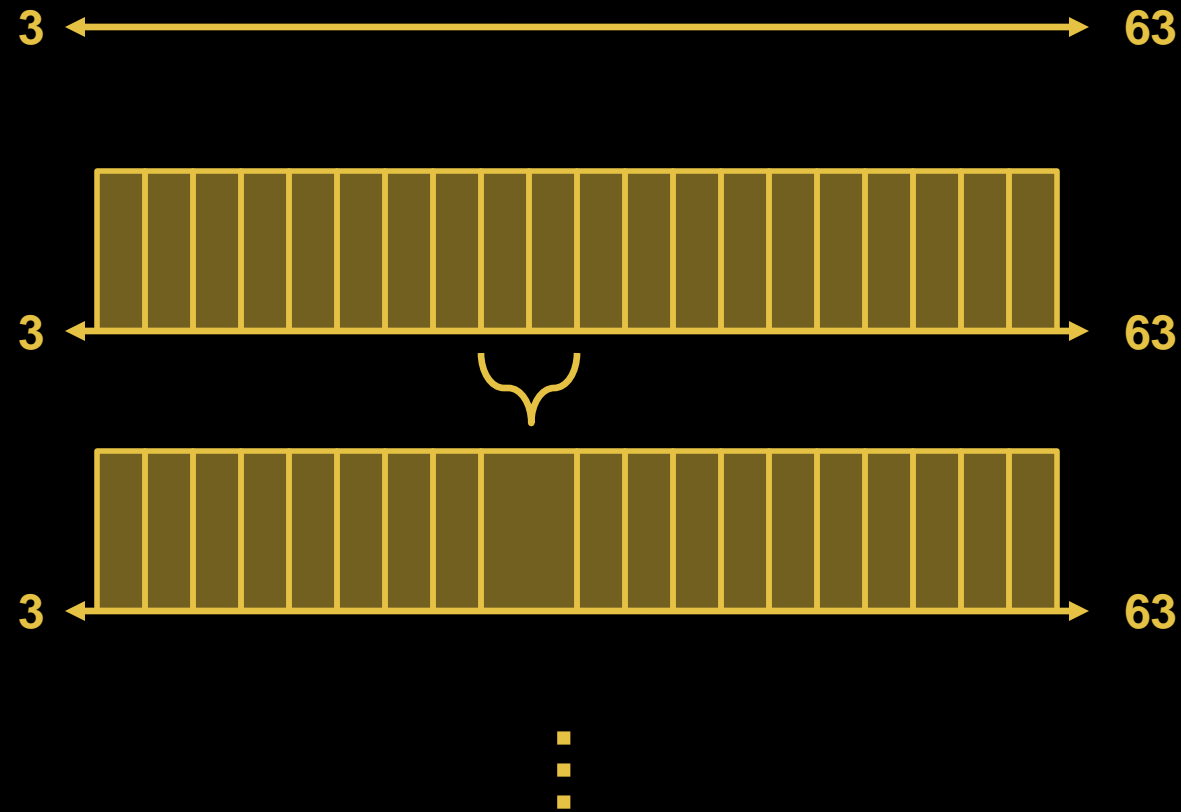
Initial Characteristic Analysis – Pre-binning



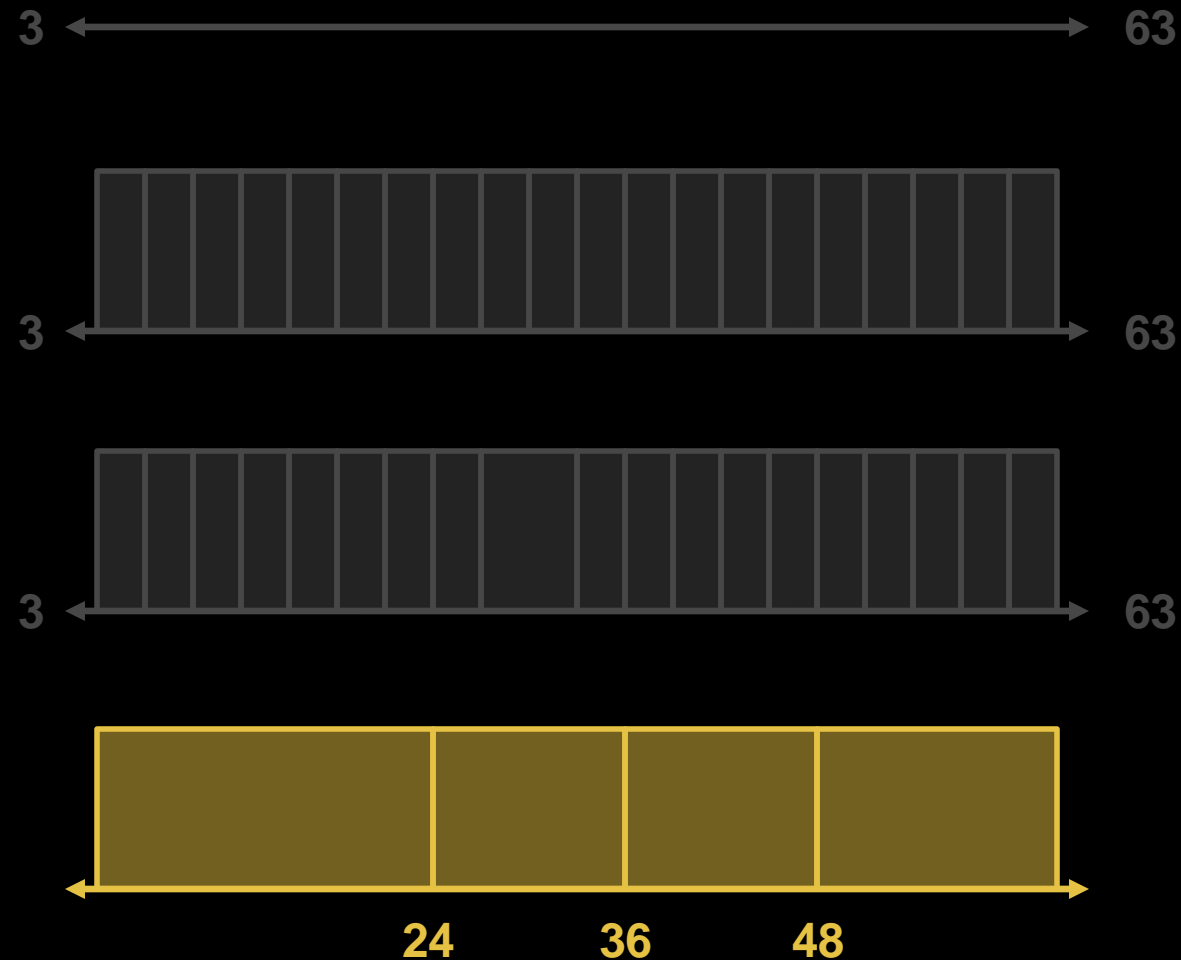
Initial Characteristic Analysis – Pre-binning



Initial Characteristic Analysis – Pre-binning



Initial Characteristic Analysis – Pre-binning



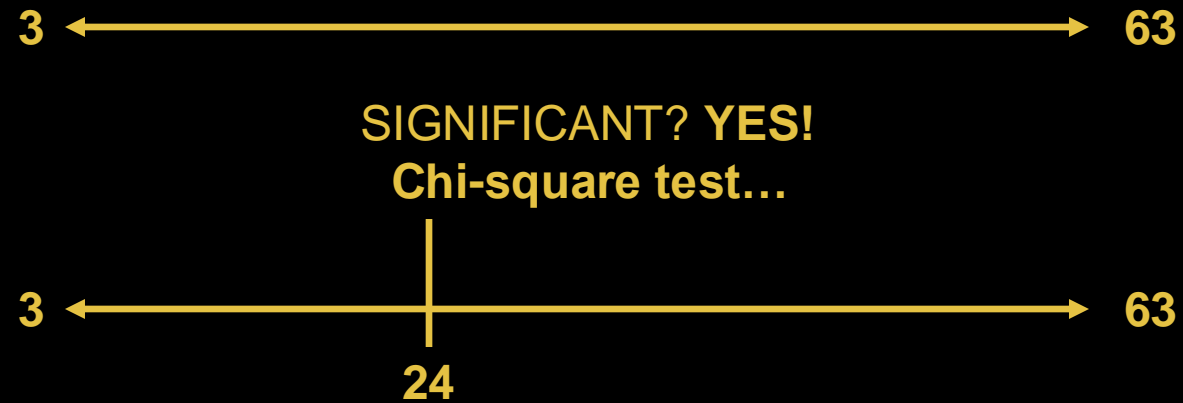
Initial Characteristic Analysis – Tree-based

- Another approach to binning is through tree-based methods like decision trees or conditional inference trees.
- Conditional Inference Trees (CIT):
 - CART methods potentially have inherent bias – variables with more levels → more likely to be split on if split on Gini and Entropy.
 - CIT method adds extra statistical step before splits occur – statistical tests of significance.
 - What is **MOST** significant variable? → What is the best split (Chi-square) on **THIS** variable? → **REPEAT**.

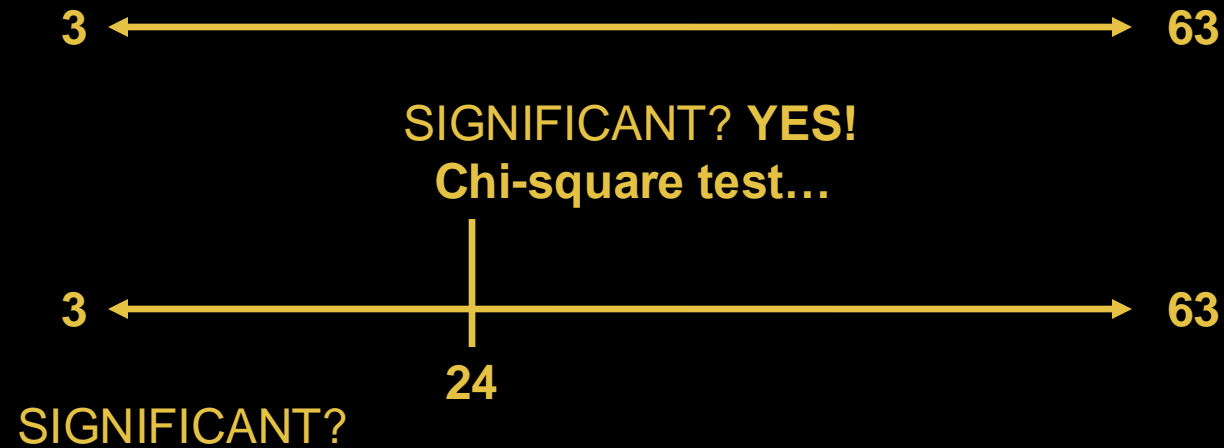
Initial Characteristic Analysis – CIT



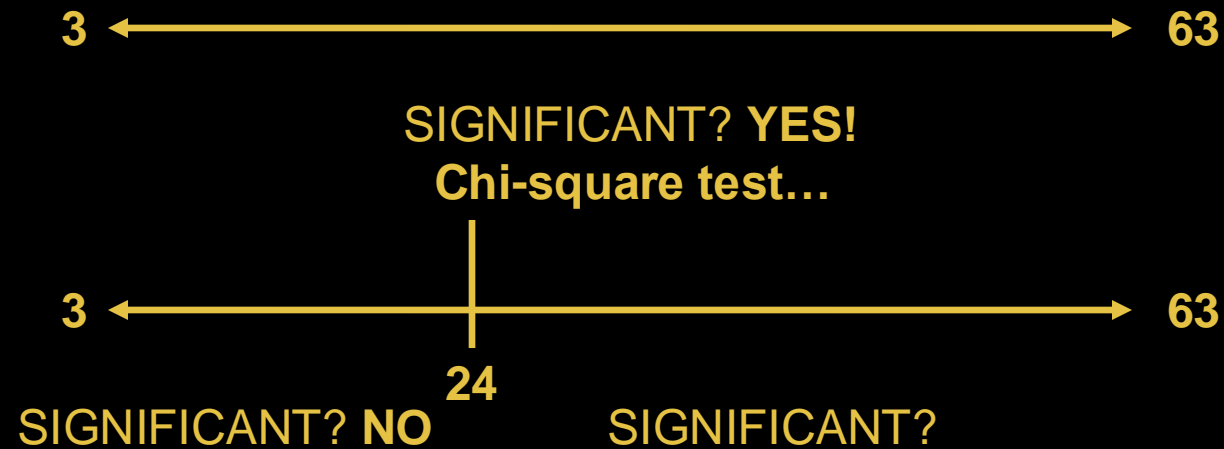
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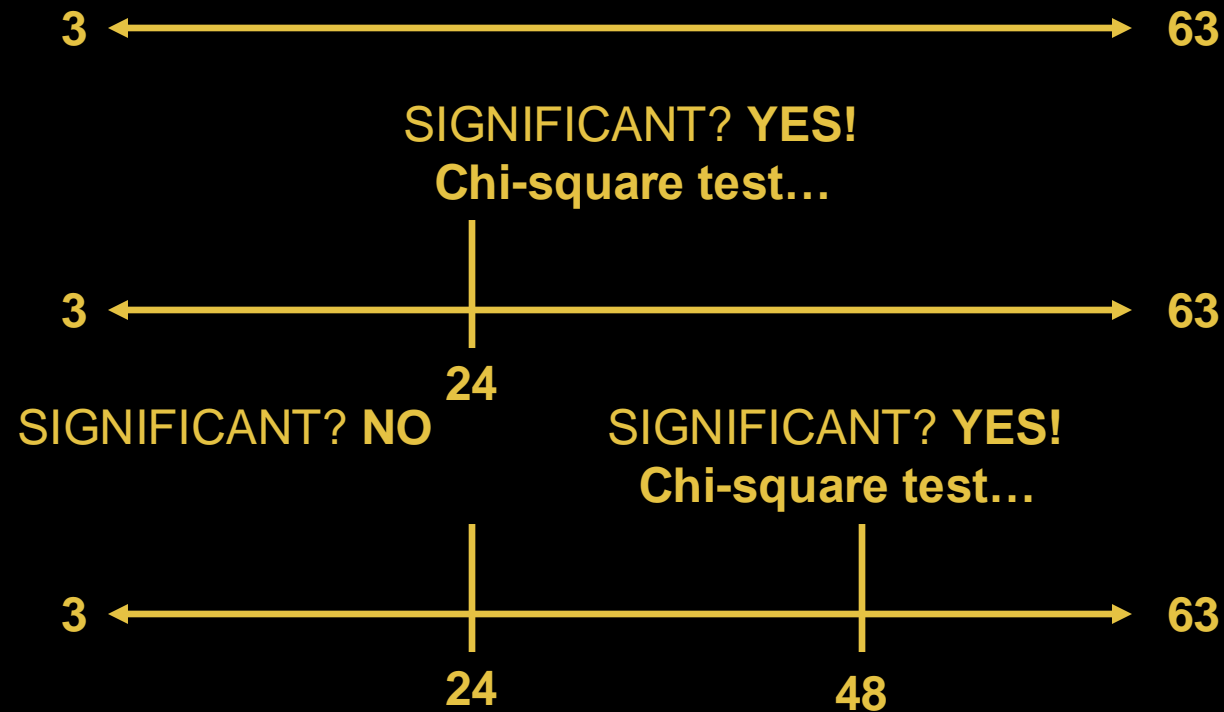
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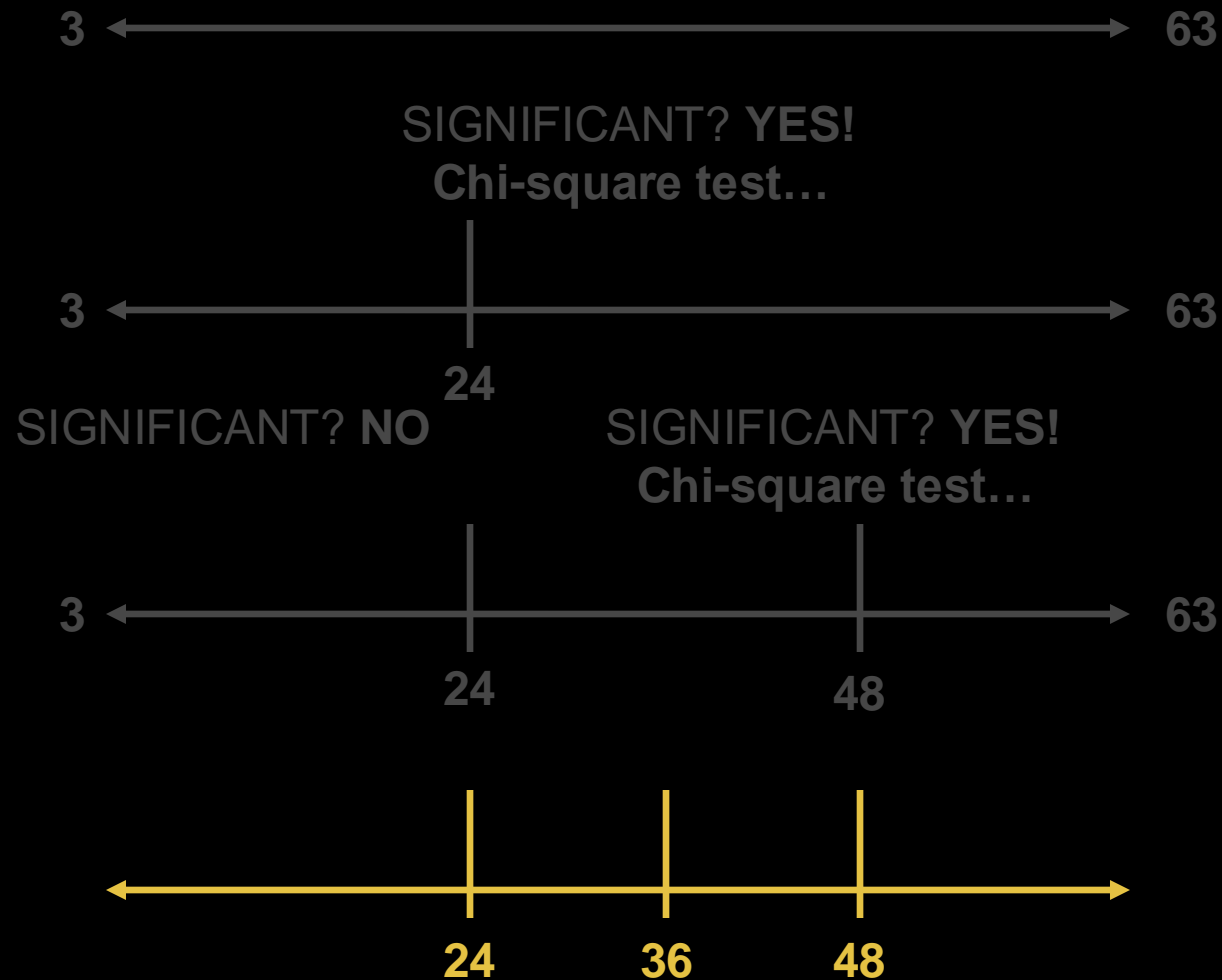
Initial Characteristic Analysis – CIT



Initial Characteristic Analysis – CIT



Initial Characteristic Analysis – CIT



Initial Characteristic Analysis

- Cut-offs may be rough from decision tree combining.
- **Optional to override** automatically generated groups to conform to business rules.
- Overrides may make groups suboptimal.

Group Definition
Missing
< \$35,200
\$35,200 - \$60,000
\$60,000 - \$85,000
\$85,000 - \$110,000
\$110,000 - \$142,530
> \$142,530

Initial Characteristic Analysis

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\$35,200 - \$60,000	\$35,000 - \$60,000
\$60,000 - \$85,000	\$60,000 - \$85,000
\$85,000 - \$110,000	\$85,000 - \$110,000
\$110,000 - \$142,530	\$110,000 - \$140,000
> \$142,530	> \$140,000

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\$85,000 - \$110,000	\$85,000 - \$110,000
\$110,000 - \$142,530	\$110,000 - \$140,000
> \$142,530	> \$140,000

Initial Characteristic Analysis

- Calculate and examine the key assessment metrics:
 - **Weight of Evidence (WOE)** – how well attributes discriminate for each given characteristic
 - **Information Value (IV)** – evaluate a characteristic's overall predictive power
 - **Gini Statistic** – alternate to IV for selecting characteristics for final model.



WEIGHT OF EVIDENCE

Weight of Evidence (WOE)

- WOE measures the strength of the attributes of a characteristic in **separating good and bad accounts**.
- WOE is based on comparing the proportion of goods to bads at each attribute level (levels of the predictor variable).

$$WOE_i = \log \left(\frac{Dist. Good_i}{Dist. Bad_i} \right)$$

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$$Dist. Good_i = \frac{Number\ Good\ in\ group\ i}{Total\ Number\ Good}$$

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$$Dist. Bad_i = \frac{Number\ Bad\ in\ group\ i}{Total\ Number\ Bad}$$


Weight of Evidence (WOE)

- What are we looking for?
 - Looking for “big” differences in WOE between groups.
 - Monotonic changes within an attribute for **interval variables** (not always required).
- Why monotonic increases?
 - Oscillation back and forth of positive to negative values of WOE typically sign of variable that has trouble separating good vs. bad.
 - Not always required **if makes business sense** – credit card utilization for example.

WOE – Example

WOE for Bureau Score				
Group	Values	Event Count	Non-event Count	WOE
1	< 607	129	127	
2	607 – 640	181	285	
3	641 – 653	103	215	
4	654 – 667	86	262	
...
12	> 786	5	219	
	MISSING	89	155	
Total		900	3,477	

WOE – Example

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$$Dist. Good_1 = \frac{127}{3477}$$

$$= 0.0365$$

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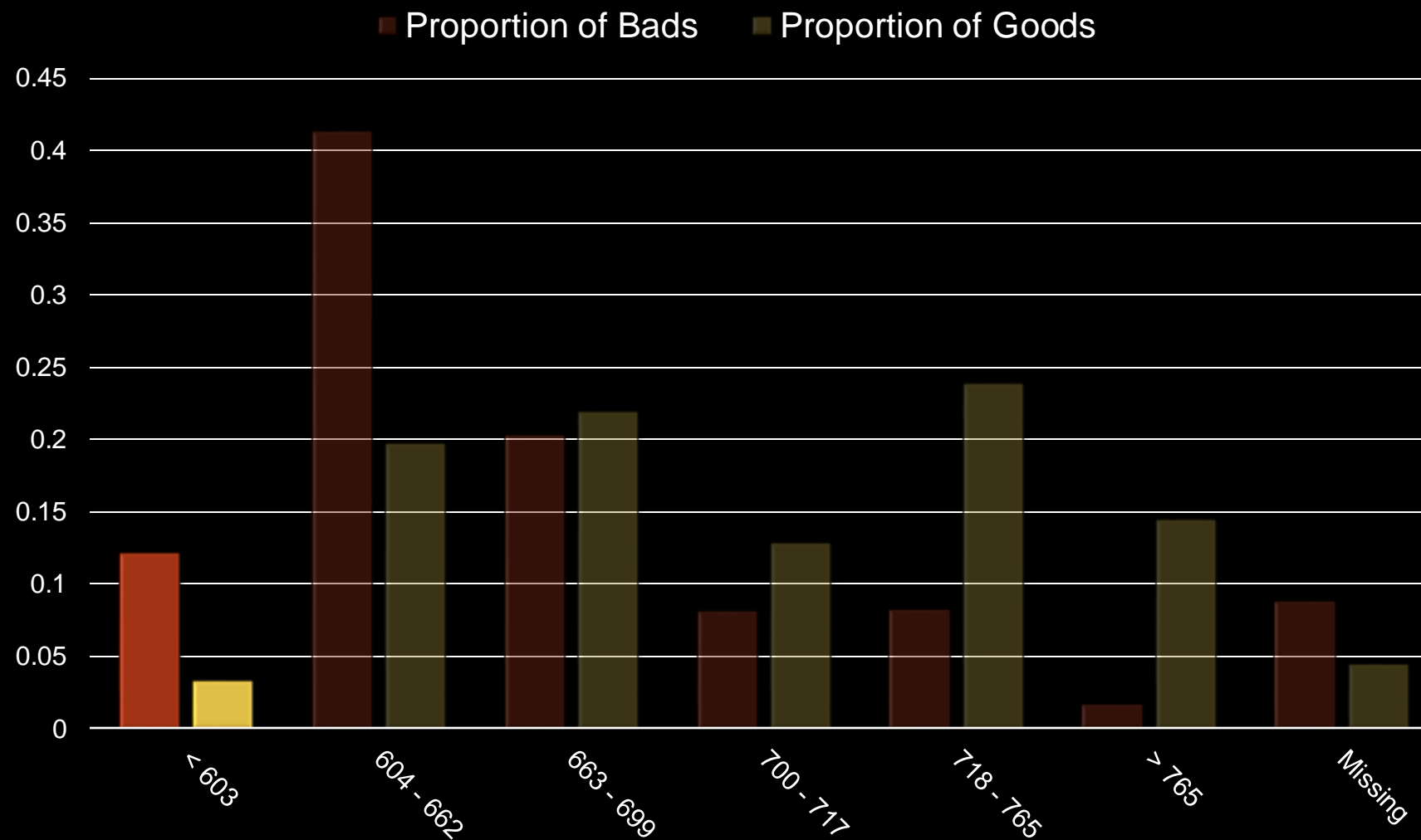
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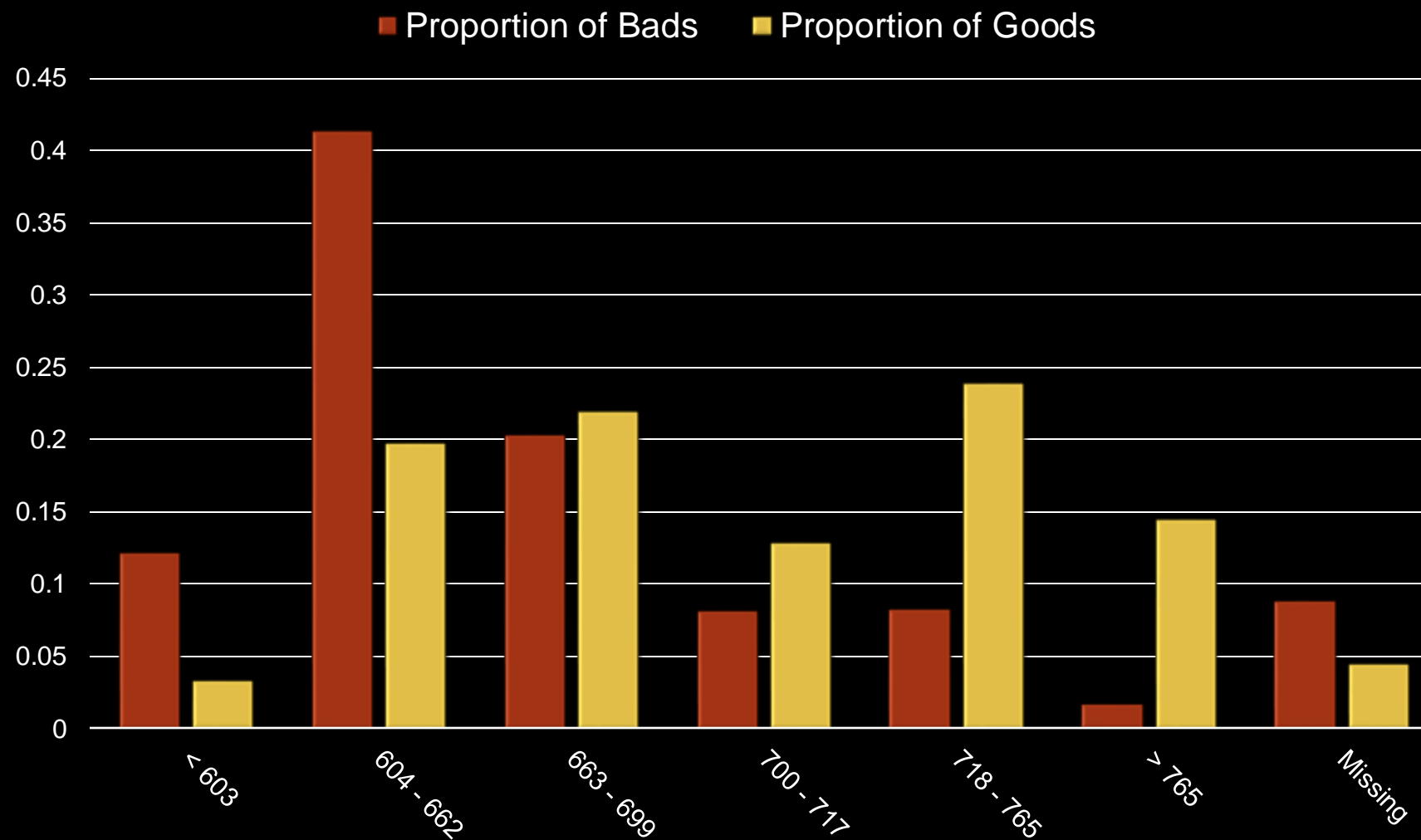
$$Dist. Bad_1 = \frac{129}{900}$$

$$= 0.1433$$

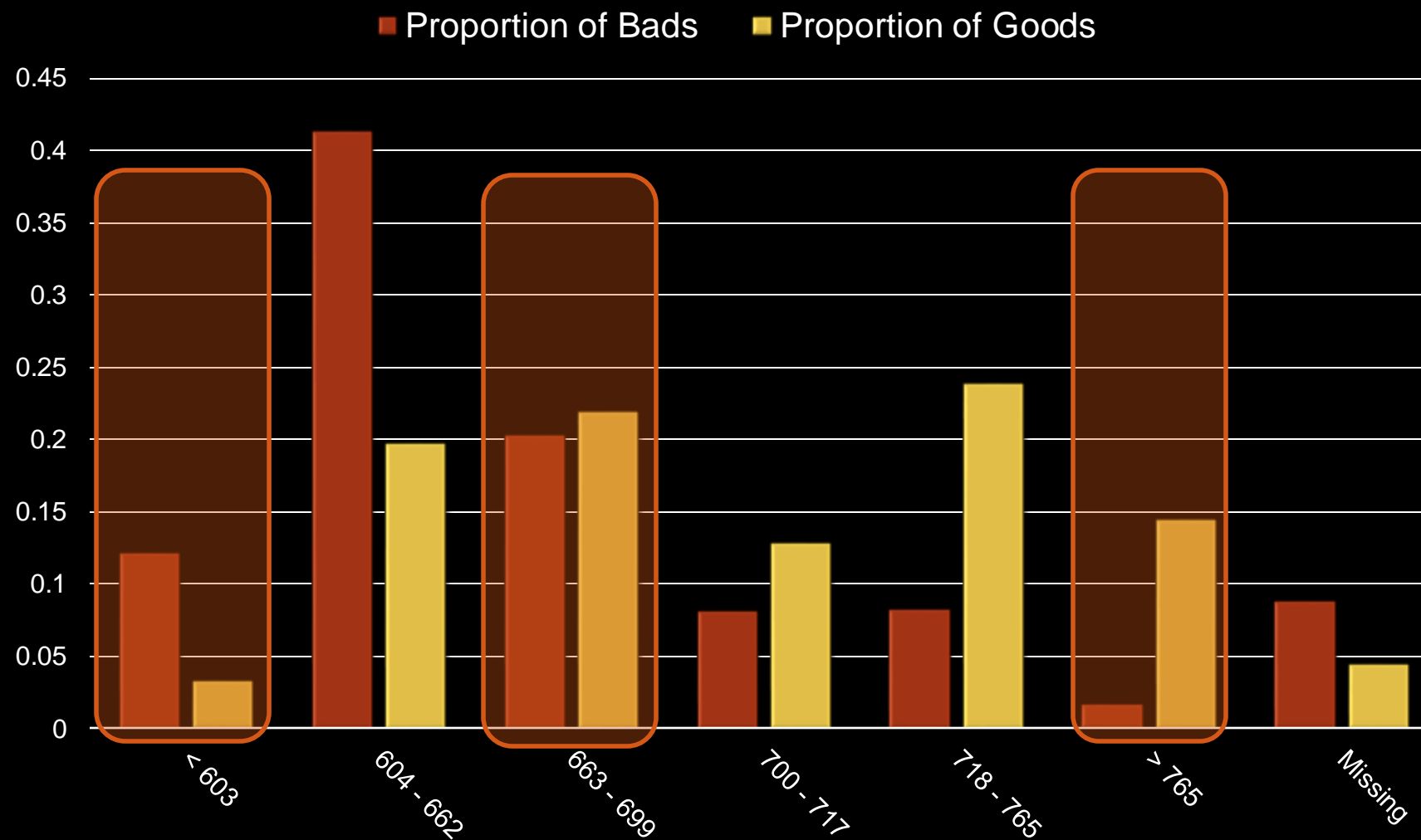
WOE – Example



WOE – Example



WOE – Example



WOE – Example

WOE for Bureau Score				
Group	Values	Event Count	Non-event Count	WOE
1	< 607	129	127	-1.367
2	607 – 640	181	285	
3	641 – 653	103	215	
4	654 – 667	86	262	
...
12	> 786	5	219	
	MISSING	89	155	
Total		900	3,477	

$$\begin{aligned} Dist. Good_1 &= \frac{127}{3477} \\ &= 0.0365 \end{aligned}$$

$$\begin{aligned} Dist. Bad_1 &= \frac{129}{900} \\ &= 0.1433 \end{aligned}$$

$$\begin{aligned} WOE_1 &= \log\left(\frac{0.0365}{0.1433}\right) \\ &= -1.367 \end{aligned}$$

WOE – Example

WOE for Bureau Score				
Group	Values	Event Count	Non-event Count	WOE
1	< 607	129	127	-1.367
2	607 – 640	181	285	-0.898
3	641 – 653	103	215	-0.616
4	654 – 667	86	262	-0.238
...
12	> 786	5	219	2.428
	MISSING	89	155	-0.797
Total		900	3,477	

Weight of Evidence (WOE)

- WOE measures the strength of the attributes of a characteristic in **separating good and bad accounts**.

$$WOE_i = \log \left(\frac{Dist. Good_i}{Dist. Bad_i} \right)$$

- WOE approximately zero implies what?

Weight of Evidence (WOE)

- WOE measures the strength of the attributes of a characteristic in **separating good and bad accounts**.

$$WOE_i = \log \left(\frac{Dist. Good_i}{Dist. Bad_i} \right)$$

- WOE approximately zero implies % good approximately equal to % bad so group doesn't separate good vs. bad well.

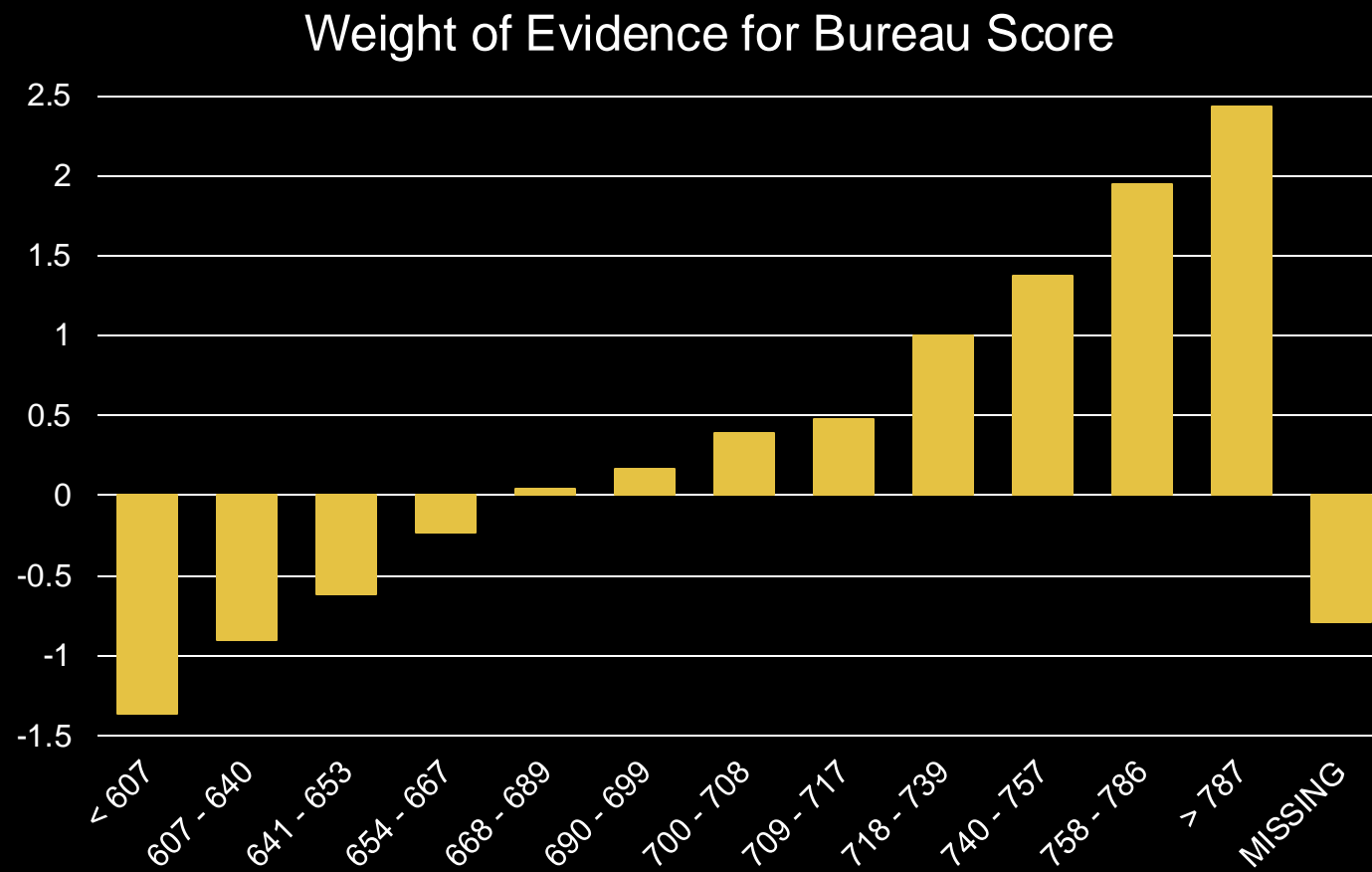
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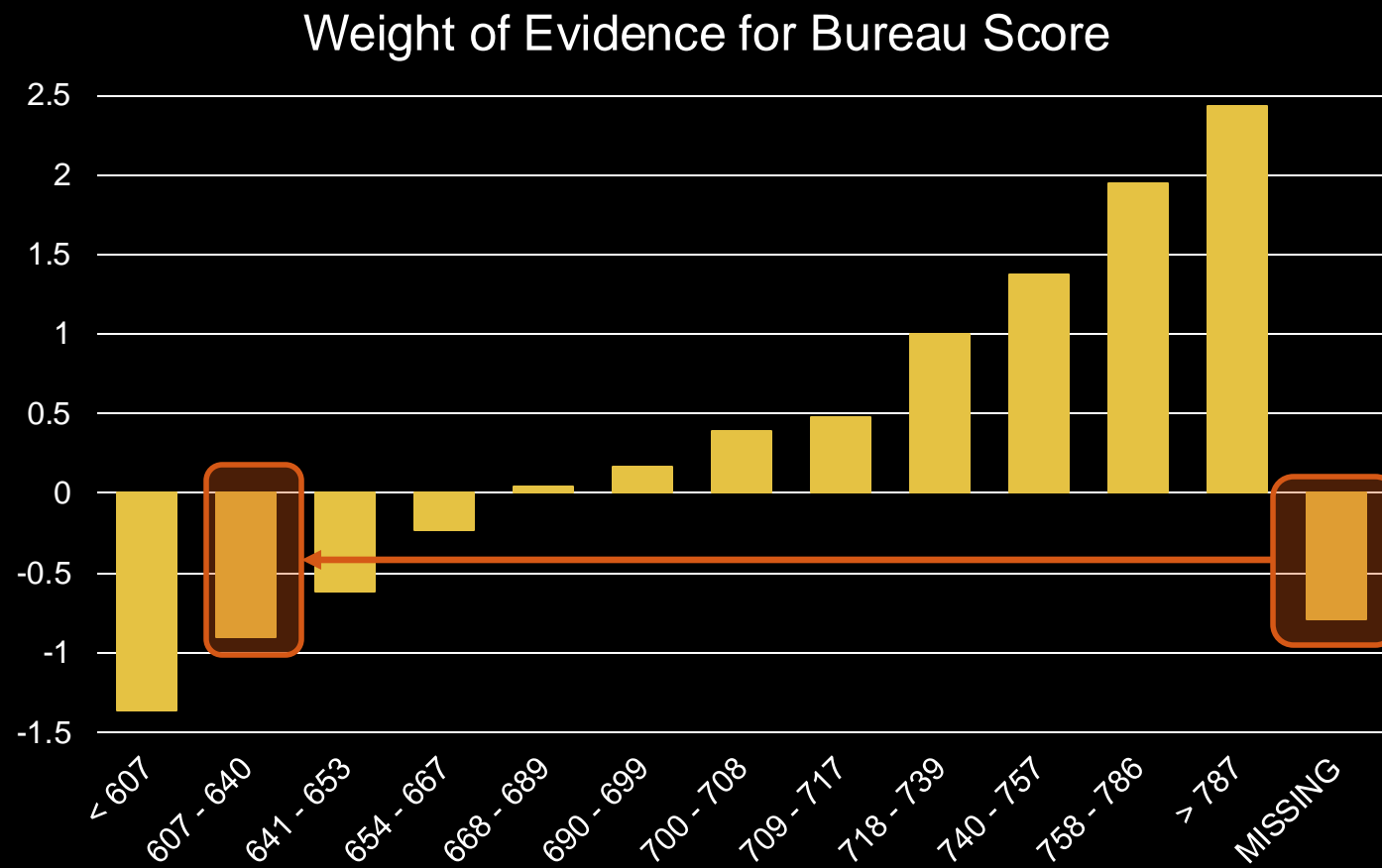
$$WOE_i = \log \left(\frac{Dist. Good_i}{Dist. Bad_i} \right)$$

- WOE approximately zero implies % good approximately equal to % bad so group doesn't separate good vs. bad well.
- WOE positive implies group identifies people who are good.
- WOE negative implies group identifies people who are bad.

WOE – Example



WOE – Example



WOE – Python

```
import numpy as np  
from optbinning import OptimalBinning
```

```
X = train["bureau_score"]  
y = train["bad"]
```

```
optbin = OptimalBinning(name = "bureau_score", dtype = "numerical")
```

```
optbin.fit(X, y)
```

```
optbin.splits
```

```
array([606.5, 640.5, 653.5, 667.5, 689.5, 699.5, 708.5, 717.5, 739.5, 757.5, 786  
.5])
```

WOE – Python

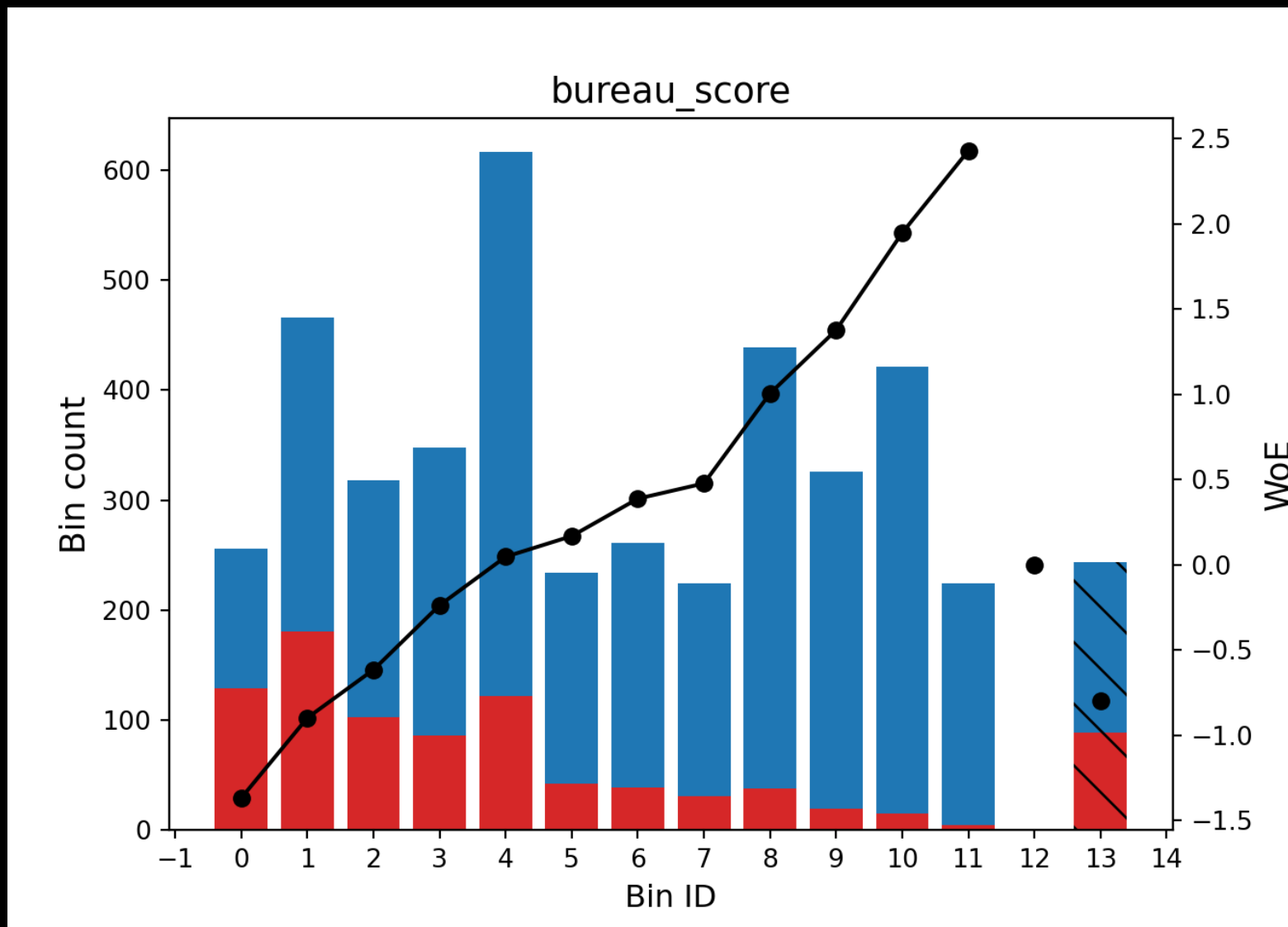
```
iv_table = optbin.binning_table  
iv_table.build()
```

WOE – Python

	Bin	Count	Count (%)	...	WoE	IV	JS
0	(-inf, 606.50)	256	0.058488	...	-1.367156	0.146023	0.016952
1	[606.50, 640.50)	466	0.106466	...	-0.897538	0.106936	0.012936
2	[640.50, 653.50)	318	0.072653	...	-0.615621	0.032388	0.003986
3	[653.50, 667.50)	348	0.079507	...	-0.237533	0.004799	0.000598
4	[667.50, 689.50)	616	0.140736	...	0.046984	0.000306	0.000038
5	[689.50, 699.50)	234	0.053461	...	0.168295	0.001439	0.000180
6	[699.50, 708.50)	261	0.059630	...	0.387585	0.007951	0.000988
7	[708.50, 717.50)	224	0.051177	...	0.477173	0.010051	0.001245
8	[717.50, 739.50)	439	0.100297	...	1.004845	0.073461	0.008815
9	[739.50, 757.50)	326	0.074480	...	1.376322	0.090541	0.010501
10	[757.50, 786.50)	421	0.096185	...	1.946773	0.194873	0.021120
11	[786.50, inf)	224	0.051177	...	2.428103	0.139445	0.014113
12	Special	0	0.000000	...	0.0	0.000000	0.000000
13	Missing	244	0.055746	...	-0.796742	0.043271	0.005270
Totals		4377	1.000000	...	0.851485	0.096741	
[15 rows x 9 columns]							

WOE – Python

```
iv_table.plot(metric = "woe")
```



WOE – Python

```
X = train["purpose"]
y = train["bad"]

optbin = OptimalBinning(name = "purpose", dtype = "categorical")
optbin.fit(X, y)

iv_table = optbin.binning_table
iv_table.build()
```

	Bin	Count	Count (%)	...	WoE	IV	JS
0	[LEASE]	1458	0.333105	...	0.050268	0.000829	0.000104
1	[LOAN]	2919	0.666895	...	-0.024559	0.000405	0.000051
2	Special	0	0.000000	...	0.0	0.000000	0.000000
3	Missing	0	0.000000	...	0.0	0.000000	0.000000
Totals		4377	1.000000	...	0.001234	0.000154	

[5 rows x 9 columns]

Separation Issues Remain

- Quasi-complete separation still a problem:

	Non-Event	Event	WOE
A	28	7	-0.032
B	16	0	∞
C	94	11	0.728
D	23	21	-1.327
Total	161	39	

Adjusted WOE

- Adjust the WOE calculation to account for possible quasi-complete separation:

$$\text{Adjusted } WOE_i = \log \left(\frac{\text{Dist. Good}_i + \eta_1}{\text{Dist. Bad}_i + \eta_2} \right)$$

- The η_1 and η_2 parameters are smoothing parameters that correct for potential overfitting and also protect against quasi-complete separation.
- Most software just sets $\eta_1 = \eta_2$ and has one parameter.

Adjusted WOE ($\eta_1 = \eta_2 = 0.005$)

- Quasi-complete separation no longer a problem:

	Non-Event	Event	WOE
A	28	7	-0.031
B	16	0	3.039
C	94	11	0.719
D	23	21	-1.302
Total	161	39	

Smoothed WOE (SWOE)

- SAS has recently proposed a slightly different smoothed version of the WOE calculation to account for possible quasi-complete separation:

$$SWOE_i = \log \left(\frac{\#Bad_i + (Overall\ Prop.\ Bad) \times c}{\#Good_i + (Overall\ Prop.\ Good) \times c} \right)$$

- This is just a smoothing parameter put in a slightly different place in the WOE calculation based on more Bayesian inference techniques.
- Haven't seen it really used elsewhere.



INFORMATION VALUE

Information Value (IV)

- How big is a “big” difference when looking across groups for WOE?
- IV measures the ability of the characteristic to separate goods vs. bads.

$$IV = \sum_{i=1}^L (Dist.Good_i - Dist.Bad_i) \times \log \left(\frac{Dist.Good_i}{Dist.Bad_i} \right)$$

Information Value (IV)

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$$IV = \sum_{i=1}^L (Dist.Good_i - Dist.Bad_i) \times \log \left(\frac{Dist.Good_i}{Dist.Bad_i} \right)$$

Weight of Evidence!

Information Value (IV)

- How big is a “big” difference when looking across groups for WOE?
- IV measures the ability of the characteristic to separate goods vs. bads.

$$IV = \sum_{i=1}^L (Dist.Good_i - Dist.Bad_i) \times \log \left(\frac{Dist.Good_i}{Dist.Bad_i} \right)$$

- Used to select characteristics with strong predictive value.

Information Value (IV)

- Characteristics of IV:
 - $IV \geq 0$
 - Bigger is Better!
- Rules of Thumb:
 - $IV < 0.02$ – Not predictive
 - $0.02 < IV < 0.1$ – Weak predictor
 - $0.1 < IV < 0.25$ – Medium predictor
 - $0.25 < IV$ – Strong predictor

Information Value (IV) – Python

```
from optbinning import BinningProcess
```

```
colnames = list(train.columns[0:20])
```

```
X = train[colnames]
```

```
selection_criteria = {"iv": {"min": 0.1, "max": 1}}
```

```
bin_proc = BinningProcess(colnames,  
                           selection_criteria = selection_criteria,  
                           categorical_variables = ["bankruptcy",  
                                                    "purpose",  
                                                    "used_ind"])
```

```
iv_all = bin_proc.fit(X, y).summary()
```

```
iv_all[iv_all.columns[0:6]].sort_values(by = ["iv"], ascending = False)
```

Information Value (IV) – Python

	name	dtype	status	selected	n_bins	iv
10	bureau_score	numerical	OPTIMAL	True	12	0.851485
8	tot_rev_line	numerical	OPTIMAL	True	10	0.512358
9.	rev_util	numerical	OPTIMAL	True	10	0.363525
4	age_oldest_tr	numerical	OPTIMAL	True	10	0.322788
2	tot_derog	numerical	OPTIMAL	True	6	0.244956
17	ltv	numerical	OPTIMAL	True	7	0.193863
3	tot_tr	numerical	OPTIMAL	True	8	0.187039
7	tot_rev_debt	numerical	OPTIMAL	True	5	0.114815
13	down_pyt	numerical	OPTIMAL	True	5	0.113488
18	tot_income	numerical	OPTIMAL	True	9	0.108861
6	tot_rev_tr	numerical	OPTIMAL	True	6	0.1028
12	msrp	numerical	OPTIMAL	False	8	0.060786
15	loan_term	numerical	OPTIMAL	False	5	0.059987
11	purch_price	numerical	OPTIMAL	False	6	0.046384
5	tot_open_tr	numerical	OPTIMAL	False	5	0.040953
1	app_id	numerical	OPTIMAL	False	6	0.029569
19	used_ind	categorical	OPTIMAL	False	2	0.019464
16	loan_amt	numerical	OPTIMAL	False	4	0.014432
0	bankruptcy	categorical	OPTIMAL	False	2	0.001872
14	purpose	categorical	OPTIMAL	False.	2	0.001234

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 - $IV > 0.5$ – Over-predicting?

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 - $0.1 < IV < 0.25$ – Medium predictor
 - $0.25 < IV < 0.5$ – Strong predictor
 - $IV > 0.5$ – Over-predicting?
- Over-predicting Example:
 - All previous mortgage decisions have been made only on bureau score so of course bureau score is highly predictive – becomes only significant variable!
 - Create two models – one with bureau score, one without bureau score and **ensemble**.



GINI STATISTIC

Gini Statistic

- **Gini statistic** is optional technique that tries to answer the same question as Information Value – which variables are strong enough to enter the scorecard model?
- IV is more in line with WOE calculation and used more often.
- Characteristics:
 - Range is 0 to 100.
 - Bigger is Better.

Gini Statistic Calculation

- More complicated technique for trying to evaluate how characteristics separate good from bad.
- Majority of the time Gini and IV agree but could be different on the borderline cases.
- Calculation:
 - Sort L groups of variable by descending order of the proportion of all events.

$$Gini = \left(1 - \frac{\left(2 \sum_{i=2}^L (n_{i,E} \times \sum_{j=1}^{i-1} n_{j,NE}) + \sum_{i=1}^L (n_{i,E} \times n_{i,NE}) \right)}{N_E \times N_{NE}} \right) \times 100$$

Gini Statistic Calculation

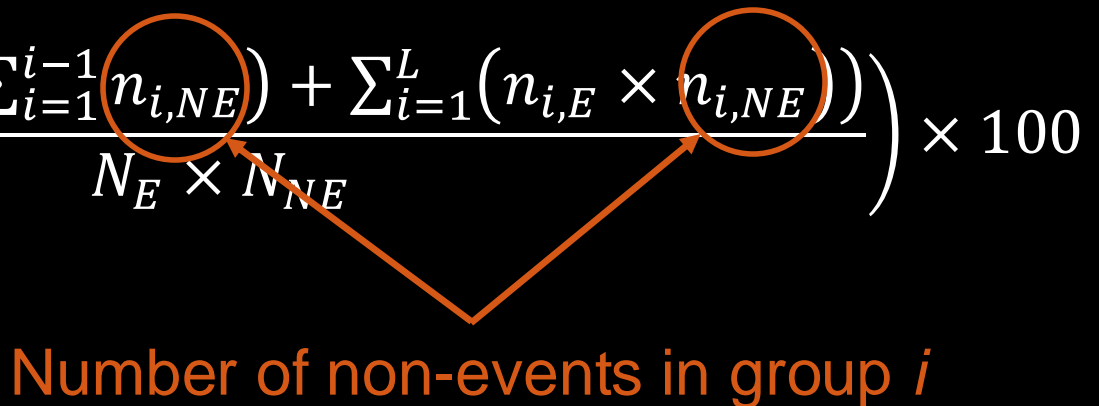
- More complicated technique for trying to evaluate how characteristics separate good from bad.
- Majority of the time Gini and IV agree but could be different on the borderline cases.
- Calculation:
 - Sort L groups of variable by descending order of the proportion of all events.

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Number of events in group i

Gini Statistic Calculation

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Number of non-events in group i

Gini Statistic Calculation

- More complicated technique for trying to evaluate how characteristics separate good from bad.
- Majority of the time Gini and IV agree but could be different on the borderline cases.
- Calculation:
 - Sort L groups of variable by descending order of the proportion of all events.

$$Gini = \left(1 - \frac{\left(2 \sum_{i=2}^L (n_{i,E} \times \sum_{j=1}^{i-1} n_{j,NE}) + \sum_{i=1}^L (n_{i,E} \times n_{i,NE}) \right)}{N_E \times N_{NE}} \right) \times 100$$

Total number of events and non-events

