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You're braver than you believe,  
stronger than you seem, and smarter  
than you think. - A.A. Milne



# Optimization

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# Why Optimization?

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Optimization is important in many businesses to find the ***best set of decisions*** for a particular performance. For example...

***Optimize operational efficiency:*** capital, personnel, equipment, vehicles, facilities.

Create measurable return on investment:

***Optimize costs, earnings and service.***

There are applications of optimization in most industries including: manufacturing, transportation, logistics, financial services, utilities, energy, telecommunications, government, defense and retail.



# What is optimization in the mathematical sciences?

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Optimizing a function is finding the maximum (or minimum) a function can take.

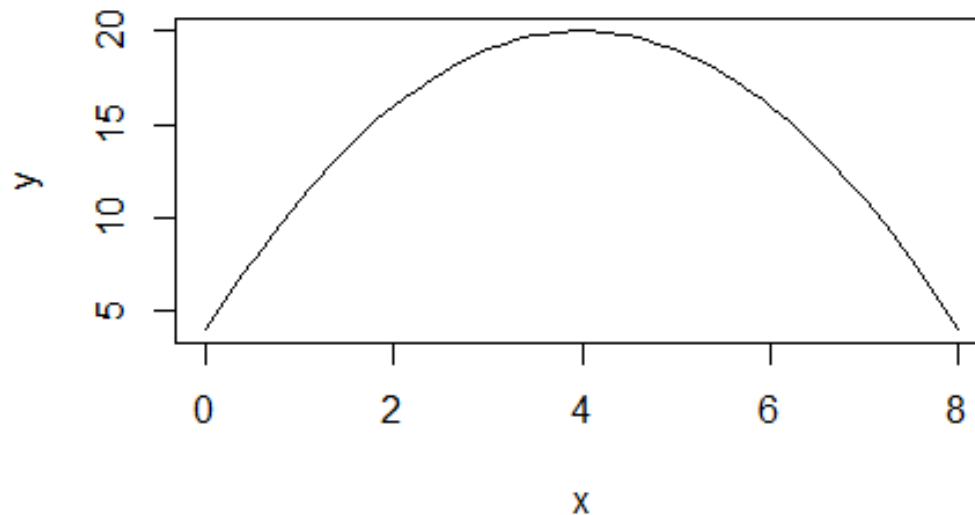


# What is optimization in the mathematical sciences?

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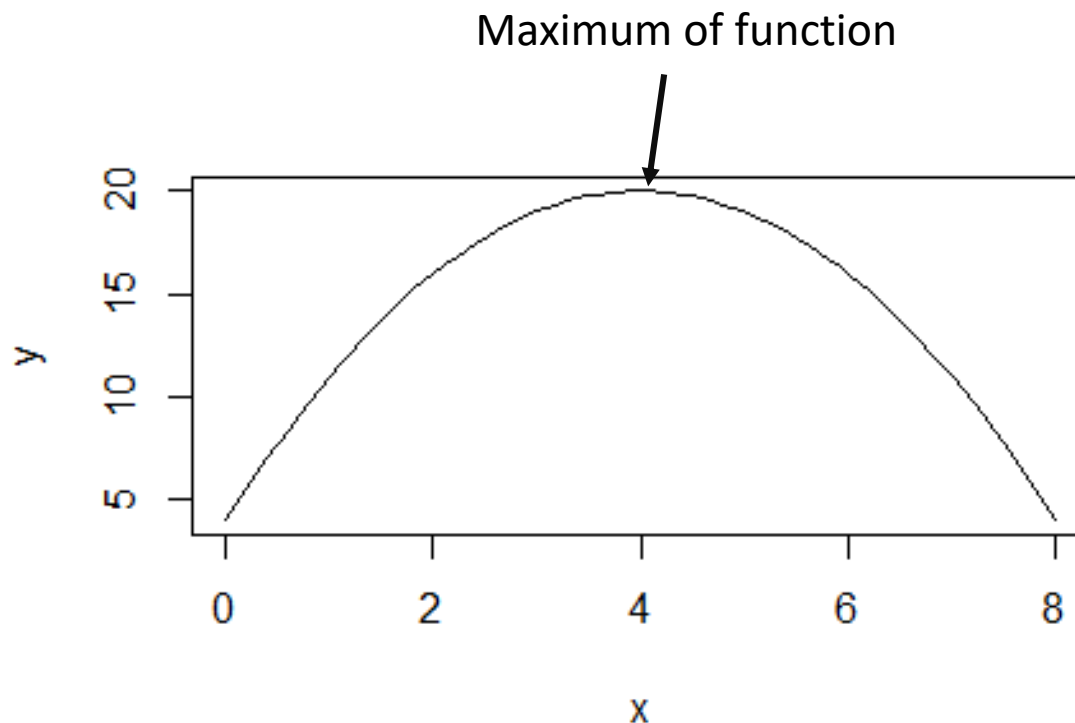
Optimizing a function is finding the maximum (or minimum) a function can take.

Goal is find out what values of the “decision variables” (or input variables) optimize this function



# What is optimization in the mathematical sciences?

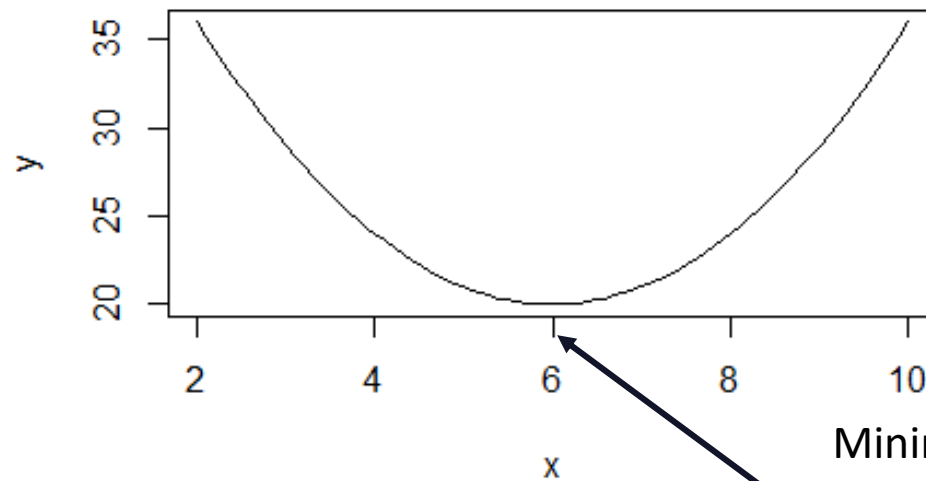
In example below, the x-variable is the “decision variable” and the y is the function we are trying to optimize...



The maximum occurs when the decision or “input” variable is 4 (the optimal value of the “output” is 20).

# Minimize a function

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Minimum occurs at "input" of 6 and "output"(function) at this value is 20.

# Terminology

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The “input” variables are the variables in which we can change to optimize a function. These variables are referred to as the **decision variables**.

The **objective function** is the function in which we are trying to optimize (either maximize or minimize). This function is a function of the decision variables. We are trying to find the best values of the decision variables that optimize this function.

The **constraints** are functions of the decision variables that define the constraints of the problem.

**Parameters** are values inherent in the problem that we are not able to control



# Optimization layout

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**Decision variables:**  $x_1, x_2, \dots, x_k$

**Objective function:**

$$\sum a_i x_i = a_1 x_1 + a_2 x_2 + a_3 x_3 + \dots + a_k x_k$$

$a_1, a_2, \dots, a_k$  are the coefficients in the objective function

**Constraints:**

$$\sum b_{1i} x_i \leq c_1$$

$$\sum b_{2i} x_i \geq c_2$$

$$\sum b_{3i} x_i = c_3$$

...

$b_{ji}$  are the constraint coefficients;  $c_1, c_2, \dots$  are **parameters** defined in the model

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**Constraints:**

$$\sum b_{1i} x_i \leq c_1$$

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...

$b_{ji}$  are the constraint coefficients;  $c_1, c_2, \dots$  are **parameters** defined in the model

# Outputs from an optimization

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No optimization exists

More than one solution exists

There exists one unique solution to the problem

Other possibilities, but these are the most recognized



# 4 main types of optimization problems

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Linear programming – objective function and constraints are linear (LP)

Integer linear programming – objective function and constraints are linear, but decision variables MUST be integers (ILP)

Mixed integer linear programming (MILP)– same as ILP with only some decision variables restricted to integers

Non-linear programming – objective function and constraints are continuous, but not all are linear

# Linear Programming

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The **feasible region** is the region defined by the constraints (need to find the optimal solution to the objective function over this region)

One of the easiest solutions for solving a linear programming problem is the **Simplex** method

- Strategy is to move along the edges of the feasible region until the optimal value of the objective function is found

# Example

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Decision variables:  $x_1, x_2$

Find maximum of  $2x_1 + 3x_2$  (this is the objective function)

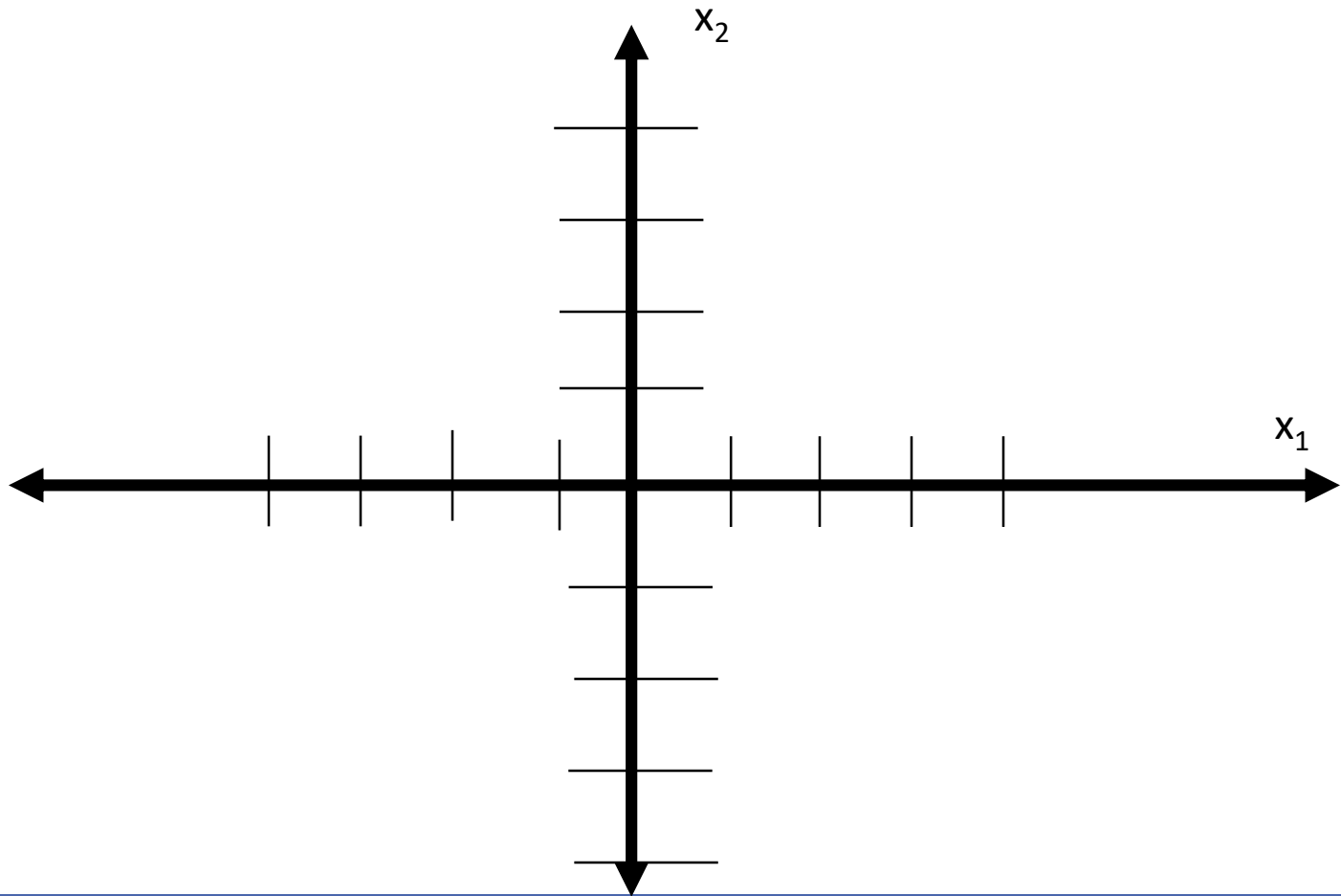
Constraints:

$$0 \leq x_1 \leq 3$$

$$0 \leq x_2 \leq 3$$

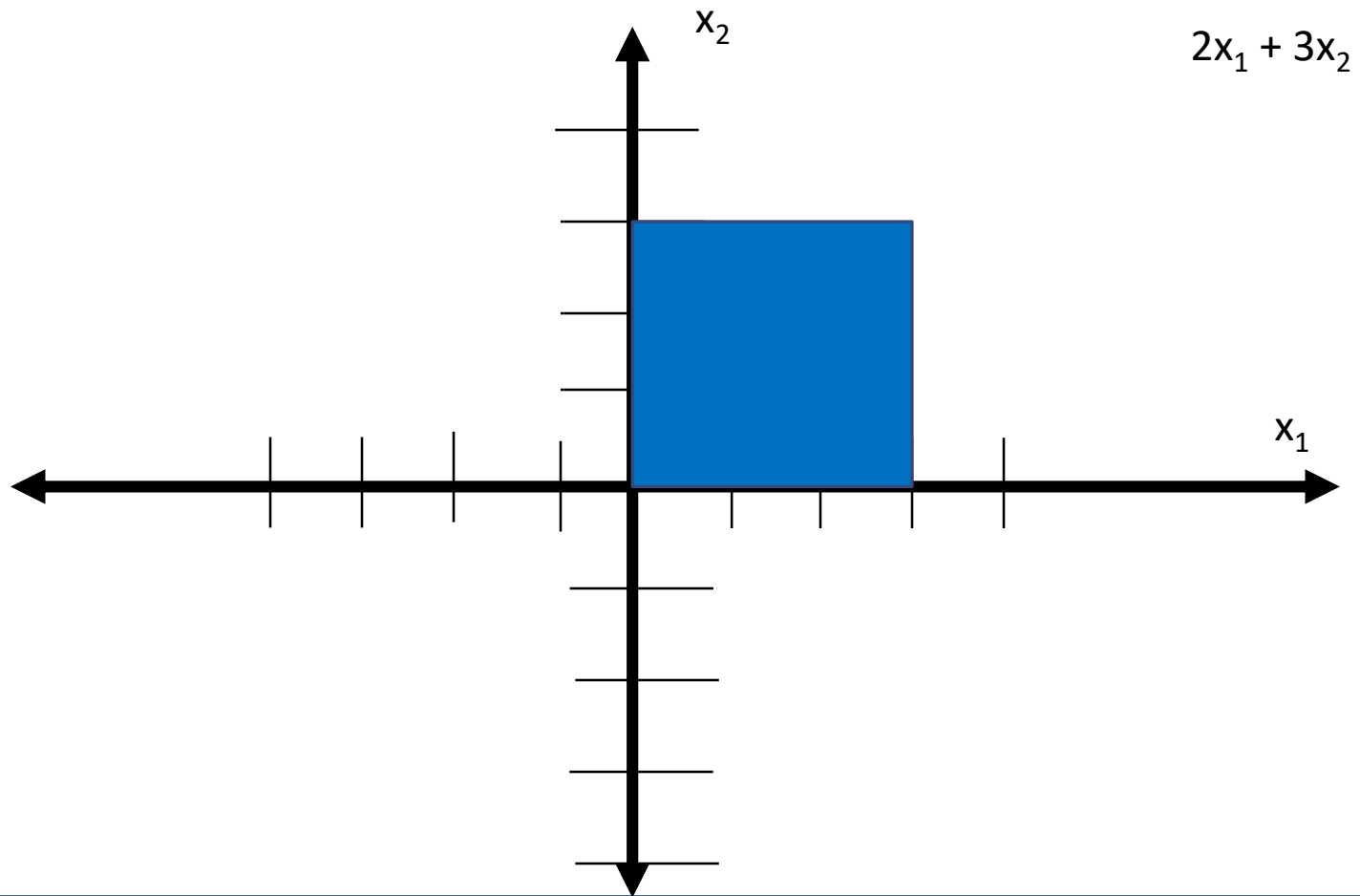
# Feasible Region?

---



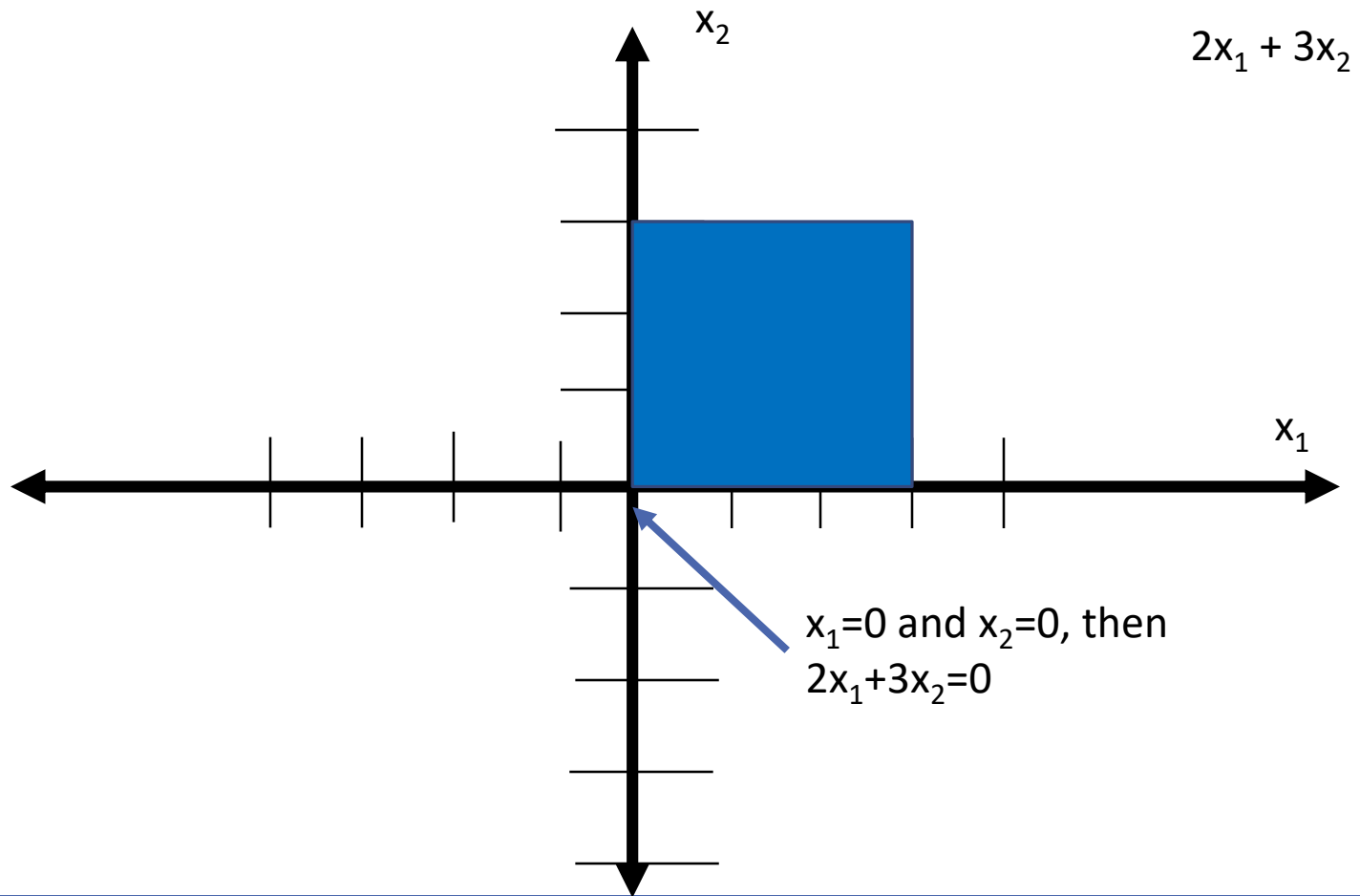
# Feasible Region?

---



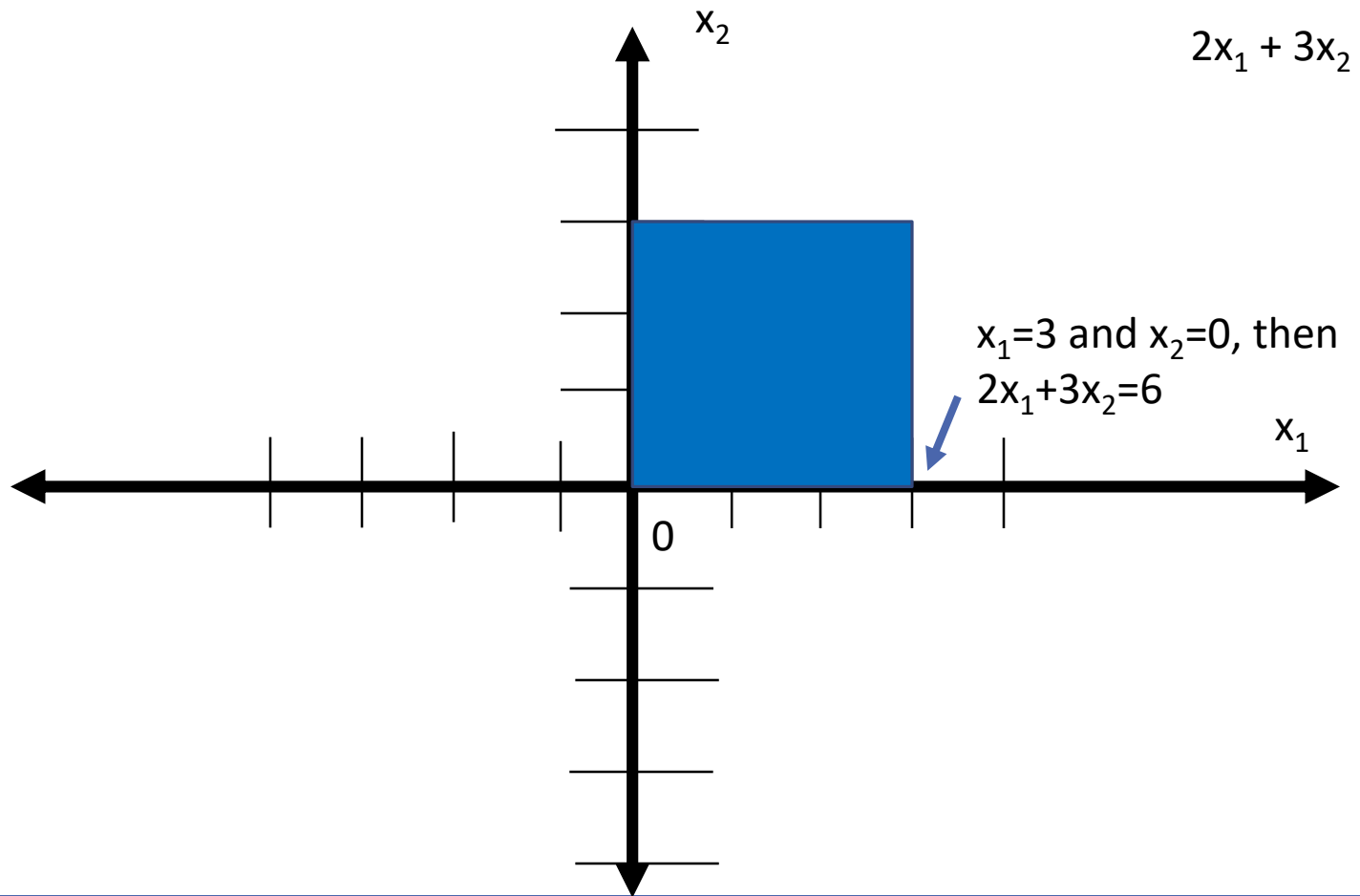
# Feasible Region?

---



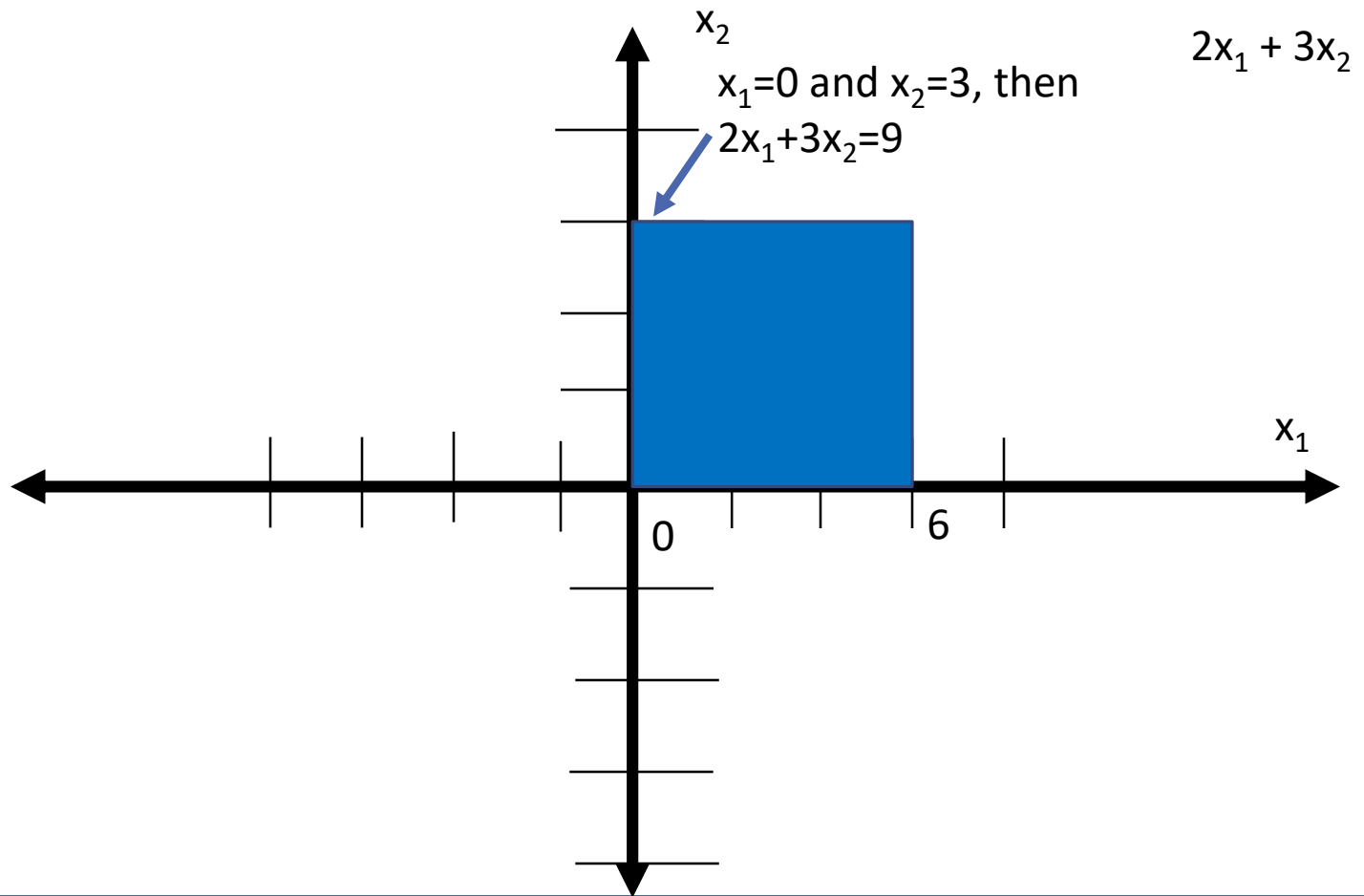
# Feasible Region?

---



# Feasible Region?

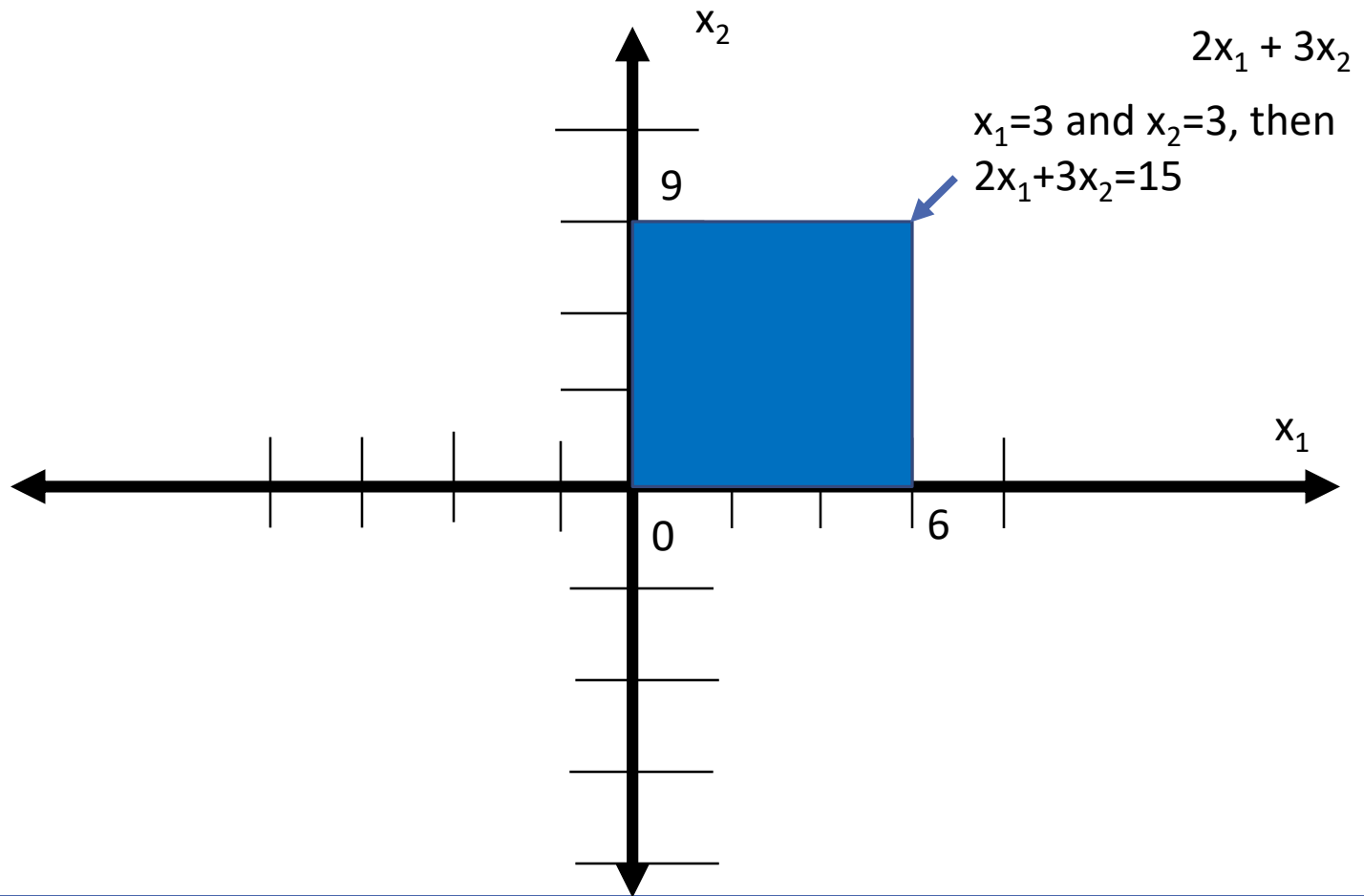
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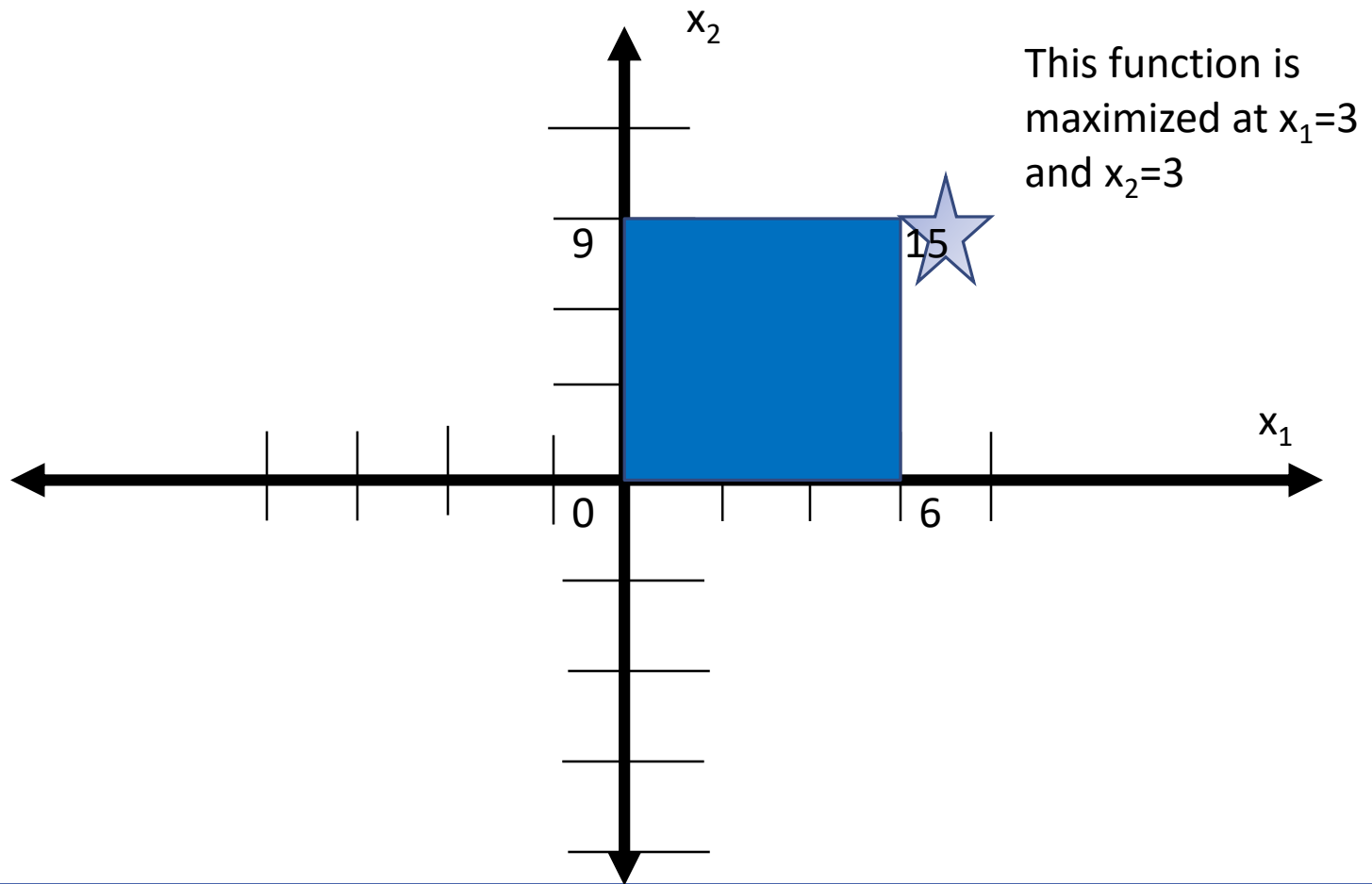
# Feasible Region?

---



# Feasible Region?

---



# Second Example of Simplex algorithm (Chairs=C, Desks=D)

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MAXIMIZE Profit:  $15C + 24D$

CONSTRAINTS:

$$3C + 5D \leq 2400$$

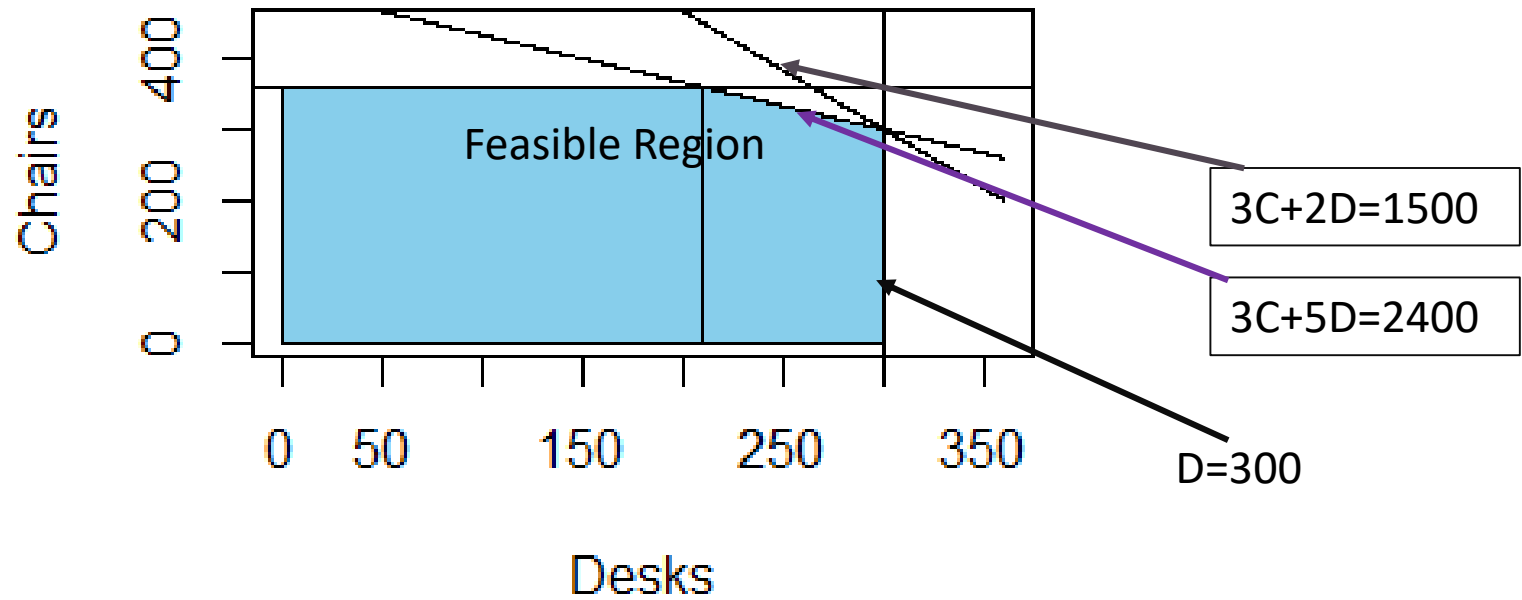
$$3C + 2D \leq 1500$$

$$0 \leq C \leq 360$$

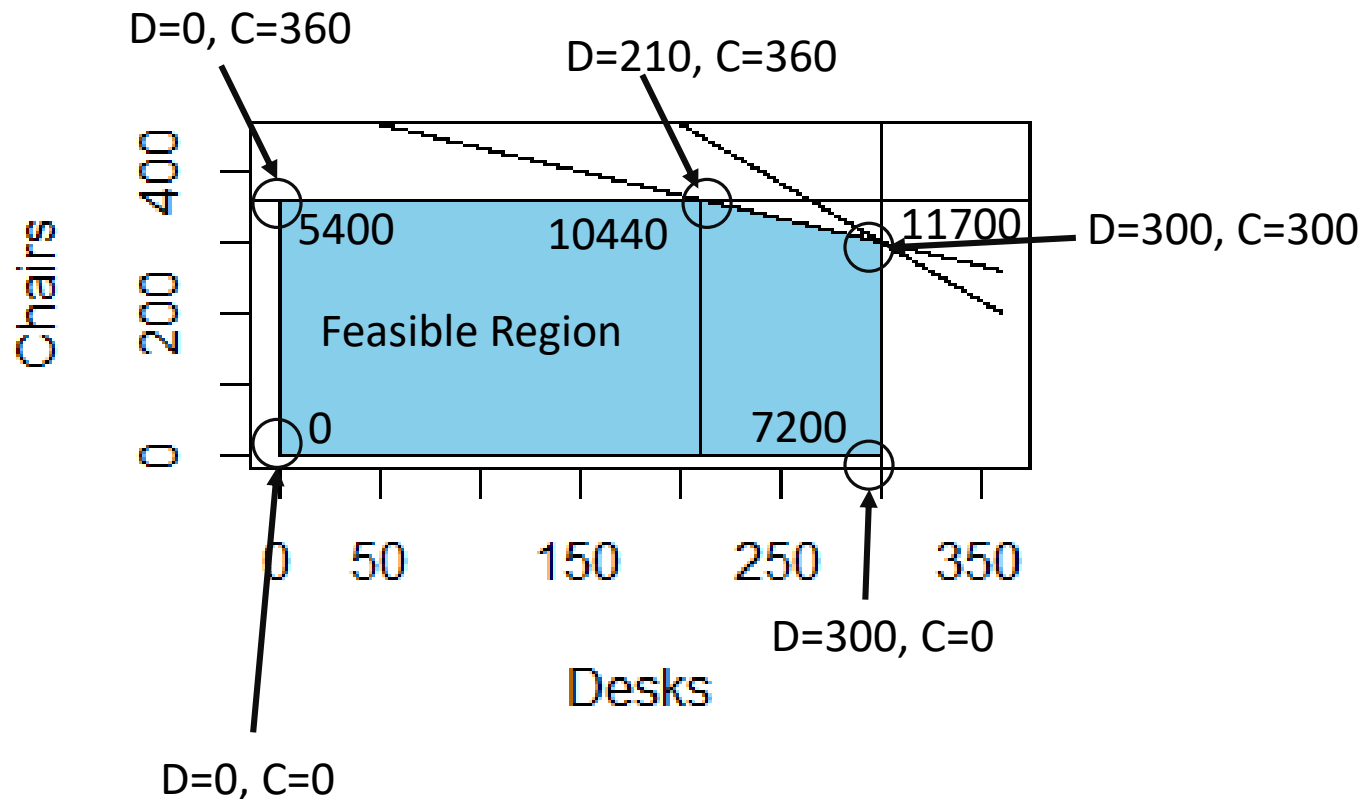
$$0 \leq D \leq 300$$

# Feasible region

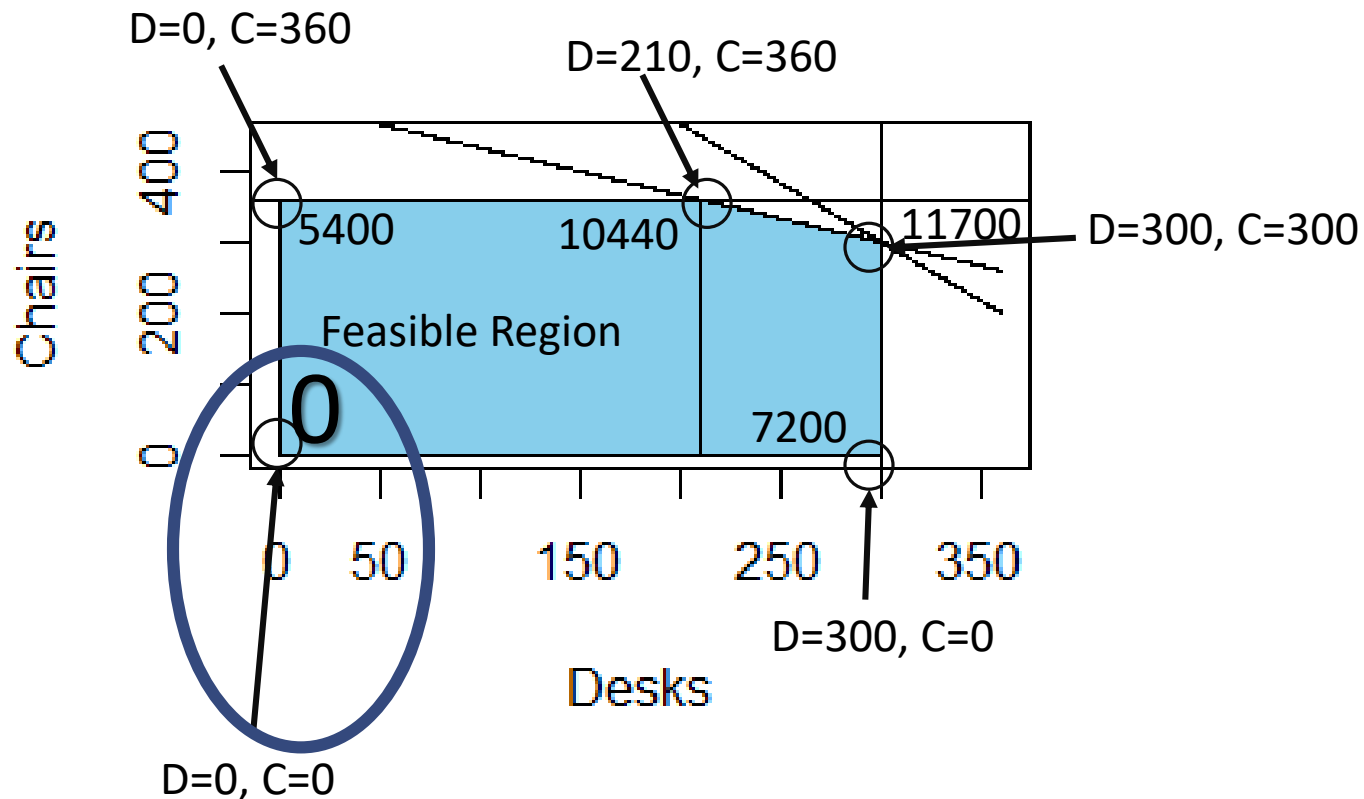
---



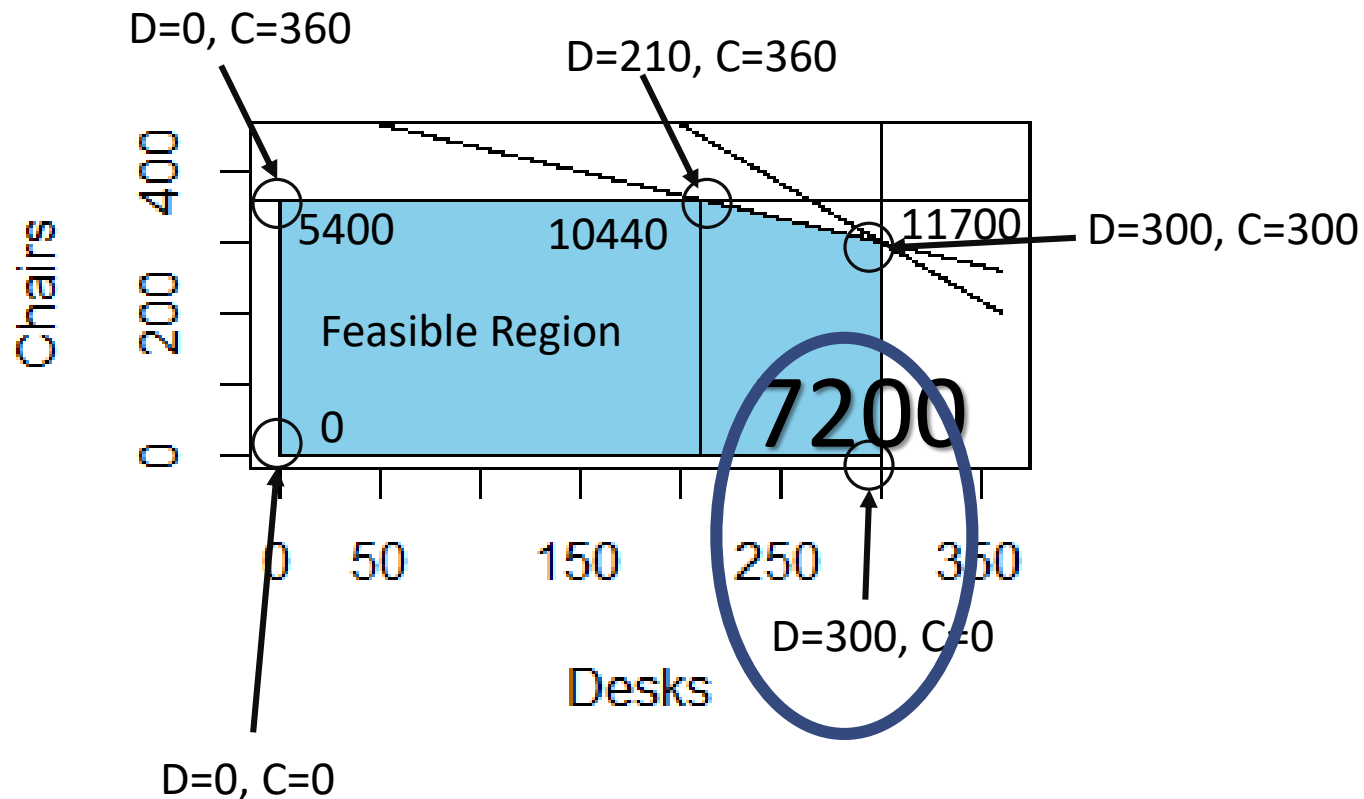
# Simplex method



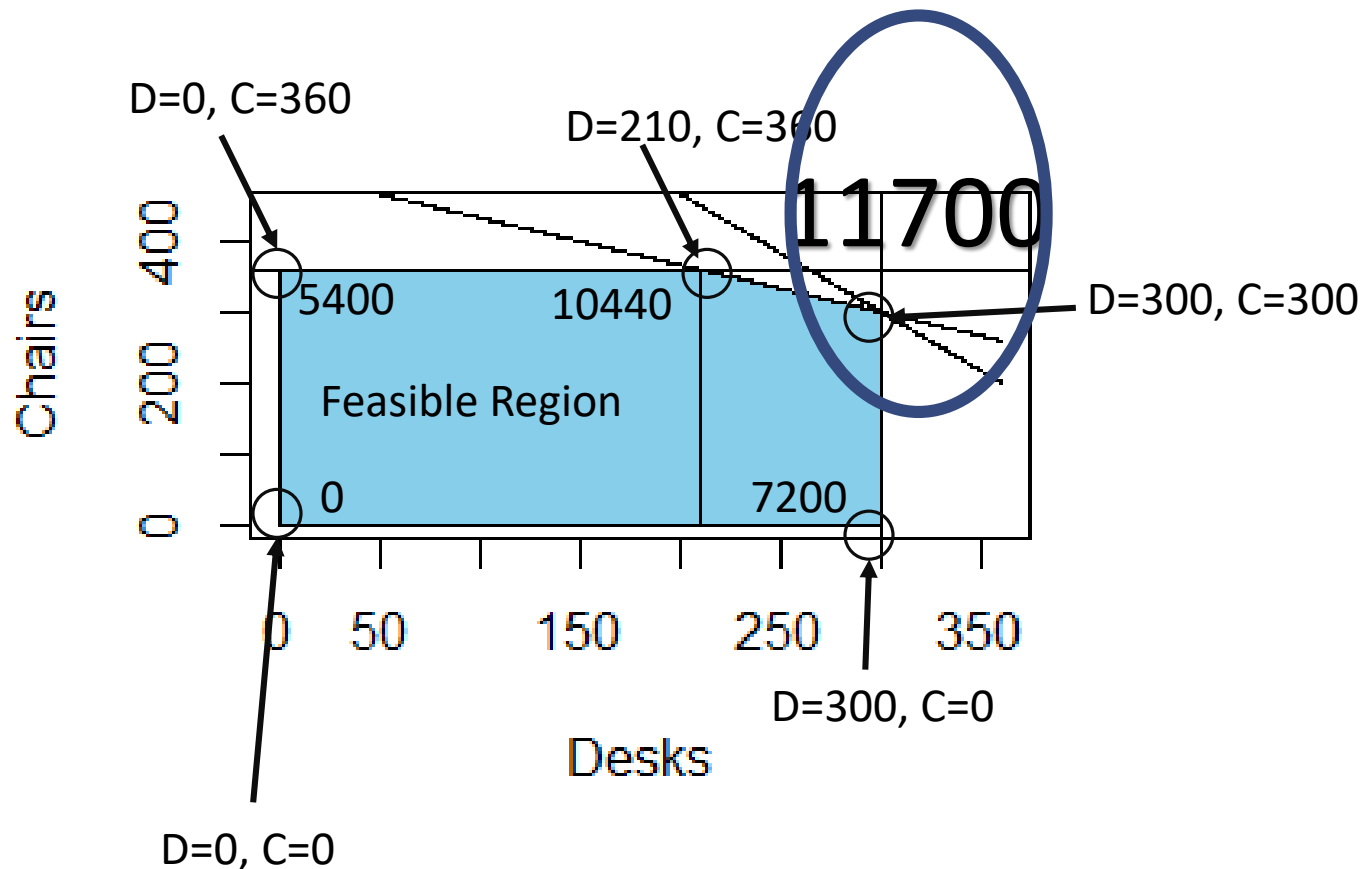
# Simplex method



# Simplex method

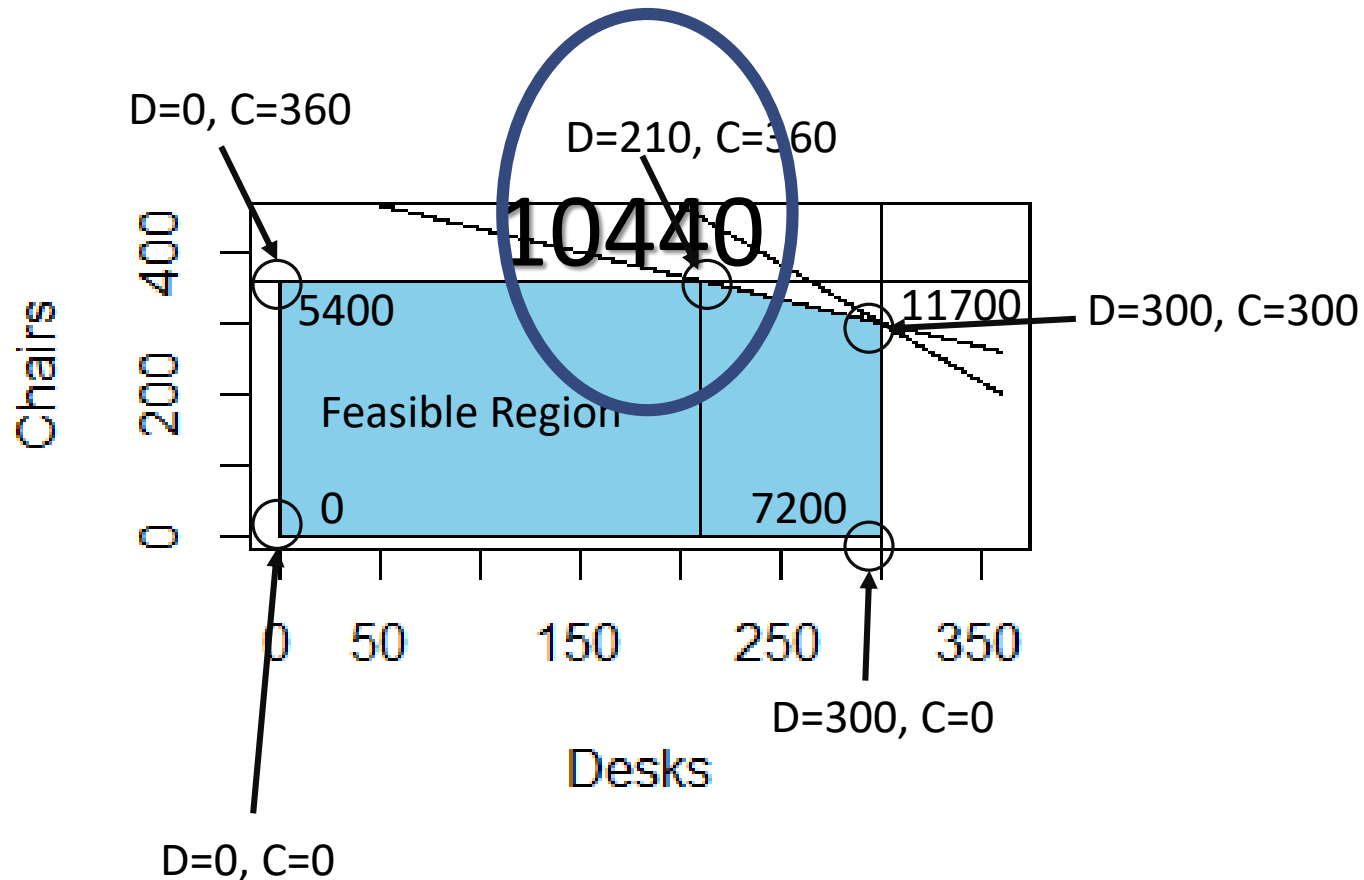


# Simplex method

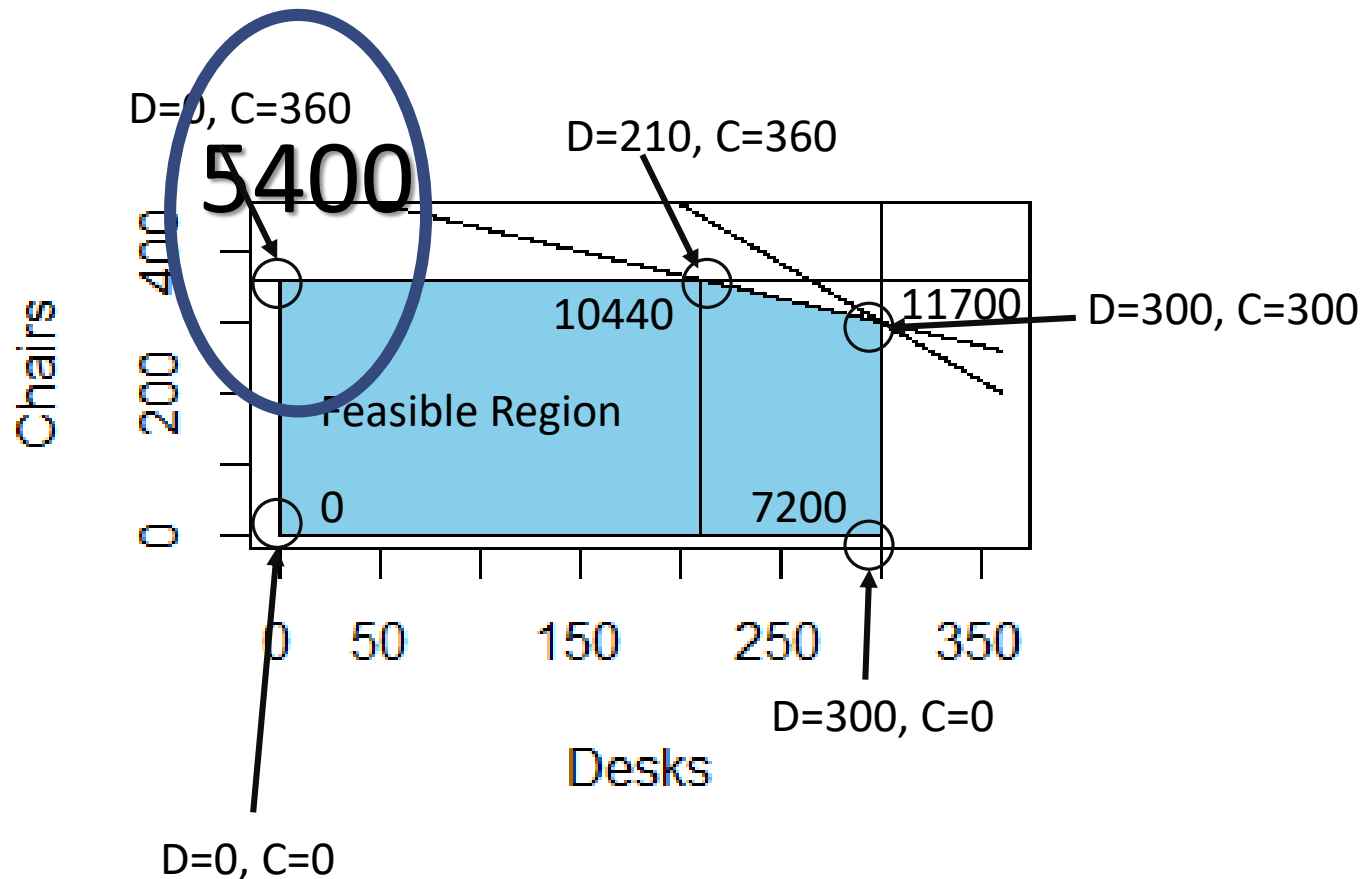




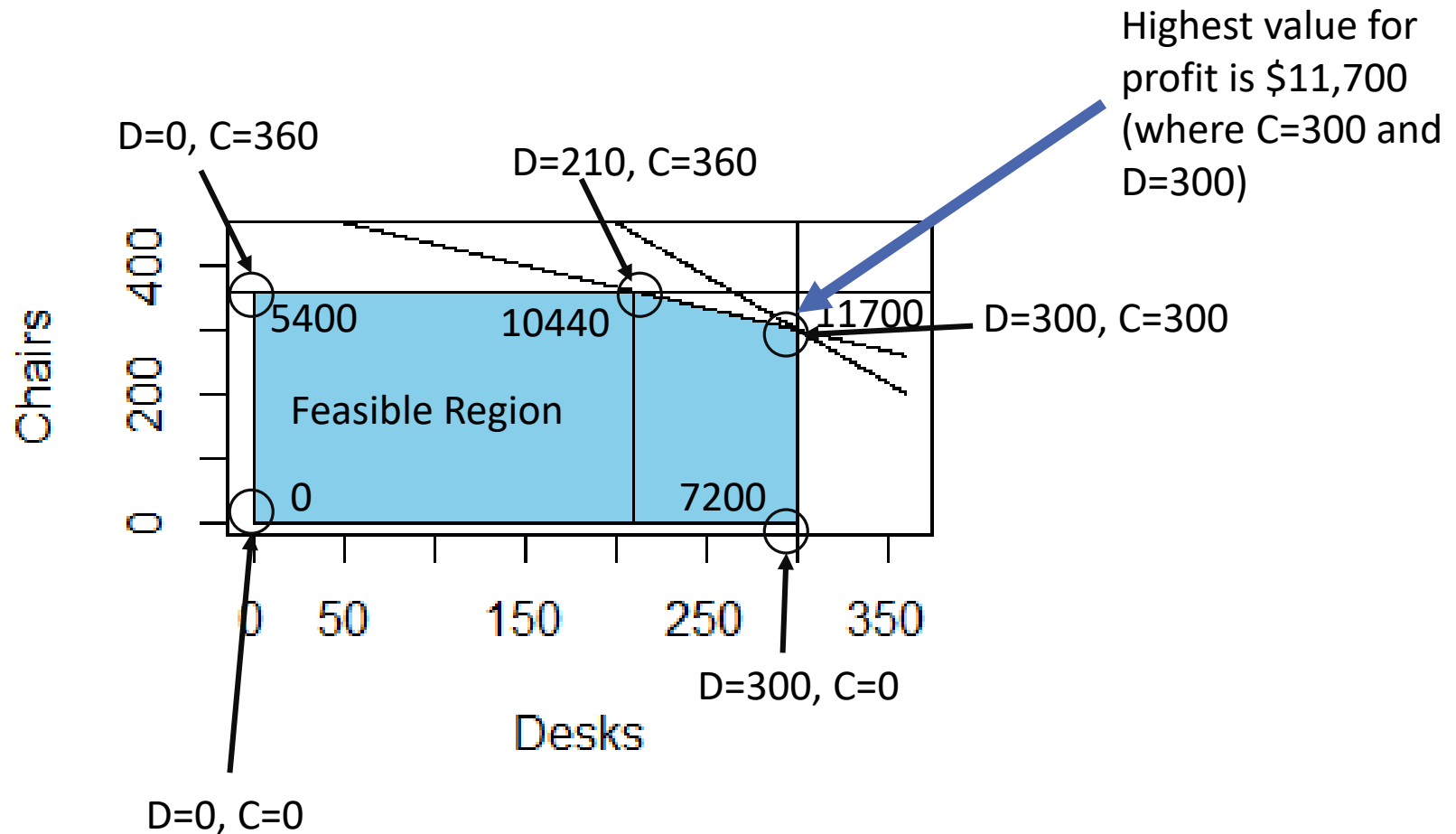
# Simplex method



# Simplex method



# Simplex method



# Example

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Veerman Furniture Company makes chairs, desks and tables with the following information

	Hours per unit			
Department	Chairs	Desks	Tables	Hours Avail
Fabrication	4	6	2	1850
Assembly	3	5	7	2400
Shipping	3	2	4	1500
Demand potential	360	300	100	
Profit	\$15	\$24	\$18	

Want to maximize profit

# Example:

---

Objective function:

- MAXIMIZE:  $15C + 24D + 18T$

Constraints:

- Fabri:  $4C + 6D + 2T \leq 1850$
- Assem:  $3C + 5D + 7T \leq 2400$
- Shipp:  $3C + 2D + 4T \leq 1500$
- $C \leq 360$
- $D \leq 300$
- $T \leq 100$
- $C \geq 0, D \geq 0, T \geq 0$

# SAS Code

---


```
proc optmodel;  
var Chairs>=0, Desks>=0, Tables>=0;  
max Profit = 15*Chairs + 24*Desks + 18*Tables;  
con Assembly: 3*Chairs + 5*Desks + 7*Tables<=2400;  
con Shipping: 3*Chairs + 2*Desks + 4*Tables<=1500;  
con Fabrication: 4*Chairs+6*Desks+2*Tables<=1850;  
con DemandC: Chairs <=360;  
con DemandD: Desks<=300;  
con DemandT: Tables<=100;  
solve with lp;  
print Chairs Desks Tables;  
quit;
```

# SAS Code

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proc optmodel;  
var Chairs>=0, Desks>=0, Tables>=0;  
max Profit = 15*Chairs + 24*Desks + 18*Tables;  
con Assembly: 3*Chairs + 5*Desks + 7*Tables<=2400;  
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solve with lp;  
print Chairs Desks Tables;  
quit;
```

Define decision  
variables




# SAS Code

---

```
proc optmodel;  
var Chairs>=0, Desks>=0, Tables>=0;  
max Profit = 15*Chairs + 24*Desks + 18*Tables;  
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solve with lp;  
print Chairs Desks Tables;  
quit;
```

Define objective  
function





# SAS Code

---

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quit;
```

Define constraints



# SAS Code

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print Chairs Desks Tables;  
quit;
```

Call the solver



# SAS Code

---

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con DemandC: Chairs <=360;  
con DemandD: Desks<=300;  
con DemandT: Tables<=100;  
solve with lp;  
print Chairs Desks Tables;  
quit;
```

Print the results

# Output

---

## The SAS System

### The OPTMODEL Procedure

Problem Summary	
Objective Sense	Maximization
Objective Function	Profit
Objective Type	Linear
Number of Variables	3
Bounded Above	0
Bounded Below	3
Bounded Below and Above	0
Free	0
Fixed	0
Number of Constraints	6
Linear LE ( $\leq$ )	6

# Output cont

---

Chairs	Desks	Tables
0	275	100

## The OPTMODEL Procedure

Solution Summary	
Solver	LP
Algorithm	Dual Simplex
Objective Function	Profit
Solution Status	Optimal
Objective Value	8400
Primal Infeasibility	0
Dual Infeasibility	0
Bound Infeasibility	0
Iterations	2
Presolve Time	0.00
Solution Time	0.00

# Gurobi in Python

```
from gurobipy import *

# Create a new model
m = Model("Veerman")

# Create variables
c = m.addVar(vtype=GRB.CONTINUOUS, lb=0,
name="Chair")
d = m.addVar(vtype=GRB.CONTINUOUS, lb=0,
name="Desk")
t = m.addVar(vtype=GRB.CONTINUOUS, lb=0,
name="Table")

# Set objective
m.setObjective(15*c+24*d+18*t, GRB.MAXIMIZE)
```

```
# Add constraints
m.addConstr(4*c + 6*d + 2*t <=
1850, "c0")
m.addConstr(3*c + 5*d + 7*t <=
2400, "c1")
m.addConstr(3*c + 2*d + 4*t <=
1500, "c2")

m.addConstr(c <= 360, "c3")
m.addConstr(d <= 300, "c4")
m.addConstr(t <= 100, "c5")

m.optimize()

for v in m.getVars():
    print('%s %g' % (v.varName, v.x))
print('Obj: %g' % m.objVal)
```

# Gurobi in Python

```
from gurobipy import *
```

```
# Create a new model  
m = Model("Veerman")
```

**DEFINE MODEL**



```
# Create variables
```

```
c = m.addVar(vtype=GRB.CONTINUOUS, lb=0,  
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```

```
d = m.addVar(vtype=GRB.CONTINUOUS, lb=0,  
name="Desk")
```

```
t = m.addVar(vtype=GRB.CONTINUOUS, lb=0,  
name="Table")
```

```
# Set objective
```

```
m.setObjective(15*c+24*d+18*t, GRB.MAXIMIZE)
```

```
# Add constraints
```

```
m.addConstr(4*c + 6*d + 2*t <=  
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m.addConstr(c <= 360, "c3")
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m.addConstr(d <= 300, "c4")
```

```
m.addConstr(t <= 100, "c5")
```

```
m.optimize()
```

```
for v in m.getVars():
```

```
    print('%s %g' % (v.varName, v.x))
```

```
print('Obj: %g' % m.objVal)
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2400, "c1")
m.addConstr(3*c + 2*d + 4*t <=
1500, "c2")
← DEFINE DECISION VARIABLES
m.addConstr(c <= 360, "c3")
m.addConstr(d <= 300, "c4")
m.addConstr(t <= 100, "c5")

m.optimize()

for v in m.getVars():
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```



# Gurobi in Python

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t = m.addVar(vtype=GRB.CONTINUOUS, lb=0,  
name="Table")
```

```
# Set objective  
m.setObjective(15*c+24*d+18*t, GRB.MAXIMIZE)
```

```
# Add constraints
```

```
m.addConstr(4*c + 6*d + 2*t <= 1850, "c0")  
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m.addConstr(3*c + 2*d + 4*t <= 1500, "c2")
```

```
m.addConstr(c <= 360, "c3")  
m.addConstr(d <= 300, "c4")  
m.addConstr(t <= 100, "c5")
```

```
m.optimize()
```

**DEFINE OBJECTIVE FUNCTION**

```
for v in m.getVars():  
    print('%s %g' % (v.varName, v.x))  
print('Obj: %g' % m.objVal)
```

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```
# Add constraints
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m.addConstr(3*c + 5*d + 7*t <=
2400, "c1")
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1500, "c2")

m.addConstr(c <= 360, "c3")
m.addConstr(d <= 300, "c4")
m.addConstr(t <= 100, "c5")

m.optimize()

DEFINE CONSTRAINTS
for v in m.getVars():
    print('%s %g' % (v.varName, v.x))
print('Obj: %g' % m.objVal)
```

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1500, "c2")
```

```
m.addConstr(c <= 360, "c3")
m.addConstr(d <= 300, "c4")
m.addConstr(t <= 100, "c5")
```

```
m.optimize()
```

**TELL IT TO OPTIMIZE**

```
for v in m.getVars():
    print('%s %g' % (v.varName, v.x))
print('Obj: %g' % m.objVal)
```

# Gurobi in Python

```
from gurobipy import *

# Create a new model
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# Create variables
c = m.addVar(vtype=GRB.CONTINUOUS, lb=0,
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name="Desk")
t = m.addVar(vtype=GRB.CONTINUOUS, lb=0,
name="Table")


# Set objective
m.setObjective(15*c+24*d+18*t, GRB.MAXIMIZE)
```

```
# Add constraints
m.addConstr(4*c + 6*d + 2*t <=
1850, "c0")
m.addConstr(3*c + 5*d + 7*t <=
2400, "c1")
m.addConstr(3*c + 2*d + 4*t <=
1500, "c2")
```

```
m.addConstr(c <= 360, "c3")
m.addConstr(d <= 300, "c4")
m.addConstr(t <= 100, "c5")
```

```
m.optimize()
```

**PRINT RESULTS**



```
for v in m.getVars():
    print('%s %g' % (v.varName, v.x))
print('Obj: %g' % m.objVal)
```

# Output from Gurobi (Python)

---

Solved in 1 iterations and 0.02 seconds

Optimal objective 8.400000000e+03

Chair 0

Desk 275

Table 100

Obj: 8400

# Example (recall..):

---

Objective function:

- MAXIMIZE:  $15C + 24D + 18T$

Constraints:

- Fabri:  $4C + 6D + 2T \leq 1850$
- Assem:  $3C + 5D + 7T \leq 2400$
- Shipp:  $3C + 2D + 4T \leq 1500$
- $C \leq 360$
- $D \leq 300$
- $T \leq 100$
- $C \geq 0, D \geq 0, T \geq 0$

# Gurobi in R

---

```
library(gurobi)
library(prioritizr)
model <- list()
model$obj      <- c(15,24,18)
model$model sense <- "max"
model$rhs      <- c(1850,2400,1500,360,300,100)
model$sense    <- c("<=", "<=", "<=", "<=", "<=", "<=")
model$vttype   <- "C"
model$A        <- matrix(c(4,6,2,3,5,7,3,2,4,1,0,0,0,1,0,0,0,1),nrow=6,byrow=T)
result <- gurobi(model, list())
print(result$status)
f.names=c('Chairs','Desks','Tables')
names(result$x)=f.names
print(result$x)
print(result$objval)
```

# Gurobi in R

```
library(gurobi)
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model <- list()
model$obj      <- c(15,24,18)
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result <- gurobi(model, list())
print(result$status)
f.names=c('Chairs','Desks','Tables')
names(result$x)=f.names
print(result$x)
print(result$objval)
```

Need to define all parts of optimization  
in a 'list' (we will call it 'model')



# Gurobi in R


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model$modelense <- "max"
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result <- gurobi(model, list())
print(result$status)
f.names=c('Chairs','Desks','Tables')
names(result$x)=f.names
print(result$x)
print(result$objval)
```

The objective function..only put in the coefficients...be sure to note order and MUST keep same order throughout!!

# Gurobi in R

```
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model$rhs      <- c(1850,2400,1500,360,300,100)
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f.names=c('Chairs','Desks','Tables')
names(result$x)=f.names
print(result$x)
print(result$objval)
```

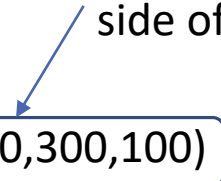
This is where you define if you want to maximize or minimize



# Gurobi in R

```
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model$vttype   <- "C"
model$A        <- matrix(c(4,6,2,3,5,7,3,2,4,1,0,0,0,1,0,0,0,1),nrow=6,byrow=T)
result <- gurobi(model, list())
print(result$status)
f.names=c('Chairs','Desks','Tables')
names(result$x)=f.names
print(result$x)
print(result$objval)
```


These are the values on the right hand side of the constraints (parameters)



# Gurobi in R

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model$vttype   <- "C"
model$A        <- matrix(c(4,6,2,3,5,7,3,2,4,1,0,0,0,1,0,0,0,1),nrow=6,byrow=T)
result <- gurobi(model, list())
print(result$status)
f.names=c('Chairs','Desks','Tables')
names(result$x)=f.names
print(result$x)
print(result$objval)
```

The inequalities for each line of the constraints (the length of the rhs vector should equal length of this vector)




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model$vttype   <- "C"
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result <- gurobi(model, list())
print(result$status)
f.names=c('Chairs','Desks','Tables')
names(result$x)=f.names
print(result$x)
print(result$objval)
```

This indicates decision variables are continuous

# Gurobi in R

```
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model$rhs      <- c(1850,2400,1500,360,300,100)
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model$vttype   <- "C"
model$A        <- matrix(c(4,6,2,3,5,7,3,2,4,1,0,0,0,1,0,0,0,1),nrow=6,byrow=T)
result <- gurobi(model, list())
print(result$status)
f.names=c('Chairs','Desks','Tables')
names(result$x)=f.names
print(result$x)
print(result$objval)
```



These are the coefficients for  
the left hand side of the  
constraints....

# Writing out 'left-hand' side

---

```
model$A <-  
matrix(c(4,6,2,3,5,7,3,2,4,1,0,0,0,1,0,0,0,1),nrow=6,byrow=T)
```



Diagram illustrating the mapping of matrix elements to coefficients in the equations. Arrows point from the first three columns of the matrix (4, 6, 2; 3, 5, 7; 3, 2, 4) to the coefficients of C, D, and T in the equations.

$$4C + 6D + 2T$$

$$3C + 5D + 7T$$

$$3C + 2D + 4T$$

$$C$$


$$D$$

$$T$$

byrow=T tells R that  
the numbers should be  
read 'by rows'

# Gurobi in R

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model$vttype   <- "C"
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result <- gurobi(model, list())
print(result$status)
f.names=c('Chairs','Desks','Tables')
names(result$x)=f.names
print(result$x)
print(result$objval)
```




Runs the model



# Gurobi in R

```
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result <- gurobi(model, list())
print(result$status)
f.names=c('Chairs','Desks','Tables')
names(result$x)=f.names
print(result$x)
print(result$objval)
```



Print the output (f.names is just to make it look nicer and to label the output)

# Output from Gurobi (R)

---

```
print(result$status)
```

```
[1] "OPTIMAL"
```

```
> f.names=c('Chairs', 'Desks', 'Tables')
```

```
> names(result$x)=f.names
```

```
> print(result$x)
```

```
Chairs Desks Tables 0 275 100
```

```
> print(result$objval) [1] 8400
```