

1. Determine the solution to the heat equation  $u_t = \alpha^2 u_{xx}$  with  $\alpha \neq 1$  (We did the  $\alpha = 1$  case in class).

2. Use Fourier Transforms to determine the solution to  $u_t = cu_x$  is  $u(x, t) = f(x + ct)$  where  $u(x, 0) = f(x)$ .

3. Determine d'Alembert's solution for  $u_{tt} = c^2 u_{xx}$

4. Derive d'Alembert's formula for  $u_{tt} = u_{xx}$  by assuming that  $u(x, t) = v(x+t, x-t) = v(y, z)$ . Next show that the wave equation yields  $v_{yz} = 0$  and hence  $v = A(y) + B(z)$  and solve for  $A$  and  $B$  using the initial conditions  $u(x, 0) = f(x)$  and  $u_t(x, 0) = g(x)$ .