

Toggle()

Time Complexity $O(n)$

Toggle() switches the heapState between Min-Heap and Max-Heap. After toggling the state, the heap is rebuilt using the heapify method. Each downheap operation is $\log(n)$, but the combined cost of all downheap operations is $O(n)$ because most nodes are closer to the leaves, and fewer downheap operations involve the deeper parts of the heap

Remove(e)

Time Complexity: $O(n)$

Remove() searches through the array, scanning through all elements which requires $O(n)$. Once the entry is found, the entry is replaced with the last entry in the heap. The heap property is then restored using either upheap or downheap which take $O(\log n)$. The $O(n)$ search dominates the overall time complexity.

ReplaceKey(e,k)

Time Complexity: $O(n)$

ReplaceKey() begins by scanning through each element to find the target element which takes $O(n)$. Once found, the key is then swapped which takes $O(1)$. The overall time complexity is dominated by $O(n)$.

replaceValue(e,v)

Time Complexity: $O(n)$

replaceValue() begins by scanning through each element to find the target element which takes $O(n)$. Once found, the value is then swapped which takes $O(1)$. The overall time complexity is dominated by $O(n)$. Once the swap is complete the heap property must be restored using the upheap or downheap method. Both operations take $O(\log n)$. The $O(n)$ search dominates the overall time complexity