

Physik HÜ 1.2) 1-5

1) a)

$$m_1 := 35 \cdot 10^{-3} \rightarrow \frac{7}{200} \text{ kg} \quad x := 15 \cdot 10^{-2} \rightarrow \frac{3}{20} \text{ m}$$

$$F := k \cdot x$$

$$F_2 := m_1 \cdot 9.81 \quad k := F = F_2 \xrightarrow{\text{solve}, k} 2.289$$

$$k \xrightarrow{\text{float}, 3} 2.29 \text{ N/m}$$

1) b)

$$m_2 := 60 \cdot 10^{-3} \rightarrow \frac{3}{50} \text{ kg}$$

$$T_F := 2 \cdot \pi \cdot \sqrt{\frac{m_2}{k}} \rightarrow 1.0172614742830297564$$

$$T_F \xrightarrow{\text{float}, 3} 1.02 \text{ s}$$

$$\text{clear } (T_F, m_2, k, m_1, F, F_2, x)$$

2) a)

$$m := 325 \cdot 10^{-3} \rightarrow \frac{13}{40} \text{ kg}$$

$$F_1 := 0.85 \text{ N}$$

$$x := 13.5 \cdot 10^{-2} \rightarrow 0.135 \text{ cm}$$

$$F_2 := k \cdot x$$

$$k := F_1 = F_2 \xrightarrow{\text{solve}, k} 6.2962962962962963$$

$$T_F := 2 \cdot \pi \cdot \sqrt{\frac{m}{k}} \rightarrow 1.4275093787231548601$$

$$T_F \xrightarrow{\text{float}, 3} 1.43 \text{ s} \quad k \xrightarrow{\text{float}, 4} 6.296 \text{ N/m}$$

2) b)

$$E_{pot} = E_{kin} \quad v := \frac{1}{2} \cdot k \cdot x^2 = \frac{1}{2} m \cdot v^2 \xrightarrow[\text{assume, } v > 0]{\text{solve, } v} 0.59420276259617228148$$

$$v \xrightarrow{\text{float}, 2} 0.59 \text{ m/s}^2$$

3)

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clear  $(T_F, m_2, k, m_1, F, F_2, x, m)$ 
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$$T := 2 \cdot \pi \cdot \sqrt{\frac{l}{9.81}}$$

$$l_1 := T = \frac{25}{60} \xrightarrow{\text{solve}, l} 0.043140660227141292496$$

$$l_2 := T = \frac{100}{60} \xrightarrow{\text{solve}, l} 0.690250563563426067994$$

$$\frac{l_1}{l_2} \rightarrow 0.0624999999999999999964$$

Es muss um ca. $1/16$ verkürzt werden.

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clear  $(T_F, m_2, k, m_1, F, F_2, x, m, v)$ 
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4)

a)

$$m := 20 \text{ kg} \quad F := 75 \text{ N} \quad x := 15 \cdot 10^{-2} \rightarrow \frac{3}{20} \text{ m}$$

$$k := \frac{75}{x} \rightarrow 500$$

$$T_F := 2 \cdot \pi \cdot \sqrt{\frac{m}{k}} \rightarrow \frac{2 \cdot \pi}{5} \xrightarrow{\text{float}, 3} 1.26 \text{ s}$$

$$f := \frac{1}{T_F} \xrightarrow{\text{float}, 2} 0.79 \text{ Hz}$$

b)

$$E_{pot} := \frac{1}{2} \cdot k \cdot x^2 \xrightarrow{\text{float}, 3} 5.63 \text{ J} \quad v := \frac{1}{2} \cdot k \cdot x^2 = \frac{1}{2} m \cdot v^2 \xrightarrow[\text{assume, } v > 0]{\text{solve, } v} \frac{3}{4} \text{ m/s}^2$$

$$a := v' = \frac{d}{dx} v \rightarrow v' = 0 \quad \text{m/s}^2$$

c) `clear (v, x, k, v')`

$$x := 15 \cdot 10^{-2} \quad A := 7.5 \cdot 10^{-2}$$

$$k := \frac{F}{x} \rightarrow 500$$

$$\omega := \sqrt{\frac{k}{m}} \rightarrow 5$$

$$a := -A \cdot \omega^2 \cdot \cos(\omega \cdot T_F) \xrightarrow{\text{float}, 3} -1.87 \quad \text{m/s}^2$$

$$v := \sqrt{\frac{k \cdot x^2 + A^2}{m}} \xrightarrow{\text{float}, 3} 0.75 \quad \text{m/s}$$

5) `clear (T_F, m_2, k, m_1, F, F_2, x, m, v)`

$$l := 10 \quad \text{m}$$

$$m := 20 \cdot 10^3 \quad \text{kg} \quad \omega := 0.5 \quad \text{m}$$

$$T_F := 2 \cdot \pi \cdot \sqrt{\frac{l}{9.81}} \xrightarrow{\text{float}} 6.3437398492194134954$$

$$T_F \xrightarrow{\text{float}, 3} 6.34 \quad \text{s}$$

$$E := \frac{1}{2} \cdot m \cdot \left(\sqrt{\frac{m \cdot 9.81}{l} \cdot \omega^2} \right)^2 \xrightarrow{\text{float}} 2452.5 \quad \text{J}$$