SCHENO's Binaries and C++ Classes

Justus Hibshman

April 2024

Outline

- 1 Introduction to SCHENO
- 2 Features of this Repository
- ullet 3 Setup and Compilation
- 4 Using the Executables
- 5 Interface
- 6 Simple Example

1 Introduction to SCHENO

The core idea behind SCHENO is that real-world graphs are messy manifestations of underlying patterns. SCHENO offers a principled way to measure how well you've done at uncovering those patterns.

The formal definitions and explanations can be read in the article located at: LINK

2 Features of This Repository

The code in this repository offers C++ wrappers around the nauty and traces C code. These wrappers provide the following:

- 1. A more convenient interface for the nauty and traces features mentioned in Section 1.
- 2. The ability to call nauty and traces in multiple C++ threads without errors.
- 3. The ability to find the automorphism orbits of $edges^1$.
- 4. The ability to conveniently manipulate graphs in nauty and traces' input format in amortized constant time, rather than needing to re-create the graph every time you want to modify it.
- 5. The ability to specify an initial edge coloring¹.
- 6. The ability to run traces on directed graphs¹.
- 7. A fast "fake" isomorphism algorithm that works on most graphs especially most graphs with varying node degrees².

¹not a direct feature of the original code – requires an augmentation of the input graph

²not associated with nauty or traces – based on the Weisfeiler Lehman algorithm (aka color refinement)

3 Setup and Compilation

Setting up the code is a simple as entering the nt_wrappers folder and running: ./setup.sh

Whatever code you write will need to include the fuke nauty_traces.h from the nt_wrappers folder.

To compile your own code using the wrappers, you will need to include the static library nt_wrappers.a located inside the nt_wrappers folder.

Example compilation:

g++ -Wall -Wextra -o my_output -std=c++11 my_program.cpp nt_wrappers/nt_wrappers.a

3.1 Esoteric Note

If for some reason you want to experience the pain modifying the NTSparseGraph class, you may want to debug it using the SCHENO_NT_SPARSE_GRAPH_FULL_DEBUG_MODE preprocessor flag.

You can see an example of using this feature in test_nt_code.cpp. The flag is defined in nt_wrappers/nt_sparse_graph.h.

- 4 Using the Executables
- 4.1 SCHENO_score
- 4.2 SCHENO_ga

5 Interface

5.1 Essential Components

The key classes and structs you will need are NTSparseGraph which stores a graph that can be loaded directly into nauty and/or traces, NautyTracesOptions which stores info on what you would like nauty/traces to compute, and NautyTracesResults which contains the result of a call to nauty/traces.

5.1.1 NTSparseGraph

}

NTSparseGraph is a subclass of SparseGraph, which is a subgraph of Graph. The NTSparseGraph and the SparseGraph always label their n nodes 0 through n-1.

There are three main ways to get an NTSparseGraph. The first is to load an edge list text file (see Section 5.4), then initialize your nauty/traces graph. For example:

```
#include "nt_wrappers/nauty_traces.h"
     int main( void ) {
         bool directed = 0;
         NTSparseGraph g_nt(read_graph(directed, "nt_test_graphs/karate.txt"));
     }
The second way is to build up the graph from scratch using the add_edge() function. For example:
     #include "nt_wrappers/nauty_traces.h"
     int main( void ) {
         bool directed = 1;
         size_t n = 12;
         NTSparseGraph g_nt(directed, n);
         g_nt.add_edge(0, 5);
         g_nt.add_edge(3, 5);
         g_nt.add_edge(5, 3);
         g_nt.add_edge(11, 10);
         return 0;
The third way is to copy a pre-existing SparseGraph or NTSparseGraph. For example:
     #include "nt_wrappers/nauty_traces.h"
     int main( void ) {
         bool directed = 1;
         SparseGraph g(directed); // Defaults to 1 node
         g.add_node();
         g.add_node();
         g.add_edge(0, 1);
         g.add_edge(1, 2);
         g.add_edge(2, 0);
         // Three ways of copying a graph:
         NTSparseGraph g_nt_1(g);
         NTSparseGraph g_nt_2(directed);
         g_nt_2 = g;
         NTSparseGraph g_nt_3(g_nt_1);
         return 0;
```

The methods from the NTSparseGraph class that you are most likely to use are the following:

- NTSparseGraph(bool directed)
- NTSparseGraph(bool directed, size_t num_nodes)
- NTSparseGraph(const Graph& g)
- size_t num_nodes()
- size_t num_edges()
- size_t num_loops() Returns the number of self-loops
- directed Not a function just a constant boolean
- int add_node() Adds a node and returns the new node's ID
- int delete_node(int a) Deletes node a. Relabels the node with the largest label to have the label a. Then returns what used to be the label of what used to be the largest node.
- bool add_edge(int source, int target) Returns true iff the edge was new
- bool delete_edge(int source, int target) Returns true iff the edge was there to be deleted
- void flip_edge(int s, int t) Deletes edge (s,t) if it was present, adds edge (s,t) if it was absent.
- const std::unordered_set<int> &neighbors(int a) Returns an unordered set (C++ standard library) of all the nodes connected to node a
- const std::unordered_set<int> &out_neighbors(int a) Returns all the nodes that node a points to. In an undirected graph, this returns the same thing as neighbors(a).
- const std::unordered_set<int> &in_neighbors(int a) Returns all the nodes that point to node a. In an undirected graph, this returns the same thing as neighbors(a).

5.1.2 NautyTracesOptions

The NautyTracesOptions struct contains three boolean fields:

- get_node_orbits
- get_edge_orbits
- get_canonical_node_order

They are largely self-explanatory. If they are set to true, then a call to nauty/traces using these options will populate the corresponding fields in the relevant NautyTracesResults struct. Setting them to false may improve runtime, so only set them to true when you want the information.

5.1.3 NautyTracesResults

The NautyTracesOptions struct stores the output of a nauty/traces computation. It has the following fields:

- int error_status Will be non-zero if an error occurred
- size_t num_node_orbits Number of automorphism orbits of the nodes
- size_t num_edge_orbits Number of automorphism orbits of the edges
- double num_aut_base
- int num_aut_exponent The number of automorphisms of the graph is roughly num_aut_base ×10 num_aut_exponent.
- std::vector<int> canonical_node_order Stores the node IDs (0 through num_nodes() 1) in a canonical order. This field is only populated when the get_canonical_node_order option is used.
- Coloring<int> node_orbits Stores a "coloring" which gives every node a color corresponding to which automorphism orbit it is in. The Coloring class is described in Section 5.2. This field is only populated when get_node_orbits option is used.
- Coloring<Edge, EdgeHash> edge_orbits Stores a "coloring" which gives every edge a color corresponding to which automorphism orbit it is in. The Coloring class is described in Section 5.2 and the Edge class is described in Section 5.3. This field is only populated with the get_edge_orbits option is used.

5.2 Colorings

Colorings are used to store automorphism orbit information. They can also be used to force automorphisms to match nodes to other nodes of the same color.

5.2.1 Reading a Coloring

If you simply want to read the colorings that nauty and traces provide, then the only feature you really need is the access operator [].

For example, if node_col is a node coloring, then to see what color node 7 is, simply use node_col[7]. Accessing the color of an edge is a tiny bit more complicated. If edge_col is an edge coloring and dir is a boolean indicating whether or not you have directed edges, then the color of edge (a, b) is accessed as edge_col[EDGE(a, b, dir)]. The EDGE macro produces an Edge (which is really just a std::pair<int, int>) that respects a convention the code uses for undirected edges.

There are a few other methods for accessing the Coloring class that can be useful:

- size_t size() Returns the number of colored elements.
- const std::set<int>& colors() Returns a set of all the colors in the coloring.
- const std::unordered_set<T, THash>& cell(int color) Returns the set of nodes (type int) or edges (type Edge) that have the color color.

5.2.2 Creating a Coloring

If you want to *create* a Coloring for nodes, it should be initialized as follows:

```
Coloring<int> my_node_coloring();
```

If you want to *create* a Coloring for edges, it should be initialized as follows:

```
Coloring<Edge, EdgeHash> my_edge_coloring();
```

To set the color of an element or to remove an element from the coloring, use the following two methods:

- set(const T& elt, int color) Sets node or edge elt to color color.
- erase(const T& elt) Removes node or edge elt from the coloring.

5.3 Edge Class for Edge Colorings

The Edge class is only needed if you want to work with edge colorings. It is simply a typedef for std::pair<int, int>. The code requires that undirected edges put the smaller node ID first. The easiest way to create an Edge is probably to use the EDGE(source, target, directed) macro, where source and target are integers and directed is a boolean.

5.4 File Utils

To load a graph from a file or write a graph to a file, you can use the following functions:

Read Graph from File Version 1

This function assumes that the nodes are numbered 0 through the largest node ID found in the edge list.

Read Graph from File Version 2

This function puts all nodes in the nodelist into the graph, even if they do not appear in the edgelist. Note that if the nodes in the node list are not labeled 0 through n-1, they will be relabeled in sorted order as they are loaded.

Write Graph to File

If nodelist_filename is empty then no nodelist is written. SparseGraph and NTSparseGraph are both subclasses of Graph.

Construct a node list file from an edge list file

Reads the edgelist file and makes a nodelist for it.

If full_range is true, then the nodelist will consist of the interval from 0 through the largest node ID in the edgelist. If full_range is false, only nodes mentioned in the edgelist will be listed in the nodelist.

6 Simple Example

```
// minimal_nt_example.cpp
#include "nt_wrappers/nauty_traces.h"
#include<cmath>
#include<iostream>
int main(void) {
    bool directed = false;
    NTSparseGraph karate(directed);
    karate = read_graph(directed, "nt_test_graphs/karate.txt");
    std::cout<<"# Nodes: "<<karate.num_nodes()<<std::endl;</pre>
    std::cout<<"# Edges: "<<karate.num_edges()<<std::endl<<std::endl;</pre>
    NautyTracesOptions nto;
    nto.get_node_orbits = true;
    nto.get_edge_orbits = true;
    nto.get_canonical_node_order = true;
    NautyTracesResults ntr = traces(karate, nto);
    double log10_aut = std::log10(ntr.num_aut_base) + ntr.num_aut_exponent;
    std::cout<<"Log10 of Automorphisms: "<<log10_aut<<std::endl;</pre>
    std::cout<<"Number of Automorphisms: "<<(std::pow(10.0, log10_aut))<<std::endl;</pre>
    std::cout<<"Number of Node Orbits:</pre>
                                           "<<ntr.node_orbits.colors().size()<<std::endl;</pre>
    std::cout<<"Number of Edge Orbits:</pre>
                                           "<<ntr.edge_orbits.colors().size()<<std::endl;</pre>
    std::cout<<"First Node in Canonical Ordering: "
             <<ntr.canonical_node_order[0]<<std::endl;</pre>
    return 0;
}
   The above example can be compiled with the following command:
g++ -Wall -Wextra -o minimal_nt_example -std=c++11 minimal_nt_example.cpp \
                         nt_wrappers/nt_wrappers.a
```