Norm_Asymp_WithMLE.R

This simulation generates data from a N(0.5,1) distribution and observes the asymptotic behavior of ECIC using the model set $\mathcal{M} = \{N(0,1), N(\mu, 1), N(\mu, \sigma)\}$

Warning: package 'RcppArmadillo' was built under R version 4.0.5

```
# load C++ script that is used for simulation steps in ECIC
sourceCpp("FnsInCPlusPlus\\Simulation_Rcpp_Fns_Norm.cpp")
# load function in written in R
source("FnsInR\\Simulation_R_Fns.R")
# set true normal model parameters
trueMu <- 0.5
trueSig <- 1</pre>
trueParams <- c("trueMu"=trueMu, "trueSig"=trueSig)</pre>
trueModel <- "N(0.5,1)"
MNames \leftarrow c("N(0,1)","N(mu,1)","N(mu,sigma)")
# model that should be selected
closestMod <- "N(mu,1)"</pre>
# cardinality of the model set
MLen <- length(MNames)</pre>
M <- list()
for(i in 1:MLen)
  M[[i]] <- MNames[i]</pre>
}
# set different sample sizes
ns \leftarrow c(3,10,50,100,200)
# cardinality of the sample sizes
nsLen <- length(ns)</pre>
# set the number of draws for each sample size
noDraws <- 200
# sample size for estimating the probability of choosing the observed best
# model under the assumption an
# alternative model is true
```

```
N1 <- 300
# sample size for simulating the DGOF distribution under the assumption that
# an alternative model is true
N2 <- 700
# pre-specified type-1 error rate
alpha <- 0.15
datList <- list()</pre>
set.seed(225)
# generate data from the true normal distribution
for(i in 1:nsLen)
 tempN <- ns[i]</pre>
  datList[[i]] <- generateData(tempN,noDraws,trueParams,"Normal")</pre>
}
# compute MLE estimates from the generated data
MLEList <- list()</pre>
for(i in 1:nsLen)
 MLEList[[i]] <- list()</pre>
}
for(i in 1:nsLen)
  tempN <- ns[i]</pre>
  tempDatList <- datList[[i]]</pre>
  tempMeanMLEs <- apply(X=tempDatList, MARGIN=2, FUN=function(x) mean(x))
  tempSigMLEs <- apply(X=tempDatList, MARGIN=2, FUN=function(x) sd(x))</pre>
  # convert from unbiased estimate to MLE
  tempSigMLEs <- tempSigMLEs*sqrt((tempN-1))/sqrt(tempN)</pre>
  # MLE's for N(0,1) (just 0,1 b/c no parameter estimation)
  MLEList[[i]][[1]] <- matrix(rep(c(0,1),noDraws),nrow=2,ncol=noDraws)
  rownames(MLEList[[i]][[1]]) <- c("fixedMean", "fixedsig")</pre>
  # MLE's for N(mu,1)
  MLEList[[i]][[2]] <- rbind(tempMeanMLEs,1)</pre>
  rownames(MLEList[[i]][[2]]) <- c("MLEMean", "fixedSig")</pre>
  # MLE's for N(mu, sigma)
 MLEList[[i]][[3]] <- rbind(tempMeanMLEs,tempSigMLEs)</pre>
  rownames(MLEList[[i]][[3]]) <- c("MLEMean", "MLESig")</pre>
  colnames(MLEList[[i]][[1]]) <- colnames(MLEList[[i]][[2]]) <-</pre>
    colnames(MLEList[[i]][[3]]) <- paste("Draw",1:noDraws,sep="")</pre>
 names(MLEList[[i]]) <- paste("MLEs for Model", MNames)</pre>
names(MLEList) <- paste("Draws of n=",ns,sep="")</pre>
Begin ECIC
# ECIC step #1
# compute the IC under each model in the model set for each sample size
ICComps <- list()</pre>
for(i in 1:nsLen)
```

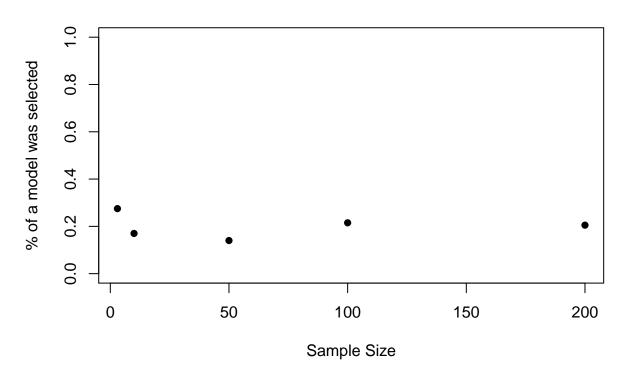
```
ICComps[[i]] <- ICComputations(datMat=datList[[i]],M=M,MLen=MLen,</pre>
                                   noDraws=noDraws,
                                   ICType="BICNorm", MNames=MNames)
names(ICComps) <- paste("True Model",trueModel,",Draws of n=",ns,sep="")</pre>
# ECIC step #2
# determine the observed best models for each draw of each sample size
MbList <- list()</pre>
for(i in 1:nsLen)
  MbList[[i]] <- MbComputations(ICComps[[i]],MNames)</pre>
names(MbList) <- paste("Mbs for ","Draws of n=",ns,sep="")</pre>
# ECIC step #3
# compute the observed DGOFs for each draw of each sample size
obsDGOFs <- list()</pre>
obsDGOFs <- obsDGOFsComputations(ICComps,nsLen)</pre>
# ECIC step #4
set.seed(19)
ptm <- proc.time() #Start timing</pre>
simDat1List <- normDatSimRcpp(ns,MLEList,N1)</pre>
## Iteration 1 Complete
## Iteration 2 Complete
## Iteration 3 Complete
## Iteration 4 Complete
## Iteration 5 Complete
simDat2List <- normDatSimRcpp(ns,MLEList,N2)</pre>
## Iteration 1 Complete
## Iteration 2 Complete
## Iteration 3 Complete
## Iteration 4 Complete
## Iteration 5 Complete
proc.time() - ptm
##
      user system elapsed
##
     17.23
              0.99
                     13.02
names(simDat1List) <- paste("Draws of n=",ns,sep="")</pre>
names(simDat2List) <- paste("Draws of n=",ns,sep="")</pre>
# provide names for both simulated sets
for(i in 1:nsLen)
  for(j in 1:MLen) # indexes the models in the model set
```

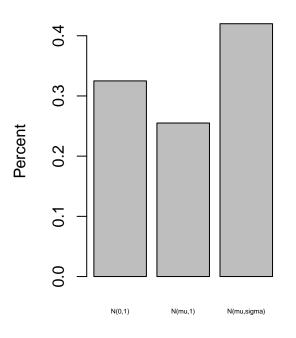
```
names(simDat1List[[i]][[j]]) <- paste("Obs",1:noDraws,";",N1,</pre>
                                             "Simulated Draws")
    names(simDat2List[[i]][[j]]) <- paste("Obs",1:noDraws,";",N2,</pre>
                                             "Simulated Draws")
  names(simDat1List[[i]]) <- paste("Generated from", MNames)</pre>
  names(simDat2List[[i]]) <- paste("Generated from", MNames)</pre>
}
# simulate distributions to estimate probabilities
ptm=proc.time()
ICsSimDat1 <- ICCompsRcpp(simDat1List,MNames)</pre>
## Its. for Sample Size Index 1 completed
## Its. for Sample Size Index 2 completed
## Its. for Sample Size Index 3 completed
## Its. for Sample Size Index 4 completed
## Its. for Sample Size Index 5 completed
proc.time() - ptm
      user system elapsed
##
     10.83
              0.34
                      11.68
# label the elements in ICsSimDat1
for(i in 1:nsLen)
  for(j in 1:MLen)
    for(k in 1:noDraws)
      colnames(ICsSimDat1[[i]][[j]][[k]]) <- paste("BIC Under", MNames)</pre>
    names(ICsSimDat1[[i]][[j]]) <- paste("Normal Fit for Obs",1:noDraws)</pre>
  }
  names(ICsSimDat1[[i]]) <- paste("Generated from", MNames)</pre>
names(ICsSimDat1) <- paste("Draws of n=",ns,sep="")</pre>
# determine the model with the minimum IC for each set of draws
minICList <- list()</pre>
for(i in 1:nsLen)
  minICList[[i]] <- list()</pre>
  for(j in 1:MLen)
    minICList[[i]][[j]] <- list()</pre>
for(i in 1:nsLen) # i indexes sample size
  for(j in 1:MLen) # j indexes assumed true parameter
```

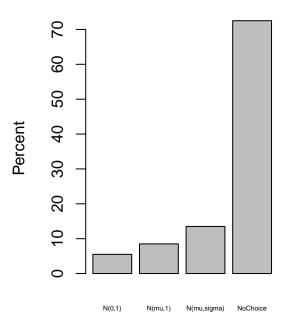
```
for(k in 1:noDraws)
      minICList[[i]][[j]][[k]] <- apply(ICsSimDat1[[i]][[j]][[k]],</pre>
                                           MARGIN=1, FUN=function(x)
                                              MNames[which.min(x)])
    }
    names(minICList[[i]][[j]]) <- paste("Normal Fit for Obs",1:noDraws)</pre>
  names(minICList[[i]]) <- paste("Generated from", MNames)</pre>
  print(i)
}
## [1] 1
## [1] 2
## [1] 3
## [1] 4
## [1] 5
names(minICList) <- paste("Draws of n=",ns,sep="")</pre>
# ECIC step #4b
# create a list of matrices that hold P i(q(F)=M b)
piHatList <- list()</pre>
for(i in 1:nsLen)
  piHatList[[i]] <- list()</pre>
  for(k in 1:noDraws)
    piHatList[[i]][[k]] <- list()</pre>
  names(piHatList[[i]]) <- paste("Normal Fit for Obs",1:noDraws)</pre>
names(piHatList) <- names(piHatList) <- paste("n=",ns,sep="")</pre>
# compute the probabilities
for(i in 1:nsLen) # indexes the sample size
  piHatList[[i]] <- piHatMatComputationsMLEs(minICList[[i]], MLen, N1,</pre>
                                                 MNames, noDraws)
  print(i)
## [1] 1
## [1] 2
## [1] 3
## [1] 4
## [1] 5
names(piHatList) <- paste("n=",ns,sep="")</pre>
rm(ICsSimDat1)
rm(minICList)
gc()
```

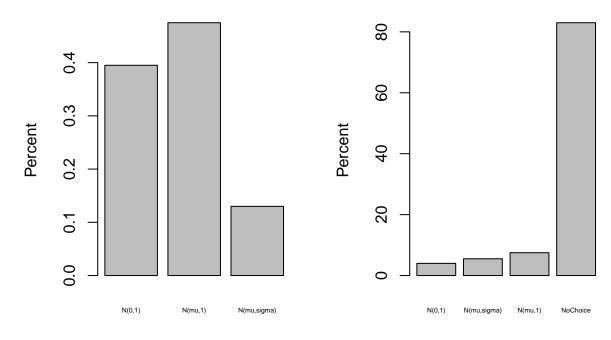
```
(Mb) gc trigger
                                     (Mb) max used
             used
## Ncells
           636272 34.0
                           1351012 72.2
                                           1351012 72.2
## Vcells 219059070 1671.3 335451809 2559.3 224879514 1715.7
# ECIC step #4c
DGOFList <- simDGOFsRcpp(simDat2List,MNames)</pre>
## Its. for Sample Size Index 1 completed
## Its. for Sample Size Index 2 completed
## Its. for Sample Size Index 3 completed
## Its. for Sample Size Index 4 completed
## Its. for Sample Size Index 5 completed
# label the elements in DGOFList
for(i in 1:nsLen)
 for(j in 1:MLen)
   for(k in 1:noDraws)
     colnames(DGOFList[[i]][[j]][[k]]) <- paste("DGOF Under", MNames,</pre>
                                             " Observed Best")
   }
   names(DGOFList[[i]][[j]]) <- paste("Normal Fit for Obs",1:noDraws)</pre>
 }
 names(DGOFList[[i]]) <- paste("Generated from", MNames)</pre>
names(DGOFList) <- paste("Draws of n=",ns,sep="")</pre>
# ECIC steps 4d, 5, and 6
resultList <- ECICDecisionsMLEs(MbList,obsDGOFs,piHatList,DGOFList,alpha,
                             MNames, nsLen, MLen, noDraws)
## [1] 1
## [1] 2
## [1] 3
## [1] 4
## [1] 5
Plot Results
# list to store the decision thresholds
thresholds <- resultList[[1]]</pre>
# decision list
aOrRList <- resultList[[2]]
# assess observed best model with ECIC choice
assessList <- list()</pre>
for(i in 1:nsLen)
```

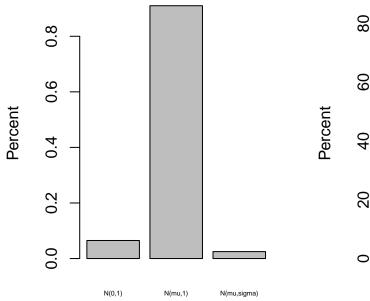
Proportion of runs a model was selected

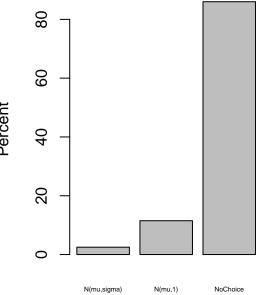


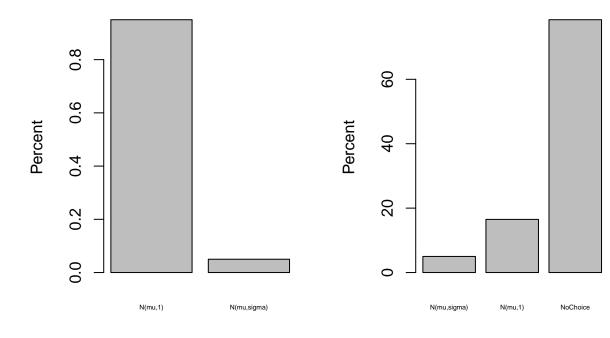


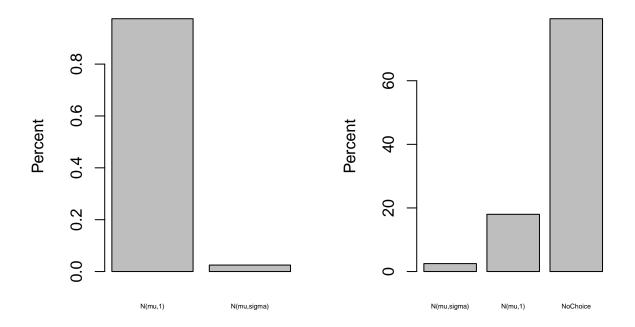




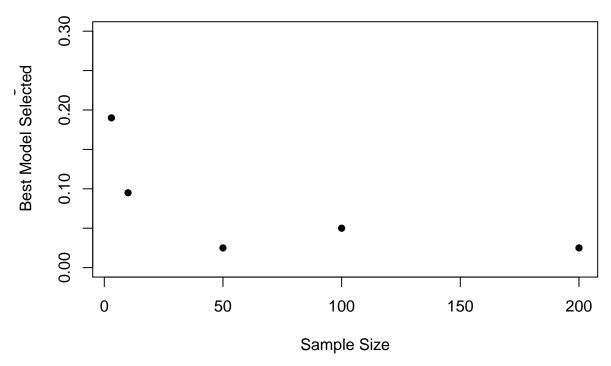








Type 1 Error Rates by Sample Size at alpha= 0.15



Rate that correct model was selected

