

Month-by-Month Staffing Plan

Determine the optimal number of agents per country for each month of 2025, balancing:

Cost efficiency – Minimizing idle agents while meeting advertiser demand
 Timely advertiser support – Reducing wait times and maximizing revenue uplift
 Scalability – Adjusting for market fluctuations with hiring/firing constraints

Assumptions:

1. We only hire / send fire notices on the 1st of each month.

Decision Variables:

h_t^c : # of agents hired in country c at month t



f_t^c : # of agents fired in country c at month t



Input Parameters:

US

$$\begin{pmatrix} h_1 & h_2 & \dots & h_{12} \\ f_1 & \dots & \dots & f_{12} \end{pmatrix}$$

A_0^c : Initial # of agents in country c (Jan 2025)

S^c : Annual salary for an agent in country c

T^c : Threshold in country c

N_t^c : # of new advertisers in country c at month t

B_i : Projected annual advertising budget for advertiser i

u_i : Expected uplift % based on :

$$\begin{aligned} P(0\% \text{ uplift}) &= 0.05 & P(15\% \text{ uplift}) &= 0.25 \\ P(5\% \text{ uplift}) &= 0.15 & P(20\% \text{ uplift}) &= 0.2 \\ P(10\% \text{ uplift}) &= 0.25 & P(25\% \text{ uplift}) &= 0.1 \end{aligned}$$

\Rightarrow Expected revenue uplift multiplier

$$\begin{aligned} E[u] &= 0.05 \times 0 + 0.15 \times 0.05 + 0.25 \times 0.1 + 0.25 \times 0.15 + 0.2 \times 0.2 + 0.1 \times 0.25 \\ &= 0.135 \end{aligned}$$

Dependent Variables:

A_t^c : Total # of active agents in country c at month t

$$A_t^c = A_{t-1}^c + h_{t-1}^c - f_{t-1}^c$$

* Agents hired in month $t-1$ are available in t ,
agents noticed-to-fire in $t-1$ leave in t .

* G_t^c : Advertisers who graduated after 60 days.

$$G_t^c = \sum_{i=t-2}^t (\bar{E}_i^c - U_i^c)$$

↑ 60 days ago

D_t^c : Total occupied spots at month t

$$D_t^c = D_{t-1}^c + 10 A_t^c - G_t^c$$

L_t^c : Available slots for new advertisers

$$L_t^c = 10 A_t^c - D_t^c$$

U_t^c : # of unassigned advertisers in country c
at the 1st of month t .

$$U_t^c = \max(0, \underset{\substack{\uparrow \\ \text{New in}}}{P_t^c} + \underset{\substack{\uparrow \\ \text{pool}}}{U_{t-1}^c} + \underset{\substack{\uparrow \\ \text{total capacity at month } t}}{D_t^c} - 10 A_t^c)$$

E_t^c : # of eligible advertisers in country c at month t

$$E_t^c = \sum_{i \in N_t^c} 1 \mid \underline{\underline{B_i^c > T^c}}$$

R_t^c : Incremental Revenue uplift

Objective:

Maximize Net Profit

Income	Cost
Revenue uplift $R_t^c = \mathbb{E}[\text{uplift}]$ $= \sum_i B_i \cdot U_i$ $= 0.135 \cdot \sum_i B_i$	Salary : $A_t^c \cdot \frac{S^c}{12} : C_{\text{salary},t}^c$ Firing Cost : $0.4 \cdot S^c \cdot F_t^c : C_{\text{fire},t}^c$ Hiring Cost : $h_t^c \cdot \frac{S^c}{12} : C_{\text{hire},t}^c$ Idle Agent : $\left(1 - \frac{\text{Assigned Advertisers}}{10 \cdot A_t^c}\right) \times C_{\text{salary},t}^c$ <div style="text-align: center; margin-left: 150px;"> \uparrow Idle Ratio </div> $: C_{\text{idle},t}^c$

$$\max \sum_c \sum_t (R_t^c - C_{\text{salary},t}^c - C_{\text{fire},t}^c - C_{\text{hire},t}^c - C_{\text{idle},t}^c)$$

Constraints:

$$A_t^c, h_t^c, f_t^c \in \mathbb{Z}^+$$

$$\text{Track agents \# : } A_t^c = A_{t-1}^c + h_{t-1}^c - f_{t-1}^c$$

$$\text{Waiting limit : } U_t^c = 0$$

(60 days)

$$\text{firing : } f_t^c \leq A_t^c$$